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## The Experiment Report of Machine Learning

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**SCHOOL: SCHOOL OF SOFTWARE ENGINEERING**

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# Recommender System Based on Matrix Decomposition

**Abstract—** In this experiment, we implement the matrix decomposition based recommender system and conduct the experiment on the Movielens-100k dataset. According to the result, we noticed the importance of proper parameter setting, especially the parameter  $k$ . After the experiment, we have a better comprehension on recommender system and SGD algorithm.

## I. INTRODUCTION

In recent years, recommendation system has been widely used. The system recommend items for its latent customer based on the previous purchase record that the customer or the similar customer had.

However, we haven't realized a recommendation system in machine learning class. In order to explore the construction of recommended system, understand the principle of matrix decomposition, getting us familiar to the use of SGD, and construct a recommendation system under small-scale dataset, we conduct the recommender system experiment.

In this experiment, we implement the matrix decomposition based recommender system on MovieLens-100k dataset, achieving a satisfying result.

## II. METHODS AND THEORY

Recommender System applies statistical and knowledge discovery techniques to the problem of making product recommendations.

The Matrix Factorization is a model based collaborative filtering algorithm. It is based on a rating matrix, with sparse ratings form  $m$  users to  $n$  items.

It assume rating matrix  $R$  can be factorized into the multiplication of two low-rank feature matrices  $P$  and  $Q$ . We use SGD to get the proper  $P$  and  $Q$  in order to fill the matrix. The objective function of SGD is in figure 1, where  $r$  denotes the actual rating of user  $u$  for item  $i$ ,  $\Omega$  denotes the set of observed samples from rating matrix  $R$ ,  $\lambda_p$  and  $\lambda_q$  are regularization parameters to avoid overfitting.

$$\mathcal{L} = \sum_{u,i \in \Omega} (r_{u,i} - \mathbf{p}_u^\top \mathbf{q}_i)^2 + \lambda_p \|\mathbf{p}_u\|^2 + \lambda_q \|\mathbf{q}_i\|^2$$

Figure 1 The objective function of SGD

In order to apply SGD to obtain the proper  $P$  and  $Q$ , we calculate the gradient of  $P$  and  $Q$ . The formula is in figure 2.

$$\begin{aligned} \frac{\partial \mathcal{L}}{\partial \mathbf{p}_u} &= E_{u,i}(-\mathbf{q}_i) + \lambda_p \mathbf{p}_u \\ \frac{\partial \mathcal{L}}{\partial \mathbf{q}_i} &= E_{u,i}(-\mathbf{p}_u) + \lambda_q \mathbf{q}_i \end{aligned}$$

Figure 2 The gradient of  $P$  and  $Q$

### Algorithm 1 SGD

- 1: **Require** feature matrices  $P$ ,  $Q$ , observed set  $\Omega$ , regularization parameters  $\lambda_p$ ,  $\lambda_q$  and learning rate  $\alpha$ .
- 2: **Randomly** select an observed sample  $r_{u,i}$  from observed set  $\Omega$ .
- 3: Calculate the **gradient** w.r.t to the objective function:
 
$$\begin{aligned} E_{u,i} &= r_{u,i} - \mathbf{p}_u^\top \mathbf{q}_i \\ \frac{\partial \mathcal{L}}{\partial \mathbf{p}_u} &= E_{u,i}(-\mathbf{q}_i) + \lambda_p \mathbf{p}_u \\ \frac{\partial \mathcal{L}}{\partial \mathbf{q}_i} &= E_{u,i}(-\mathbf{p}_u) + \lambda_q \mathbf{q}_i \end{aligned}$$
- 4: **Update** the feature matrices  $P$  and  $Q$  with learning rate  $\alpha$  and gradient:
 
$$\begin{aligned} \mathbf{p}_u &= \mathbf{p}_u + \alpha(E_{u,i} \mathbf{q}_i - \lambda_p \mathbf{p}_u) \\ \mathbf{q}_i &= \mathbf{q}_i + \alpha(E_{u,i} \mathbf{p}_u - \lambda_q \mathbf{q}_i) \end{aligned}$$
- 5: **Repeat** the above processes until **convergence**.

## III. EXPERIMENT

### A. Dataset

We implement the experiment on Movielens-100k dataset. It consists 10000 comments from 943 users out of 1682 movies. We use the `u1.data` and `u1.test` for the splitting of training set and test set.

### B. Result

We implement the matrix decomposition based recommender system using python3 and anaconda toolkit. We set the regularization parameters to 0.3, set the learning Rate to 0.01, set  $K$  to 100 and make 2000 iterations. According to the experiment result, we can see that during the iterations, the loss value drops significantly.

We also noticed that different  $k$  value may lead to different

result. In this experiment, we set  $K$  to 10, the loss value drops relatively smaller than when  $k$  equals to 100. However, when we set  $k$  to 1000, the experiment failed.

We also realized that the result also relies on the initial value of  $P$  and  $Q$  matrix. If the initial value is too large, there may be an overflow value during the experiment. So we set the initial value to a value that between 0 and 1.

After the experiment, we are more interested in recommender system, and we will read more paper about this area.

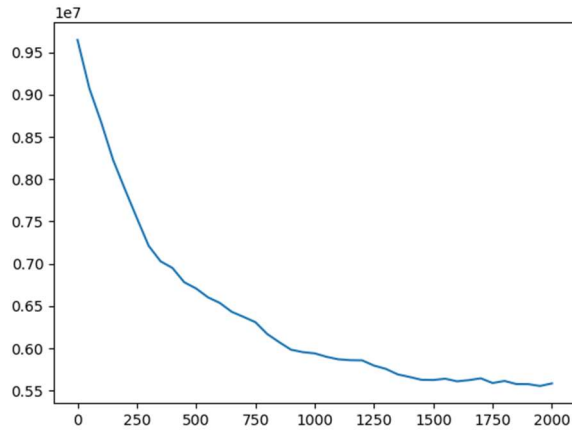


Figure 3 experiment result with  $k = 100$

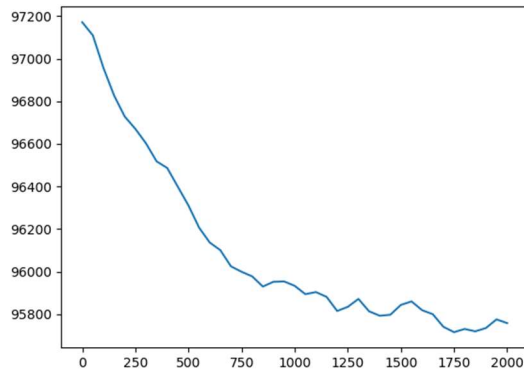


Figure 4 experiment result with  $k = 10$

#### IV. CONCLUSION

In this experiment, we implement the recommender system based on matrix decomposition. After this experiment, we have got a deeper comprehension to recommender system.

We also get a deeper knowledge on SGD algorithm and its application.

We realize the important of setting parameters one more time. Meanwhile, we realize the role of parameter  $k$  in this algorithm.