

## Integer Multiplication - 20200808058

```
static long largeMultiply(long a, long b) {
    long[] df = new long[32]; // Array to store multiplication results
    Stack<Boolean> addStack = new Stack<>(); // Stack to track binary
    while (b > 1) {
        if (b % 2 == 0)
            addStack.push(true); // Push true onto the stack if b is even
        else {
            addStack.push(false); // Push false onto the stack if b is odd
            b--; // Subtracted to make the number b even
        }
        b = b / 2; // Update b by dividing it by 2
    }
    df[0] = a; // Initialize df array with the first element as a
    int i = 0; // Variable i for array index tracking
    while (!addStack.isEmpty()) {
        if (!addStack.pop())
            df[i + 1] = 2 * df[i] + df[0];
        else
            df[i + 1] = 2 * df[i];
        i++;
    }
    return df[i]; // Result is the last element of the df array
}
```

### Explanation of Algorithm:

Firstly, an array is determined for the multiplication operation performed in each step, then a stack is used to hold the true and false values. In the  $a*b$  operation, the number  $b$  is taken and started to be divided by two. Then, if the remainder is 0 when divided by two, true is added to the stack, otherwise false is added and 1 is subtracted to make the number  $b$  even and this cycle continues until the number  $b$  is equal to 1. Then the number  $a$  is set to  $df[0]$  and the stack is popped with for loop. If the value in the stack is false,  $df[i + 1] = 2*df[i] + df[0]$  is done. If true,  $df[i + 1] = 2*df[i]$  is done. By doing this, it goes from bottom to top. Then the last processed element in the array is returned as a result. For example, in this case, the  $df$  array of  $7*30$  is as follows:

$$[7, 21, 49, 105, 210] = 210$$

The code was coded by **referring** to Tabulation examples on other topics on the internet and the bottom-up computation on slide 10, pages 98 and 136.

### Possible Issues:

**Inefficiency:** According to the articles written on the internet, dynamic programming is not recommended for this problem because dynamic programming does not provide any gain in time or space complexity.

**Array Size:** The  $df$  array is fixed at size 32, which might not be sufficient for all cases. The size should be dynamically determined based on the binary representation of  $b$ .

**Time Complexity:** The time complexity is  $O(\log b)$ , this is because we create a binary representation by dividing  $b$  by 2 until it equals 1.

**Space Complexity:** The space complexity is  $O(\log b)$  because of the space used by  $addStack$ . The  $df$  array has a fixed size of 32, which is constant. The size of the stack depends on the number of bits of  $b$ , because it stores boolean values for whether the remainder after each division of  $b$  by two is equal to 0.