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## The SAS System

## The Mixed Procedure

| Model Information         |                     |  |  |
|---------------------------|---------------------|--|--|
| Data Set                  | WORK.STRENGTH_DATA  |  |  |
| Dependent Variable        | strength            |  |  |
| Covariance Structure      | Variance Components |  |  |
| Estimation Method         | Type 3              |  |  |
| Residual Variance Method  | Factor              |  |  |
| Fixed Effects SE Method   | Model-Based         |  |  |
| Degrees of Freedom Method | Containment         |  |  |

| Class Level Information |   |      |  |  |
|-------------------------|---|------|--|--|
| Class Levels Values     |   |      |  |  |
| machine                 | 4 | 1234 |  |  |
| operator                | 3 | 123  |  |  |

| Dimensions            |    |  |
|-----------------------|----|--|
| Covariance Parameters | 4  |  |
| Columns in X          | 1  |  |
| Columns in Z          | 19 |  |
| Subjects              | 1  |  |
| Max Obs Per Subject   | 24 |  |

| Number of Observations          |    |  |
|---------------------------------|----|--|
| Number of Observations Read     | 24 |  |
| Number of Observations Used     |    |  |
| Number of Observations Not Used | 0  |  |

| Type 3 Analysis of Variance |    |                   |                |   |                          |             |            |        |
|-----------------------------|----|-------------------|----------------|---|--------------------------|-------------|------------|--------|
| Source                      | DF | Sum of<br>Squares | Mean<br>Square | Expected Mean Square  | Error Term               | Error<br>DF | F<br>Value | Pr > F |
| machine                     | 3  | 12.458333         | 4.152778       | Var(Residual) + 2 Var<br>(machine*operator) + 6 Var<br>(machine)  | MS<br>(machine*operator) | 6           | 0.56       | 0.6619 |
| operator                    | 2  | 160.333333        | 80.166667      | Var(Residual) + 2 Var<br>(machine*operator) + 8 Var<br>(operator) | MS<br>(machine*operator) | 6           | 10.77      | 0.0103 |
| machine*operator            | 6  | 44.666667         | 7.444444       | Var(Residual) + 2 Var<br>(machine*operator)                       | MS(Residual)             | 12          | 1.96       | 0.1507 |
| Residual                    | 12 | 45.500000         | 3.791667       | Var(Residual)   |                          |             |            |        |

| <b>Covariance Parameter Estimates</b> |         |  |  |
|---------------------------------------|---------|--|--|
| Cov Parm Estimate                     |         |  |  |
| machine                               | -0.5486 |  |  |
| operator                              | 9.0903  |  |  |

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| Covariance Parameter Estimates |        |  |  |
|--------------------------------|--------|--|--|
| Cov Parm Estima                |        |  |  |
| machine*operator               | 1.8264 |  |  |
| Residual                       | 3.7917 |  |  |

| Fit Statistics           |       |  |  |
|--------------------------|-------|--|--|
| -2 Res Log Likelihood    | 109.5 |  |  |
| AIC (smaller is better)  | 117.5 |  |  |
| AICC (smaller is better) | 119.7 |  |  |
| BIC (smaller is better)  | 115.1 |  |  |

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## The SAS System

## **The Mixed Procedure**

| Model Information         |                     |  |  |
|---------------------------|---------------------|--|--|
| Data Set WORK.STRENGTH    |                     |  |  |
| Dependent Variable        | strength            |  |  |
| Covariance Structure      | Variance Components |  |  |
| Estimation Method         | REML                |  |  |
| Residual Variance Method  | Profile             |  |  |
| Fixed Effects SE Method   | Model-Based         |  |  |
| Degrees of Freedom Method | Satterthwaite       |  |  |

| Class Level Information |               |      |  |  |
|-------------------------|---------------|------|--|--|
| Class                   | Levels Values |      |  |  |
| machine                 | 4             | 1234 |  |  |
| operator                | 3             | 123  |  |  |

| Dimensions            |    |  |
|-----------------------|----|--|
| Covariance Parameters | 4  |  |
| Columns in X          | 1  |  |
| Columns in Z          | 19 |  |
| Subjects              | 1  |  |
| Max Obs Per Subject   | 24 |  |

| Number of Observations          |    |  |
|---------------------------------|----|--|
| Number of Observations Read     | 24 |  |
| Number of Observations Used     | 24 |  |
| Number of Observations Not Used | 0  |  |

| Iteration History |             |                 |            |  |  |  |  |
|-------------------|-------------|-----------------|------------|--|--|--|--|
| Iteration         | Evaluations | -2 Res Log Like | Criterion  |  |  |  |  |
| 0                 | 1           | 124.48875799    |            |  |  |  |  |
| 1                 | 3           | 109.85258730    | 0.00025935 |  |  |  |  |
| 2                 | 1           | 109.84333612    | 0.00000208 |  |  |  |  |
| 3                 | 1           | 109.84326553    | 0.00000000 |  |  |  |  |

Convergence criteria met.

| Covariance Parameter Estimates |          |  |  |  |
|--------------------------------|----------|--|--|--|
| Cov Parm                       | Estimate |  |  |  |
| machine                        | 0        |  |  |  |
| operator                       | 9.2275   |  |  |  |
| machine*operator               | 1.2777   |  |  |  |
|                                |          |  |  |  |

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| Covariance Parameter Estimates |          |  |  |  |
|--------------------------------|----------|--|--|--|
| Cov Parm                       | Estimate |  |  |  |
| Residual                       | 3.7917   |  |  |  |

| Fit Statistics           |       |  |  |  |  |
|--------------------------|-------|--|--|--|--|
| -2 Res Log Likelihood    | 109.8 |  |  |  |  |
| AIC (smaller is better)  | 115.8 |  |  |  |  |
| AICC (smaller is better) | 117.1 |  |  |  |  |
| BIC (smaller is better)  | 114.0 |  |  |  |  |

| Solution for Fixed Effects |          |                |    |         |         |       |        |        |  |
|----------------------------|----------|----------------|----|---------|---------|-------|--------|--------|--|
| Effect                     | Estimate | Standard Error | DF | t Value | Pr >  t | Alpha | Lower  | Upper  |  |
| Intercept                  | 207.29   | 1.8277         | 2  | 113.42  | <.0001  | 0.05  | 199.43 | 215.16 |  |

| Estimates            |          |                |    |         |         |       |        |        |
|----------------------|----------|----------------|----|---------|---------|-------|--------|--------|
| Label                | Estimate | Standard Error | DF | t Value | Pr >  t | Alpha | Lower  | Upper  |
| Avg. solder strength | 207.29   | 1.8277         | 2  | 113.42  | <.0001  | 0.05  | 199.43 | 215.16 |