

	Shankar's (lindbladInit)	Mine (lindbladInit_for-DMD-4.4)
Output data files (required by later real-time dynamics)	A single file ldbd.dat	Multi files in the folder ./ldbd_data, each storing one kind of quantity (additionally ImSigma_ePh)
Output electron- phonon quantities	$G^- = g^- \sqrt{\delta}$ stored in sparse form	E-ph-related matrices for both Lindblad and conventional equation. For Lindblad, $P_{1234}^I = \sum_{\pm\lambda} G_{13}^{\pm} G_{24}^{\pm,*} n^{\pm}$ $P_{1234}^{II} = \sum_{\pm\lambda} G_{31}^{\pm} G_{42}^{\pm,*} n^{\mp}$ For conventional, $P_{1234}^I = \sum_{\pm\lambda} g_{13}^{\pm} g_{24}^{\pm,*} n^{\pm}$ $P_{1234}^{II} = \sum_{\pm\lambda} g_{31}^{\pm} g_{42}^{\pm,*} n^{\mp}$ $G = g\delta$ of a k pair (ik,jk) with ik <= jk ($P^{I,kk'} = P^{II,k'k,*}$ and $P^{II,kk'} = P^{I,k'k,*}$) in dense form. Due to the difference of output e-ph quantities, energy conservation for k pair selection is not the same
Information in std::out		Spin-relaxation time calculated using P? matrices and G matrices with different kind of smearings (constant or ImSigma_ePh)
Energy ranges	Two – one for probe ; one for pump and e-ph for both conduction and valance bands	Three – for probe ; for pump ; for e-ph, if ePhOnlyElec (ePhOnlyHole) = 1, only e-ph of conduction (valence) bands will be written down; Parameter nkBT is added to control energy range, default 7, 7 is enough for real-time but may not be for rate formula
Energy conservation input	Delta function is non- standard Gaussian $\frac{1}{\sqrt{\pi}\sigma} e^{-x^2/\sigma^2}$	Delta function is Gaussian $\frac{1}{\sqrt{2\pi}\sigma} e^{-x^2/(2\sigma^2)}$, smearing parameter ePhDelta in my code's input is $\frac{1}{\sqrt{2}}$ of ePhDelta in Shankar's code's input

Energy conservation techniques	<p>(i) Detailed balance: $n_q(\omega_q)$ replaced by $n_q(\varepsilon_k - \varepsilon_{k-q})$</p> <p>(ii) Varied Delta: $\sigma = \min\left(\sigma_0, \frac{\omega_q}{N+1}\right)$, N is input parameter nEphDelta</p>	<p>Technique (i) can be turned on/off by setting input parameter <code>detailBalance=1/0</code></p> <p>Technique (ii) can be turned on/off by setting input parameter <code>variedDelta=1/0</code></p>
Energy conservation range	<code>nEphDelta = 4</code>	<p><code>nEphDelta</code> is an input parameter. This is important for spin lifetime computations inside the code, since different smearings (e.g., max of <code>ImSigme_ePh</code> can be much larger than <code>ePhDelta</code>) will be used</p> <p>Notice that <code>nEphDelta</code> in my code's input is $\sqrt{2}$ of <code>nEphDelta</code> in Shankar's code's input</p>
VBM & CBM determination		In case VBM is not zero (metal, Fermi smearing or finite electric field), parameter <code>band_skipped</code> , starting band index of wannier relative to DFT, can be used to determine VBM and CBM correctly
k-point selection		In 3D cases, there can be too many k points. To speed up <code>eLoop</code> , we need temporally turn off spin and velocity matrices computations. This is achieved by introducing <code>eEneOnly</code> in <code>FeynWann</code> (see <code>if (eEneOnly) return;</code> in <code>setState</code> in <code>FeynWann.cpp</code>)
Parallel for e-ph	K points	K pairs
E-ph matrix elements computation	Use <code>ePhLoop</code> with mask (whether satisfying energy conservation)	<p>Firstly, run <code>eCalc</code> at all selected k points in parallel (and use <code>bcastState_inEphLoop</code> to collect them) and store electronic states in <code>std::vector<FeynWann::StateE> state_elec;</code></p> <p>Secondly, use <code>ePhCalc</code> for each k pair with stored <code>FeynWann::StateE state_elec[ik]</code> and <code>state_elec[jk]</code>.</p> <p>In some cases, <code>compute1</code> is slow, e.g., GaN, it is very helpful to run <code>eCalc</code> only once and reuse them in e-ph computations. Otherwise, <code>compute1</code> must be run for each k pair instead of for each k point</p> <p>My code is however not suitable to the cases where most k points are selected (e.g., iron) or there are more than 10,000 k points so that <code>state_elec</code> will take too huge memory</p>