

Summary: Lecture 3

Summary for the chapters X and X . [1]

Notes in the lecture:

Basic relations between complexity classes

Deterministic space includes nondeterministic time:

$\text{NTIME}(f(n)) \subseteq \text{SPACE}(f(n)^2)$

d choices in every step (in TM): $1, \dots, d$

fill something with 1 in first step

second step: simulate nondeterministic TM

pick something and simulate it? Until we get to d because we increment by 1 in each step.

The reachability method:

graphs/graph edges are constructed

M empties the tape and puts all the heads to the start

there is only a single node that is accepting

Savitch's theorem:

complexity function is at least $\log n$

we are doing an intuitive sketch now

this theorem grabs some internal node k , check recursively if there is a path from 1 to k and from k to n

test if path from 1 to k with picking a midpoint again...

we can have $\log n$ many segments to work on

$\text{PATH}(\text{startnode}, \text{endnode}, \text{pathlength})$ checks if there is a path from startnode to endnode with the length pathlength (?)

References

- [1] Christos H. Papadimitriou. *Computational Complexity*. Addison-Wesley Publishing Company, 1994.