



# Algebra 1 Workbook

---

*krista king*  
MATH

## IDENTIFYING MULTIPLICATION

■ 1. Give three different examples of how you can write “ $a$  times  $b$ ” mathematically.

■ 2. Simplify the following expression.

$$5(2 \cdot 3) \times (1)(a)$$

■ 3. What number would make the expression true?

$$4 \times 3(1)(?? \cdot 1) = 24$$

■ 4. What term would make the expression true?

$$??(3 \cdot x) \times (5)(2) = 60x^2$$

■ 5. Why do we have different ways to write multiplication?

■ 6. If  $(3)(x^2) = 10 \times 2$ , what does  $9x^2$  equal?



## THE ASSOCIATIVE PROPERTY

- 1. Give an example of an expression that demonstrates the associative property with multiplication.
- 2. What are the two main operations that the associative property works for?
- 3. Using the associative property, rewrite and simplify  $2 \times (3 \times 4)$ .
- 4. According to the associative property, what number would make the most sense in the expression?

$$42 + (31 + 17) = (42 + ??) + 17$$

- 5. What does the word “associate” refer to in math?
- 6. Rearrange  $(3 + 6) + 2$  using the associative property, then simplify.



■ 7. Give an example of an expression that demonstrates the associative property with addition.

■ 8. What number would make the following expression true?

$$(4 \times 2) \times 9 = ?? \times (2 \times 9)$$

■ 9. Give an example of an expression that does not demonstrate the associative property.



## THE COMMUTATIVE PROPERTY

- 1. Using the commutative property, rewrite  $6 + 19$  and then simplify.
- 2. Give an example of an expression that demonstrates the commutative property with multiplication.
- 3. According to the commutative property, what number would make the most sense in the expression?

$$11 + (23 + 6) = 11 + (6 + ??)$$

- 4. Using the commutative property, rewrite  $3 \times 4$  and then simplify.
- 5. Rearrange  $(3 + 6) + 2$  using the commutative property and then the associative property.
- 6. Give an example of an expression that demonstrates the commutative property with addition.



- 7. What number would make the following expression true?

$$(4 \times 2) \times 9 = (?? \times 9) \times 4$$

- 8. What are the two main operations that the commutative property works for?



## THE TRANSITIVE PROPERTY

- 1. If  $AB = CD$  and  $CD = EF$  then what is the value of  $EF$ ?
- 2. If  $x = 2$  and  $y = x$ , then what does the transitive property tell us?
- 3. According to the transitive property, if  $x = 2y$  and  $2y = 5z$ , then what is the value of  $x$ ?
- 4. Give an example that demonstrates the transitive property.
- 5. Use the transitive property to solve for  $z$ .

$$x = y$$

$$y = 3 - z$$

$$x = -2z + 7$$

- 6. Transitive comes from the word “transit,” which means, to what?



■ 7. By the transitive property, what expression would make the following statement true?

If  $2 + 3 = ??$  and  $4 + 1 = 5$ , then  $2 + 3 = 5$ .

■ 8. Use the transitive property to solve for  $x$ .

$$y = 2x + 3$$

$$y = z$$

$$z = 5x - 9$$

■ 9. According to the transitive property, what expression would make the most sense in the following statement?

If  $x = 2y$  and  $2y = ??$ , then  $x = 5z$ .





## THE DISTRIBUTIVE PROPERTY

- 1. Use the distributive property to solve for  $x$ .

$$5(x - 2) = \frac{1}{2}(6 - 2x)$$

- 2. Use the distributive property to expand the expression.

$$-\frac{2}{5}(10 - 5x)$$

- 3. Give an example that demonstrates the distributive property with subtraction.

- 4. What three main operations are used in the distributive property?

- 5. What does distributing remove from the expression?

- 6. Use the distributive property to solve for  $x$ .

$$2(5 - 3x) = x - 4$$



■ 7. What value would make the following expression true?

$$2(x + 3) = ?? + 6$$



## THE DISTRIBUTIVE PROPERTY WITH FRACTIONS

- 1. Perform the indicated operation and then simplify.

$$\frac{4y^3z^2}{3x} \times \frac{x^2y}{2z^2}$$

- 2. Use the distributive property to expand the expression.

$$-\frac{x^2z}{y^3} \left( \frac{y^2}{2} - \frac{xz^3}{z^2} \right)$$

- 3. Fill in the blank with the correct words: When we are distributing fractions, we multiply the outside numerator with the \_\_\_\_\_ of the terms inside the parentheses and the outside denominator with the \_\_\_\_\_ of the inside terms.

- 4. Use the distributive property to solve for  $x$ .

$$-\frac{3xy^2}{z} \left( \frac{2z}{3y^2} - z \right) = 3(3 + xy^2)$$

- 5. Use the distributive property to show that  $x = -10$ .



$$\frac{2}{3} \left( \frac{x}{2} - 6 \right) = 4 \left( \frac{x}{3} + \frac{3}{2} \right)$$

- 6. Explain why the two sides of the equation aren't equal to one another.

$$\frac{3}{2} \left( \frac{x}{5} - \frac{y}{2} \right) \neq \frac{3x}{10} - \frac{y}{2}$$

- 7. What term would make the following expression true?

$$\frac{2ab}{c^2} \left( \frac{3ac}{b} + a^2c^2 \right) = \frac{6a^2}{c} + ??$$

- 8. What term would make the following expression true?

$$\frac{??}{??} \left( \frac{2x}{z} + y^2 \right) = \frac{2x^3}{3z^2} + \frac{x^2y^2}{3z}$$



## THE DISTRIBUTIVE PROPERTY AND BINOMIAL MULTIPLICATION

- 1. Perform the indicated operation and simplify.

$$(x - 1)(x + 4)$$

- 2. How many terms does a binomial have?

- 3. Use the distributive property to expand the expression.

$$4(2 - x)(3 + 2x)$$

- 4. What term would make the following expression true?

$$(2x + 1)(5 - x) = ?? + 10x - x + 5$$

- 5. Use the distributive property to show that  $x = 3$ .

$$2(x - 1)(x + 1) = 2x^2 + x - 5$$

- 6. Explain why  $(x - 2)(x + 1) \neq x^2 - 2$ .



- 7. Use the distributive property to expand the expression.

$$\frac{1}{2}(6x + 4)(x - 1)$$

- 8. What term would make the following expression true?

$$(3 + x)(?) = 3x + 3 + x^2 + x$$



## GROUPING SYMBOLS WITH PEMDAS AND ORDER OF OPERATIONS

- 1. Write the expression with parentheses.

$$\frac{a}{b + c}$$

- 2. Simplify the expression.

$$2([3 + 1] - 4) - [6 + 3]$$

- 3. Put in grouping symbols that will make the equation true.

$$2x + 1 / 3 + 5x - 2 = \frac{2(x + 1)}{3 + 5x - 10}$$

- 4. Simplify the expression.

$$|2(1 - 4)| - (2 - 5)[(-1)(3 + 2) + 9]$$

- 5. What number would make the expression true?

$$(3 + 1)[2(?? - 5) + 7] - |(4 - 6)| = 4[-2 + 7] - |-2|$$



■ 6. Give three different examples of a grouping symbol.

■ 7. Rewrite the following as a fraction.

$$[2(x + 1) - 3]/[5x - 3(4x)]$$

■ 8. Simplify the following expression.

$$\sqrt{2(5 - 3)} - |3[6 - 7]|$$

■ 9. Using PEMDAS, evaluate each expression separately to show that they are not equal.

$$4 \times (3 - 1) - (4 \div 2 + 2) \text{ and } (4 \times 3 - 1) - 4 \div (2 + 2)$$

■ 10. Use the order of operations to simplify the expression.

$$\left(10 - [(-1)^2 + 1 - 6 \div 6]\right)^{1/2} + 4 \div 2$$

■ 11. What do the letters in PEMDAS stand for?





- 12. What number would make the equation true?

$$2^2 + 4 \cdot [(2 - ??) \div |-4|] = 4 + 4 \cdot [1 \div 4]$$

- 13. Use the order of operations to simplify the expression.

$$3 - [(-2)^2x + (3 - 7)]$$

- 14. Using the order of operations, explain why  $9 + 6 \div 3 \neq 5$ .

- 15. Put symbols of inclusion that make the equation true.

$$4 - 5 \cdot 3x + (-1)^2 = 4 - 15x - 5$$

- 16. What operations must be performed before multiplication and division?

- 17. Using the order of operations, explain why  $\sqrt{(2 + 7)} \neq \sqrt{2} + \sqrt{7}$ .

- 18. Simplify this expression.

$$3\{2[4 + 3(7 - 5) - 4]\}$$



- 19. Use the order of operations to simplify the expression.

$$3 + 2(x + 1)$$

- 20. Use order of operations to simplify the expression.

$$\frac{-2 + 3 - 10 \cdot 2 \cdot [(5 - 4) + 2]}{2}$$



## UNDERSTOOD 1

■ 1. What is  $x + 4x + x + x$ ?

■ 2. What happens when you multiply something by 1?

■ 3. Simplify the following expression.

$$\frac{1x^1}{1(1^1)} + \frac{1}{1(1x)} - 1^1$$

■ 4. What number would make the expression true?

$$1(2^1) - \frac{1}{1(1)^1} + \frac{??^1}{1 \times 1} = 4$$

■ 5. Simplify the following expression.

$$x(x^2 + 3x^2) - x^3$$

■ 6. Simplify the following expression.



$$\frac{x^1}{4x^3} + \frac{5x^4}{1x}$$

■ 7. Give an example of an expression where it would be useful to write out the understood 1.

■ 8. Simplify the following expression.

$$\frac{x}{1^1} \cdot \frac{x^2 + 1(1)}{5x^2}$$



## EVALUATING EXPRESSIONS

- 1. Explain what went wrong in the following statement?

If  $x^2 - x + 1$  when  $x = -2$ , then  $-2^2 - -2 + 1 = -4 + 2 + 1 = -1$ .

- 2. In your own words, what does it mean to “evaluate an expression”?

- 3. Find the value of  $x$  in  $x + 1 = y - 2z$ , when  $y = 4$  and  $z = -3$ .

- 4. Evaluate the expression when  $a = 1$ ,  $b = -3$ , and  $c = -4$ .

$$\frac{\sqrt{b^2 - 4ac}}{2a}$$

- 5. Show that  $x = -4$  by plugging it into the following expression.

$$x^2 - 4 = -3x$$



## INVERSE OPERATIONS

■ 1. Use inverse operations to solve for  $x$  in  $3x = 5$ .

■ 2. What is the inverse operation of division?

■ 3. Using division and multiplication, write two ways that we can solve for  $x$ .

$$\frac{1}{5}x = 10$$

■ 4. What value of the missing exponent would make the equation true?

$$(x^3)^? = x$$

■ 5. Put an expression in place of the question mark that would make the equation true.

$$\frac{1}{7} ? = 7$$

■ 6. Using inverse operations, solve for  $x$ .



$$2x^2 = 8$$

■ 7. What went wrong in the following set of steps?

$$2 - \frac{1}{3}x = 1$$

$$-\frac{1}{3}x = 3$$

$$x = -9$$



## SIMPLE EQUATIONS

- 1. Solve for  $x$ .

$$2x - 5 = 11$$

- 2. If  $x = 16$ , what number would make the following equation true?

$$x - ?? = 11$$

- 3. Solve for  $x$ .

$$\frac{x + 1}{3} = 7$$

- 4. What went wrong in the following set of steps?

$$2x - 11 = -3$$

$$2x = 8$$

$$x = 16$$





## BALANCING EQUATIONS

- 1. How would you solve for  $x$  in the following equation?

$$\frac{x}{4} = -5$$

- 2. What is the next step in balancing the following equation? In words, explain why.

$$2x - 3 = 5x$$

- 3. Solve for  $x$  in the following equation.

$$2(-3x + 5) - 1 = -3(1 - 5x)$$

- 4. What went wrong in the following steps?

$$-2x + 3 = 3x$$

$$-2x + 3 - 2x = 3x - 2x$$

$$3 = x$$

- 5. What missing term makes sense in the following series of steps?



$$-3(4 - 10x) + 2 = 5x$$

$$-12 + 30x + 2 = 5x$$

$$-10 + ?? = 5x$$

- 6. Solve for  $x$  in the following equation.

$$(x - 1) + 2(3x + 1) = -4(1 - x) + 9$$

- 7. What would be your next step in balancing the equation? Explain why.

$$2x - 6 + 5x + 10 = 11 - 3x + x + 4$$

- 8. Solve for  $x$  in the following equation.

$$x - 2(1 - x) + 5 = 3(2x + 4) - 6$$

- 9. What missing equation would make the solution true?

$$-2(4 - x) = 5(-3x + 1) + 7$$

$$-8 + 2x = -15x + 12$$

$$????? = ???????$$

$$17x = 20$$



$$x = \frac{20}{17}$$

- 10. Explain what's incorrect in the following set of steps.

$$2x - 1 = 4 - 3x$$

$$1 - 4 = -3x - 2x$$

- 11. What number would make the following true?

$$-7x + 4 = 3x - 11$$

$$??x = -15$$

- 12. Solve for  $x$  in the given equation.

$$5 - x = 17 - 4x$$

- 13. What went wrong in the following set of steps?

$$-4 - x - 2x = 5x - 11$$

$$-4 - 3x = 5x - 11$$

$$-15 = 8x$$



- 14. If  $x = -2$ , solve for  $y$  in the given equation.

$$3x + 2y - 7 = 1 - 5x - y$$

- 15. What missing equation would make the solution true?

$$6x - 13 + 5x = -x + 9$$

$$11x - 13 = -x + 9$$

$$12x - 13 = 9$$

$$?? = ??$$

$$x = \frac{22}{12}$$

- 16. What missing value would make the following true?

$$2y + 5 = -x + 3 - 5x$$

$$2y + 5 = ??x + 3$$

- 17. If  $y = -3$ , solve for  $x$  in the given equation.

$$2x - (x + y) = 5y - x + 7$$



- 18. Solve for  $y$  in the given equation.

$$3x - 2y + 5 = -5x + 7$$

- 19. Solve for the variable by keeping the equation balanced.

$$-(6c - 5) = 4(7c - 8) + 3$$

- 20. Solve for the variable.

$$7(4a - 3) = -(6a - 5) + 8$$

- 21. Solve the equation.

$$4x - 3 = 17$$



## SIMPLE EQUATIONS WITH SUBSCRIPTS

■ 1. Give three different examples of the variable  $Y$  with a subscript.

