Agnostic Language Bias

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In this paper I show that Agnosticism of any kind has a language bias that can not use excluded middle and the Sesh axiom at the same time. It is fine to use either, but not both.

In the debate about Theism vs Atheism vs Agnosticism, I came across a discussion where a person used sets to clarify the positions why Atheism is distinct from Agnosticism[1]:

- Theist: Anyone who believes it is more probable than not that a deity exists.
- Atheist: Anyone who is not in the set "theist".
- Gnostic: Anyone who makes the positive claim that a deity does or does not exist.
- Agnostic: Anyone who is not in the set "gnostic".

The problem is that Agnostics might agree with the proposition that a deity either exists or does not exists, given that the deity is well defined. The argument is clear for a debate, but formally I think it is ambiguous and upon exploring what this meant in logic, I came up with the following proof:

∵	!~(Theism^true) & !~(false^Theism)	
∴	~!(Theism^true) & !~(false^Theism)	using Sesh
∴	~(false^Theism) & !~(false^Theism)	using excluded middle
∴	false	

The result is that Agnosticism has a language bias built into it that can not allow use of excluded middle and the Sesh axiom at the same time.

The excluded middle is an axiom, which in HOOO EP[2] is written as following:

(a | !a)^true   for all `a`

The Sesh axiom in HOOO EP (for more information, see "Overview of Path Semantical Logics"[3]):

(!~a == ~!a)^true   for all `a`

Most logicians know that when excluded middle is added to constructive logic, one gets classical logic. However, the Sesh axiom is much more mysterious. Here, the easiest way to think of it is that if you have some proposition `a`, there is a proposition `~a` that hold all information about some set of people who believe `a`. We do not know in detail what the proposition `~a` implies, but neither do we care as long we can prove the theorems we need to make progress.

The following is a tautology in HOOO EP: (a | !a)^true → (!(a^true) == false^a)^true   for all `a` For proof, see Lemma 1 in Appendix A. It means, under excluded middle one can get tautological equality, which is needed for substituting the argument of the path semantical qubit operator `~`. Therefore, `~!(a^true)` becomes `~false^a`.

The Sesh axiom tells us that when we negate the proposition `~a` to `!~a`, which might be thought of as inverting the set of people who believe `a`, this set is equal to a second set of people. This second set of people are those who believe `!a`, described as `~!a`. In standard Path Semantics, the Sesh axiom is assumed, so this means that Agnosticism in standard Path Semantics is constructive.

References:

[1]   "Comment on clarified definitions of Theism vs Atheism vs Agnosticism"
        https://old.reddit.com/r/DebateAnAtheist/comments/1fdnsd4/new_atheist_epistemology/lmhkb3l/

[2]   "Hooo"
        AdvancedResearch – Propositional logic with exponentials
        https://github.com/advancedresearch/hooo

[3]   "Overview of Path Semantical Logics"
        Sven Nilsen, 2024
        https://github.com/advancedresearch/path_semantics/blob/master/papers-wip2/overview-of-path-semantical-logics.pdf

