

# Algebra 1 Workbook

**Operations** 



## **IDENTIFYING MULTIPLICATION**

- $\blacksquare$  1. Give three different examples of how you can write "a times b" mathematically.
- 2. Simplify the following expression.

$$5(2 \cdot 3) \times (1)(a)$$

■ 3. What number would make the expression true?

$$4 \times 3(1)(?? \cdot 1) = 24$$

■ 4. What term would make the expression true?

$$??(3 \cdot x) \times (5)(2) = 60x^2$$

- 5. Why do we have different ways to write multiplication?
- **6.** If  $(3)(x^2) = 10 \times 2$ , what does  $9x^2$  equal?

## THE ASSOCIATIVE PROPERTY

- 1. Give an example of an expression that demonstrates the associative property with multiplication.
- 2. What are the two main operations that the associative property works for?
- $\blacksquare$  3. Using the associative property, rewrite and simplify  $2 \times (3 \times 4)$ .
- 4. According to the associative property, what number would make the most sense in the expression?

$$42 + (31 + 17) = (42 + ??) + 17$$

- 5. What does the word "associate" refer to in math?
- $\blacksquare$  6. Rearrange (3+6)+2 using the associative property, then simplify.

- 7. Give an example of an expression that demonstrates the associative property with addition.
- 8. What number would make the following expression true?

$$(4 \times 2) \times 9 = ?? \times (2 \times 9)$$

■ 9. Give an example of an expression that does not demonstrate the associative property.



#### THE COMMUTATIVE PROPERTY

- $\blacksquare$  1. Using the commutative property, rewrite 6 + 19 and then simplify.
- 2. Give an example of an expression that demonstrates the commutative property with multiplication.
- 3. According to the commutative property, what number would make the most sense in the expression?

$$11 + (23 + 6) = 11 + (6 + ??)$$

- $\blacksquare$  4. Using the commutative property, rewrite  $3 \times 4$  and then simplify.
- 5. Rearrange (3+6)+2 using the commutative property and then the associative property.
- 6. Give an example of an expression that demonstrates the commutative property with addition.

■ 7. What number would make the following expression true?

$$(4 \times 2) \times 9 = (?? \times 9) \times 4$$

■ 8. What are the two main operations that the commutative property works for?



# THE TRANSITIVE PROPERTY

- $\blacksquare$  1. If AB = CD and CD = EF then what is the value of EF?
- $\blacksquare$  2. If x=2 and y=x, then what does the transitive property tell us?
- 3. According to the transitive property, if x = 2y and 2y = 5z, then what is the value of x?
- 4. Give an example that demonstrates the transitive property.
- $\blacksquare$  5. Use the transitive property to solve for z.

$$x = y$$

$$y = 3 - z$$

$$x = -2z + 7$$

■ 6. Transitive comes from the word "transit," which means, to what?

■ 7. By the transitive property, what expression would make the following statement true?

If 
$$2 + 3 = ??$$
 and  $4 + 1 = 5$ , then  $2 + 3 = 5$ .

 $\blacksquare$  8. Use the transitive property to solve for x.

$$y = 2x + 3$$

$$y = z$$

$$z = 5x - 9$$

■ 9. According to the transitive property, what expression would make the most sense in the following statement?

If 
$$x = 2y$$
 and  $2y = ??$ , then  $x = 5z$ .

## THE DISTRIBUTIVE PROPERTY

 $\blacksquare$  1. Use the distributive property to solve for x.

$$5(x-2) = \frac{1}{2}(6-2x)$$

2. Use the distributive property to expand the expression.

$$-\frac{2}{5}(10-5x)$$

■ 3. Give an example that demonstrates the distributive property with subtraction.

- 4. What three main operations are used in the distributive property?
- 5. What does distributing remove from the expression?
- $\blacksquare$  6. Use the distributive property to solve for x.

$$2(5 - 3x) = x - 4$$



# ■ 7. What value would make the following expression true?

$$2(x+3) = ?? + 6$$



## THE DISTRIBUTIVE PROPERTY WITH FRACTIONS

1. Perform the indicated operation and then simplify.

$$\frac{4y^3z^2}{3x} \times \frac{x^2y}{2z^2}$$

■ 2. Use the distributive property to expand the expression.

$$-\frac{x^2z}{y^3}\left(\frac{y^2}{2}-\frac{xz^3}{z^2}\right)$$

■ 3. Fill in the blank with the correct words: When we are distributing fractions, we multiply the outside numerator with the \_\_\_\_\_ of the terms inside the parentheses and the outside denominator with the \_\_\_\_\_ of the inside terms.

