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Summary: Lecture 5

Summary for the chapters X and X. [2]

Reduction

Examples of NP-problems:

- Travelling Salesman Problem
- SATISFIABLE
- REACHBILITY (in P)
- CIRCUIT VALUE (in P)

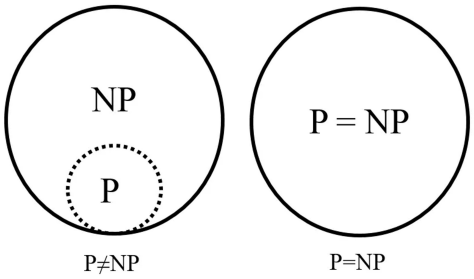

Figure 1: P and NP sets [1]

- reduction: a problem is at least as hard as another
- problem A is at least as hard as problem B if B reduces to A
- B reduces to A if there is a transformation R
  - R produces for every input x of B an equivalent input $R(x)$ of A
  - the answer of input x on B and input $R(x)$ on A have to be the same

Reduction

Problem A is at least as hard as problem B if B reduces to A.

TODO
Questions:

Reduction HAMILTONIAN PATH to SATISFIABLE

- instance: Graph G
  question: Is there a path in G that visits each node one?
- log space reduction from HP to S
- demonstrates HP not significantly harder that SAT
- write a logical formular that only becomes true when it is HP
- 4, 3, 1, 2 as path
  $x_{1,4} = T, x_{2,3} = T, x_{3,1} = T, x_{4,2} = T,$
- slide is not quite correct
- $(notx_{1,1}ornotx_{2,1})and(notx_{1,1}ornotx_{3,1})$
  $and(notx_{1,1}ornotx_{4,1})and(notx_{2,1}ornotx_{3,1})$
  $and(notx_{2,1}ornotx_{4,1})and(notx_{3,1}ornotx_{4,1})and...$
  first index: step, second: node

TODO
Questions:

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Boolean Circuits

TODO
Questions:

Reduction REACHABILITY PATH to CIRCUIT VALUE

TODO
Questions:

Further examples

TODO
Questions:

Closedness under Composition

TODO
Questions:

References

[1] *Image source: P-NP sets.* `https://www.techno-science.net/actualite/np-conjecture-000-000-partie-denouee-N21607.html`.

[2] Christos H. Papadimitriou. *Computational Complexity*. Addison-Wesley Publishing Company, 1994.