

Algebra 2 Final Exam Solutions

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Algebra 2 Final Exam Answer Key

- 1. (5 pts)
- Α
- В
- D
- E

E

- 2. (5 pts)

- 3. (5 pts)

- 4. (5 pts)
- В
- D

- 5. (5 pts)
- В
- C
- D
- Ε

- 6. (5 pts)
- В
- Е

- 7. (5 pts)

- 8. (5 pts)

- 9. (15 pts)
- (4,6) and (-1, -4)
- 10. (15 pts)
- $\frac{-21-i}{13}$
- 11. (15 pts)
- 30 miles
- 12. (15 pts)

$$f(g(x)) = \frac{4x}{1+2x}$$
 with $x \neq -1/2$, 0

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1. C. If the woman spends x to make the soap and marked it up by 72%, then the price she's selling it to customers for is 1.72 times the cost to make it.

$$1.72x = $18$$

$$\frac{1.72x}{1.72} = \frac{\$18}{1.72}$$

$$x = $10.47$$

It costs the woman \$10.47 to make a 4-pack of soap. Her markup is 72%, or \$10.47(0.72) = \$7.53, and she sells the soap for \$18.

2. B. Multiply by the conjugate of the denominator.

$$\frac{4-\sqrt{2}}{\sqrt{2}+3}$$

$$\frac{4-\sqrt{2}}{\sqrt{2}+3}\cdot\frac{\sqrt{2}-3}{\sqrt{2}-3}$$

Use FOIL to multiply the numerators and denominators.

$$\frac{(4-\sqrt{2})(\sqrt{2}-3)}{(\sqrt{2}+3)(\sqrt{2}-3)}$$



$$\frac{4\sqrt{2} - 12 - 2 + 3\sqrt{2}}{2 - 3\sqrt{2} + 3\sqrt{2} - 9}$$

$$\frac{-14+7\sqrt{2}}{-7}$$

$$\frac{14-7\sqrt{2}}{7}$$

3. A. Square both sides of the equation.

$$\sqrt{x^2 - 10x - 16} = x - 4$$

$$(\sqrt{x^2 - 10x - 16})^2 = (x - 4)^2$$

The square and square root will cancel on the left. Use FOIL to expand the right side of the equation.

$$x^2 - 10x - 16 = x^2 - 4x - 4x + 16$$

$$x^2 - 10x - 16 = x^2 - 8x + 16$$

Solve for *x*.

$$x^2 - x^2 - 10x - 16 = x^2 - x^2 - 8x + 16$$

$$-10x - 16 = -8x + 16$$

$$-2x - 16 = 16$$

$$-2x = 32$$



$$x = -16$$

4. E. Direct variation is modeled by x = ky. If we let w be weight and d be distance, we can write w = kd. Plugging the pair (d, w) = (4,120) into the direct variation equation gives

$$120 = k \cdot 4$$

$$k = 30$$

Plugging in the other value of w (135) and k = 30 gives

$$135 = 30d$$

$$d = 4.5$$
 inches

5. A. Remember that the standard form of a quadratic expression is $ax^2 + bx + c$. For the equation $8x^2 - 10x + 3$, we identify a = 8, b = -10, and c = 3. Multiply $a \cdot c$ to get $8 \cdot 3 = 24$, then find factors of the result that combine to b. We'll make a table with all of the factors, and their sum.

Factors of 24	Sum
-1, -24	-25
-2, -12	-14
-3, -8	-11
-4, -6	-10



We know -4 + -6 = -10, so they're the factors we're looking for. Now we'll divide each factor by a and reduce the fractions, if possible.

$$\frac{-4}{8} = \frac{-1}{2}$$

One factor of the quadratic is (2x - 1) because the denominator of the reduced fraction becomes the coefficient on x. Then we add or subtract the numerator depending on the sign (in this case we'll subtract since -1 was the numerator).

$$\frac{-6}{8} = \frac{-3}{4}$$

The other factor of the quadratic is (4x - 3) because the denominator of the reduced fraction becomes the coefficient on x. Then we add or subtract the numerator depending on the sign (in this case we'll subtract since -3 was the numerator).

$$(2x-1)(4x-3)$$

Use FOIL to check your work.

