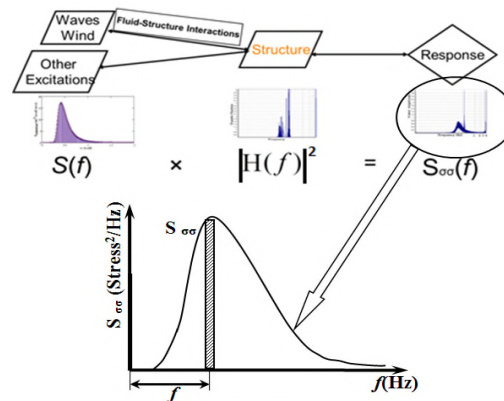


# 非线性动力学应用于结构疲劳分析与评估

贾军波  
Aker Solutions

2020年6月16日



$$D_{j,q} = \frac{\tau(8\lambda_0)^{\frac{m}{2}}}{A} \cdot \sqrt{\frac{\lambda_2}{\lambda_0}} \cdot \Gamma\left(\frac{2+m}{2}\right)$$

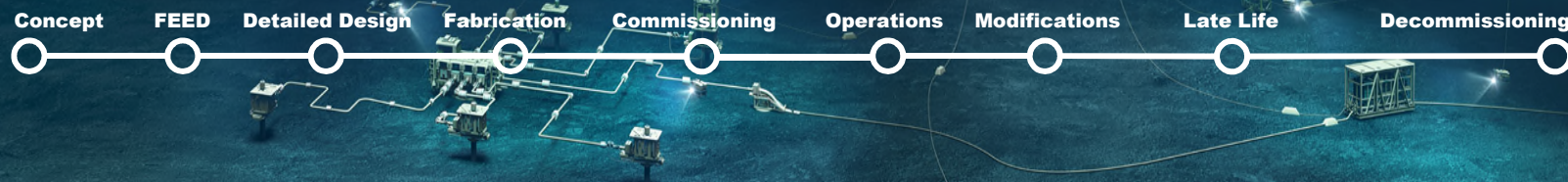
$$D_{\text{total}} = \sum_j \sum_q (\Psi_{j,q} \cdot D_{j,q})$$

$$L_{\text{total}} = \frac{1}{D_{\text{total}}} \text{ years}$$





We deliver **integrated solutions** from subsea to surface and through the life of an energy asset





## 我们的愿景 Our Vision

打造为全球能源行业可持续发展的领导者

**A leader in forging a sustainable future  
for the global energy industry and the world  
it serves**



# Global Presence

**16 000**

EMPLOYEES

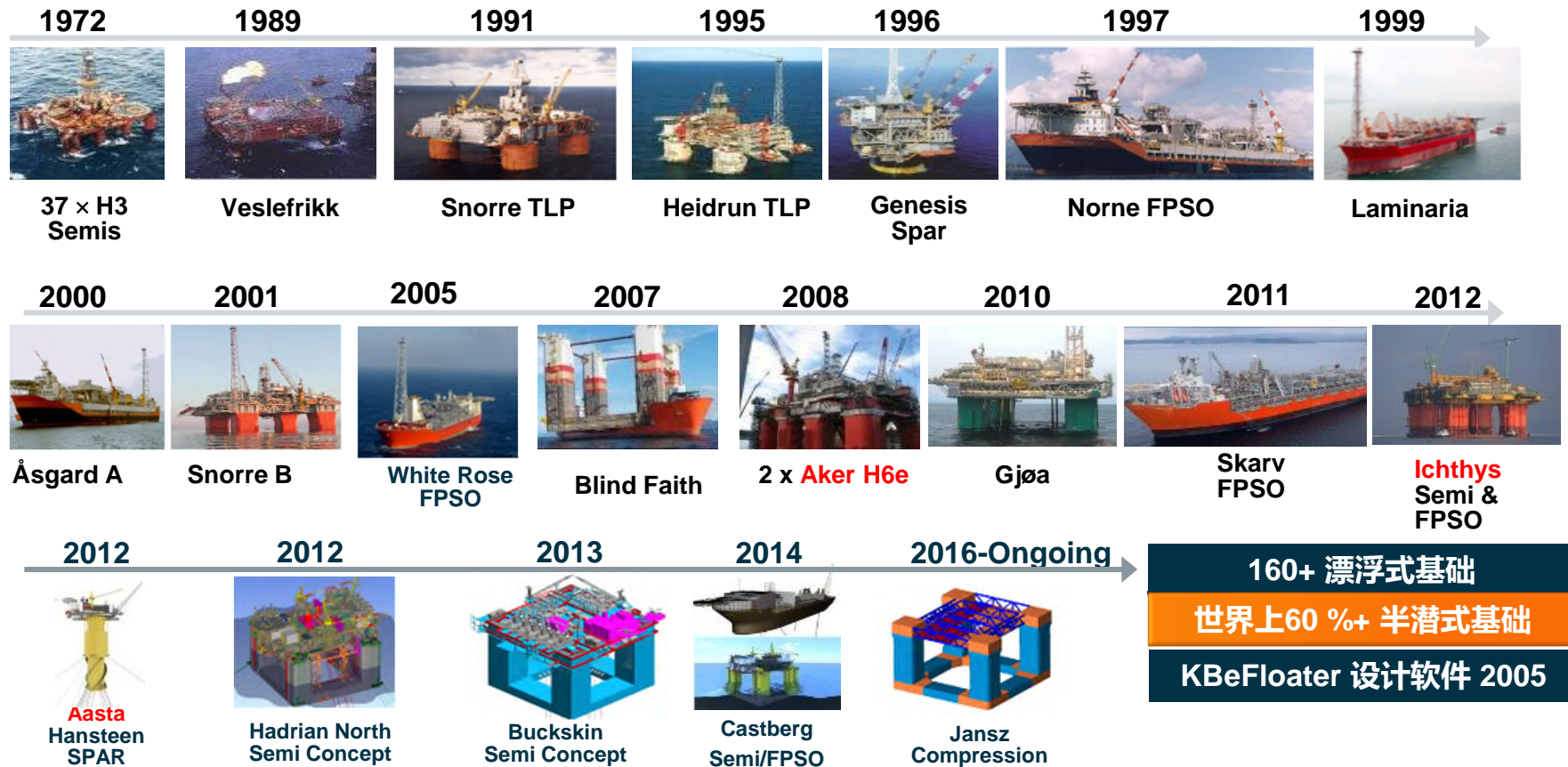
**20+**

COUNTRIES

**50+**

LOCATIONS

# 40多年的漂浮式基础设计经验



# 动态电缆工程实例 Dynamic Power Cables

## ■ GirRI (安哥拉)

- Water depth: 1500m
- Manufactured: Q2 2014
- Installed: Q1 2016
- Cables: 3x300mm<sup>2</sup> 18/30kV
- Length: 12km single helix



## ■ Goliat (挪威)\*

- Water depth: 370m
- Manufactured: Q3 2013
- Installed: Q2 2014
- Cables: 4x1600mm<sup>2</sup> 6/10(12)kV
- Length: 1750m



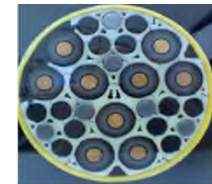
## ■ Ichthys (澳大利亚)\*

- Water depth: 250m
- Manufactured: Q3 2014
- Installed: 2015
- Cables: 3x500mm<sup>2</sup> 18/30kV
- Length: 5000m, dynamic in both ends



## ■ Cascade & Chinook (美国墨西哥湾)

- Water depth: 2700m
- Manufactured: 2010
- Installed: 2014
- Cables: 9x150mm<sup>2</sup> 12/20kV
- Length: 3km



*\*the design is tuned to meet a high weight to outer diameter ratio to avoid clashing with neighboring risers and are operating in **harsh environment with extreme wave and current conditions.***

Offshore Wind Solutions

## Plan for presentation

- Background
- Fatigue analysis procedure
- Structural and wave modelling for a prototype jacket structure
- Sensitivity analysis of the fatigue life influenced by the numerical and modelling parameters
- Statistical and frequency check of the structure's response
- Recommendations and conclusions for modelling and analysis practice

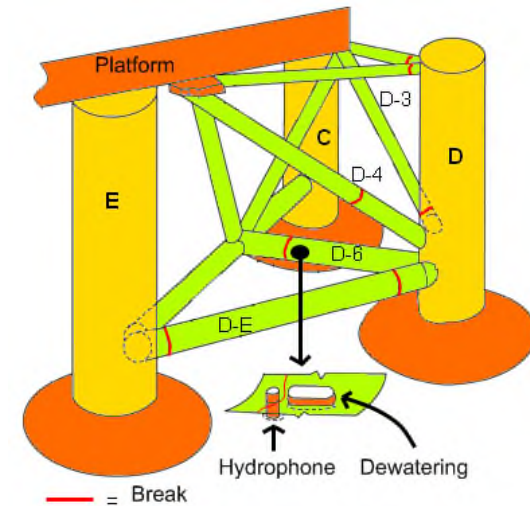


# Fatigue Accidents

Eschede accident, 3<sup>rd</sup> of June 1998, speed before crash: 200 km/h, 102 dead, 88 injured, cracks in the wheel tire on the first middle car caused by vibrations



Capsizing of *Alexander Kielland*, 1980, 123 dead, fatigue of brace → loss of column → flooding into deck → capsizing