■ 2. It takes Peter 6 hours to paint a room and Laura 8 hours to paint that same room. Use the equation below to determine how long it would take for Peter and Laura to paint the room together, where  $R_1$  is the number of hours it takes Peter,  $R_2$  is the number of hours it takes Laura, and  $T$  is the number of hours it takes them together.

$$\frac{R_1 R_2}{R_1 + R_2} = T$$

■ 3. Solve for  $P_2$  in the following equation.

$$P_1 R + \frac{P_2}{V} = d$$

■ 4. The profit function for a The Coat Company is given by  $P = Rx - C_1 - C_2x$ , where  $P$  is the profit,  $R$  is the selling price,  $C_1$  is the fixed cost,  $C_2$  is the variable cost, and  $x$  is the total number of coats sold. What is the selling price  $R$  when  $P = 114$ ,  $C_1 = 550$ ,  $C_2 = 3.50$ , and  $x = 16$ ?



■ 5. Give an example of a subject besides math that uses variables with subscripts.

■ 6. The volume of the medium size box at the post office is given by

$$V = x_1 \times \frac{x_2}{2} \times \frac{x_3}{9}$$

where  $V$  is the volume of the box,  $x_1$  is the length,  $x_2/2$  is the width, and  $x_3/9$  is the height. Find the height of the box that has a volume of  $120 \text{ in}^3$ , a length of 4 in, and a width of 5 in.

■ 7. Solve for  $x_1$  in the following equation.

$$\frac{3V}{x_1} = td_0 + 2x_2d_1$$

■ 8. Solve the following equation for  $Y_2$  when  $t_1 = 2$ ,  $t_2 = 11$ ,  $D = 1/3$ , and  $Y_1 = 25$ .

$$3t_1 + \frac{15t_2D}{Y_2} = Y_1 - 5$$



## EQUATIONS WITH PARENTHESES

- 1. Simplify the following expression.

$$-(2x^0 + 3^0y) - 3y + x$$

- 2. Solve for  $x$  in the given equation.

$$2(x - 1) - 5(7 + 2x) = -(6 - x)$$

- 3. Simplify  $-(2x^2y)^0$ .

- 4. Simplify  $-2x^2y^0$ .

- 5. Solve for  $a$  in the given equation.

$$-2(3^0 - a) + 3(a + 7) = -(a^0 + 1)$$

- 6. What missing number would make the following true?

$$-3(4^0x - 5) = 2x - (3 - x)$$

$$??x + 15 = 3x - 3$$





■ 7. Write out the equation of the first step in solving the following for  $x$ .

$$6(1 - x) - 3(2x + 4) = -(5x + 7) - 10$$

■ 8. What went wrong in the following set of steps?

$$-(6 - 2x) - 3x = 7(x - 1)$$

$$-6 - 2x - 3x = 7x - 7$$

■ 9. Solve for  $y$  in the given equation.

$$-2^0(9 - y) + 3(3y - 1) = 4y^0 + 1$$



## WORD PROBLEMS INTO EQUATIONS

■ 1. Give three different words that mean “addition”.

■ 2. Write  $2 \times 5$  as a phrase using the word “product”.

■ 3. Write the phrase as an algebraic expression.

Six more than three times a number

■ 4. Find the value of the expression.

The quotient of 150 and 5

■ 5. Write the phrase as an algebraic expression.

Half of five times a number

■ 6. Write  $8 - 3$  as a phrase using the word “less”.

■ 7. Find the value of the expression.



3 less than the product of 2 and 7

■ 8. Give three different words that mean “subtraction.”

■ 9. Find the value of the expression.

$\frac{1}{3}$  of 2 more than 7



## CONSECUTIVE INTEGERS

- 1. Write the next five consecutive integers following  $-4$ .
- 2. Give an example of three consecutive negative integers.
- 3. Write the inequality sign that relates the two integers.

$$-6 \quad -10$$

- 4. Write the previous four consecutive integers before  $-3$ .

- 5. Write the following numbers in ascending order (smallest to largest).

$$-1 \quad 0 \quad -4 \quad 2 \quad -3$$

- 6. Circle the numbers that are not integers.

$$-10 \quad \frac{6}{7} \quad 3 \quad 7.34 \quad \frac{8}{4} \quad 9.0$$



■ 7. Write the following in descending order (largest to smallest).

$-11$        $-13$        $-5$        $11$        $3$

■ 8. Give an example of two types of numbers that are not integers.



## ADDING AND SUBTRACTING LIKE TERMS

■ 1. Give an example of like terms.

■ 2. Simplify the expression.

$$-x + 6x - 8x + 3x$$

■ 3. What stays the same when adding or subtracting like terms?

■ 4. Simplify the expression.

$$x + 2x^2 - y - 5x^2 + 7y - 4x$$



## MULTIPLYING AND DIVIDING LIKE TERMS

- 1. Simplify the expression.

$$\frac{x^2(-x + 3x^3 + 2x^2)}{x^3}$$

- 2. Simplify the expression.

$$\frac{(2x + 1)(x^2 - x - 4)}{2x}$$

- 3. Simplify the expression.

$$\frac{6x^a}{3x^b}$$

- 4. Simplify the expression.

$$3x^a \cdot 5x^b$$



## ADDING AND SUBTRACTING POLYNOMIALS

- 1. What stays the same when adding and subtracting like terms?

- 2. Simplify the expression.

$$(2x^3 - 5x^2 + x - 3) - (x^2 - 2x + 7)$$

- 3. What went wrong in the following set of steps?

$$6x^3 + 7 + x^2$$

$$7x^3 + 7$$

- 4. What is the coefficient in the following expression?

$$5x^8$$

- 5. Simplify the expression.

$$(10a^2b + 3ab^2 - ab) + (2ab^2 - a^2b + ab)$$

- 6. What is the exponent in the following expression?





$$3z^8$$

- 7. Simplify the expression.

$$(x^4 - 5y^3 + z - xy) - (2y^4 + 6xy - z + x^4)$$

- 8. What is the variable in the following expression?

$$-y^4$$

- 9. What went wrong in the following set of steps?

$$9 - x^3 + 3 + 4x^3$$

$$12 + 3x^6$$



## MULTIPLYING POLYNOMIALS

- 1. Expand the expression.

$$(2x - y)^2$$

- 2. What does FOIL stand for?

- 3. What went wrong in the following set of steps?

$$(a - 2)^2$$

$$a^2 - 4$$

- 4. Expand the expression.

$$(3x + 2y)(3x - 2y)$$

- 5. Fill in the blank.

$$(3 - a)(5 + a) = 15 + \underline{\hspace{1cm}} - a^2$$

- 6. Expand the expression.



$$(x^2 - 3)(2 - x)$$

■ 7. What went wrong in the following set of steps?

$$(x - y)(x + y)$$

$$x^2 - 2xy - y^2$$



## DIVIDING POLYNOMIALS

- 1. In words, what is the first question you should ask when solving the problem using long division?

$$(2x^2 + 4x - 4) \div (x - 1)$$

- 2. Simplify the expression using polynomial long division.

$$(3x^3 - x^2 + 5) \div (x + 2)$$

- 3. What went wrong in setting up the long division problem?

$$(5x^4 - 3x^2 + x - 2) \div (x^2 + 1)$$

$$5x^4 - 3x^2 + x - 2 \overline{) x^2 + 1}$$

- 4. Given the following long division, write the answer as

$$\text{quotient} + \frac{\text{remainder}}{\text{divisor}}$$



$$\begin{array}{r}
 3x-1 \\
 \hline
 x^2-3 \overline{) 3x^3 - x^2 + x - 5} \\
 \underline{-3x^3} \qquad +9x \\
 -x^2 + 10x - 5 \\
 \underline{x^2} \qquad -3 \\
 10x - 8
 \end{array}$$

- 5. Use long division to simplify the expression.

$$(2x^5 - 3x^3 + x^2 + 4x - 1) \div (x^2 + 2)$$

- 6. How would you rewrite the expression before starting the long division process?

$$(6x^3 - x + 7) \div (x + 1)$$

- 7. Set up but do not solve the following division problem.

$$\begin{array}{r}
 x^5 - x^3 + 4x^2 - x + 6 \\
 \hline
 2x^3 - 5
 \end{array}$$



- 8. Simplify the expression using polynomial long division.

$$(3x^2 + 2x + 5) \div (3x + 5)$$



## MULTIPLYING MULTIVARIABLE POLYNOMIALS

- 1. Why can we not add the following two terms?

$$2x^3y + x^3y^2$$

- 2. Simplify the expression.

$$(a - 3y)(2a + y)$$

- 3. What went wrong in the following set of steps?

$$(x + 3b)(-2x - b)$$

$$-2x^2 - bx - 6bx + 3b^3$$

- 4. Simplify the expression.

$$(x - 2y)(x + y) + (3x - y)(4x + 4y)$$

- 5. Fill in the blanks with the correct terms.

$$(5a - b)(7b - 3a)$$

$$35ab - 15a^2 + \underline{\hspace{1cm}} + 3ab$$



\_\_\_  $- 15a^2 +$  \_\_\_

■ 6. What does FOIL stand for when used in multiplying multivariable polynomials?

■ 7. Fill in the following chart for the multiplication of the following two expressions.

$(2x - 3y)(x^2 + y)$

	2x	-3y
x <sup>2</sup>		
y		

■ 8. What went wrong in the following set of steps?

$(a^2 + 6b)(-a - b^2)$

$-a^3 - a^2b^2 - 6ab - b^3$

$-a^3 - 7ab - b^3$

■ 9. Fill in the blanks of the multiplication chart with the correct terms when given the following problem.





$$(4a + 3b)(-a + 2b^2)$$

		<b>3b</b>
<b>-a</b>		-3ab

- 10. Simplify the following expression.

$$(5ax - 3by)(a + y) - (a - y)(2ax + 4by)$$

- 11. What went wrong in this set of steps?

$$(-2x)(3y - x^2)$$

$$-6xy - 2x^3$$



## DIVIDING MULTIVARIABLE POLYNOMIALS

- 1. Set up but do not solve the long division problem.

$$\frac{y^3 - 3yx^2 + x^3}{y - x}$$

- 2. Find the quotient.

$$\frac{3x^2 + 6xy - 2y^2}{x - 2y}$$

- 3. Given the following long division, identify the quotient, remainder, and divisor.
- .....



$$\begin{array}{r}
 x^2 - xy + y^2 \\
 \hline
 x+y \overline{) x^3 + 0x^2y + 0xy^2 + y^3} \\
 \underline{-(x^3 + x^2y)} \\
 -x^2y + 0xy^2 \\
 \underline{-(-x^2y - xy^2)} \\
 xy^2 + y^3 \\
 \underline{-(xy^2 + y^3)} \\
 0
 \end{array}$$

- 4. How would you rewrite the expression before starting the long division process?

$$\frac{2y^3 - xy^2 + x^3}{x - y}$$

- 5. Find the quotient.

$$\frac{6x^2 - xy + 2y^2}{2x - y}$$

- 6. In words, what is the first question you should ask when solving this long division problem?



$$2x+3y \overline{) 6x^4 - x^2y + xy^2 + 4y^4}$$

- 7. What went wrong in setting up the long division?

$$\frac{7x^3 + x^2y - 2xy^2 + y^3}{x - 2y}$$

$$7x^3 + x^2y - 2xy^2 + y^3 \overline{) x - 2y}$$

- 8. Fill in the blanks with the correct terms.

$$(2x - y)( \underline{\hspace{2cm}} ) = 6x^2 - 3xy$$

- 9. Find the quotient.

$$(y^2 + xy - 3x^2) \div (y + x)$$



## GREATEST COMMON FACTOR OF TRINOMIALS

- 1. Factor out the greatest common factor.

$$3x^2y^3 + 12x^3y^2 - 9x^4y^4$$

- 2. Fill in the blank with the correct term.

$$4a^3b - 10ab^2 + \underline{\hspace{1cm}} = 2ab(2a^2 - 5b + 3a^2b^2)$$

- 3. What went wrong in the following factoring?

$$10x^3y^4 - 5x^4y^2 - 20x^6y^3$$

$$x^3y^2(10y^2 - 5x - 20x^3y)$$

- 4. Factor out the greatest common factor.

$$2x + 8xy^2 - 16bx^2$$

- 5. Fill in the blank with the correct term.

$$6axy + \underline{\hspace{1cm}} - 2abx^2y = ax(6y + 3ab - 2bxy)$$



■ 6. Give an example of a trinomial in the variable  $x$ .

■ 7. Factor out the greatest common factor.

$$16ab^2c^3 + 8a^3b^3c - 12a^2b^3c^2$$



## GREATEST COMMON FACTOR OF POLYNOMIALS

- 1. Factor the expression.

$$\frac{4x^2 + 6x - 4}{2}$$

- 2. Fill in the blank with the correct term.

$$\frac{3x^3 - 12x}{3x} = x^2 - \underline{\hspace{2cm}}$$

- 3. What is the greatest common factor of the polynomial?

$$9s^3t^2 + 15s^2t^5 - 24s^5t + 6s^4t^2$$

- 4. What is the difference between a trinomial and a polynomial?