 $\blacksquare$  4. Use the distributive property to solve for x.

$$-\frac{3xy^2}{z}\left(\frac{2z}{3y^2} - z\right) = 3(3 + xy^2)$$

■ 5. Use the distributive property to show that x = -10.

$$\frac{2}{3}\left(\frac{x}{2} - 6\right) = 4\left(\frac{x}{3} + \frac{3}{2}\right)$$

■ 6. Explain why the two sides of the equation aren't equal to one another.

$$\frac{3}{2}\left(\frac{x}{5} - \frac{y}{2}\right) \neq \frac{3x}{10} - \frac{y}{2}$$

■ 7. What term would make the following expression true?

$$\frac{2ab}{c^2} \left( \frac{3ac}{b} + a^2 c^2 \right) = \frac{6a^2}{c} + ??$$

8. What term would make the following expression true?

$$\frac{??}{??}\left(\frac{2x}{z} + y^2\right) = \frac{2x^3}{3z^2} + \frac{x^2y^2}{3z}$$



# THE DISTRIBUTIVE PROPERTY AND BINOMIAL MULTIPLICATION

1. Perform the indicated operation and simplify.

$$(x-1)(x+4)$$

- 2. How many terms does a binomial have?
- 3. Use the distributive property to expand the expression.

$$4(2-x)(3+2x)$$

■ 4. What term would make the following expression true?

$$(2x+1)(5-x) = ?? + 10x - x + 5$$

 $\blacksquare$  5. Use the distributive property to show that x = 3.

$$2(x-1)(x+1) = 2x^2 + x - 5$$

**6.** Explain why  $(x-2)(x+1) \neq x^2 - 2$ .

7. Use the distributive property to expand the expression.

$$\frac{1}{2}(6x+4)(x-1)$$

8. What term would make the following expression true?

$$(3+x)(??) = 3x + 3 + x^2 + x$$



## GROUPING SYMBOLS WITH PEMDAS AND ORDER OF OPERATIONS

1. Write the expression with parentheses.

$$\frac{a}{b+c}$$

2. Simplify the expression.

$$2([3+1]-4)-[6+3]$$

■ 3. Put in grouping symbols that will make the equation true.

$$2x + 1/3 + 5x - 2 = \frac{2(x+1)}{3+5x-10}$$

4. Simplify the expression.

$$|2(1-4)| - (2-5)[(-1)(3+2) + 9]$$

■ 5. What number would make the expression true?

$$(3+1)[2(??-5)+7] - |(4-6)| = 4[-2+7] - |-2|$$

- 6. Give three different examples of a grouping symbol.
- 7. Rewrite the following as a fraction.

$$[2(x+1)-3]/[5x-3(4x)]$$

8. Simplify the following expression.

$$\sqrt{2(5-3)} - |3[6-7]|$$

■ 9. Using PEMDAS, evaluate each expression separately to show that they are not equal.

$$4 \times (3-1) - (4 \div 2 + 2)$$
 and  $(4 \times 3 - 1) - 4 \div (2 + 2)$ 

10. Use the order of operations to simplify the expression.

$$(10 - [(-1)^2 + 1 - 6 \div 6])^{1/2} + 4 \div 2$$

■ 11. What do the letters in PEMDAS stand for?

12. What number would make the equation true?

$$2^{2} + 4 \cdot [(2 - ??) \div | -4|] = 4 + 4 \cdot [1 \div 4]$$

■ 13. Use the order of operations to simplify the expression.

$$3 - [(-2)^2x + (3-7)]$$

- 14. Using the order of operations, explain why  $9 + 6 \div 3 \neq 5$ .
- 15. Put symbols of inclusion that make the equation true.

$$4-5 \ 3 \ x+-1^2 = 4-15x-5$$

- 16. What operations must be performed before multiplication and division?
- 17. Using the order of operations, explain why  $\sqrt{(2+7)} \neq \sqrt{2} + \sqrt{7}$ .
- 18. Simplify this expression.

$$3\{2[4+3(7-5)-4]\}$$

■ 19. Use the order of operations to simplify the expression.

$$3 + 2(x + 1)$$

20. Use order of operations to simplify the expression.

$$\frac{-2+3-10\cdot 2\cdot \left[ (5-4)+2\right] }{2}$$

## **UNDERSTOOD 1**

- **1.** What is x + 4x + x + x?
- 2. What happens when you multiply something by 1?
- 3. Simplify the following expression.

$$\frac{1x^1}{1(1^1)} + \frac{1}{1(1x)} - 1^1$$

■ 4. What number would make the expression true?

$$1(2^1) - \frac{1}{1(1)^1} + \frac{??^1}{1 \times 1} = 4$$

■ 5. Simplify the following expression.

$$x(x^2 + 3x^2) - x^3$$

■ 6. Simplify the following expression.

$$\frac{x^1}{4x^3} + \frac{5x^4}{1x}$$

- 7. Give an example of an expression where it would be useful to write out the understood 1.
- 8. Simplify the following expression.

$$\frac{x}{1^1} \cdot \frac{x^2 + 1(1)}{5x^2}$$