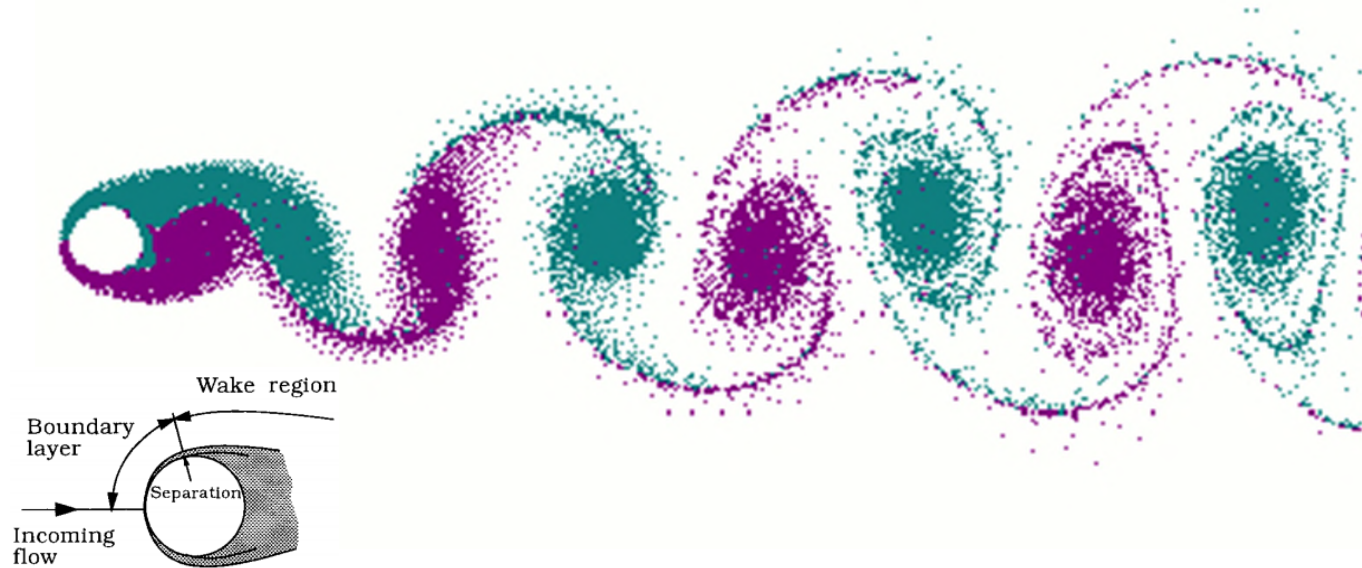


Sinking of *MS Estonia* occurred on 28<sup>th</sup> of September 1994, 852 dead, fatigue of bow door visor locking devices due to repeated bow wave loadings





# Fatigue due to Vortex Induced Vibration



Severe vibrations have been reported on several flare booms in the North Sea - the actual vibration amplitude was up to 20 times higher than the one from the model testing of individual members



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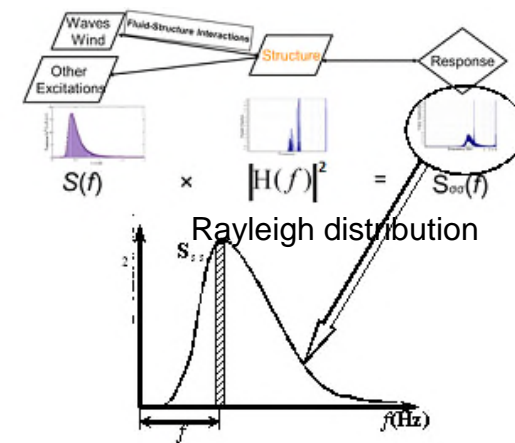
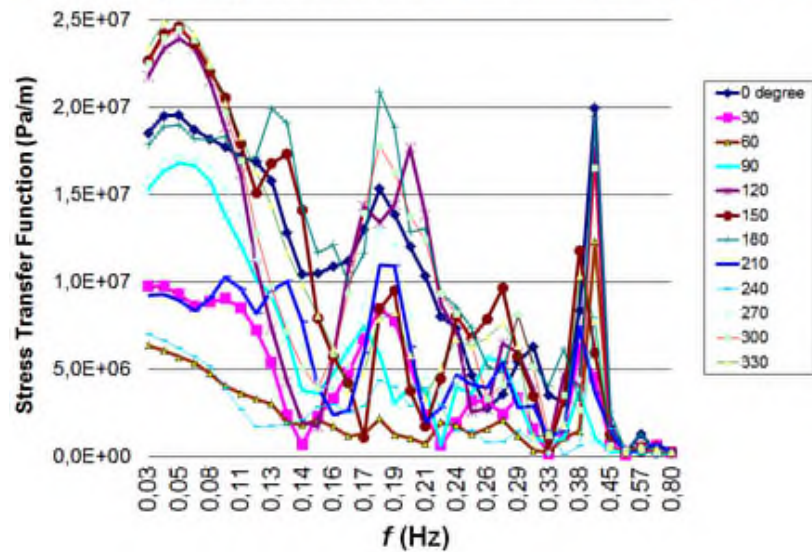


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# Stochastic Fatigue Analysis of Gullfaks C

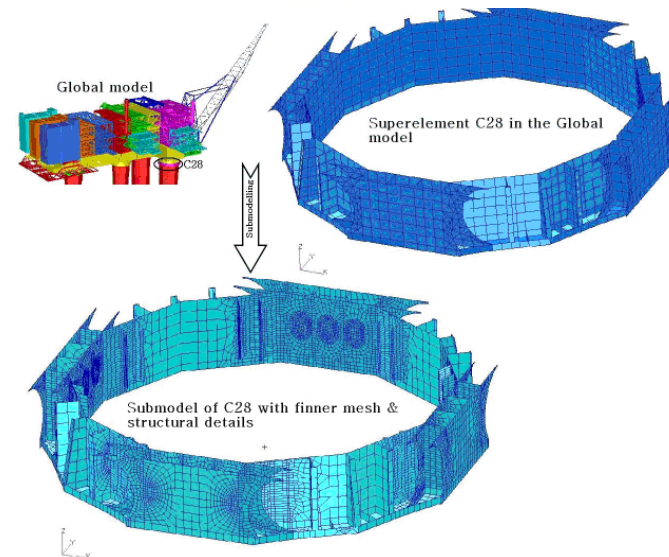


Modulus of principal stress transfer function at shell element surface



$$D_{i,q} = \frac{\tau(8\lambda_0)^2}{\Lambda} \cdot \frac{\sqrt{\lambda_0}}{\lambda_0} \cdot I\left(\frac{2+m}{2}\right)$$

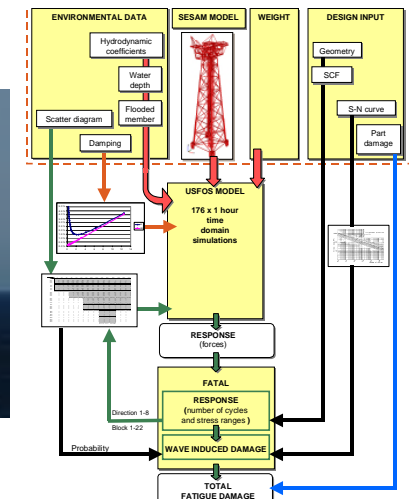
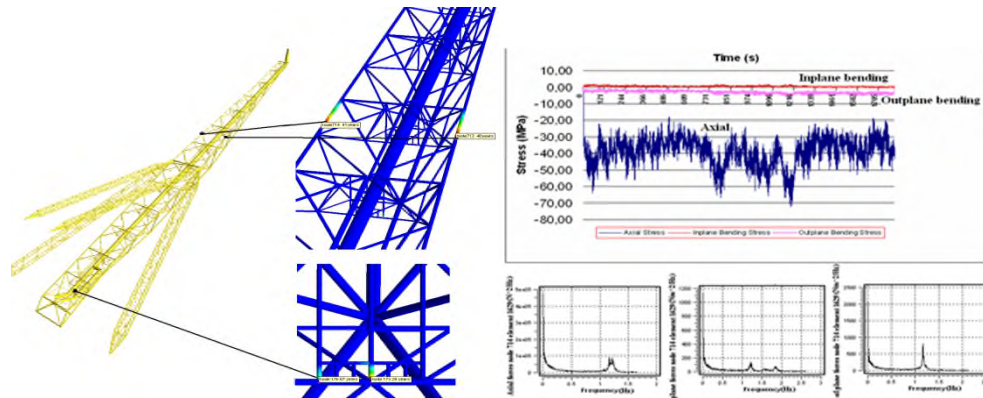
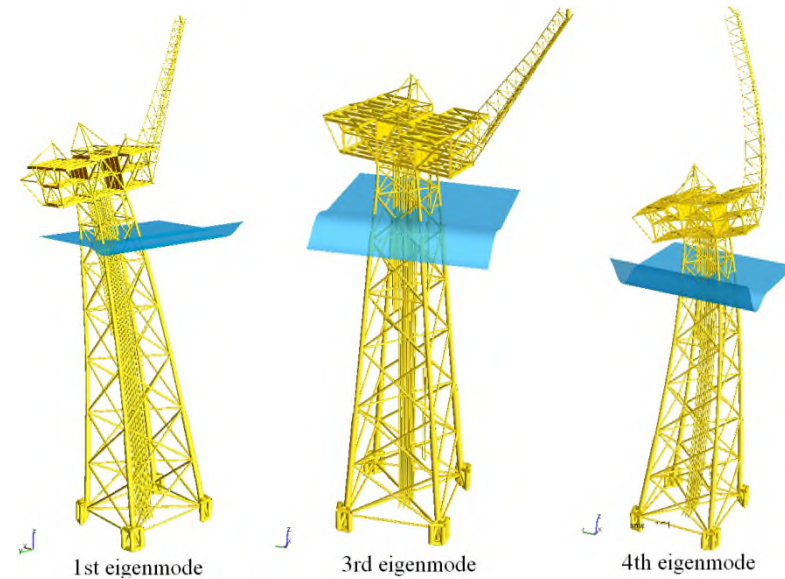
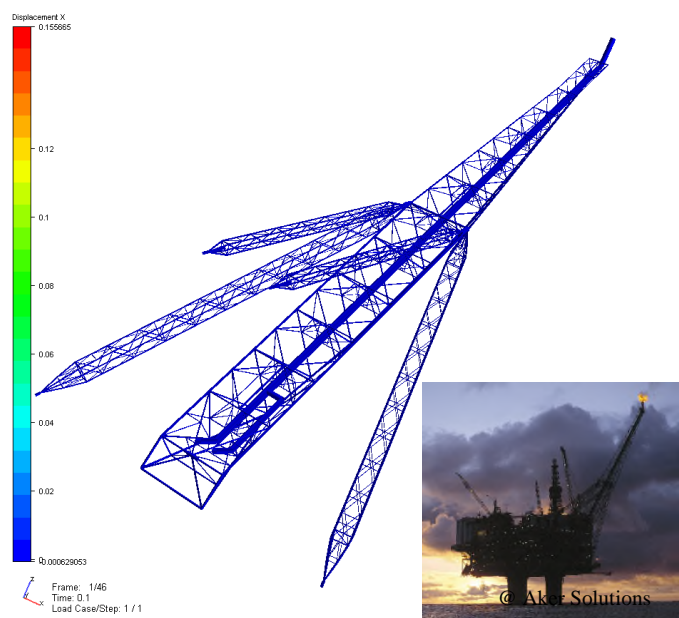
$$D_{total} = \sum_f \sum_q (\psi_{i,q} \cdot D_{i,q})$$





