

Probability Assignments.

Basic Probability

* 1. Two dice are rolled at once. Find out the prob. for sum of nos. being even and one of the die shows 6.

$$\begin{aligned} & * P(\text{Sum of } \times \text{ being even}) \\ &= \frac{\text{No. of fav. outcomes}}{\text{All possible outcomes}} \\ &= \frac{18}{36} \\ &= \frac{1}{2} \end{aligned}$$

		Die 1					
		1	2	3	4	5	6
Die 2	1	2	3	4	5	6	7
	2	3	4	5	6	7	8
	3	4	5	6	7	8	9
	4	5	6	7	8	9	10
	5	6	7	8	9	10	11
	6	7	8	9	10	11	12

↑
even \times

$$\begin{aligned} & * P(6 \text{ at least in one die}) = 1 - P(\text{Not } 6 \text{ in die 1}) \times P(\text{not } 6 \text{ in die 2}) \\ & \quad \text{getting} \quad \text{getting} \\ &= 1 - \left(\frac{5}{6}\right) \times \left(\frac{5}{6}\right) \\ &= 1 - \frac{25}{36} \\ &= \frac{11}{36} \end{aligned}$$

* 2. Two dice are rolled at once. Find out the prob. for sum of no. being less than 7.

$$\begin{aligned} P(\text{Sum less than 7}) &= \frac{\text{No. of fav outcomes}}{\text{All poss. outcomes}} \\ &= \frac{15}{36} \\ &= \frac{5}{12} \end{aligned}$$

#3. You toss a fair coin three times: Given that you have observed at least one heads, what is the prob. that you observe at least two heads?

\checkmark
 \underline{HHH} \underline{THH}
 \underline{HHT} \underline{THT}
 \underline{HTH} \underline{TTH}
 HTT TTT

$$P(\text{at least 1 heads}) = 7/8$$

$$P(\text{at least 2 heads}) = 4/8$$

$$P(2 \text{ heads} / 1 \text{ heads}) = 4/8 / 7/8 = 4/7$$

#4. A and B are married couple with two kids. One of them is a girl. What is the prob. that ^{Other} their kid is also girl?

$$P(\overset{\text{at least}}{1} \text{ Girl}) = 3/4$$

$$P(2 \text{ Girl}) = 1/4$$

$$P(2 \text{ Girl} / 1 \text{ Girl}) = \frac{1/4}{3/4}$$

$$= 1/3$$

$\left\{ \begin{array}{l} \text{GG} \\ \text{GB} \\ \text{BG} \\ \text{BB} \end{array} \right.$