

Homework 5: Problem Solving

Mathematic: Optimization Model

Decision Variable

X_1 : The number of vanilla ice cream (boxes)

X_2 : The number of strawberry ice cream (boxes)

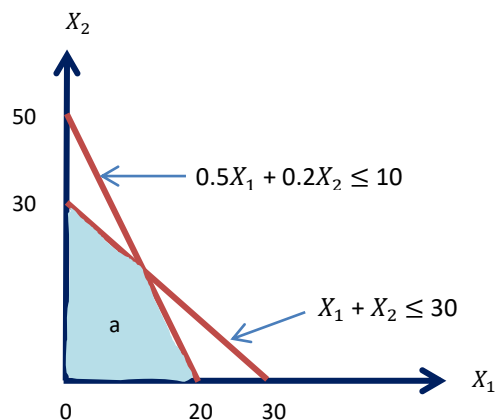
Objective

Max profit: $2X_1 + 3X_2$

Constraints

1. Fresh milk: $0.5X_1 + 0.2X_2 \leq 10$ (1)
2. Doll: $X_1 + X_2 \leq 30$ (2)
3. $X_1, X_2 \geq 0$

Result



- Find the maximum profit from the possible values of X_1 and X_2

Way 1: $X_1 = 0$ and $X_2 = 0$

Profit = $2(0) + 3(0)$

Profit = 0

Way 2: $X_1 = 0$ and $X_2 = 30$

Profit = $2(0) + 3(30)$

Profit = 90

Way 3: $X_1 = 20$ and $X_2 = 0$

Profit = $2(20) + 3(0)$

Profit = 40

Way 4: $X_1 = 13$ and $X_2 = 17$

$$(1)*2: \quad X_1 + 0.4X_2 = 20 \quad (3)$$

$$(2)-(3) \quad 0.6X_2 = 10$$

$$X_2 = 16.67$$

$$\text{Plug } X_2 \text{ in (2)} \quad X_1 + 16.67 = 30$$

$$X_1 = 13.33$$

$$\text{Profit} = 2(13) + 3(17)$$

$$\text{Profit} = 77$$

As a result, way 2 get the optimize profit of \$90. So, we will produce only strawberry ice cream in 30 boxes to get a maximum profit.