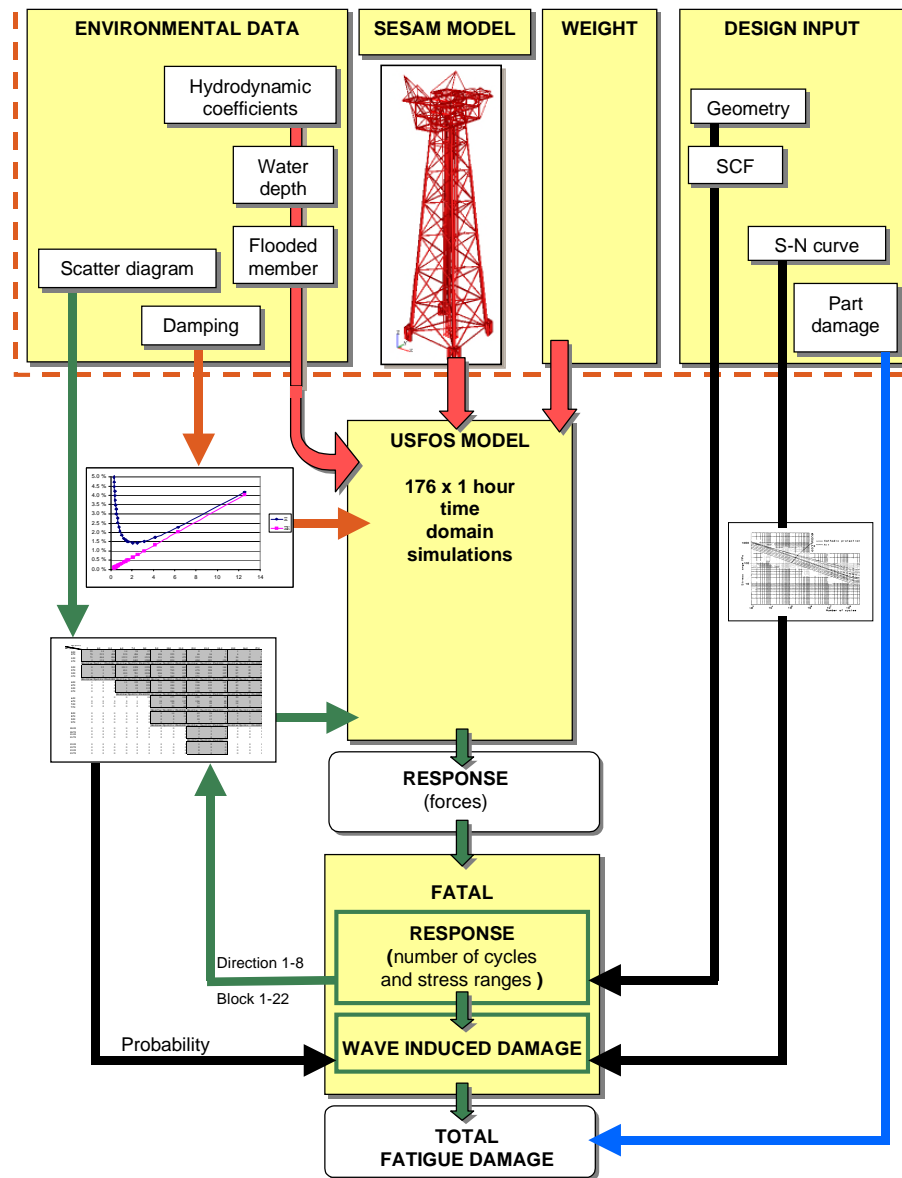
# Wind and Wave Induced Fatigue — Nonlinear dynamics

Wind Induced Response Case.

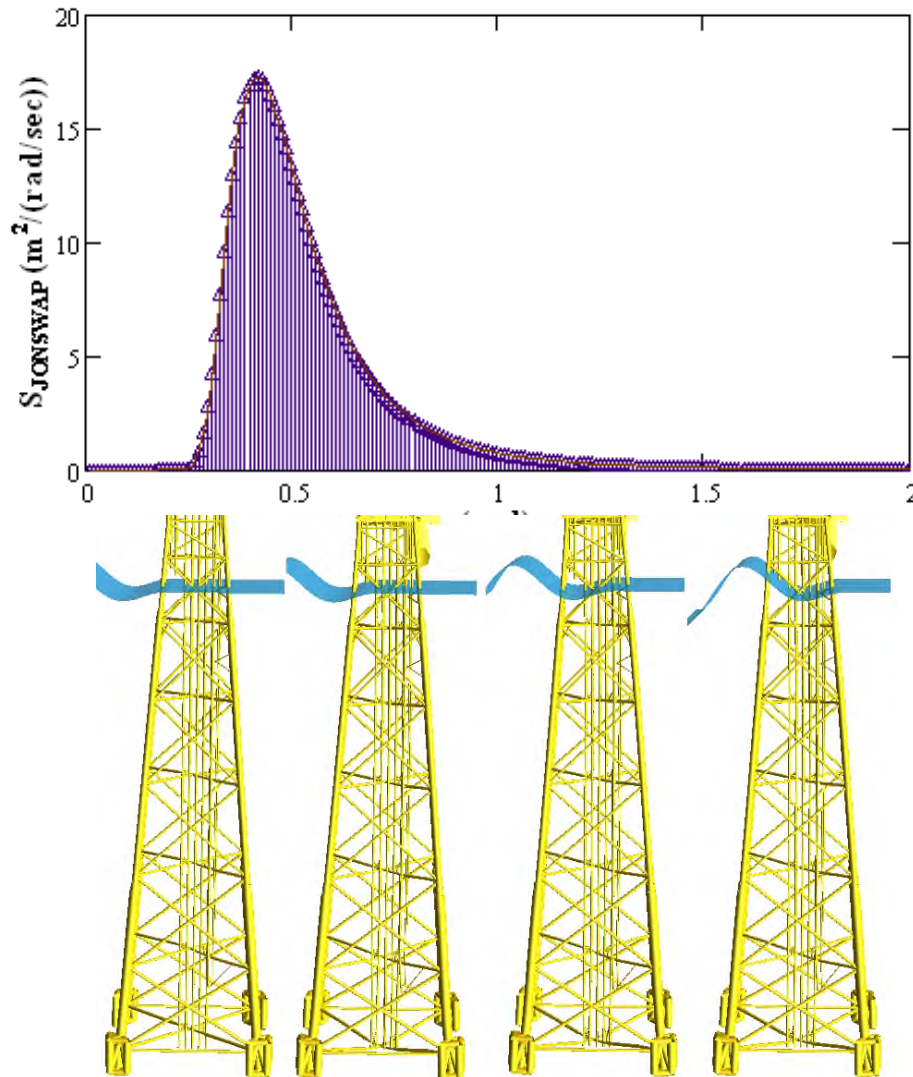




# Analysis procedure



# Wave descriptions



$$S_{JONSWAP}(\omega) = \frac{A}{\omega^5} e^{-\frac{D}{\omega^4}} \cdot \gamma^\delta$$

$$\xi(x, t) = \sum_{n=1}^N a_n \cos(k_n x - \omega_n t + \gamma_n)$$

$$a_n = \sqrt{2\Delta S(\omega_n)}$$

# Wave statistics

194

J. Jia / Applied Ocean Research 30 (2008) 189–198

**Table 2**

Scatter diagram divided into 22 blocks (duration: 3 h)

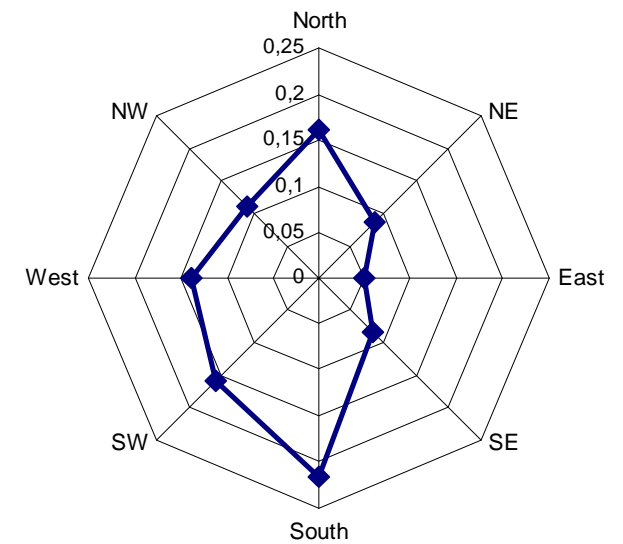
$H_s$ (m)	$T_p$ (s)																		
	2	4.5	5.5	6.5	7.5	8.5	9.5	10.5	11.5	12.5	13.5	14.5	15.5	16.5	17.5	18.5	19.5	20>	
0.25	25	14	18	14	24	17	8	9	5	0	2	3	1	1	6	2	0	7	156
0.75	79	235	408	539	496	488	426	225	111	46	16	7	6	3	2	0	2	17	3106
1.25	71	466	896	1223	1227	1219	911	626	470	252	108	70	36	12	13	2	2	49	7653
1.75	3	134	768	1342	1443	1288	1143	854	618	404	205	129	44	21	10	3	4	21	8434
	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$				
	1.4 m	5 s	0.06	1.5 m	7.5 s	0.178	1.5 m	10.3 s	0.103	1.6 m	13.1 s	0.024	1.5 m	16.1 s	0.003				
2.25	0	22	292	1013	1328	1359	1056	921	669	431	188	186	56	27	17	5	1	16	7587
2.75	1	2	79	491	1037	1276	1031	795	678	479	208	193	81	35	13	3	2	8	6412
3.25	0	1	16	189	701	1038	896	729	532	386	235	197	97	40	15	4	1	5	5082
3.75	0	0	3	57	318	814	767	562	447	371	193	168	89	50	17	3	0	3	3862
	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$				
	2.4 m	5.4 s	0.008	2.9 m	7.8 s	0.184	3 m	10.3 s	0.173	3.1 m	13.2 s	0.062	3.2 m	16 s	0.01				
4.25	1	0	1	11	130	568	731	500	341	306	146	142	67	29	25	4	3	2	3007
4.75	0	0	0	3	44	329	533	444	337	248	122	95	40	31	20	2	4	1	2253
5.25	0	0	0	1	15	112	339	396	280	195	121	98	31	26	16	5	2	0	1637
5.75	0	0	0	1	4	46	193	244	224	138	73	70	27	15	15	3	0	1	1054
				$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$				
				4.6 m	8.3 s	0.024	4.9 m	10.4 s	0.087	4.9 m	13.2 s	0.033	4.9 m	16.2 s	0.007				
6.25	0	0	0	0	0	18	91	177	156	125	65	51	20	15	7	1	2	2	730
6.75	0	0	0	0	1	1	34	108	137	106	46	40	14	5	1	2	0	0	495
7.25	0	0	0	0	0	1	11	53	93	74	50	30	14	7	8	0	1	0	342
7.75	0	0	0	0	0	0	1	29	61	63	27	19	6	3	1	1	0	1	212
							$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$				
							6.7 m	10.8 s	0.018	6.9 m	13.2 s	0.013	6.8 m	16.1 s	0.002				
8.25	0	0	0	0	0	1	0	14	31	43	24	13	6	5	1	0	0	0	138
8.75	0	0	0	0	0	0	0	8	19	27	17	8	7	1	0	0	0	0	87
9.25	0	0	0	0	0	0	0	2	5	18	13	9	2	1	1	0	0	0	51
9.75	0	0	0	0	0	0	0	1	2	7	7	4	3	3	0	0	0	0	27
							$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$				
							8.6 m	11.2 s	0.002	8.8 m	13.2 s	0.004	8.9 m	16 s	0.001				
10.25	0	0	0	0	0	0	0	0	3	3	7	4	4	1	0	0	0	0	22
10.75	0	0	0	0	0	0	0	0	0	3	1	2	0	0	0	0	0	0	6
11.25	0	0	0	0	0	0	0	0	0	4	2	1	0	0	0	0	0	0	7
11.75	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	1
							$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$				
							10.7 m	13.4 s	0.001										
12.25	0	0	0	0	0	0	0	0	0	1	0	0	1	0	0	0	0	0	2
12.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	1
13.25	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	1
13.75	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
							$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$	$H_s$	$T_p$	$P_b$				
							12.8 m	13.0 s	0.00004										