Appendix A:

```
fn lemma_1 : (a | !a)^true -> (!(a^true) == false^a)^true {
    use std::pow_transitivity;
    use std::tauto_hooo_or;

    x : (a | !a)^true;

    fn f1 : a^true | (!a)^true -> !(a^true) == false^a {
        use std::imply_lift;
        use std::refl;
        use std::tauto_not_to_para;
        use std::triv;

        x : a^true | (!a)^true;

        lam f : !(a^true) => false^a {

            y : !(a^true);

            lam f : a^true => false^a {
                z : a^true;
                let z2 = y(z) : false;
                let r = match z2 : false^a;
                return r;
            }
            lam g : (!a)^true => false^a {
                z : (!a)^true;
                let r = tauto_not_to_para(z) : false^a;
                return r;
            }
            let r = match x (f, g) : false^a;
            return r;
        }
        lam g : false^a => !(a^true) {
            y : false^a;

            lam f : a^true => !(a^true) {
                z : a^true;
                let z2 = triv(z) : a;
                let z3 = y(z2) : false;
                let r = match z3 : !(a^true);
                return r;
            }
            lam g : !(a^true) {
                z : a^true;
                let z2 = triv(z) : a;
                let r = y(z2) : false;
                return r;
            }
            let g2 = imply_lift(g) : (!a)^true => !(a^true);
            let r = match x (f, g2) : !(a^true);
            return r;
        }
        let r = refl(f, g) : !(a^true) == false^a;
        return r;
    }

    let x2 = tauto_hooo_or(x) : (a^true | (!a)^true)^true;
    let r = pow_transitivity(x2, f1) : (!(a^true) == false^a)^true;
    return r;
}
```

```
fn lemma_2 : (a | !a)^true -> (a^true == a)^true {
    use std::pow_transitivity;
    use std::tauto_hooo_or;

    x : (a | !a)^true;

    fn f : (a^true | (!a)^true) -> (a^true == a) {
        use std::imply_lift;
        use std::refl;
        use std::triv;

        y : a^true | (!a)^true;

        lam f : a^true => (a^true == a) {
            z : a^true;
            let z2 = triv(z) : a;
            let f = imply_lift(z2) : a^true => a;
            let g = imply_lift(z) : a => a^true;
            let r = refl(f, g) : a^true == a;
            return r;
        }
        lam g : (!a)^true => (a^true == a) {
            z : (!a)^true;
            lam f : a^true => a {
                z2 : a^true;
                let r = triv(z2) : a;
                return r;
            }
            lam g : a => a^true {
                z2 : a;
                let z3 = triv(z) : !a;
                let z4 = z3(z2) : false;
                let r = match z4 : a^true;
                return r;
            }
            let r = refl(f, g) : a^true == a;
            return r;
        }
        let r = match y (f, g) : a^true == a;
        return r;
    }

    let x2 = tauto_hooo_or(x) : (a^true | (!a)^true)^true;
    let r = pow_transitivity(x2, f) : (a^true == a)^true;
    return r;
}
```

Appendix B

Theism   ~Theism

Atheism   !~Theism

> Under the Sesh axiom, Atheism is equivalent to `~!Theism` which means the
> set of people who believe the non-existence of some deity is more likely than not.

Gnostic Theism   ~(Theism^true)

Gnostic Atheism   ~(false^Theism)

> This is the same as `~((!Theism)^true)`.

Gnosticism   ~(Theism^true) | ~(false^Theism)

Agnosticism   !~(Theism^true) & !~(false^Theism)

> This is the same as `!(~(Theism^true) | ~(false^Theism))`, which holds constructively.

> Under excluded middle and the Sesh axiom, Agnosticism becomes absurd.

> Agnosticism is the intersection between Agnostic Joker Theism and Agnostic Joker Atheism.

Agnostic Joker Theism   !~(Theism^true)

> In Agnostic Joker Theism, a person is not in the set that makes a positive claim
> about a deity's existence. This is modeled upon Joker Calculus where:

> !(x y)   =>   !x ?y

> So, !(Gnostic Theism)` becomes `!Gnostic ?Theism` which is Agnostic Joker Theism.

Agnostic Joker Atheism   !~(false^Theism)

> In Agnostic Joker Atheism, a person is not in the set that makes a positive claim
> about a deity's non-existence. This is modeled upon Joker Calculus where:

> !(x y)   =>   !x ?y

> So, !(Gnostic !Theism)` becomes `!Gnostic ?!Theism` which is Agnostic Joker Atheism.

For more information about Joker Calculus, see https://github.com/advancedresearch/joker_calculus

Under excluded middle, Gnostic Theism is the same as Theism.
The same holds for Gnostic Atheism which becomes the same as Atheism.
For proof, see Lemma 2 in Appendix B.

Appendix C

One can present Agnosticism visually using two connect Venn diagrams: