

Homework 5: Problem Solving

Mathematic: Optimization Model

Decision Variable

X_1 : The number of vanilla ice cream (boxes)

X_2 : The number of strawberry ice cream (boxes)

Objective:

Max profit: $C = 2X_1 + 3X_2$

Constraints

1. Fresh milk: $0.5X_1 + 0.2X_2 \leq 10$ (1)
2. Doll: $X_1 + X_2 \leq 30$ (2)
3. $X_1, X_2 \geq 0$

So, I converse all problem solving process to matrix array in python

Let A and b are constraints

obj is objective function

X is the number of each ice cream (boxes)

$$A = \begin{bmatrix} 0.5 & 0.2 \\ 1. & 1. \end{bmatrix}$$

$$b = \begin{bmatrix} 10. \\ 30. \end{bmatrix}$$

$$\text{obj} = [2. \quad 3.]$$

$$X = [X_1 \quad X_2]$$

Objective: $\text{obj} * X$

Constraints: $AX = b$

Result

To find maximize optimization, I use **"from scipy.optimize import linprog"** but `linprog()` solves only minimization (not maximization) problems. So, I modify problem before starting optimization:

Objective will be: $C = -2X_1 - 3X_2$ and $\text{obj} = [-2. \ -3.]$

Finally, I solve the problem of interest and the result as follows:

```
con: array([], dtype=float64)
fun: -90.0
message: 'Optimization terminated
successfully.'
nit: 1
slack: array([4., 0.])
status: 0
success: True
x: array([ 0., 30.])
```

The attributes of interest are

`fun`: is the objective function value at the optimum. (minimum: -90.0)

`x`: is a NumPy array holding the optimal values of the decision variables. ($X_1=0.$, $X_2=30.$)

As a result, I will produce only strawberry ice cream (X_2) in 30 boxes to get a maximum profit of \$90.