# Wave statistics

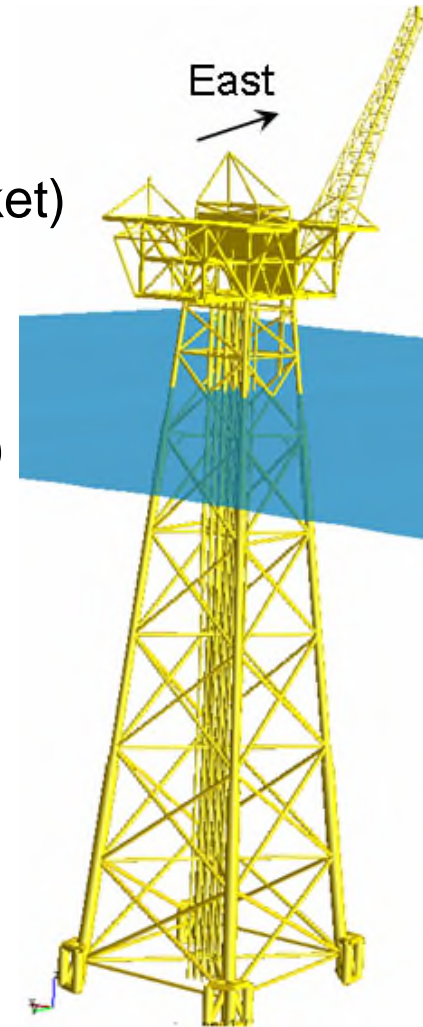
Block	$H_s$ [m]	$T_p$ [s]	$P_b$	Block	$H_s$ [m]	$T_p$ [s]	$P_b$
1	1.4	5.0	0.060	12	4.9	10.4	0.087
2	1.5	7.5	0.178	13	4.9	13.2	0.033
3	1.5	10.3	0.103	14	4.9	16.2	0.007
4	1.6	13.1	0.024	15	6.7	10.8	0.018
5	1.5	16.1	0.003	16	6.9	13.2	0.013
6	2.4	5.4	0.008	17	6.8	16.1	0.002
7	2.9	7.8	0.184	18	8.6	11.2	0.002
8	3.0	10.3	0.173	19	8.8	13.2	0.004
9	3.1	13.2	0.062	20	8.9	16.0	0.001
10	3.2	16.0	0.010	21	10.7	13.4	0.001
11	4.6	8.3	0.024	22	12.8	13.0	0.00004

The wave directional probability



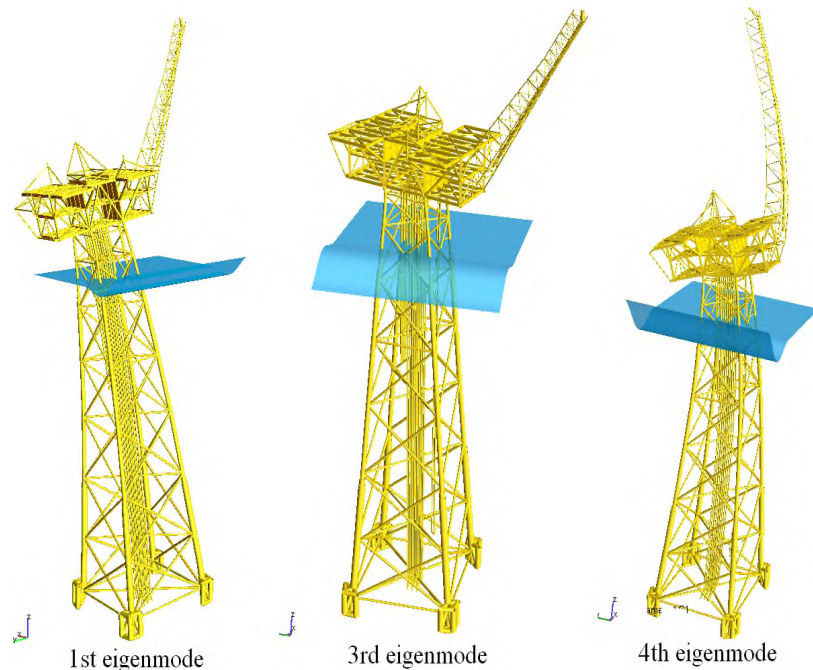
# Jacket structure modelling

- Height (jacket part): 181 m
- Water depth: 157.35 m
- Weight: 12904 tonnes (topside) and 7100 tonnes(jacket)
- Material: steel
- 1789 beam elements model
- Structure-ground connections: linear springs (Norsok)
- Marine growth
- Splash zone
- Buoyance effects
- HHT- $\alpha$  method for time integration
- SCF: Efthymiou equations



# Eigen-analysis

<i>Mode number</i>	<i>Eigen-period (s)</i>	<i>Remarks</i>
1	4.173	The first global flexural vibration along the east-west direction (Y).
2	4.115	The first global flexural vibration along the south-north direction (X).
3	2.454	The first global torsional vibration mode.
4	1.193	A global flexural vibration along the east-west direction.
5	1.189	A local vibration of centralizer on the topside.
6	1.091	A global flexural vibration along the south-north direction
7	1.018	A local vibration at the horizontal frames at EL -150 m.
8	0.990	A global flexural vibration along the south-north direction
9	0.940	A local vibration of centralizer
10	0.902	A global flexural vibration along the east-west direction





# Parameters for investigation

1.

Eigen-analysis	$\gamma$	Directional wave effects	At the dominant wave direction
	2	Yes	$N=30, 40, 60, 120, 240$
			Time step length $\Delta t=0.1$ s, 0.2 s, <b>0.25 s</b> , 0.5 s, 0.75 s
			Significant wave height
			Modal wave period
	4.1	Yes	$N=30$

