

- 1) How many different arrangements of the word CABBAGES are possible?
- a. 3,780
 - b. 5,040
 - c. 5,670
 - d. 7,560
 - e. 10,080

How many arrangements of the word CABBAGES:

- | | |
|--|--|
| 2) ... keep repeated letters together? | 3) ... have NO identical letters adjacent? |
| a. 720 | a. 3,040 |
| b. 840 | b. 3,780 |
| c. 960 | c. 5,040 |
| d. 1,020 | d. 5,760 |
| e. 1,090 | e. 7,560 |

A box contains 8 balls, of which 3 are identical and the other 5 are unique. 3 balls are chosen from the box randomly. How many unique selections:

- | | |
|----------------------|---|
| 4) ... are possible? | 5) ... contain at least 1 of the identical balls? |
| a. 24 | a. 26 |
| b. 26 | b. 16 |
| c. 28 | c. 20 |
| d. 29 | d. 24 |
| e. 30 | e. 22 |

A program randomly outputs a two-digit code using 1 to 9, with repeats allowed. How many:

- 6) ... unique codes can be formed?
- a. 81
 - b. 72
 - c. 63
 - d. 56
 - e. 45
- 7) ... codes have a second digit larger than the first?
- a. 18
 - b. 32
 - c. 34
 - d. 36
 - e. 42
- 8) ... have one odd and one even digit?
- a. 30
 - b. 32
 - c. 35
 - d. 38
 - e. 40

The program now outputs a three-letter code using letters from A to Z. How many unique codes:

- 9) ... have exactly one vowel (a vowel being A, E, I, O, U) and no repeated letters?
- a. 11,800
 - b. 12,200
 - c. 12,600
 - d. 13,200
 - e. 13,800
- 10) ... have only vowels (with repeats allowed)?
- a. 120
 - b. 125
 - c. 132
 - d. 140
 - e. 144

A soccer team has 1 goalkeeper, 4 defenders, 2 midfielders, and 4 forwards. A soccer club has 3 goalkeepers, 8 defenders, 5 midfielders, and 6 forwards on its roster. How many ways are there to:

- 11) ... choose a team from the club's members?
- a. 33,100
 - b. 32,750
 - c. 31,500
 - d. 31,200
 - e. 30,350
- 12) ... choose a team that includes exactly 1 of a pair of twins (1 midfielder, 1 forward)?
- a. 17,600
 - b. 17,200
 - c. 16,800
 - d. 16,400
 - e. 16,200
- 13) ... randomly select 3 of the chosen team members for random pre-game testing?
- a. 165
 - b. 170
 - c. 175
 - d. 180
 - e. 185

- 14) In how many ways can 2 dogs and 1 cat be selected from a group of 7 dogs and 6 cats?
- a. 102
 - b. 108
 - c. 122
 - d. 126
 - e. 132
- 15) Out of 12 books, 6 are chosen and ordered on a shelf. How many unique arrangements are possible?
- a. 44,352
 - b. 133,056
 - c. 177,408
 - d. 443,520
 - e. 665,280
- 16) How many unique 3-digit numbers can be formed using the digits 1, 2, 2, 4, 5, 6?
- a. 72
 - b. 78
 - c. 81
 - d. 84
 - e. 90
- 17) Find n if $nC_2 = 55$.
- a. 10
 - b. 11
 - c. 12
 - d. 13
 - e. 14
- 18) Simplify $\frac{1}{n!} - \frac{1}{(n+1)!}$
- a. $\frac{1}{n(n+1)!}$
 - b. $\frac{n+1}{n!}$
 - c. $\frac{n}{n!}$
 - d. $\frac{n}{(n+1)!}$
 - e. $n!$
- 19) Six dongles are randomly distributed to 2 students. In how many ways can it be done if each student must have at least 1 dongle?
- a. 62
 - b. 16
 - c. 32
 - d. 30
 - e. 64

- 20) From a party of 12 men and 8 women, a group of 5 men and 3 women is chosen. How many unique groups can be selected?
- a. 55,440
 - b. 44,352
 - c. 20,790
 - d. 13,860
 - e. 6,930

In how many ways can the integers 1, 2, 3, 4, 5, 6, 7, 8 be placed in a circle if:

- 21) ... all the even numbers are together? 22) ... the odd and even numbers alternate?
- a. 625
 - b. 576
 - c. 501
 - d. 432
 - e. 324
- 23) ... the integers 1 and 7 are adjacent?
- a. 840
 - b. 940
 - c. 1,040
 - d. 1,240
 - e. 1,440
- 24) How many three-digit numbers have NO repeated digits?
- a. 580
 - b. 600
 - c. 648
 - d. 672
 - e. 690
- 25) Of the arrangements of the digits $\{1, 2, 3, 4, 5, 7\}$, what proportion are odd numbers?
- a. $\frac{1}{3}$
 - b. $\frac{4}{5}$
 - c. $\frac{1}{2}$
 - d. $\frac{2}{3}$
 - e. $\frac{2}{5}$
- 26) Evaluate $\binom{12}{7} \div \binom{4}{2}$.
- a. 132
 - b. 81
 - c. 42
 - d. 26
 - e. 12

A bag has 15 unique pens. 6 have red ink, 5 blue, and 4 black. How many ways are there to choose

27) ... 3 pens of one color?

- a. 33
- b. 34
- c. 36
- d. 37
- e. 39

28) ... 1 pen of each color?

- a. 108
- b. 112
- c. 116
- d. 120
- e. 124

29) ... 10 pens in 2 colors?

- a. 10
- b. 11
- c. 12
- d. 14
- e. 16

30) A die is thrown twice. How many ways are there for the outcomes to sum to at most 4?

- a. 11
- b. 9
- c. 8
- d. 6
- e. 5

31) Find n if $\binom{n}{2} = 36$.

- a. 9
- b. 11
- c. 12
- d. 14
- e. 15

32) Six identical coins are lined up on a table. Find how many patterns are possible if there are 5 tails and 1 head.

- a. 2
- b. 4
- c. 5
- d. 6
- e. 8

Consider the word ELEVATED.

- 33) How many unique arrangements of its letters exist?
- a. 8,840
 - b. 6,720
 - c. 5,480
 - d. 4,720
 - e. 3,630
- 34) In how many of the arrangements are T and D not adjacent?
- a. 3,960
 - b. 4,230
 - c. 4,720
 - d. 4,800
 - e. 5,040
- 35) How many of the arrangements have alternating consonants and vowels?
- a. 192
 - b. 194
 - c. 200
 - d. 208
 - e. 212