

# Lambda Calculus

May 26, 2023

## 1 Grammar

$\text{term} ::= \backslash \text{' bindings '}' \text{ term}$   
 $\quad \mid \text{ app}$

$\text{app} ::= \text{ atom}$   
 $\quad \mid \text{ app atom}$

$\text{atom} ::= \text{ var}$   
 $\quad \mid \text{ '(' term ') '}$

$\text{var} ::= \text{ NAME}$

$\text{bindings} ::= \text{ NAME+}$

$\text{NAME} ::= [\text{'a'..'z'}]$

## 2 Examples

- $\backslash x y.x: \text{ term} \Rightarrow \backslash \text{bindings . term} \Rightarrow \backslash x y . \text{ term} \Rightarrow \backslash x y . \text{ app} \Rightarrow$   
 $\backslash x y . \text{ atom} \Rightarrow \backslash x y . \text{ var} \Rightarrow \backslash x y . x$
- $(\backslash x.x) (y z): \text{ term} \Rightarrow$   
 $\text{ app} \Rightarrow$   
 $\text{ app atom} \Rightarrow$   
 $\text{ atom atom} \Rightarrow$   
 $(\text{ term}) \text{ atom} \Rightarrow$   
 $(\text{ term}) (\text{ term}) \Rightarrow$

```
(\bindings . term) (term) =>  
(\x . term) (term) =>  
(\x.x) (term) =>  
(\x.x) (app) =>  
(\x.x) (app atom) =>  
(\x.x) (atom atom) =>  
(\x.x) (var atom) =>  
(\x.x) (y atom) =>  
(\x.x) (y var) =>  
(\x.x) (y z)
```