2. Soil-structure flexibility

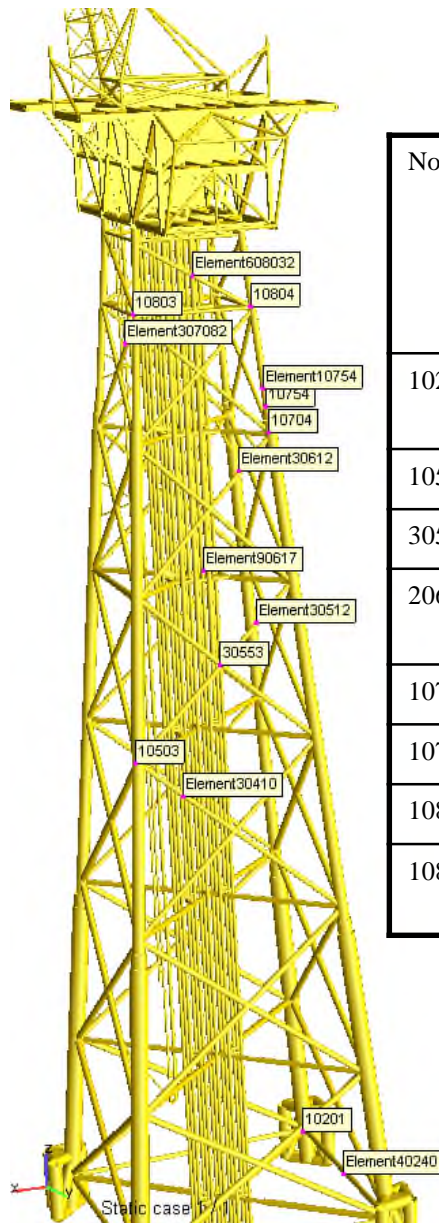
3. Structural inertia effects

4. Statistical and frequency check of the structural response

5. Gravity effects

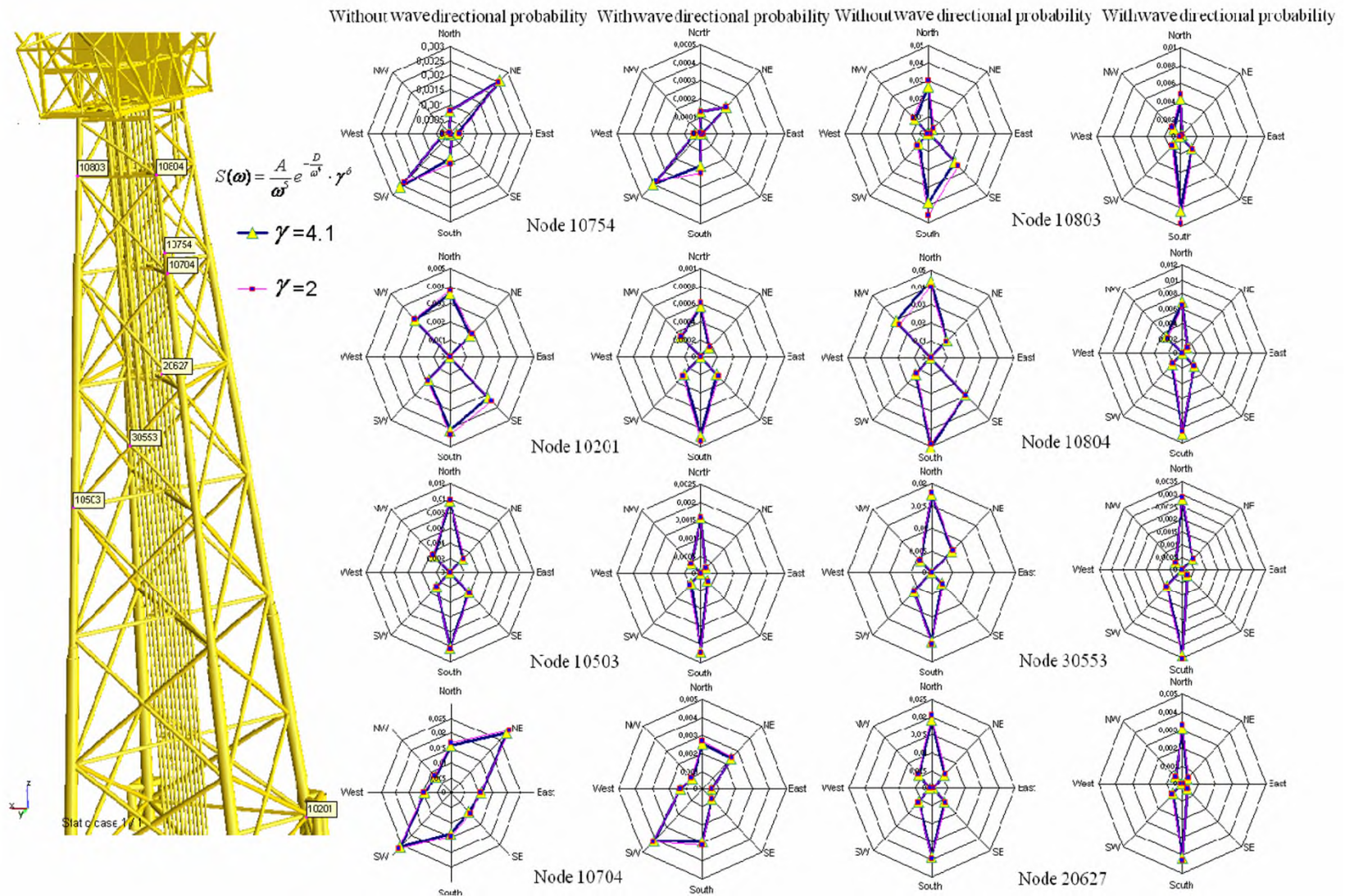
6. Natural period

# The fatigue life calculations



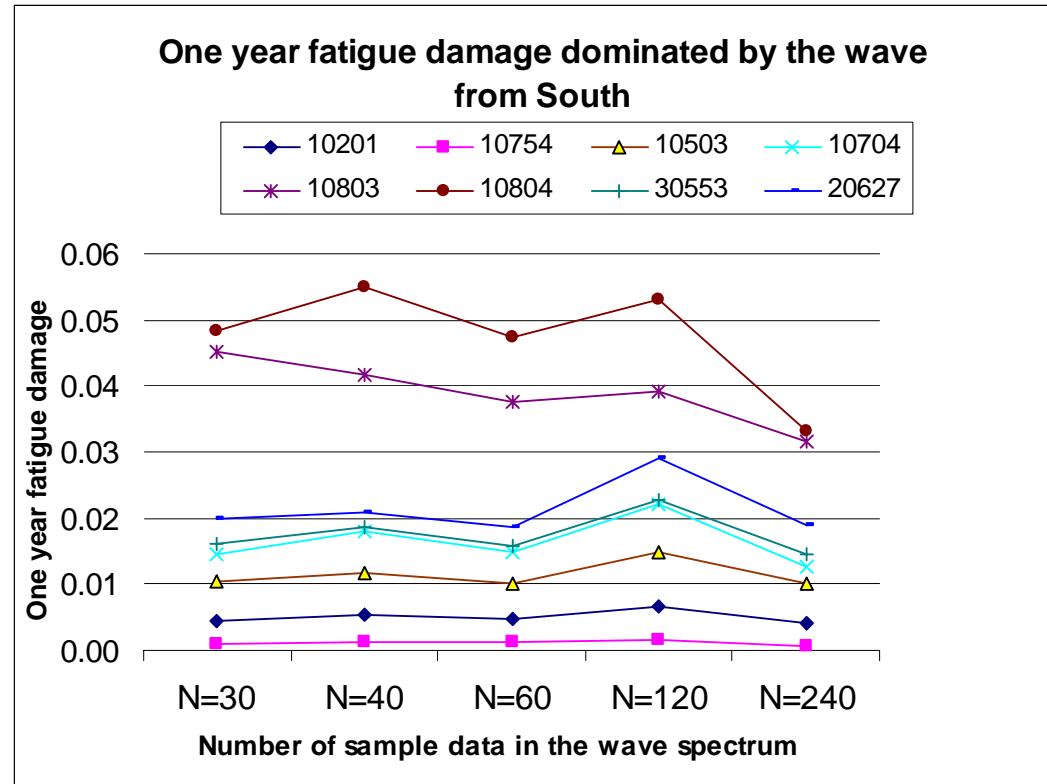
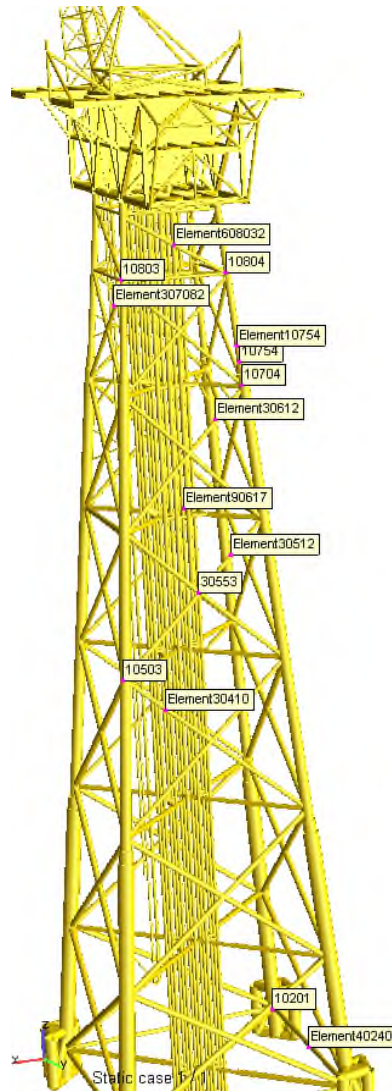
Node number	Brace (element number)	Elevation (m)	Position description	Fatigue life (years)	
				$\gamma=2$ (N=30, $\Delta t=0.25$ s )	$\gamma=4.1$ (N=30, $\Delta t=0.25$ s )
10201	40240	- 150	A leg joint at the bottom	443	468
10503	30410	- 93	A leg joint	197	202
30553	30512	- 78	A face joint	115	119
20627	90617	- 63	conductor support	101	105
10704	30612	- 36	A leg joint	73	76
10754	10754	- 35	A leg joint	1031	1047
10803	307082	- 11	A leg joint	52	60
10804	608032	- 11	A leg joint	40	37

# Influence from the wave enhancement and the wave directions



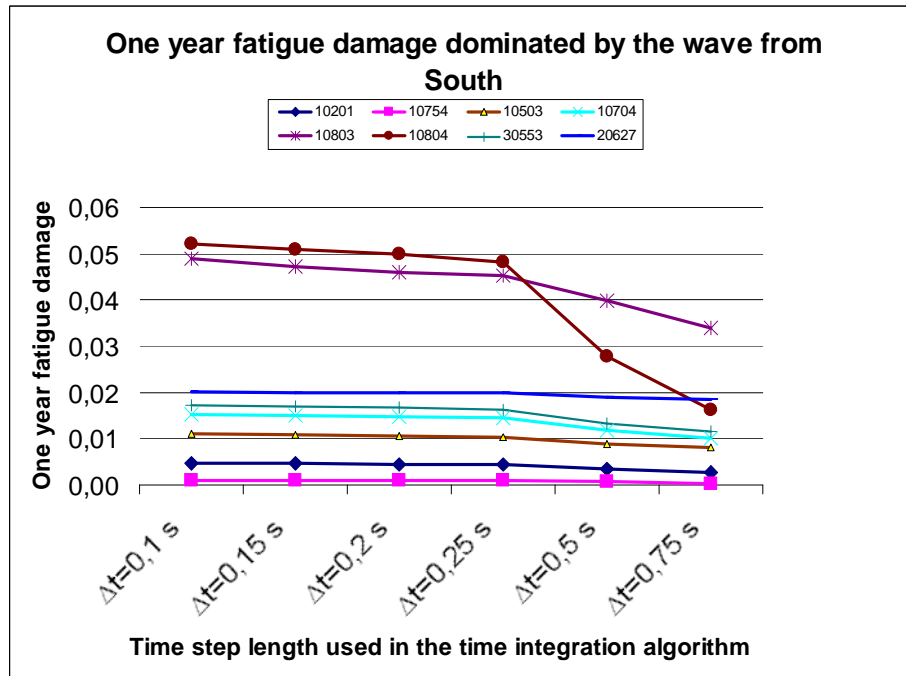


# Influence from the number of sample inputs $N$



- The trend of the variation of the fatigue damage due to the variation of the sample inputs  $N$  can not be identified.
- The ratio of total computation time for  $N= 30, 40, 60, 120$ , and  $240$  is  $1 : 1.07 : 1.18 : 1.47 : 2.09$ .

