

## You try it

Random variables  $Y_1, Y_2, \dots, Y_n$  are iid  $U(0,1)$  random variables. Find the distribution of  $Y_{(1)} = \min(Y_1, Y_2, \dots, Y_n)$ . Does it have a "named" distribution?

pdf of  $Y_{(1)}$  is  $n(1 - F(y))^{n-1} f(y)$

$$f(y) = 1 \quad 0 < y < 1 \quad (\text{D. o.w.})$$

$$F(y) = \int_0^y 1 dt = t|_0^y = y$$

$$F(y) = \begin{cases} 0 & y \leq 0 \\ y & 0 < y \leq 1 \\ 1 & y > 1 \end{cases}$$

pdf of  $Y_{(1)}$  is  $n(1 - y)^{n-1}, 0 < y < 1$

beta pdf  $y^{\alpha-1} (1-y)^{\beta-1} \times \text{constant}$

$$\alpha = 1, \beta = n$$

$$\boxed{\text{beta}(1, n)}$$