

Homework 5: Problem Solving

Mathematic: Optimization Model

Decision Variable

X_1 : The number of vanilla ice cream (boxes)

X_2 : The number of strawberry ice cream (boxes)

Objective

Max profit: $2X_1 + 3X_2$

Constraints

1. Fresh milk: $0.5X_1 + 0.2X_2 \leq 10$ (1)
2. Doll: $X_1 + X_2 \leq 30$ (2)
3. $X_1, X_2 \geq 0$

Result

- Find the proper number of vanilla ice cream and strawberry ice cream (box)

$$(1)*2: \quad X_1 + 0.4X_2 = 20 \quad (3)$$

$$(2)-(3) \quad 0.6X_2 = 10$$

$$X_2 = 16.67$$

$$\text{Plug } X_2 \text{ in (2)} \quad X_1 + 16.67 = 30$$

$$X_1 = 13.33$$

So, the proper number of vanilla ice cream (X_1) is equal to 13 boxes and the proper number of strawberry ice cream (X_2) is equal to 17 boxes.

- Find the maximum profit

Let $X_1 = 13$ and $X_2 = 17$

$$\text{Max profit} = 2(13) + 3(17)$$

$$\text{Max profit} = 77$$

As a result, we will produce vanilla ice cream in 13 boxes and produce strawberry ice cream in 17 boxes to get a maximum profit of \$77.