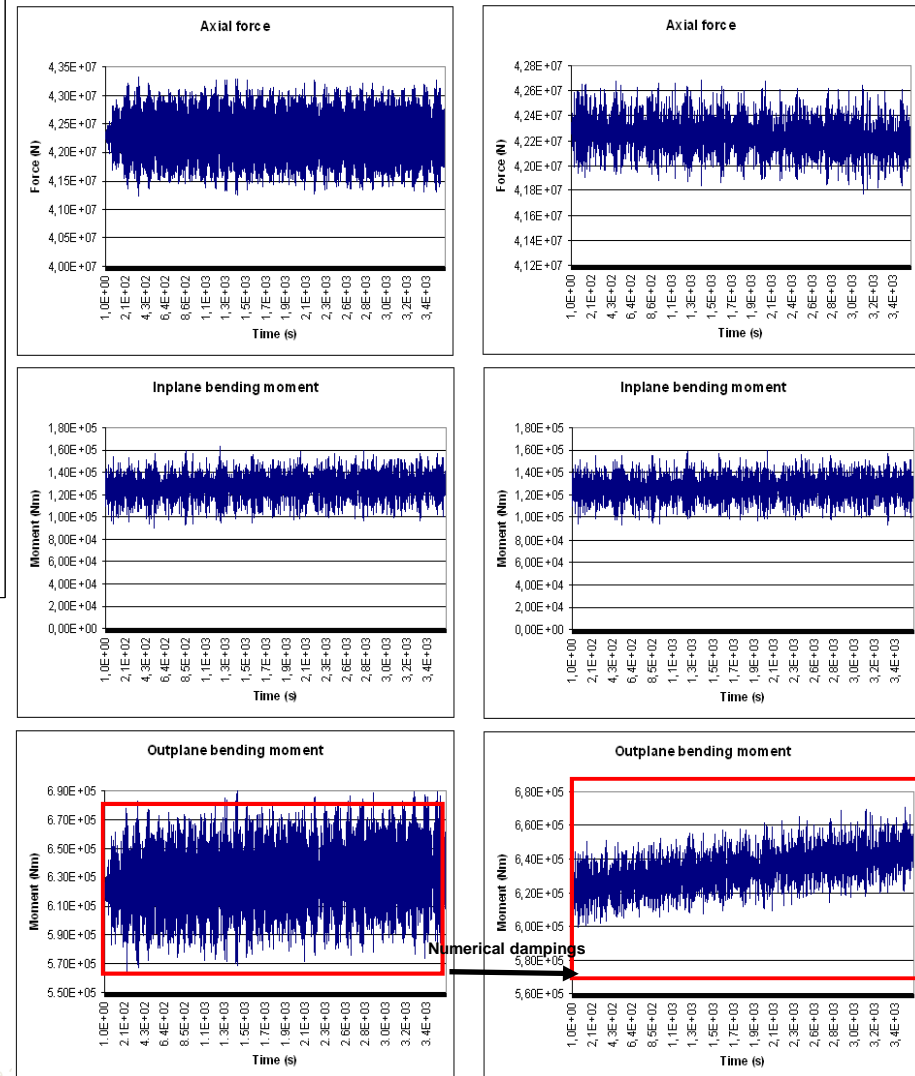
# Influence from the time step length



Joint 10754,  $H_s=2.4$  m  $T_p=5.4$  s

$\Delta t = 0.25$  s

$\Delta t = 0.75$  s

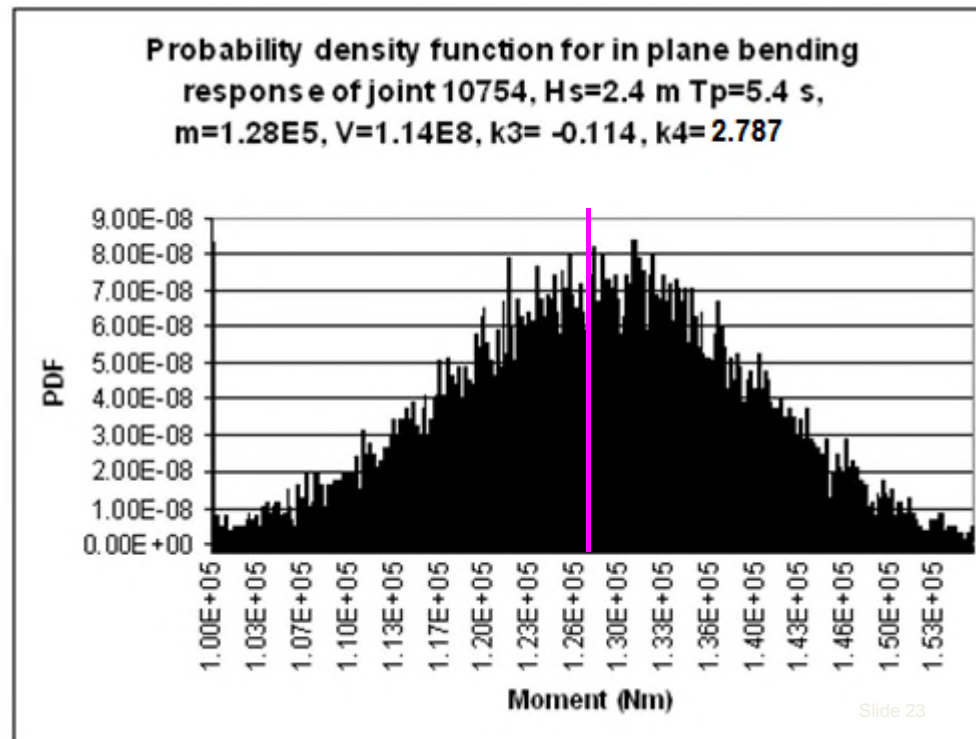


”Rule of thumb” for deciding time step:

Fixed offshore structures:  $10\% \times \min(T_{sm}, T_{Lm})$

# Statistical check of the structural response

	$H_s=2.4$ m $T_p=5.4$ s (block 6)			$H_s=4.6$ m $T_p=8.3$ s (block 11)			$H_s=6.7$ m $T_p=10.8$ s (block 15)		
	Axial force	In plane bending	Outplane bending	Axial force	In plane bending	Outplane bending	Axial force	In plane bending	Outplane bending
V(resp)	2.00E+11	1.14E+08	5.73E+08	2.98E+11	6.50E+08	6.98E+08	1.67E+11	1.36E+09	6.69E+08
K3 (偏度)	-0.00125	-0.1136	0.03366	-0.0158	-0.0493	0.044997	-0.14341	-0.17397	0.024856
K4(峰度)	1.88289	2.78655	2.10527	2.00316	3.944466	2.27622	4.152773	4.223641	4.675471



- Slight nonGaussian distribution is observed due to the nonlinear effects, dampings and numerical noises.
- The fatigue damage is directly related to the variance of the structural response.

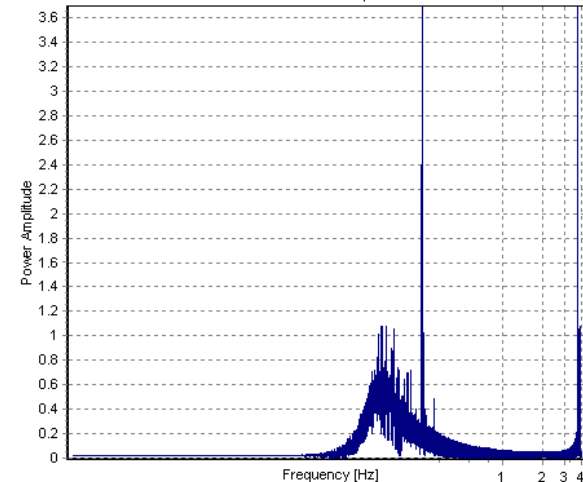
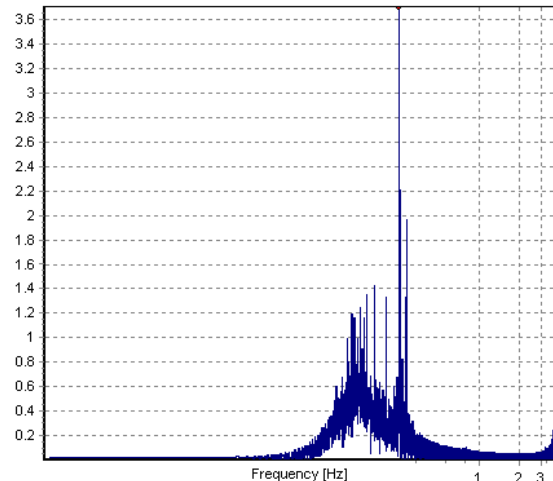
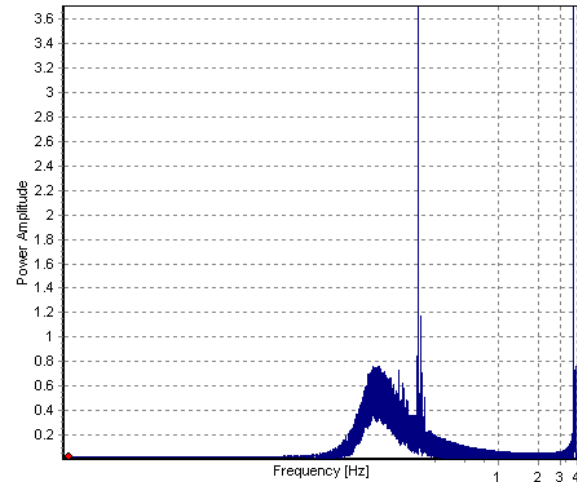
# Check in the frequency windows

Node 10754

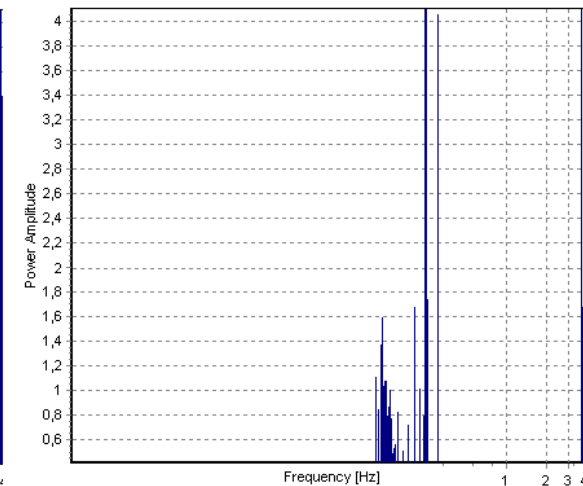
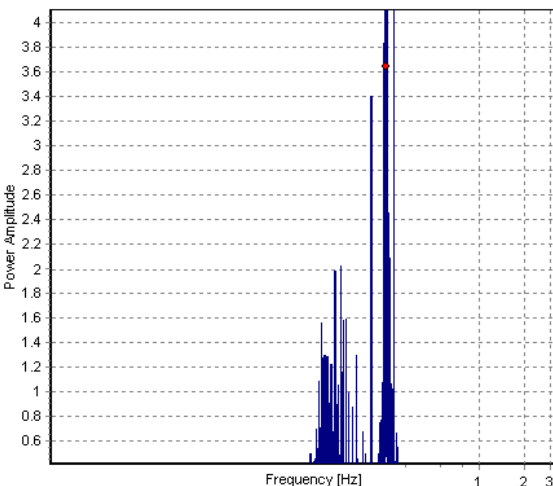
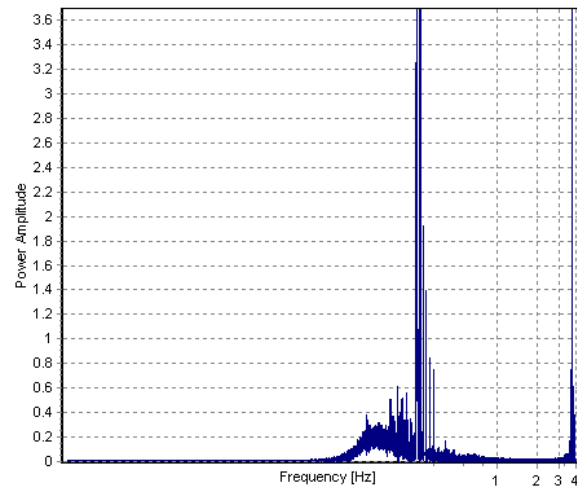
$H_s=2.4$  m  $T_p=5.4$  s

