

Summary: Lecture 7

Summary for the chapters 9.1 and 9.2. [1]

NP-Completeness

NP

Class of languages decided by nondeterministic Turing machines in polynomial time.

NP-completeness:

- easiest problems among those we do not know how to solve efficiently
- if $P \neq NP$ can be proven: exact border of efficient solvability is found
- best bet for proving $P=NP$: show that some NP-complete problem is P
- Until then, the NP-complete problems are the least likely ones in NP to be efficiently solved

Language L

$L = \{x : (x, y) \in R \text{ for some } y\}$

L gets an input x and finds a y with $((x, y) \in R$ and the relation $R \subseteq \Sigma^* \times \Sigma^*$.

Polynomially decidable:

- R is polynomially decidable if there is a deterministic Turing machine deciding the language L in polynomial time
- then the relation R (not the language L) is polynomially decidable

Polynomially balanced:

- R is polynomially balanced if $(x, y) \in R$ implies $|y| \leq |x|^k$ for some $k \geq 1$
→ length of the second component is bounded by a polynomial in the length of the first
- then the relation R (not the language L) is polynomially balanced

TODO

Questions:

Typical problems in NP

Title

Content

TODO

Questions:

3Sat is NP-complete

Title

Content

TODO

Questions:

2Sat in P (graph construction)

Title
Content

TODO

Questions:

2Sat in NL

Title
Content

TODO

Questions:

MaxSat is NP-complete

Title
Content

TODO

Questions:

NaeSat is NP-complete

Title
Content

TODO

Questions:

References

- [1] Christos H. Papadimitriou. *Computational Complexity*. Addison-Wesley Publishing Company, 1994.