- 5. Factor the expression.

$$\frac{4x^4 - 8x^3 - 32x^2}{4x^2}$$



■ 6. What went wrong in the following factoring.

$$3x^3 - 3x^2 - 6x$$

$$x(3x^2 - 3x - 6)$$

$$x(3x + 3)(x - 2)$$





## FACTORING QUADRATIC POLYNOMIALS

- 1. Factor the quadratic expression.

$$2x^2 + x - 3$$

- 2. What went wrong in the following factoring?

$$x^2 - 4x + 3$$

$$(x - 3)(x + 1)$$

- 3. Factor the quadratic expression.

$$3x^2 + 5x - 2$$

- 4. Factor the quadratic expression.

$$x^2 - 9x + 18$$

- 5. Fill in the blank with the correct term.

$$2x^2 - \underline{\hspace{1cm}} - 4 = (2x + 1)(x - 4)$$



■ 6. Factor the quadratic expression.

$$x^2 - x - 2$$



## FACTORIZING THE DIFFERENCE OF TWO SQUARES

- 1. Factor the expression.

$$4y^2 - 36$$

- 2. What went wrong in the following set of steps?

$$9a^4 - 25b^2$$

$$(9a^2 - 25b)(9a^2 + 25b)$$

- 3. Factor the expression.

$$49x^6y^2 - 36z^4$$

- 4. Fill in the blank with the correct term.

$$\underline{\hspace{2cm}} - 25y^2 = (2xz^2 - 5y)(2xz^2 + 5y)$$



## COMPLETING THE SQUARE

- 1. Solve for  $x$  by completing the square.

$$x^2 - 6x + 5 = 0$$

- 2. Fill in the blank with the correct term.

$$x^2 - \underline{\hspace{2cm}} + \frac{9}{4} = -2 + \frac{9}{4}$$

- 3. Complete the square in the following expression, but do not solve.

$$3y^2 - 12y + 3 = 0$$

- 4. Solve for  $a$  by completing the square.

$$2a^2 + 8a = -4$$

- 5. What is your first and second step in solving the problem by completing the square?

$$4x^2 - 16x + 28 = 0$$



■ 6. Explain when and why completing the square is used for factoring.

■ 7. Solve for  $y$  by completing the square.

$$3y^2 + 9y = 3$$

■ 8. Fill in the blank with the correct term.

$$\underline{\hspace{2cm}} - 4x = 6$$

$$\left(x - \frac{2}{3}\right)^2 = \frac{22}{9}$$



## COMPLETING THE SQUARE WITH COMPLEX ROOTS

- 1. Solve for  $x$  by completing the square.

$$x^2 + 6x + 11 = 0$$

- 2. What went wrong in the following set of steps toward completing the square?

$$3x^2 - 12x - 7 = 0$$

$$3x^2 - 12x + 36 = 7 + 36$$

- 3. Fill in the blank with the correct term.

$$-2y^2 - 12y = 9$$

$$y^2 + 6y + \underline{\hspace{1cm}} = -\frac{9}{2} + \underline{\hspace{1cm}}$$

- 4. Solve for  $x$  by completing the square.

$$2x^2 + 8x + 35 = 0$$

- 5. Complete the square but do not solve.



$$x^2 + 12x + 20 = 0$$

■ 6. What is the difference in the problem when completing the square with complex roots compared to real roots?

■ 7. Solve for  $z$  by completing the square.

$$z^2 - 8z + 25 = 0$$

■ 8. Fill in the blank with the correct term.

$$z^2 + \underline{\hspace{1cm}}z + \frac{25}{4} = -7 + \frac{25}{4}$$

■ 9. Give an example of a quadratic equation that would have complex roots.

■ 10. Solve for  $z$ .

$$z^2 - 4z = -5$$



## QUADRATIC FORMULA

- 1. Solve for  $x$  using the quadratic formula.

$$4x^2 - 8x - 15 = 0$$

- 2. Write the quadratic formula for the following quadratic equation.

$$x^2 - 5x - 24 = 0$$

- 3. What went wrong in the way the quadratic formula was applied?

$$3x^2 - 5x + 10 = 0$$

$$x = \frac{-5 \pm \sqrt{(-5)^2 - 4(3)(10)}}{2(3)}$$

- 4. Solve for  $z$  using the quadratic formula.

$$z^2 = z + 3$$

- 5. Fill in the blank with the correct term if the quadratic formula below was built from the quadratic equation.





$$\underline{\hspace{1cm}} x^2 + 3x - 5 = 0$$

$$x = \frac{-3 \pm \sqrt{(3)^2 - 4(-2)(-5)}}{2(-2)}$$

- 6. Simplify the expression.

$$\frac{-(-8) \pm \sqrt{(-8)^2 - 4(1)(14)}}{2(1)}$$

- 7. What are two ways to solve a quadratic equation when you cannot easily factor?

- 8. What went wrong if the quadratic formula below was built from the quadratic equation?

$$x^2 + 2x = 7$$

$$x = \frac{-2 \pm \sqrt{(2)^2 - 4(1)(7)}}{2(1)}$$

- 9. Solve for  $t$  using the quadratic formula.

$$4t^2 - 1 = -8t$$



## FACTORING TO FIND A COMMON DENOMINATOR

- 1. Simplify the expression by combining the two fractions.

$$\frac{x+1}{2x^2+5x-3} + \frac{2}{x+3}$$

- 2. What is the one thing you need in order to add or subtract rational expressions?

- 3. What is the common denominator of the rational expressions?

$$\frac{x^2-1}{x^2-4} \text{ and } \frac{x+1}{3x^2-3x-6}$$

- 4. Simplify the expression by combining the two fractions.

$$\frac{3}{x-2} - \frac{x-4}{x^2-5x+6}$$

- 5. What went wrong in the following simplification?

$$\frac{1}{x+1} + \frac{3x-1}{(2x-2)(x+1)}$$



$$\frac{1}{(x+1)(2x-2)} + \frac{3x-1}{(2x-2)(x+1)}$$

- 6. Fill in the blank with the correct term.

$$\frac{2}{\underline{\hspace{2cm}}} - \frac{x-2}{x^2-9} = \frac{2(x-3) - 4(x-2)}{4(x-3)(x+3)}$$

- 7. Simplify the expression by combining the two fractions.

$$\frac{4}{(x+1)(x-3)} - \frac{1}{(x+4)(x+1)}$$

- 8. What went wrong in the following simplification?

$$\frac{3}{x^2-25} - \frac{1}{x+5}$$

$$\frac{3-x-5}{(x-5)(x+5)}$$



## DOMAIN AND RANGE

- 1. Find the domain of  $f(x)$ .

$$f(x) = \frac{3}{x(x+1)} + x^2$$

- 2. Find the domain and range of the given set.

$$(-1, -3), \quad (0, 5), \quad (-3, 6), \quad (0, -3)$$

- 3. Find the domain and range of  $g(x)$ .

$$g(x) = \frac{\sqrt{x-2}}{3}$$

- 4. Find the domain and range of the function.

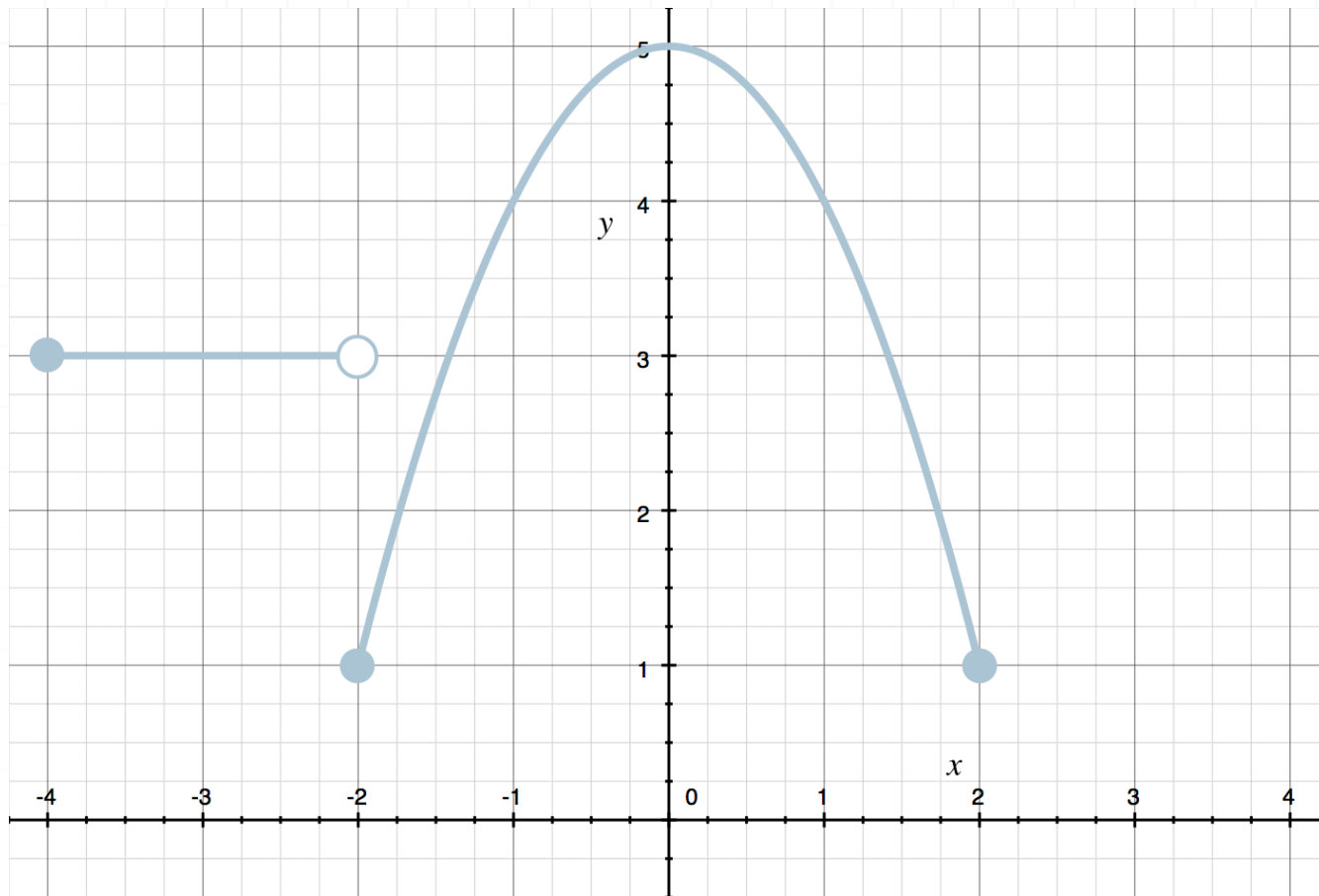
$$f(x) = \frac{2}{x} + 1$$

- 5. Give an example of a function that has a domain of  $[1, \infty)$ .



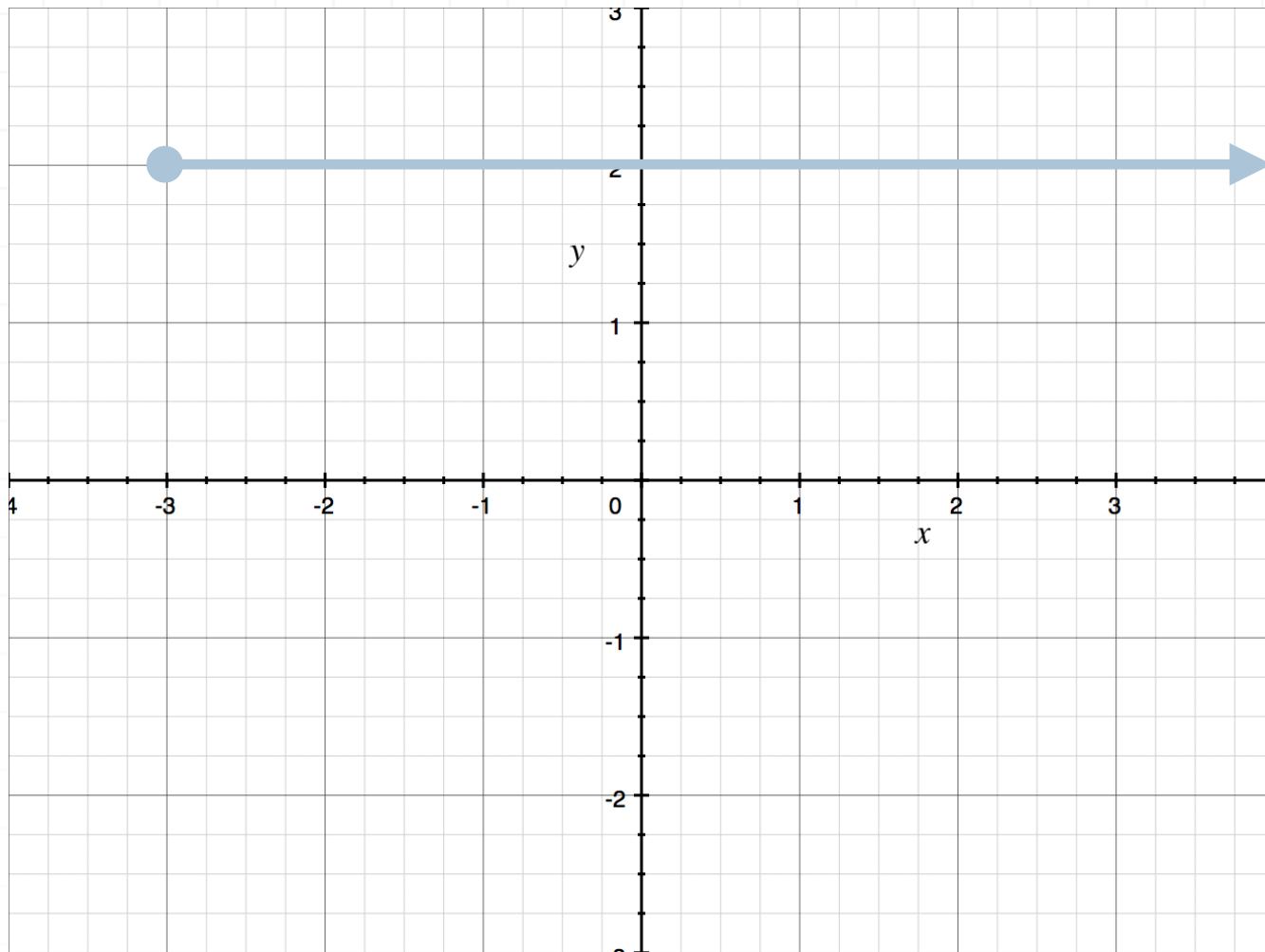
## DOMAIN AND RANGE FROM A GRAPH

- 1. What is the domain and range of the function? Assume the graph does not extend beyond the graph shown.