$H_s=6.7$  m  $T_p=10.8$  s

$H_s=4.6$  m  $T_p=8.3$  s



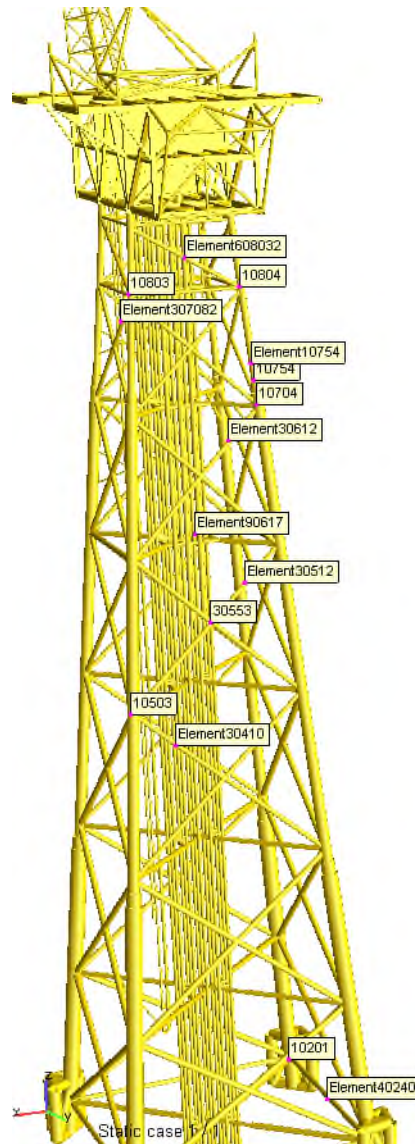
Axial force



Outplane bending moment



# Influence from the soil-structure flexibility and the inertia effects



Joint number	Elevation (m)	Fatigue life (years)		
		Consider both the soil-structure flexibility and the inertia effects	The bottom of the jacket is fully fixed	Ignoring the inertia effects of the structure
10201	- 150	711	NA	3849
10503	- 93	283	335	554
30553	- 78	162	178	392
20627	- 63	155	166	187
10704	- 36	94	94	131
10754	- 35	2335	1540	$2.47 \times 10^6$
10803	- 11	55	56	74
10804	- 11	65	42	119947

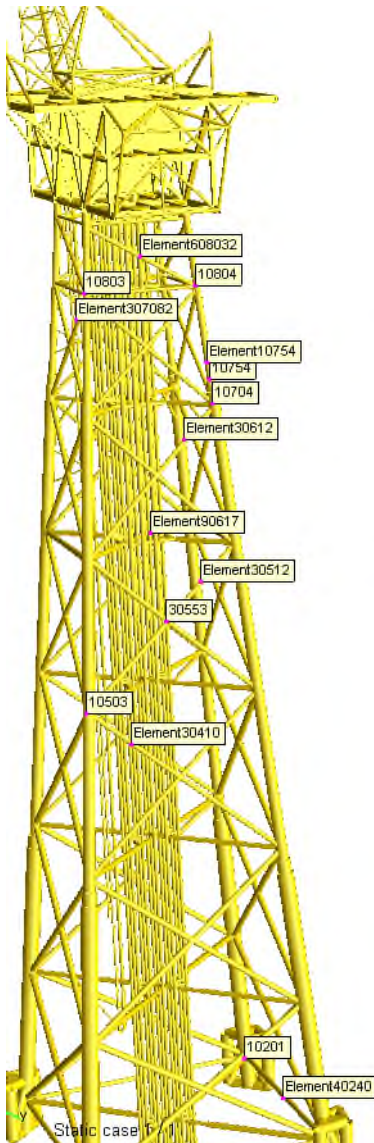
- For a first estimation, the structure-soil connection can be modelled as rigid for soft jacket structures
- The inertia effects are significant on the fatigue damage

## Influence from the selfweight induced load – calculated eigenfrequency

- Stress stiffening effects

Mode number	Eigenperiod (s)		
	With gravity	Without gravity	Diff. (%)
1	4.173	4.120	1.3
2	4.115	4.065	1.2
3	2.453	2.442	0.4
4	1.203	1.194	0.7
5	1.193	1.187	0.5
	NA	1.152	NA
6	1.090	1.086	0.4
7	1.014	NA	NA
8	0.990	0.987	0.3
9	0.914	0.939	2.7
10	0.902	0.901	0.1

# Influence from the gravity – results



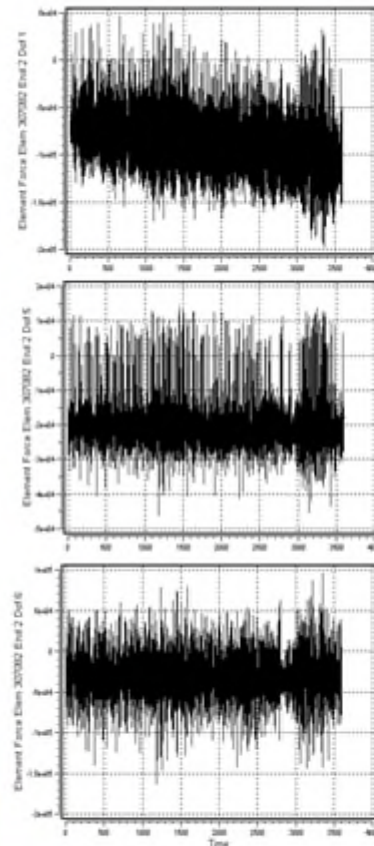
Node number	Position description	Fatigue life (years)		
		With selfweight	Without Selfweight	Error
10201	A leg joint at the bottom	443	525	19%
10503	A leg joint	197	185	-6%
30553	A face joint	115	110	-4%
20627	A conductor support	101	117	16%
10704	A leg joint	73	70	-4%
10754	A leg joint	1031	1015	-2%
10803	A leg joint	52	58.3	12%
10804	A leg joint	40	41	3%

- The ignorance of the platform's selfweight is likely to underestimate the the fatigue damage to some extent.

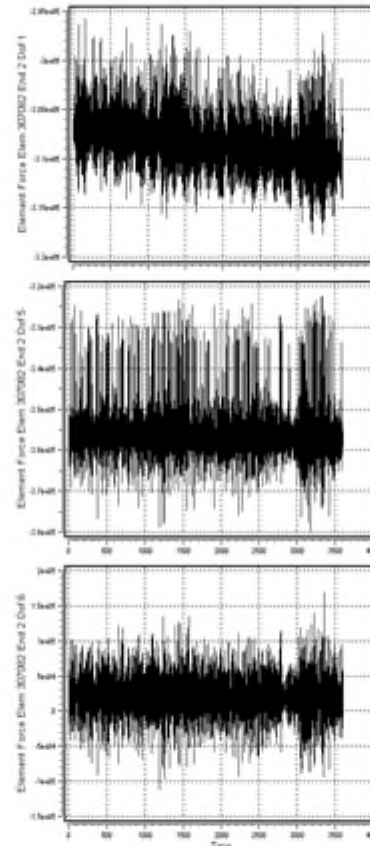
# Influence from the selfweight induced load – response time series

Mild sea state:  $H_s=2.9\text{m}$ ,  $T_p=7.8\text{s}$

High sea state:  $H_s=8.8\text{m}$ ,  $T_p=13.2\text{s}$

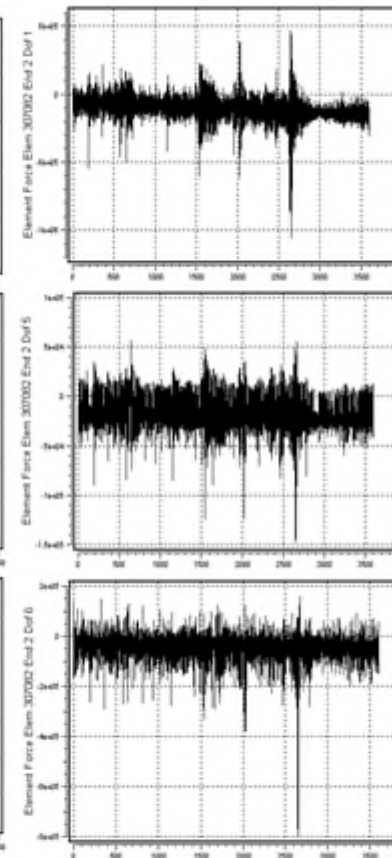


Without gravity loads

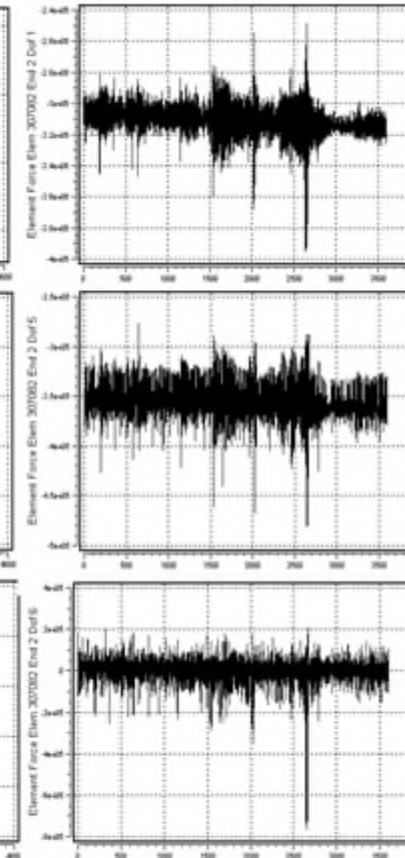


With gravity loads

for sea state block 7 ( $H_s=2.9\text{m}$ ,  $T_p=7.8\text{s}$ )



