```java
public static int[] makeHeap3(int[] a){
    //? This is probably the best solution
    for(int i =a.length/2-1;i>=0;i--){
        heapify(a,a.length,i);

    }
    return a;
}
```

→ Start at the last non leaf node
→ call heapify on each root.

```java
public static void heapify(int[] a,int size,int root){
    int minimum = root;
    int left = 2*root+1;
    int right = 2*root+2;
    if(left<size && a[left]<a[minimum]){
        minimum =left;
    }
    if(right<size && a[right]<a[minimum]){
        minimum =right;
    }
    if(minimum!=root){
        int temp = a[root];
        a[root] = a[minimum];
        a[minimum] = temp;

        heapify(a,size,minimum);
    }

}
```

→ Intitialize min index as root

} Its left & right child index

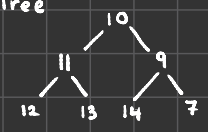
} Ensuring the index is less than the size of the array.
If the child is less than current minimum change minimum's index

} If the minimum index isn't root (root is already heapified)
then swap data of the root & minimum index
and call heapify on the minimum index

Example

array = [10, 11, 9, 12, 13, 14, 7]

Tree




```java
for(int i =a.length/2-1;i>=0;i--){
    heapify(a,a.length,i);
}
```

Start $i = \frac{7}{2} - 1$
$= 3 - 1$
$= 2$

array = [10, 11, 9, 12, 13, 14, 7]

Tree

heapify (array, 7, 2)

heapify (array, 7, 2)

```java
public static void heapify(int[] a,int size,int root){
    int minimum = root;
    int left = 2*root+1;
    int right = 2*root+2;
```

minimum ↓ Left ↓ Right ↓

array = [10, 11, 9, 12, 13, 14, 7]

Tree

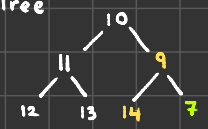

```java
if(left<size && a[left]<a[minimum]){
    minimum =left;
}
if(right<size && a[right]<a[minimum]){
    minimum =right;
}
```

← condition met

root ↓ Left ↓ minimum ↓

array = [10, 11, 9, 12, 13, 14, 7]

Tree




```java
if(minimum!=root){
    int temp = a[root];
    a[root] = a[minimum];
    a[minimum] = temp;

    heapify(a,size,minimum);
}
```

← condition met

} swap

→ heapify (array, 7, 6) [Does nothing]

array = [10, 11, 7, 12, 13, 14, 9]

Tree

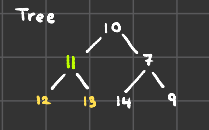
heapify (array, 7, 1) [Does nothing]

```java
public static void heapify(int[] a,int size,int root){
    int minimum = root;
    int left = 2*root+1;
    int right = 2*root+2;
```

min ↓ Left ↓ right ↓

array = [10, 11, 7, 12, 13, 14, 9]

Tree



heapify (array, 7, 0)

```java
public static void heapify(int[] a,int size,int root){
    int minimum = root;
    int left = 2*root+1;
    int right = 2*root+2;
```

array = [10, 11, 7, 12, 13, 14, 9]

Tree

Swap occur and

array = [7, 11, 10, 12, 13, 14, 9]

Tree

heapify (array, 7, 2) called and swap occur.

array = [7, 11, 9, 12, 13, 14, 10]

Tree

array = [7, 11, 9, 12, 13, 14, 10]

Done!

Tree