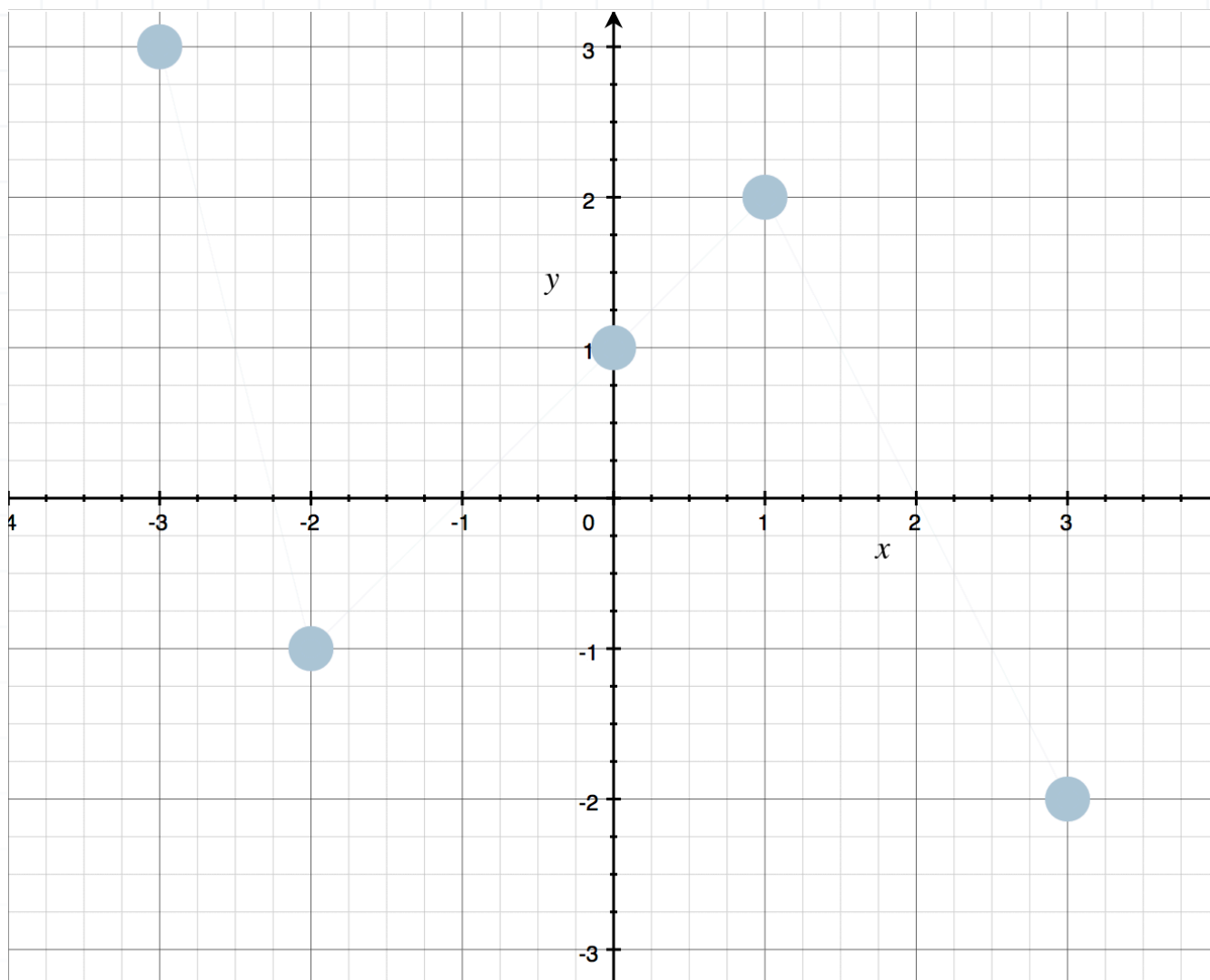
- 2. What is the domain and range of the function?





■ 3. Determine the domain and range of the function.



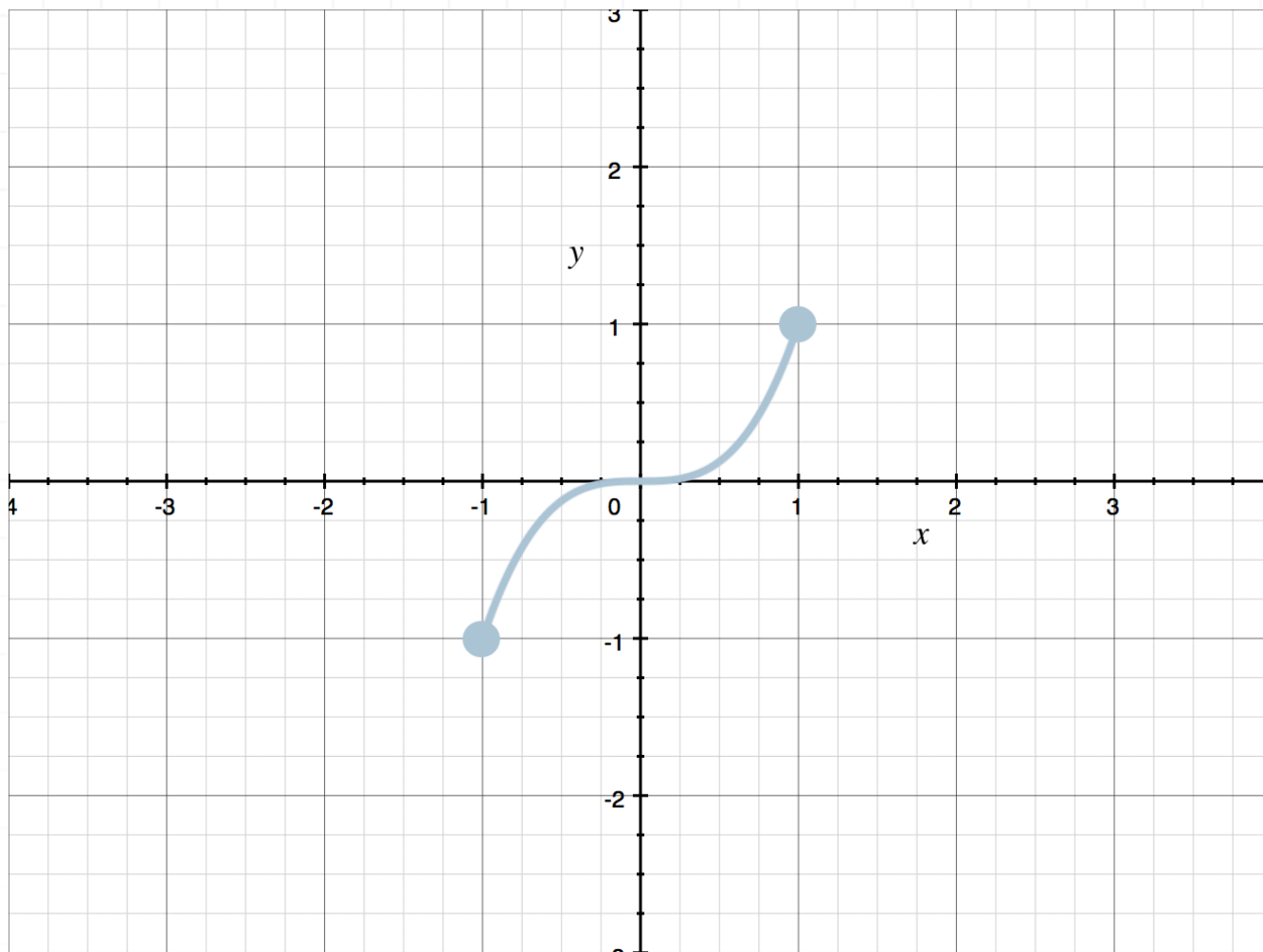


- 4. Fill in the blanks in the following description of the domain of a graph.

“The domain is all the values of the graph from \_\_\_\_\_ to \_\_\_\_\_.”

- 5. What is the domain and range of the function? Assume the graph does not extend beyond the graph shown.

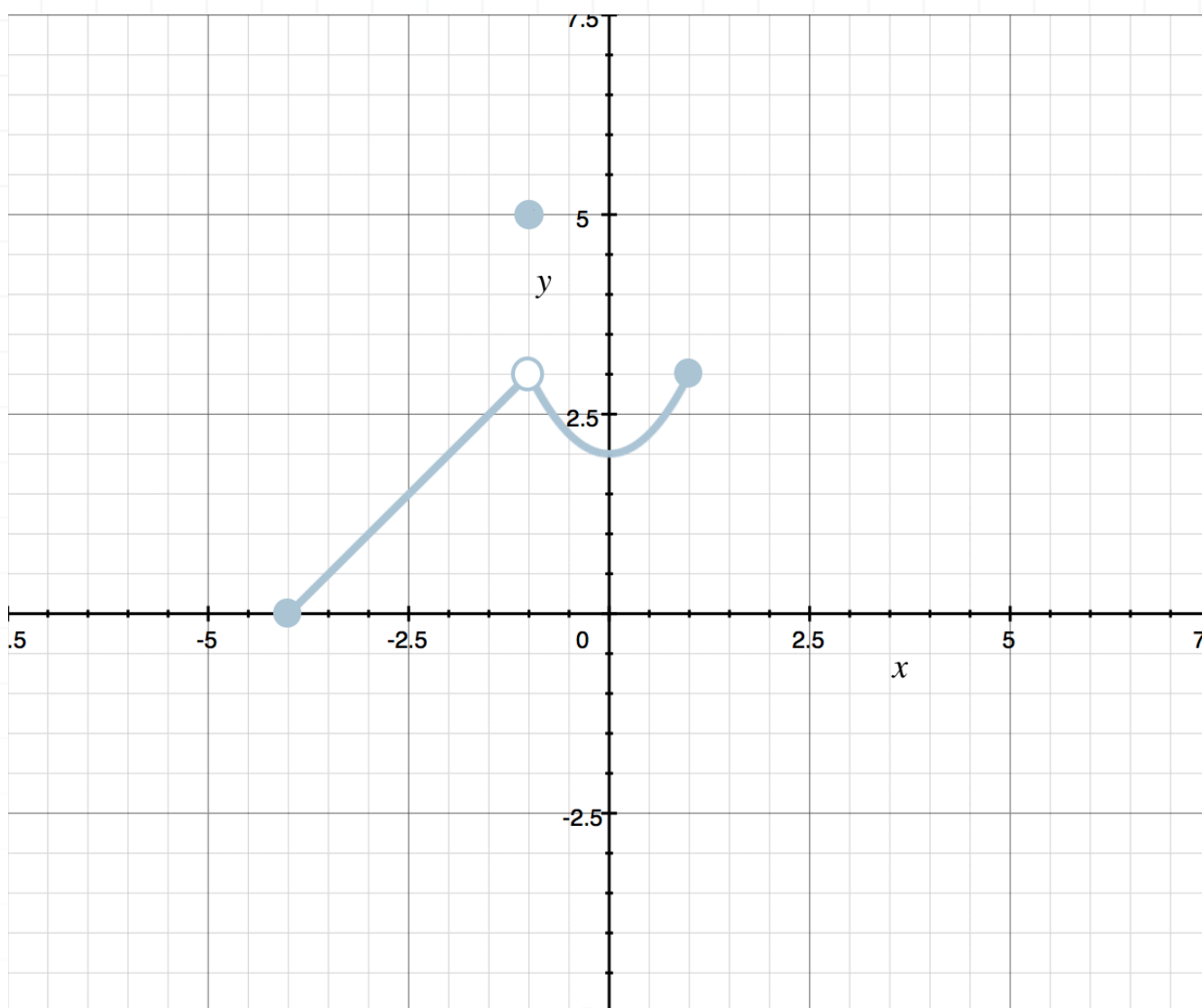




- 6. What is the domain and range of the function? Assume the graph does not extend beyond the graph shown.