Without gravity loads

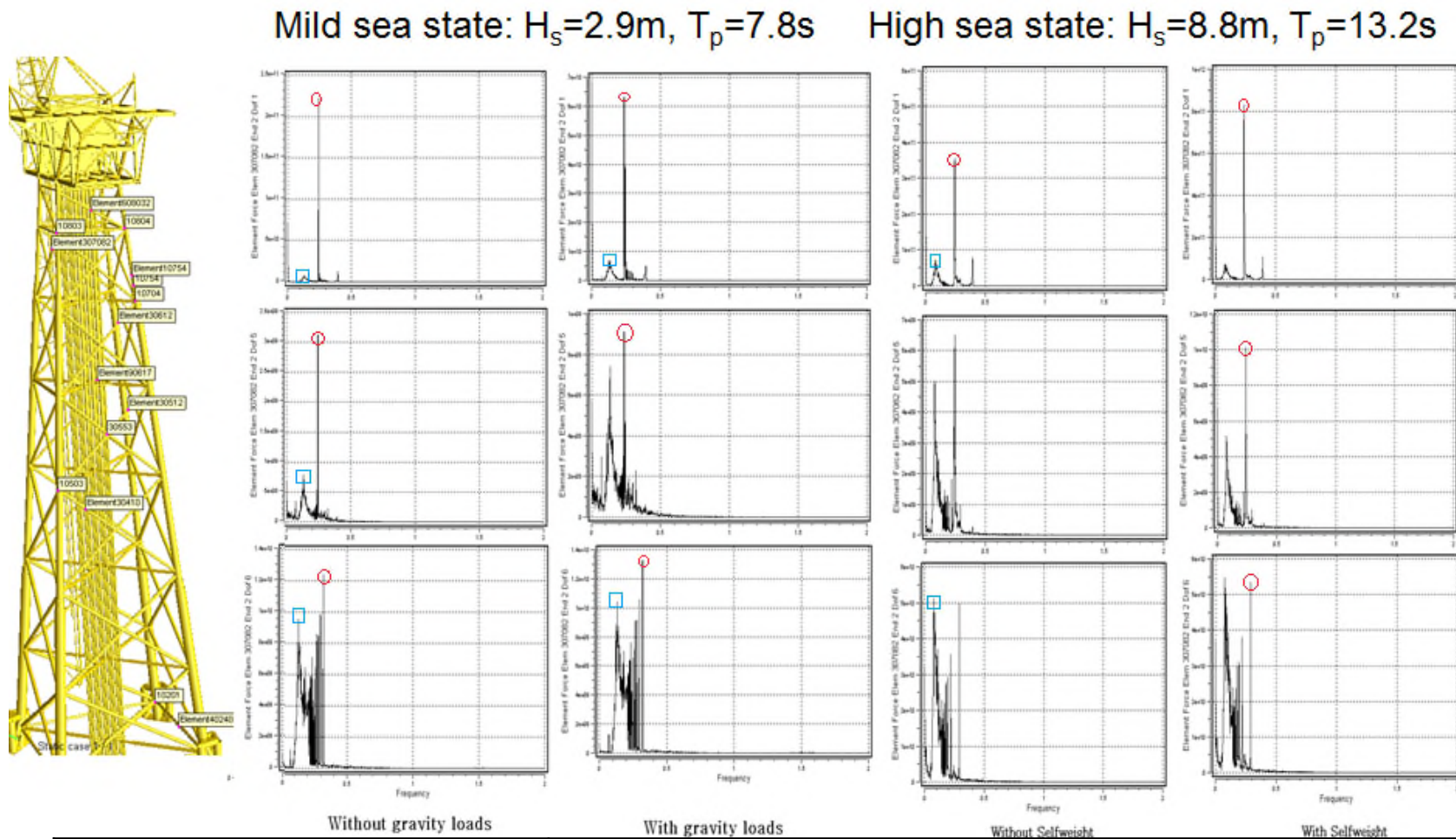


With gravity loads

for sea state block 19 ( $H_s=8.8\text{m}$ ,  $T_p=13.2\text{s}$ )



## Influence from the selfweight induced load – responses in frequency domain (joint 10803)

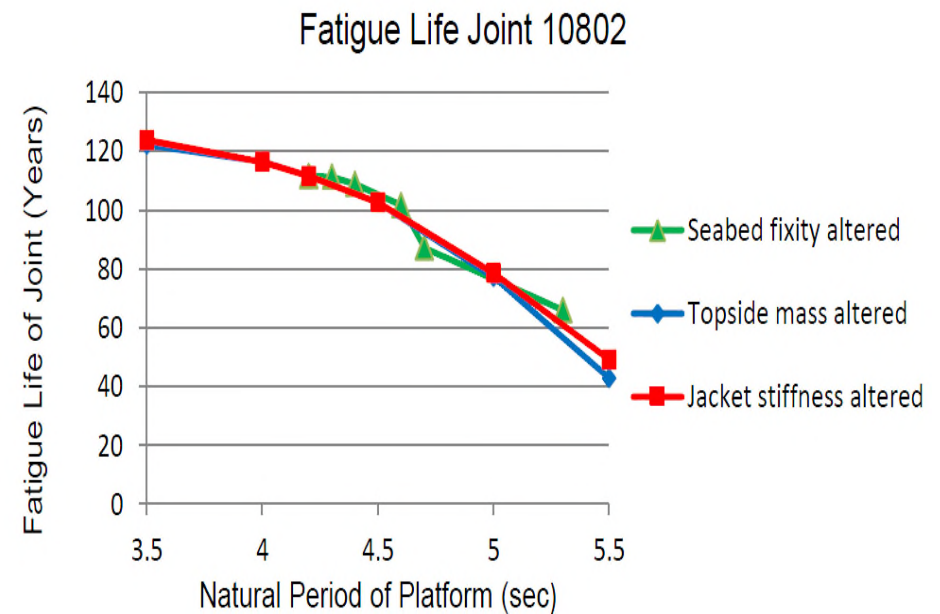
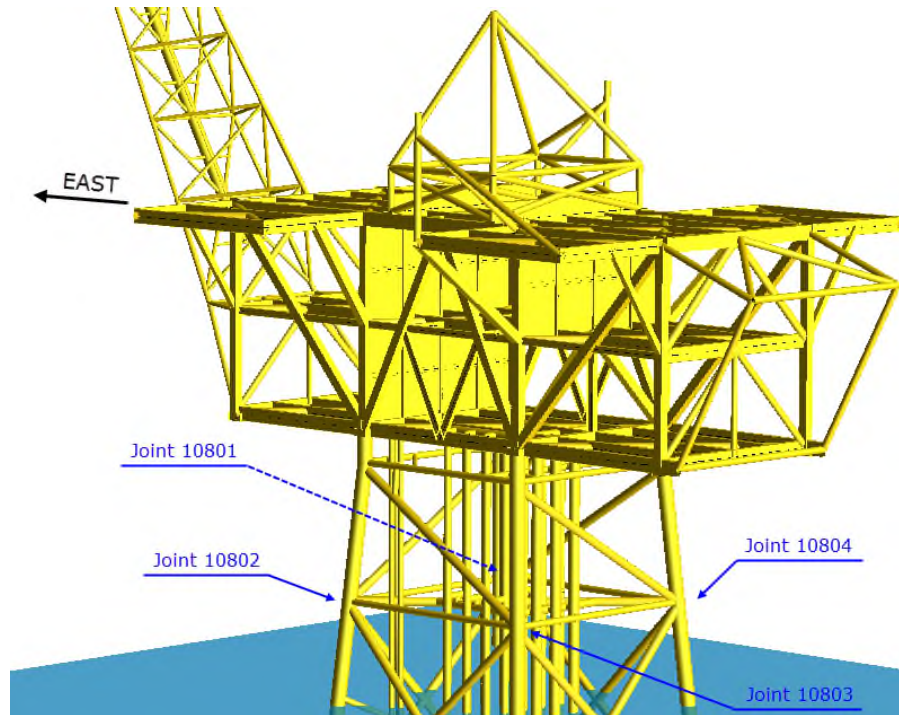


Gravity loads effects	Low Sea state	High Sea State
Axial force	Decrease	Significantly increase
In-plane bending	Decrease	Significantly increase
Out-of-plane bending	Increase	Slightly increase

## Influence from the selfweight induced load – responses statistics

Joint 10803		With gravity load			Without gravity load		
Sea State	Items	Axial force (N)	In plane bending (N·m)	Outplane Bending (N·m)	Axial force (N)	In plane bending (N·m)	Outplane Bending (N·m)
Hs=2.9m, Tp=7.8s	m	-3.08E+06	-3.55E+05	2.03E+04	-8.35E+04	-1.89E+04	-3.18E+04
	k2	8.35E+08	5.89E+07	8.75E+08	1.22E+09	6.92E+07	8.17E+08
	k3	3.90E-01	1.35E+00	-2.08E-01	2.46E-01	1.28E+00	-2.70E-01
	k4	7.41E-01	5.89E+00	9.49E-01	2.95E+00	5.37E+00	9.63E-01
Hs=8.8m, Tp=13.2s	m	-3.11E+06	-3.53E+05	-1.16E+03	-1.05E+05	-1.55E+04	-4.81E+04
	k2	9.18E+09	3.33E+08	3.59E+09	7.58E+09	3.11E+08	3.37E+09
	k3	-5.59E-01	-1.77E-01	-2.24E+00	-7.76E-01	-2.08E-01	-2.33E+00
	k <sub>4</sub>	8.47E+00	4.60E+00	4.49E+01	11.44E+00	4.72E+00	4.59E+01

# Wave Induced Fatigue – Trend of fatigue life estimate varying with natural frequency



Source: Aker Solutions and City University, London



# Contributions and conclusions

- Present a practical procedure for calculating fatigue: capable of capturing nonlinear and non-Gaussian phenomenon.
- Wave spectrum inputs are efficient: fatigue damage is not sensitive to the number of sample frequency points  $N$ .
- Fatigue damage is not sensitive to the variation of wave peak enhancement.
- Suggestions on how to decide a decent time step length.
- Slight non-Gaussian response is observed for even inertia dominated response.
- Self-vibration may in a lot of case contribute to the fatigue significantly.
- For fixed offshore structures: fatigue damage is highly influenced by the waves with low modal period.
- Hydrodynamic coefficients defined in Norsok 2007 leads to significant higher fatigue life for inertia dominated offshore structures.
- Variation of drag force coefficient has less influence on the fatigue damage than the inertia coefficient.
- Soil-structure flexibility variation does not significantly influence the critical fatigue damage for the target structure.
- The structural inertia effects are rather significant.
- Ignoring the selfweight of the platform is unconservative to some extent.

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