

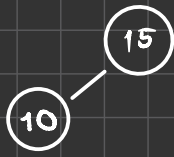
8. (2019)

The starting heap (tree form)



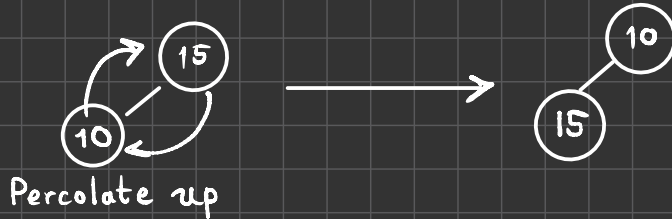
Add 10

Since this is a min-heap 10 must be above 15 so  
First insert 10 into the last available node



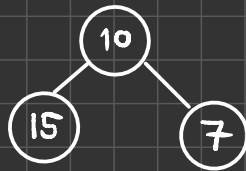
Note that I use only a single line  
to represent both node pointers  
this is for readability

Then percolate up 10 to maintain heap property, the resulting heap

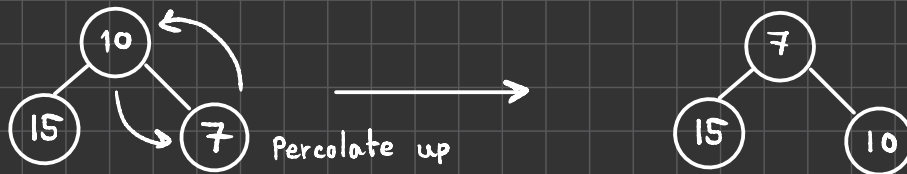


Add 7

Since 7 is less than 10 do the same as add 10, First insert at  
last available node

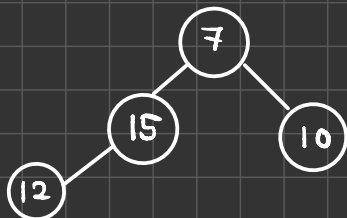


Then percolate up 7

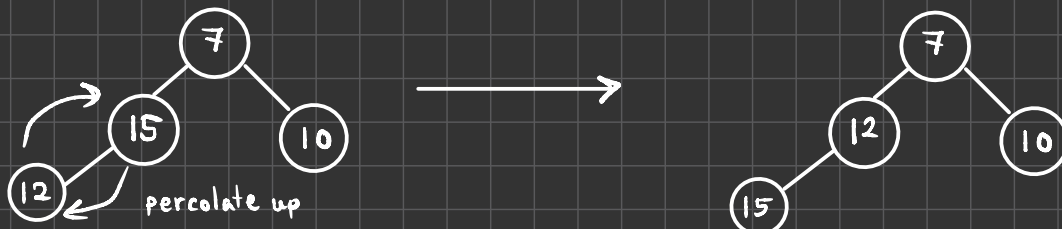


Add 12

First insert 12 at last available node



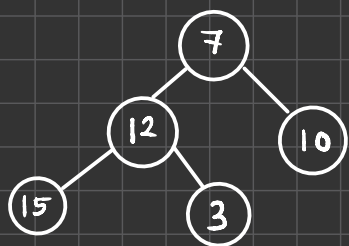
Then because  $15 > 12$  violates heap property perlocate up 12



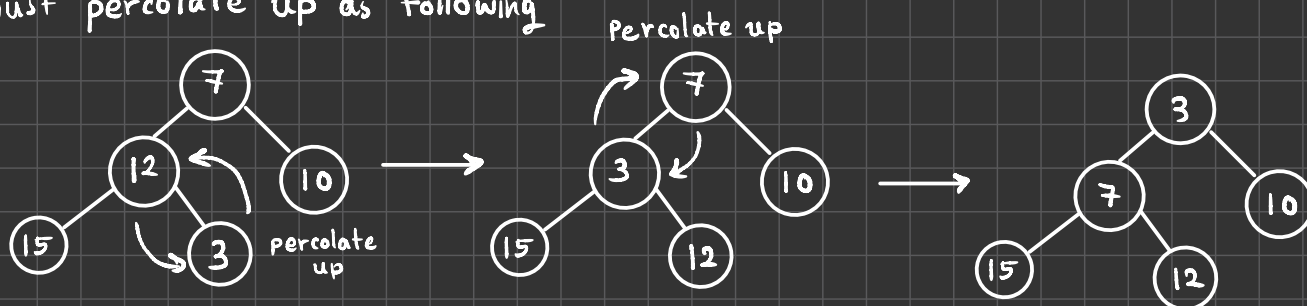
And since  $7 < 12$  12 is in the correct position

### Add 3

First insert 3 at last available node



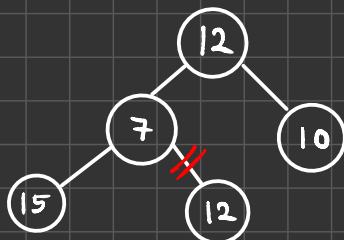
Since  $3 < 12$  and  $3 < 7$  this violate heap property. 3 must percolate up as following



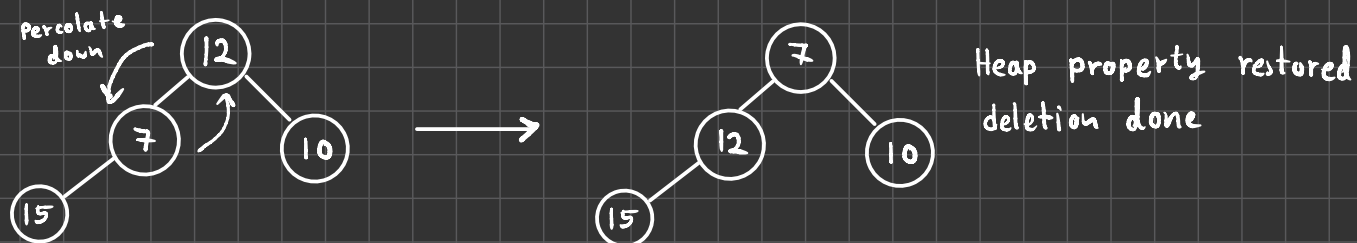
### Remove most important value

In this case remove 3

First overwrite 3's node with the last data 12, then remove pointers of the last node (make 0 in array case)

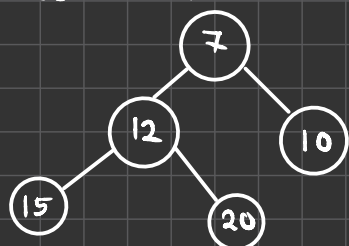


Then percolate down 12 until heap property is restored



### Add 20

Add 20 to available node

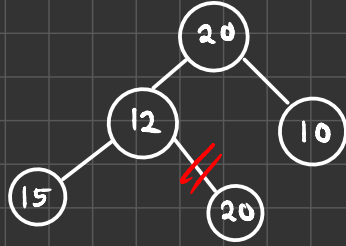


No heap property violated  
Insertion done.

## Remove most important value

In this case remove 7

First overwrite 7 with last node 20 and delete connection of 20's node



Since  $20 > 12$  &  $20 > 15$  heap property is violated percolate down 20