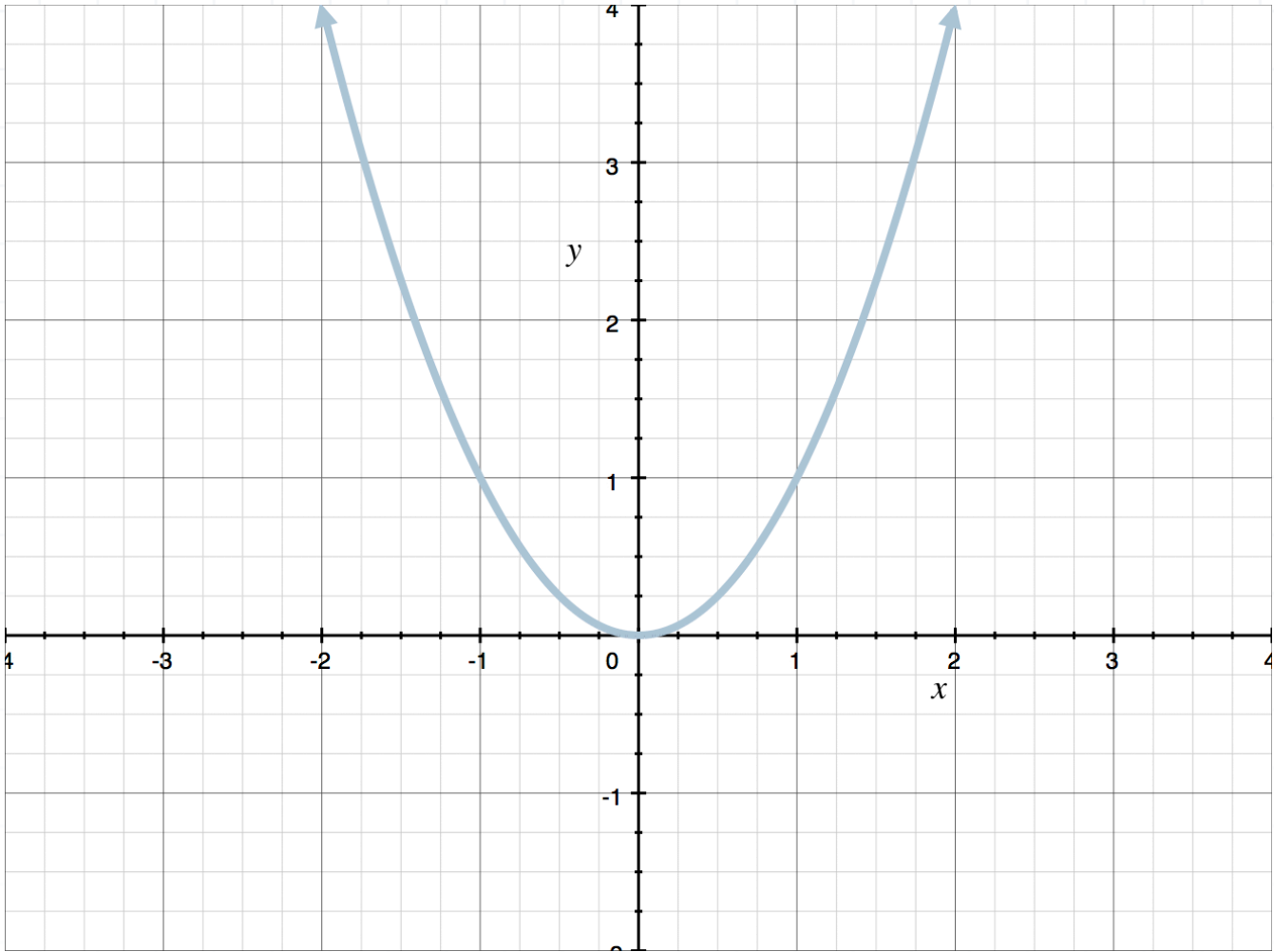


- 7. Fill in the blanks in the following description of the range of a graph.

“The range is all the values of the graph from \_\_\_\_\_ to \_\_\_\_\_.”

- 8. What is the domain and range of the function?





## FUNCTIONAL NOTATION

■ 1. If  $f(x) = 11 - 5x$ , find  $f(-2)$ .

■ 2. Find and simplify  $f(x + 1)$  if  $f(x) = 4x - 5$ .

■ 3. Correct what went wrong in the following set of steps.

At  $x = -2$  and  $f(x) = x^2 + 1$ , then

$$f(-2) = -2^2 + 1$$

$$f(-2) = -4 + 1$$

$$f(-2) = -3$$

■ 4. If  $g(t) = t^2 - t + 3$ , find  $g(-1)$ .

■ 5. Find and simplify  $h(s^2)$  if  $h(s) = -s^2 + 3s - 1$ .

■ 6. If  $g(x) = x^3 - x + 1$ , figure out what you need to plug into the function in order to get the following expression.



$$g(??) = (2x + 1)^3 - (2x + 1) + 1$$

- 7. If  $f(x) = x^2 + x - 1$ , find  $f(x + h)$  and expand as much as possible.
- 8. Correct what went wrong in the following set of steps.

If  $f(x) = x^3 + 3x^2 - 5x + 2$ , then  $f(1)$  is

$$f(1) = (1)^3 + 3(1)^2 - 5(1) + 2$$

$$f(1) = 1 + 9 - 5 + 2$$

$$f(1) = 7$$



## TESTING FOR FUNCTIONS

- 1. Determine if the following represents a function. Explain your answer.

$$(2, -1), (-1, 0), (0, -1), (3, 2)$$

- 2. Draw a graph that represents a function. Explain why it's a function.

- 3. Fill in the blanks in the following definition of a function.

For every \_\_\_\_\_, there is only one unique \_\_\_\_\_.

- 4. Give two different  $y$ -values that have the same output value for  $x$ .

$$y^2 = x$$

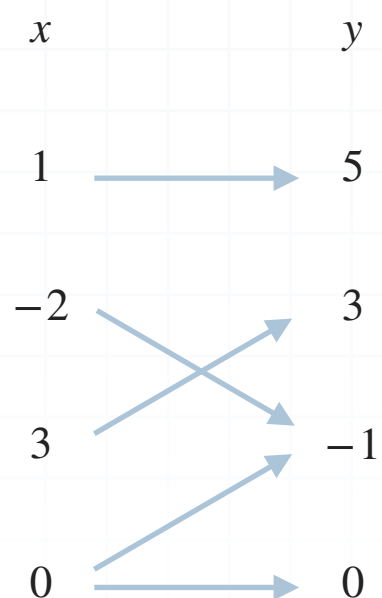
- 5. Draw a graph that does not represent a function. Explain why it's not a function.

- 6. Determine whether or not the following set of points represents a function. Explain your answer.



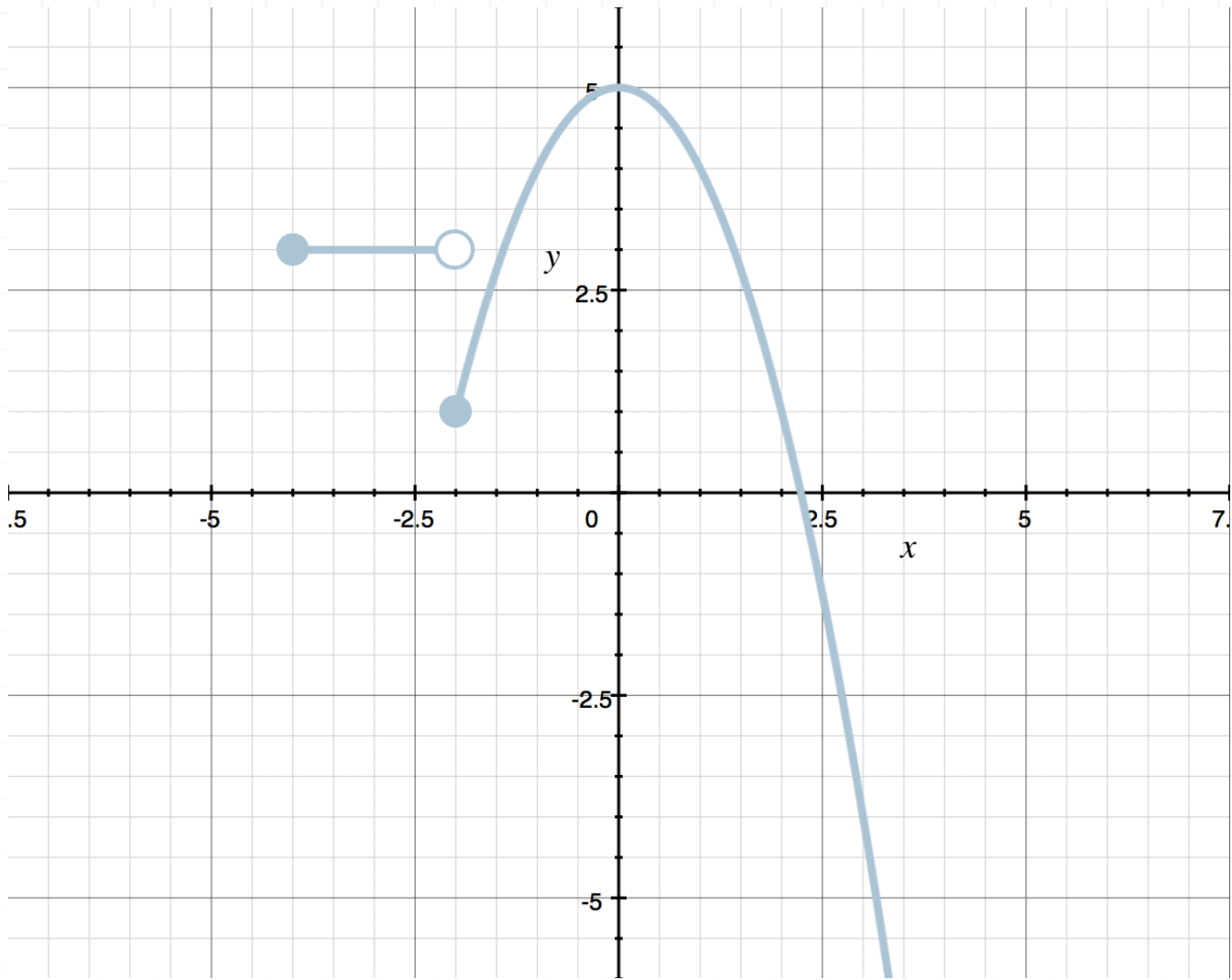
$(1,2)$ ,  $(-1,5)$ ,  $(1,-3)$ ,  $(0,1)$

■ 7. Determine if the following represents a function. Explain your answer.



■ 8. Determine if the following represents a function. Explain your answer.





## VERTICAL LINE TEST

- 1. Determine algebraically whether or not the equation represents a function.

$$(x - 1)^2 + y = 3$$

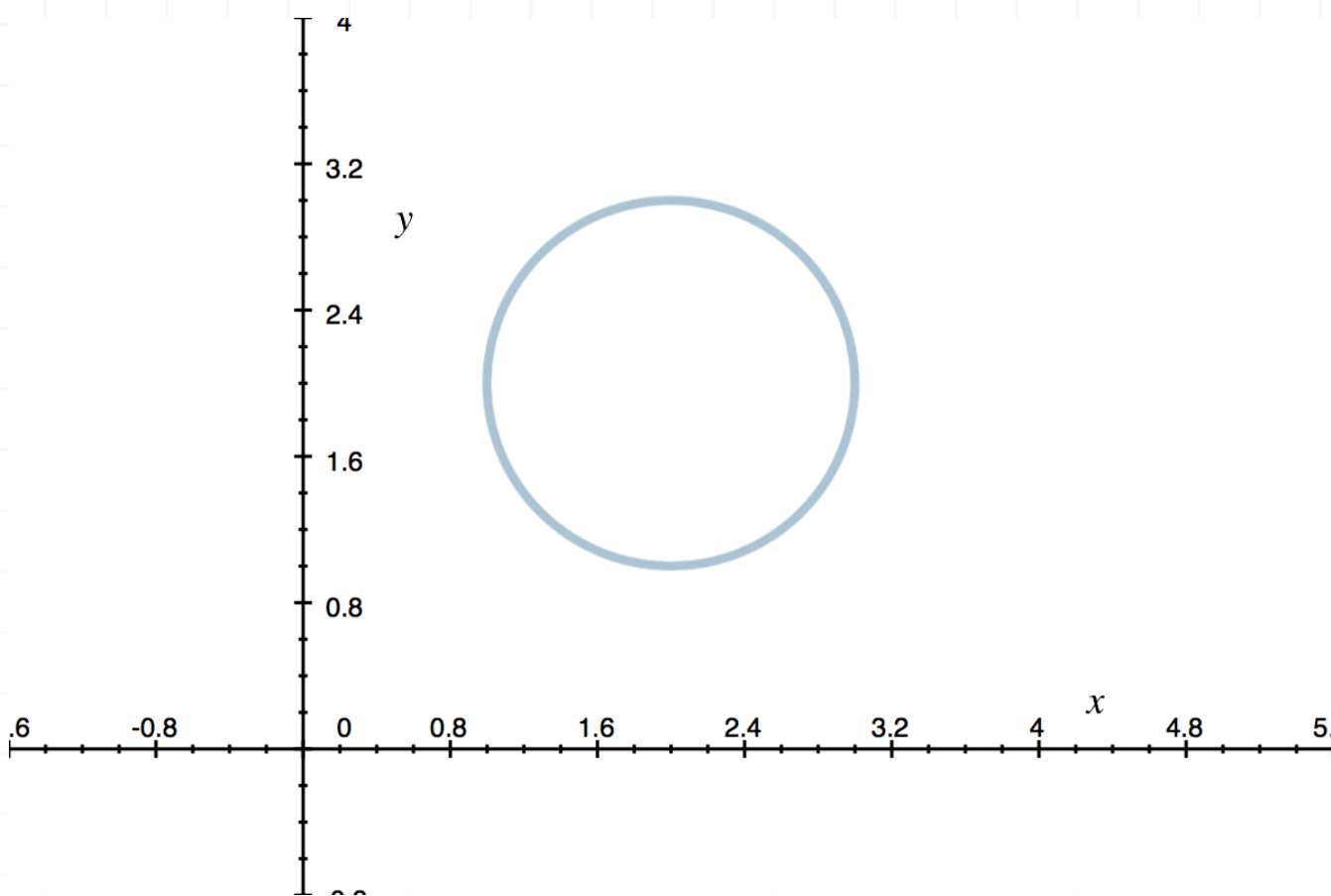
- 2. Fill in the blanks in the following statement using “equations,” and “functions.”

All \_\_\_\_\_ are \_\_\_\_\_.

- 3. Use the Vertical Line Test to determine whether or not the graph is the graph of a function.