6. D. Substitute 4x + 3 for x into f(x).

$$f(g(x)) = (4x + 3)^2 + 4(4x + 3) - 7$$

$$f(g(x)) = (16x^2 + 24x + 9) + (16x + 12) - 7$$

$$f(g(x)) = 16x^2 + 40x + 14$$



$$f(g(x)) = 2(8x^2 + 20x + 7)$$

7. C. Use these two rules to evaluate the expression.

$$\log_a x + \log_a y = \log_a xy$$

If
$$\log_a y = x$$
, then $a^x = y$.

Applying the first rule to the given expression gives

$$\log_2 \frac{1}{8} + \log_2 16$$

$$\log_2\left(\frac{1}{8}\cdot 16\right)$$

$$log_2 2$$

It's probably obvious from this that $\log_2 2 = 1$, but if not, use the second rule above. If we let $x = \log_2 2$, then

$$2^{x} = 2$$

$$x = 1$$

8. A. Switch x and y in the original equation.

$$y = \frac{x - 2}{3}$$

$$x = \frac{y - 2}{3}$$

Solve for *y*.

$$3x = y - 2$$

$$3x + 2 = y$$

9. Use the second equation to solve for y.

$$y - 2x = -2$$

$$y = 2x - 2$$

Plug y = 2x - 2 into the first equation and solve for x.

$$y = x^2 - x - 6$$

$$2x - 2 = x^2 - x - 6$$

$$0 = x^2 - 3x - 4$$

$$0 = (x - 4)(x + 1)$$

$$x = 4$$
 and $x = -1$

Plug x = 4 into the equation where we've already solved for y.

$$y = 2(4) - 2$$

$$y = 6$$

Plug x = -1 into the equation where we've already solved for y.

$$y = 2(-1) - 2$$

$$y = -4$$

The solutions are

$$(4,6)$$
 and $(-1, -4)$

10. Simplify the powers of *i* by remembering that $i^2 = -1$.

$$\frac{3+5i}{3i^3+2i^6}$$

$$\frac{3+5i}{3(-1)i+2(-1)(-1)(-1)}$$

$$\frac{3+5i}{-3i-2}$$

$$\frac{3+5i}{-2-3i}$$

Use the conjugate method to get the imaginary number out of the denominator.

$$\frac{3+5i}{-2-3i} \cdot \frac{-2+3i}{-2+3i}$$

$$\frac{(3+5i)(-2+3i)}{(-2-3i)(-2+3i)}$$



Use the FOIL method to multiply the binomials in the numerator and denominator.

$$\frac{-6 + 9i - 10i + 15i^2}{4 - 6i + 6i - 9i^2}$$

$$\frac{-6 - i + 15i^2}{4 - 9i^2}$$

Plug in
$$i^2 = -1$$
.

$$\frac{-6 - i + 15(-1)}{4 - 9(-1)}$$

$$\frac{-21-i}{13}$$

11. We'll use the formula for distance.

$$Distance = Rate \times Time$$

$$D = RT$$

Sam's rate is 20 mph, and his time is 1.5 hours. Therefore,

Distance =
$$20 \frac{\text{miles}}{\text{hour}} \times 1.5 \text{ hours}$$

Distance =
$$\frac{20 \cdot 1.5 \text{ miles} \cdot \text{hour}}{\text{hour}}$$

Distance =
$$\frac{30 \text{ miles} \cdot \text{hour}}{\text{hour}}$$



Distance = 30 miles

12. First, find the domain of g(x). The expression 1/x is undefined if the denominator is 0. That means x = 0 isn't in the domain of g(x). Therefore, the domain of g(x) is all real numbers x such that $x \neq 0$.

The algebraic expression for the composite function is

$$f(g(x)) = \frac{4}{\frac{1}{x} + 2}$$

$$f(g(x)) = \frac{4}{\frac{1}{x} + 2\left(\frac{x}{x}\right)}$$

$$f(g(x)) = \frac{4}{\frac{1+2x}{x}}$$

$$f(g(x)) = 4 \cdot \frac{x}{1 + 2x}$$

$$f(g(x)) = \frac{4x}{1 + 2x}$$

The domain of a rational functions is all real numbers such that the denominator is not equal to 0.

$$1 + 2x \neq 0$$

$$2x \neq -1$$



$$x \neq -\frac{1}{2}$$

Putting both exclusions together, the domain of the composite function is all real numbers except -1/2 and 0, so

$$f(g(x)) = \frac{4x}{1+2x}$$
 with $x \neq -1/2$, 0