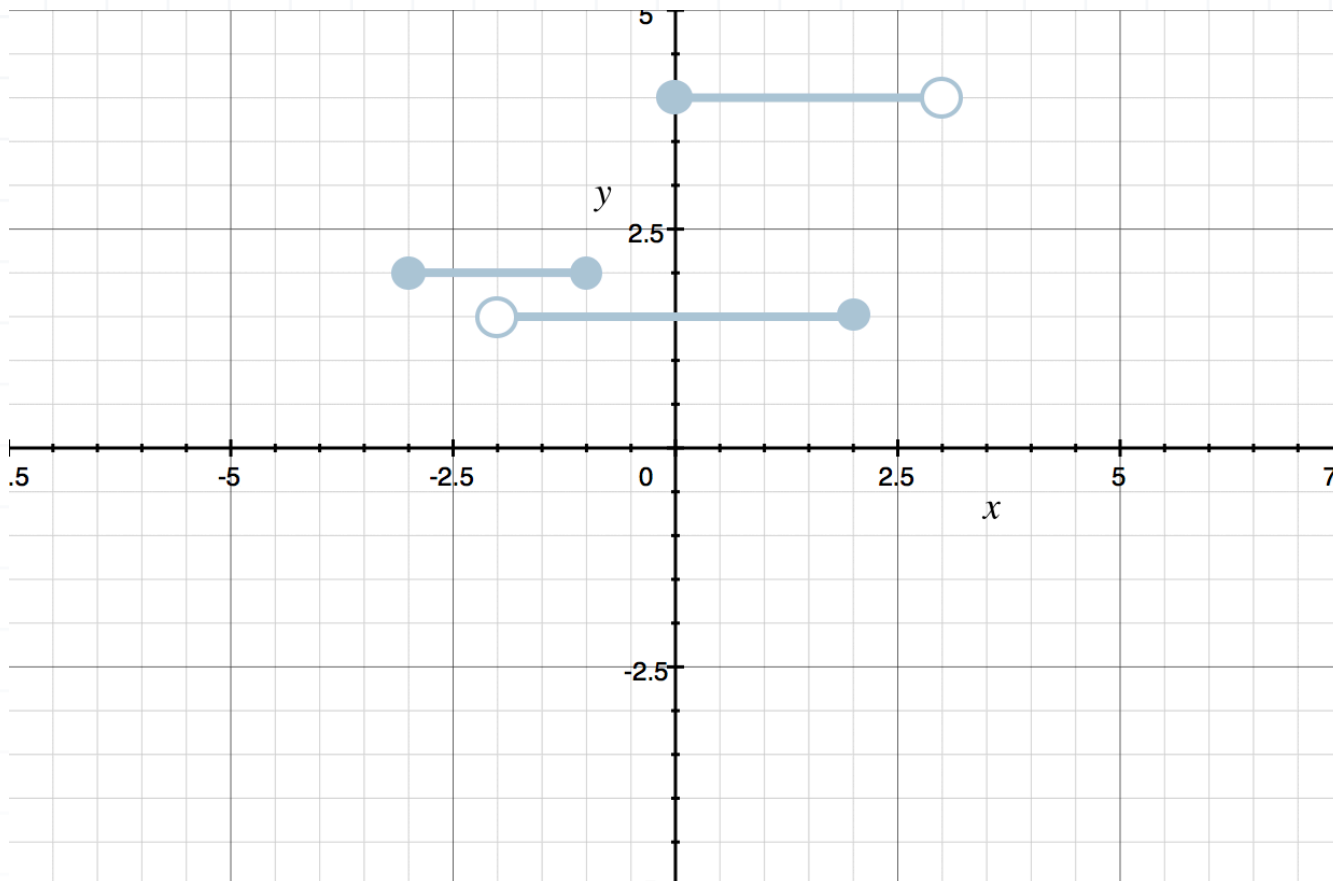


- 4. Determine algebraically whether or not the equation represents a function.

$$y^2 = x + 1$$

- 5. Use the Vertical Line Test to determine whether or not the graph represents a function.





6. Explain why the Vertical Line Test determines whether or not a graph represents a function.

7. Fill in the blanks in the following statement using: equations, functions.

Not all \_\_\_\_\_ are \_\_\_\_\_.

8. Determine algebraically whether or not the equation represents a function.

$$x^3 + y = 5$$



## SUM OF FUNCTIONS

- 1. Find  $(f + h)(-1)$  if  $f(x) = x^2 + 1$  and  $h(x) = 2x - 2$ .
- 2. Find and simplify  $(h + g)(x)$  if  $g(x) = x^2 + 3x - 1$  and  $h(x) = -2x^2 + 4x - 5$ .
- 3. If  $f(-2) = 6$ ,  $g(-2) = -3$ , and  $h(-2) = 4$ , find  $(f + g + h)(-2)$ .
- 4. Describe two ways you can add two functions together.
- 5. Find  $(h + g)(t)$  if  $h(t) = 4t^2 - 3$  and  $g(t) = -3t^2 + 4$ .

- 6. Given the expression below, determine  $f(x)$  and  $g(x)$ .

$$(f + g)(x) = (-x^2 + 3x + 2) + (x - 7)$$

- 7. Let  $a(x) = x^3 - x^2 + x - 1$  and  $b(x) = -x^3 + x^2 + x - 1$ . Determine the value of  $(a + b)(-1)$ .



- 8. What went wrong in the following set of steps?

$$(x^2 + x - 9) + (x - 1)$$

$$(3x - 9) + (x - 1)$$

$$3x - 9 + x - 1$$

$$4x - 10$$

- 9. If  $g(1) = 5$  and  $h(1) = -3$ , find  $(g + h)(1)$ .

- 10. If  $f(0) = 3$  and  $(f + g)(0) = 8$ , find  $g(0)$ .



## PRODUCT OF FUNCTIONS

■ 1. Find and simplify  $(ab)(x)$  if  $a(x) = x + 3$  and  $b(x) = 5x - 4$ .

■ 2. Find  $(fg)(-1)$  if  $f(x) = x^2 + 3$  and  $g(x) = x - 5$ .

■ 3. If  $g(0) = -2$  and  $(gh)(0) = -14$ , find  $h(0)$ .

■ 4. What went wrong in the following set of steps?

$$(x + 1)(x + 2)$$

$$x \cdot x + 2 \cdot x + 2$$

■ 5. Given the expanded expression below, determine  $f(x)$  and  $g(x)$ .

$$(gf)(x) = x^2(x - 7) - x(x - 7) + 5(x - 7)$$

■ 6. Find  $(fh)(5)$  if  $f(x) = -x^2 + 2x$  and  $h(x) = 2x + 7$ .



■ 7. Describe two different ways that you can multiply two functions together and evaluate the product at a particular point.

■ 8. Find and simplify  $(gh)(x)$  if  $g(x) = x^2 + 1$  and  $h(x) = 2x^2 + 3$ .



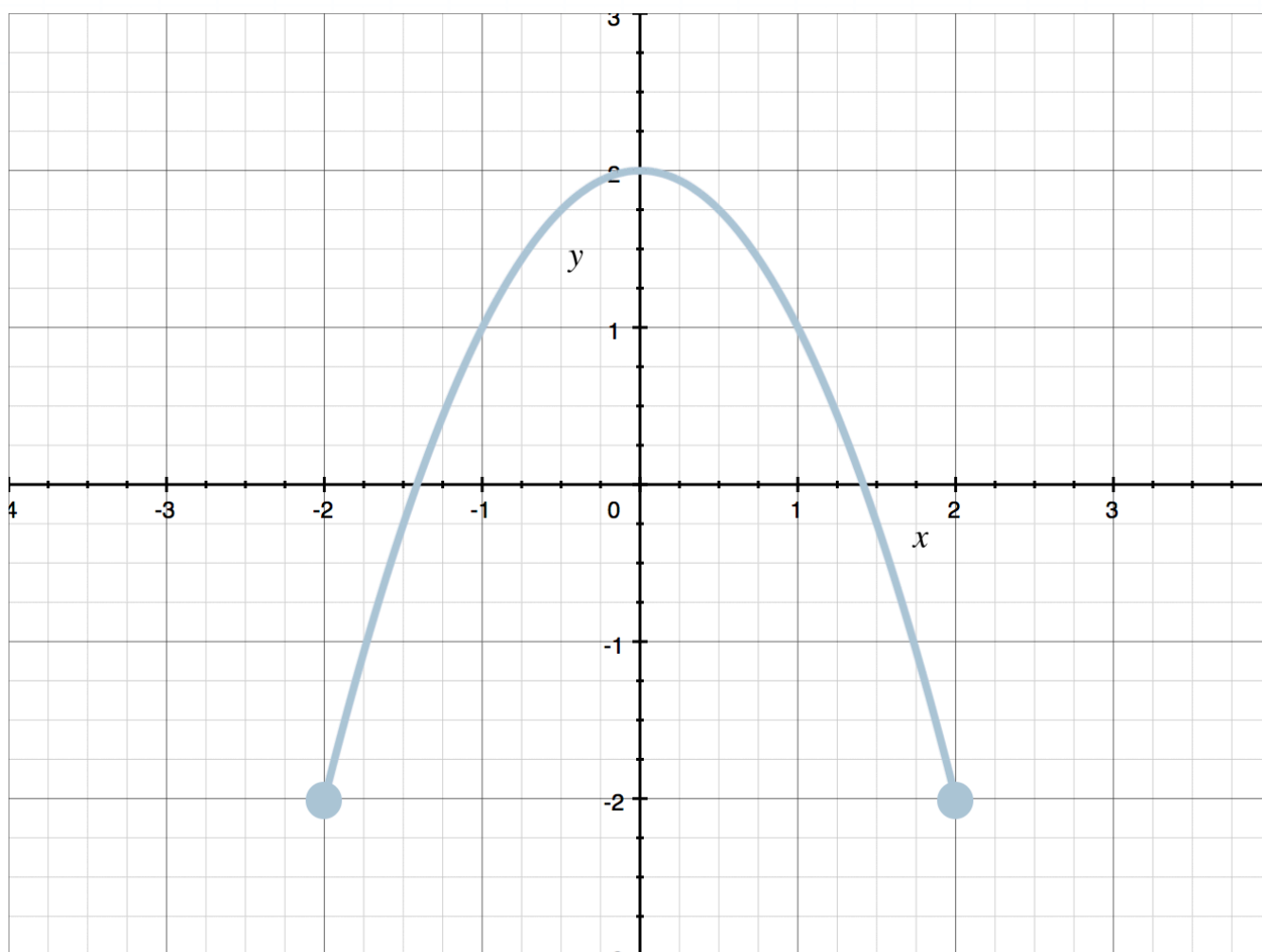
## EVEN, ODD, OR NEITHER

- 1. Is the function even, odd, or neither?

$$f(x) = -x^5 + 2x^2 - 1$$

- 2. Describe the symmetry of an even function, and give an example of an even function.

- 3. Determine if the graph is the graph of a function that is even, odd, or neither.



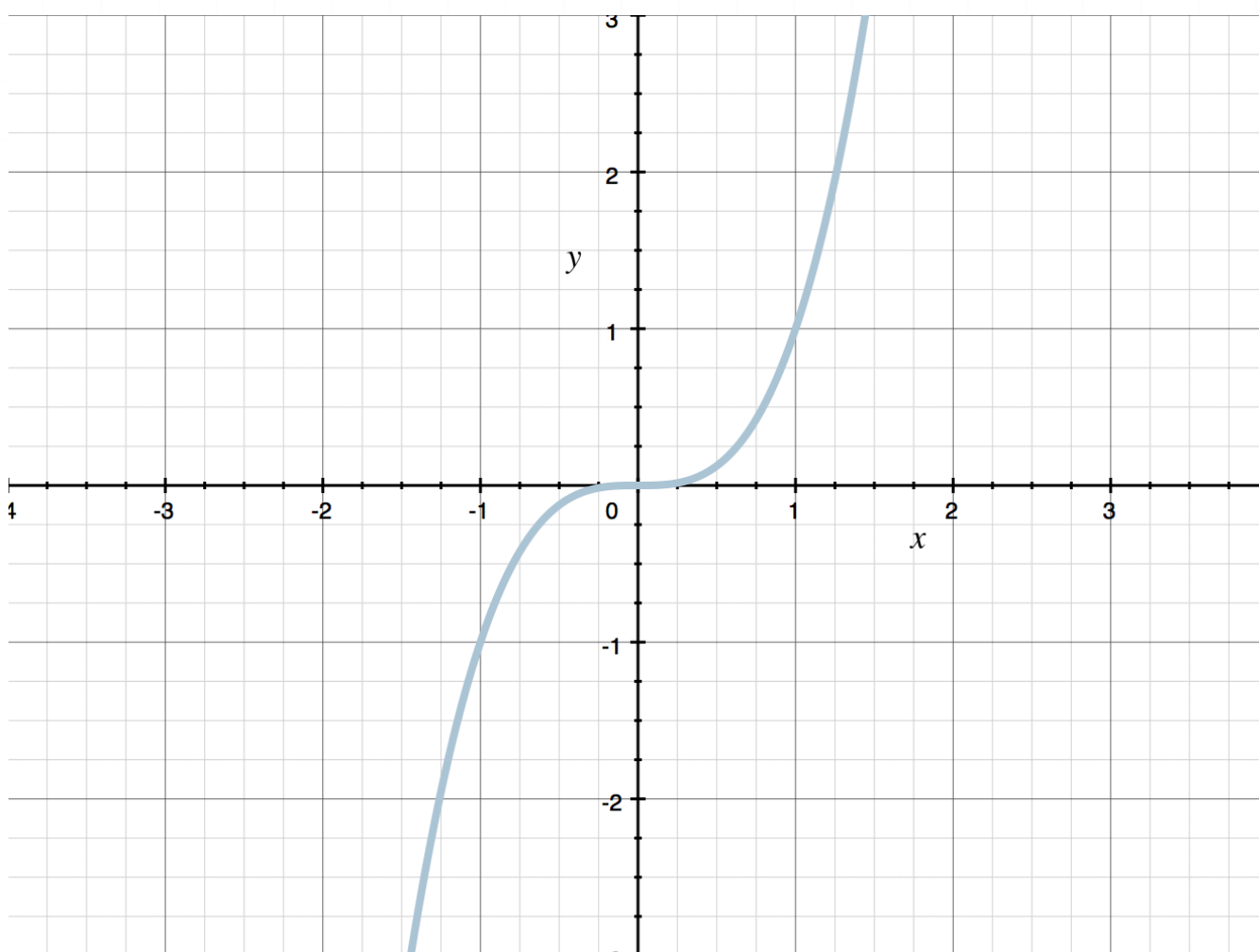
- 4. Is the function even, odd, or neither?

$$g(x) = -3x^2 + 5x^6$$

- 5. Show that the function is neither even nor odd.

$$f(x) = x^2 - 5x + 7$$

- 6. Determine if the graph is the graph of a function that is even, odd, or neither.





■ 7. Is the function even, odd, or neither?

$$h(x) = x^3 - 3x$$

■ 8. Describe the symmetry of an odd function, and give an example of an odd function.



## TRICHOTOMY

- 1. Solve the inequality.

$$2(x + 1) \not\leq -(8 - x)$$

- 2. If  $x \not\leq y$  and  $x \not> y$ , by the law of trichotomy, what do we know about the relationship between  $x$  and  $y$ ?

- 3. Give two ways to write the following sentence in mathematical notation.

“ $x^2$  is not greater than  $4y$  and is also not equal to  $4y$ .”

- 4. Solve the inequality.

$$x(3x - 2) \not\geq 3(x + x^2) + 10$$

- 5. Give the three possible relationships in the law of trichotomy.

- 6. Find a way to express the following relationships as one equality or inequality.



$$x^2 + x \not< 2 \text{ and } x^2 + x \not> 2$$

■ 7. Give two ways to write the following statement in mathematical notation.

“ $3(x + 1)$  is not less than  $-x - 5$  and is also not equal to  $-x - 5$ .”

■ 8. Solve the following statement.

$$-3(1 - x) \not> 3(7 - x) - 2x \text{ and } -3(1 - x) \not< 3(7 - x) - 2x$$



## INEQUALITIES AND NEGATIVE NUMBERS

- 1. Solve the inequality.

$$-3x + 4 < 22$$

- 2. What is the only difference between solving inequalities and solving equations? Give an example.

- 3. What went wrong in the following set of steps?

$$-5x + 6 < 9 - 2x$$

$$-3x < 3$$

$$x < -1$$

- 4. Solve the inequality.

$$-(5 - 2x) \geq 3(x - 3) + 2x$$

- 5. Of  $<$ ,  $>$ , or  $=$ , which sign is unaffected when solving inequalities? Give an example.



- 6. Solve the inequality.

$$-6x + 7 > -3x + 2$$

- 7. What went wrong in the following set of steps?

$$-2(x + 1) \geq 3(2 + x)$$

$$-2x - 2 \geq 6 + 3x$$

$$-2x - 3x - 2 \leq 6$$

- 8. Solve the inequality.

$$7(1 - x) \leq 2x$$



## GRAPHING INEQUALITIES ON A NUMBER LINE

- 1. Give two expressions that, when graphed, have open circles at 3.

- 2. Graph the inequality on a number line.

$$-2x < 4$$

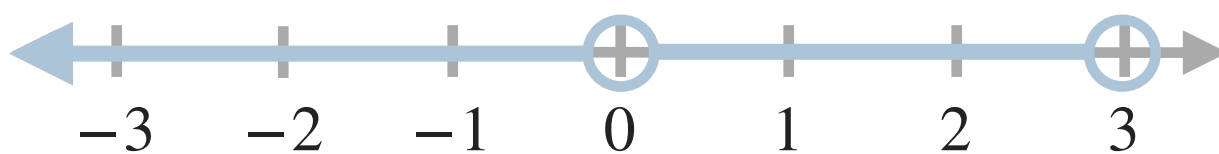
- 3. Graph the values of  $x$  that satisfy the following expressions.

$$x \leq 3 \text{ and } x \neq -2$$

- 4. Give two expressions that, when graphed, have closed circles at  $-1$ .

- 5. What is wrong with the graph of the following inequality?

$$x \leq 3 \text{ and } x \neq 0$$

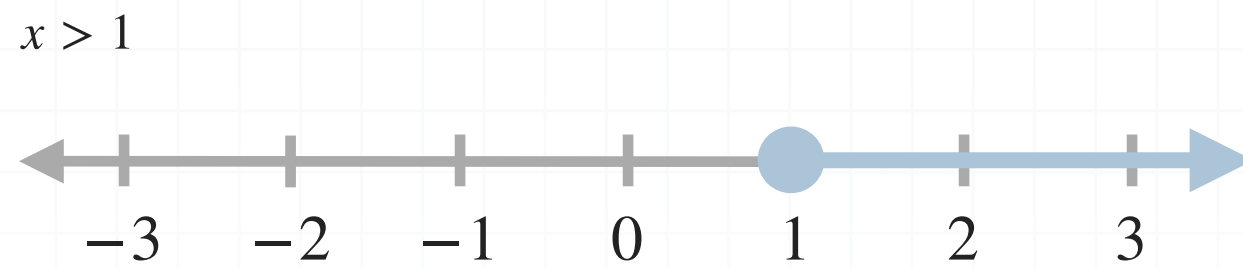


- 6. Graph the inequality on a number line.



$$x - 1 \geq 3$$

■ 7. What is wrong with the graph of the following inequality?



## GRAPHING CONJUNCTIONS ON A NUMBER LINE

- 1. Write the inequality that takes away the absolute value sign.

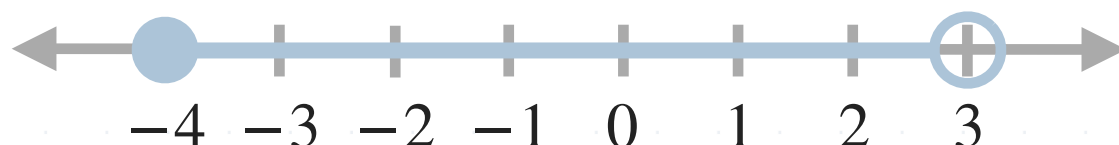
$$|3x - 7| \geq 2$$

- 2. Graph the inequality.

$$-8 \leq -2x < 10$$

- 3. What is wrong with the graph of the following inequality?

$$x \leq 3 \text{ and } x > -4$$



- 4. Graph the inequality.

$$x < 5 \text{ and } x \geq -3$$

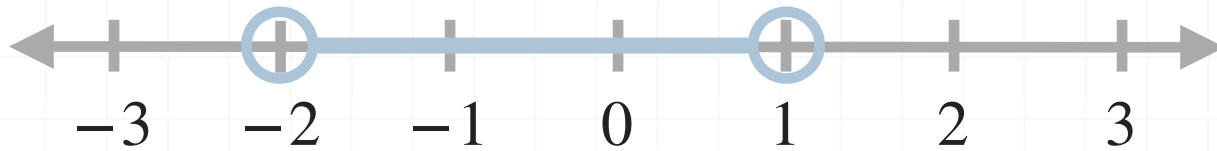
- 5. Give an example of a conjunction for which the graph is a line segment connecting two points.





- 6. What is wrong with the graph of the following inequality?

$$x < -2 \text{ and } x > 1$$



- 7. Graph the inequality.

$$|6 - 2x| \leq 4$$

- 8. Graph the inequality.

$$2x - 1 \geq 3 \text{ and } -x \geq -9$$



## CARTESIAN COORDINATE SYSTEM

- 1. What is the coordinate point of the origin?
- 2. Give a coordinate point that lies in Quadrant III.
- 3. Graph the point  $(-2, 3)$  in the Cartesian plane.
- 4. In which quadrant would you plot the point  $(1, 6)$ ?
- 5. What is the  $y$ -coordinate of the points that lie on the  $x$ -axis? Give an example of a coordinate point that lies on the  $x$ -axis.
- 6. Graph the point  $(3, -1)$  in the Cartesian plane.
- 7. Give a coordinate point that lies in Quadrant II.
- 8. Graph the point  $(-1, -5)$  in the Cartesian plane.



■ 9. In which quadrant would you plot  $(3, -7)$ ?

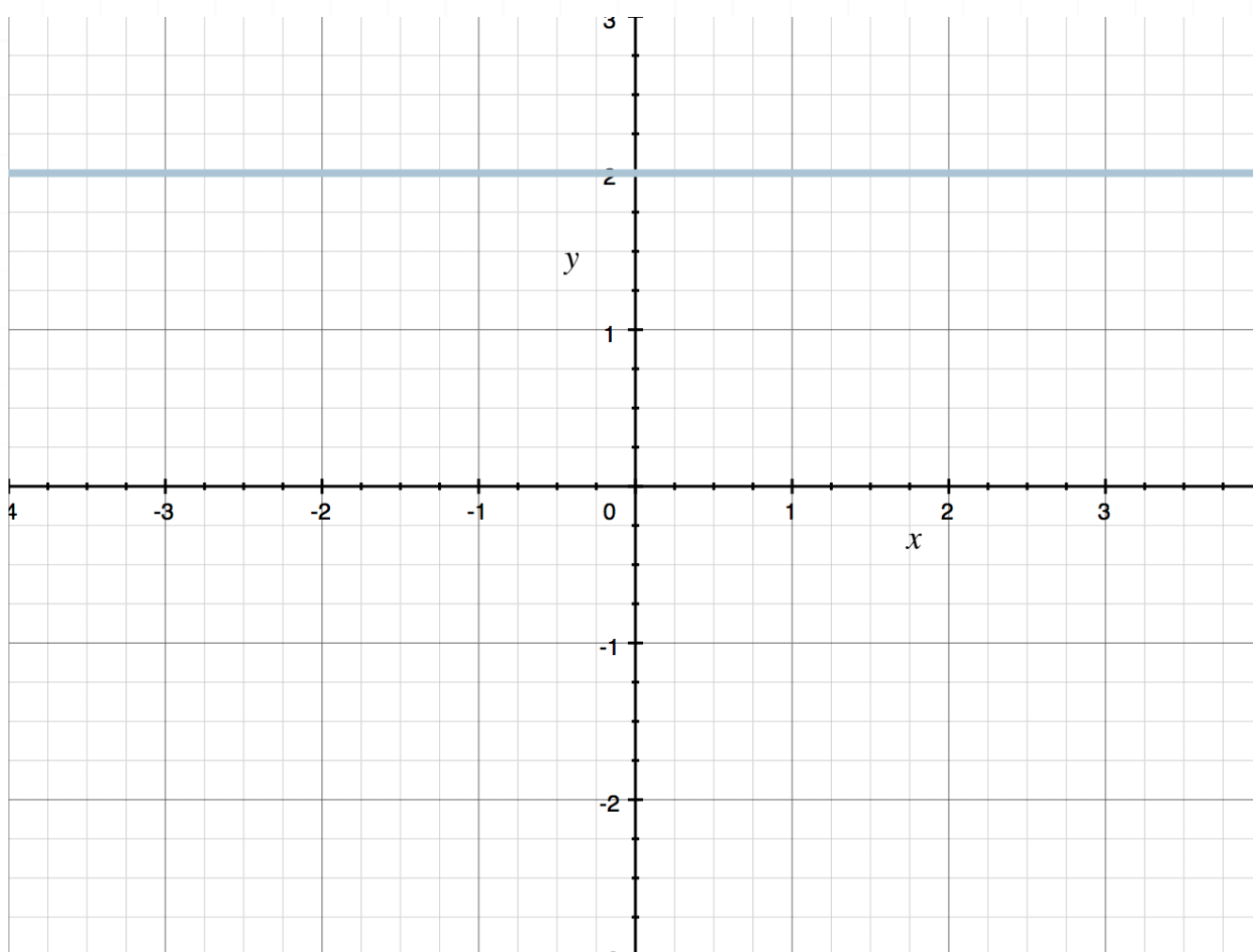
■ 10. What is the  $x$ -coordinate of the points that lie on the  $y$ -axis? Give an example of a coordinate point that lies on the  $y$ -axis.



## SLOPE

■ 1. In terms of vertical and horizontal movement, define the slope of a line.

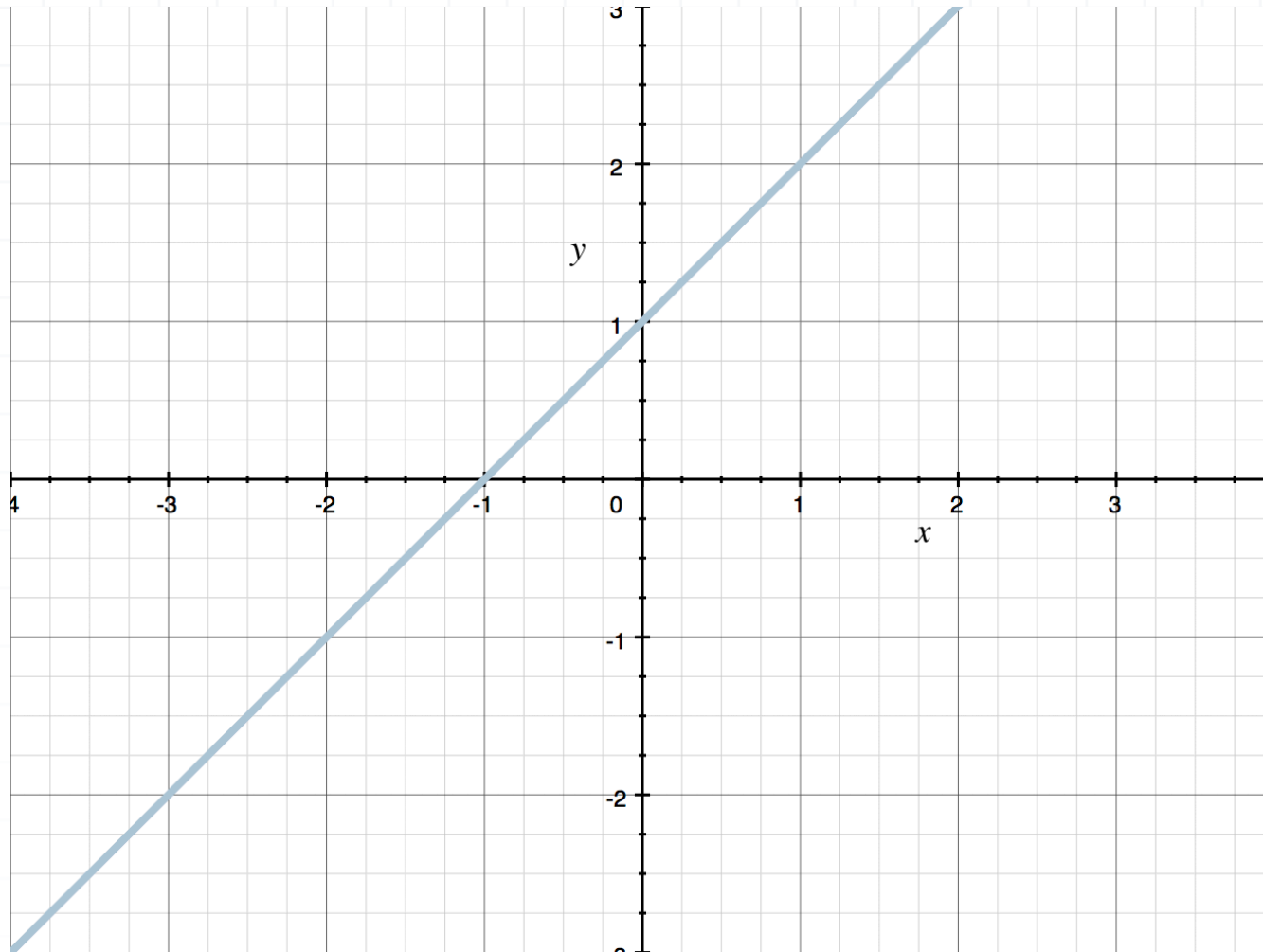
■ 2. What is the slope of the line?



■ 3. What direction is an undefined slope: horizontal or vertical? Use the formula for the slope to explain why.



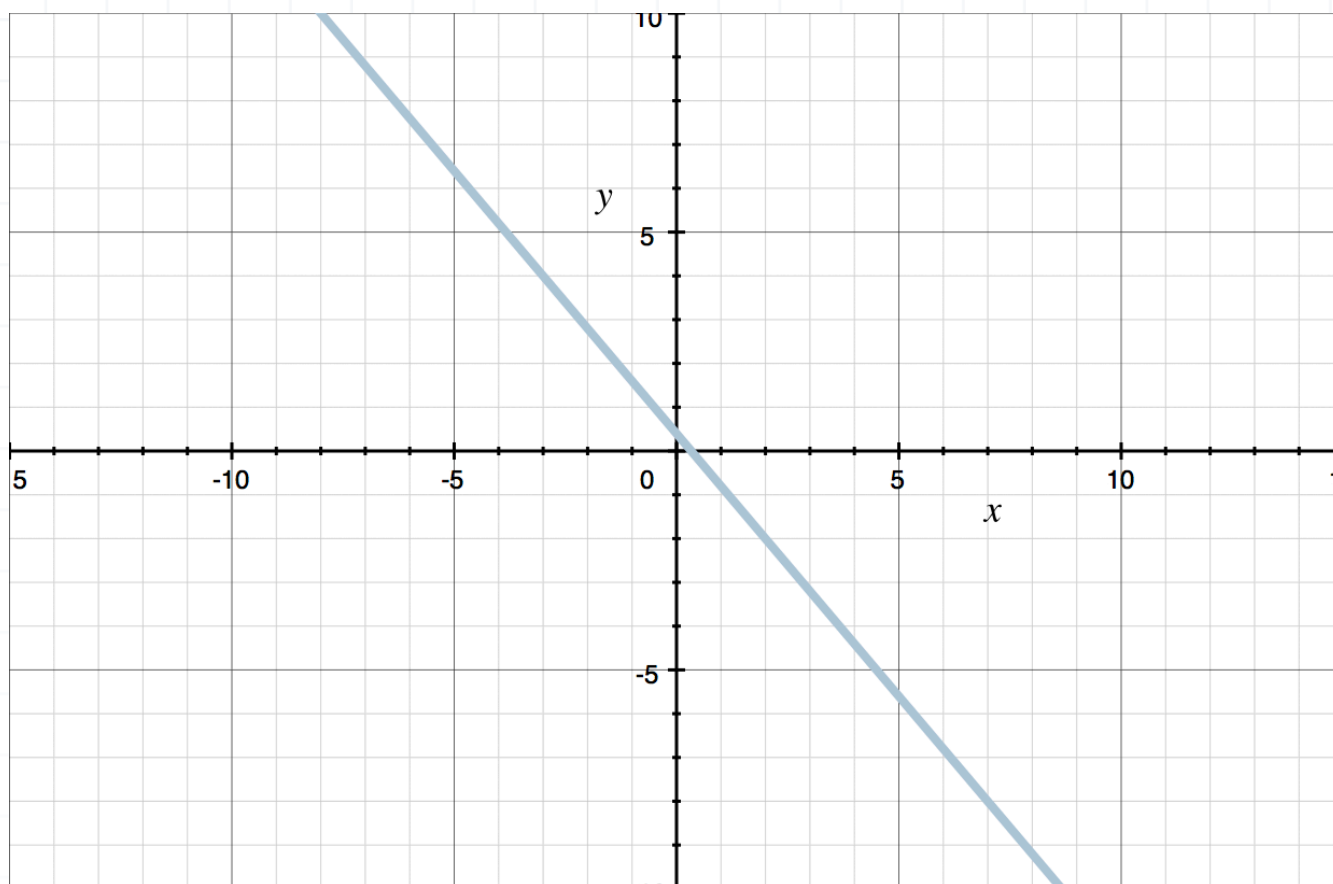
■ 4. What is the slope of the line?



■ 5. What is the slope of the line that passes through the points  $(-1, 3)$  and  $(4, -7)$ ?

■ 6. What is the slope of the line?





- 7. Find the slope of the line that passes through  $(10,1)$  and  $(5,2)$ .
- 8. Give two points that make a line with a slope of  $-2/3$ .
- 9. Find the slope of the line that passes through  $(3,5)$  and  $(-1,5)$ .
- 10. What is the slope of the line through the points  $(x_1, y_1)$  and  $(x_2, y_2)$ ?



## EQUATION OF A LINE IN POINT-SLOPE FORM

- 1. Find the equation of the line that passes through  $(3,0)$  with slope  $-2$ .
  - 2. Name two (of four possible) pieces of information about a line that are required to write an equation of the line in point-slope form.
  - 3. Find the equation of the line that passes through the points  $(-2,3)$  and  $(2, -4)$ .
  - 4. Find the equation of the line that passes through  $(-2, -5)$  with a slope 6.
- .....
- 5. Identify the point  $(x_1, y_1)$  and slope  $m$  in the equation of the line.

$$y + 3 = \frac{1}{4} (x - 6)$$

- 6. Write the following equation in point-slope form.

$$y = -\frac{1}{2} x + 4$$



■ 7. Find the equation of the line that passes through the points  $(5, -4)$  and  $(6,0)$ .





## EQUATION OF A LINE IN SLOPE-INTERCEPT FORM

■ 1. Find the equation of a line through the point (0,5) with slope  $-2$ . Write the solution in slope-intercept form.

■ 2. Identify the  $y$ -intercept and slope  $m$  defining the line.

$$y = -\frac{1}{4}(x + 12)$$

■ 3. Convert the following point-slope equation into a slope-intercept equation.

$$y - 3 = \frac{1}{3}(x - 6)$$

■ 4. Find the equation of a line that passes through the points (1,  $-1$ ) and (0,3). Write the solution in slope-intercept form.

■ 5. Determine the  $y$ -intercept of a line with slope  $-3$  that passes through the point (1,1). Write your solution as a coordinate point.



- 6. Name two (of four possible) pieces of information about a line that are required to write an equation of the line in point-slope form.
- 7. Find the equation of a line that passes through the points  $(-3, -2)$  and  $(2, -4)$ . Write the solution in slope-intercept form.



## GRAPHING LINEAR EQUATIONS

- 1. Graph the line.

$$y = \frac{4}{3}x - 1$$

- 2. Describe how you would use the slope to find another point on the graph if the slope is  $m = 2/3$  and the line passes through  $(x_1, y_1) = (-1, 2)$ .

- 3. What is the best way to write the equation of a line when graphing?

- 4. Graph the line.

$$y + 2 = -3x + 1$$

- 5. Give two points that lie on the line.

$$y = -x - 6$$



■ 6. Use the slope  $m = 1/3$  to find two more points on the line passing through  $(1,2)$ . Go forward to determine one point and backwards to determine another.

■ 7. Graph the line.

$$y = -2(3x + 1)$$

■ 8. Give two points that lie on the following line.

$$y + 3 = -\frac{1}{2}(4x + 10)$$



## GRAPHING LINEAR INEQUALITIES

- 1. Graph the inequality in the cartesian coordinate plane.

$$y < -2$$

- 2. Graph the inequality in the cartesian coordinate plane.

$$x \leq 5$$

- 3. Graph the inequality in the cartesian coordinate plane.

$$y < -2x + 4$$

- 4. Graph the inequality in the cartesian coordinate plane.

$$y \geq -\frac{1}{3}x + 5$$

- 5. Graph the inequality in the cartesian coordinate plane.

$$y \leq x - 1$$



- 6. Graph the inequality in the cartesian coordinate plane.

$$y > \frac{1}{2}x - 3$$

- 7. Graph the inequality in the cartesian coordinate plane.

$$y \geq 3x - 2$$



## 2-STEP PROBLEMS

- 1. Why can't you solve the following 2-step problem?

If  $2(x - 1) - 3 = 9 + x$ , what is  $y + 2$ ?

- 2. If  $5 - 2x = 17$ , what is  $x - 1$ ?

- 3. Describe in words how you would solve the following 2-step problem.

If  $x - 3 = 5$ , what is  $x + 5$ ?

- 4. If  $3(2 - x) + 5 = -(4x - 2)$ , what is  $(x/2) + 1$ ?

- 5. What are the two steps of a 2-step problem?

- 6. If  $2(x + y) - 6 = 3$ , what is  $x + y - 1$ ?

- 7. What went wrong in solving the following 2-step problem?

If  $2x + 3 = 7$ , what is  $x/3$ ?



$$2x + 3 = 7$$

$$2x = 4$$

$$\frac{x}{3} = \frac{4}{3}$$

■ 8. If  $a + 2b = 6 - a$  and  $b = 1$ , what is  $a/2$ ?





## SOLVING WITH SUBSTITUTION

- 1. Find the unique solution to the system of equations.

$$-x + 2y = 6$$

$$3x = y - 10$$

- 2. What is the easiest variable to get by itself? Set up but do not solve the substitution.

$$2y - x = 7$$

$$3x = 9 - 18y$$

- 3. Find the unique solution to the system of equations.

$$-5x + y = 8$$

$$y = 3x - 8$$

- 4. Find the unique solution to the system of equations.

$$3 - y = 2x$$

$$-4x + 10 = 2y$$



- 5. Fill in the blanks with the correct variables  $x$  and  $y$  if the solution to the system of equations is  $(-1, 3)$ .

$$-2 \_ + \_ = 5$$

$$2 \_ = 7 - 3 \_$$

- 6. What went wrong in the following substitution?

$$y = x - 2$$

$$2y - x = 7$$

Substitution:  $2x - 2 - x = 7$

- 7. Find the unique solution to the system of equations.

$$5y = 6 - 2x$$

$$6x + 15y = 18$$



## SOLVING WITH ELIMINATION

- 1. What is the easiest way to set up the elimination method for the system of equations? Set up but do not solve the elimination.

$$6y - 3x = 8$$

$$x - 4y = 5$$

- 2. Find the unique solution to the system of equations.

$$2x - y = 5$$

$$-3x + y = 7$$

- 3. Would it be easier to solve the system of equations using the substitution method or the elimination method?

$$7x - 3y = 2$$

$$3y - x = 11$$

- 4. What went wrong in the following elimination?

$$-4x + 3y = 7$$



$$-4x - y = 4$$

Elimination:  $2y = 3$

- 5. Find the unique solution to the system of equations.

$$x = 2y - 5$$

$$-3x + 6y = 15$$

- 6. Fill in the blanks with the correct variables  $x$  and  $y$  if the solution to the system of equations is  $(2/7, -18/7)$ .

$$3\_\_\_ - \_\_\_ = -8$$

$$-\_\_\_ = 10 + 4\_\_\_$$

- 7. Find the unique solution to the system of equations.

$$4 - 2x = 6y$$

$$7 = x + 3y$$

- 8. Would it be easier to solve the system of equations using the substitution method or the elimination method?



$$5y - x = 3$$

$$x = 7y - 10$$

- 9. Find the unique solution to the system of equations.

$$x = 2y - 8$$

$$3y = x + 5$$



## SOLVING THREE WAYS

- 1. Explain why using the graphing method would make the following system of equations easy to solve.

$$y = 3x - 4$$

$$y - 3 = 2(x + 1)$$

- 2. Find the unique solution to the system of equations using the elimination method.

$$2y = x + 5$$

$$3x - 2y = 11$$

- 3. In words, describe the graphical solution to a system of equations.

- 4. Find the unique solution to the system of equations using the substitution method.

$$5y + x = 4$$

$$3y - 3x = 6$$



■ 5. Explain why using the substitution method would make the system of equations easy to solve.

$$2y = 6 - 4x$$

$$7 - y = 3x$$

■ 6. In words, describe the solution to a system of equations.

■ 7. Explain why using the elimination method would make the system of equations easy to solve.

$$3y - 2x = 7$$

$$2x = 4 - 6y$$

■ 8. Find the unique solution to the system of equations using the graphing method.

$$y - 2 = -(x + 1)$$

$$y = x + 1$$



