## **Binary Square Matrix Combinatorics**

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*In this paper I formalize binary square matrix combinatorics using Directional Set Algebra.* 

For all `n: nat`, there is an associated binary square matrix combinatorics:

0	Empty matrix set
D	Diagonal matrix set
U	Upper triangle matrix set
L	Lower triangle matrix set
1	All matrices

The following law holds with Directional Set Algebra:

$$D + U + L => 1$$

Sizes of sets:

$$|0| = 0$$
  
 $|D| = 2^n$   
 $|1| = 2^n$   
 $|U| = |L| = 2^n$   
 $|U| = |L| = 2^n$ 

Sub-types of binary matrix sets can be constructed using elements `0`, `1` and `?`. The following laws holds with Directional Set Algebra, where `?` is top and there is no bottom:

$$0 + 1 = ?$$

For example, for n = 3:

$$?00$$
  $0??$   $000$   $???$   $000$   $????$   $000$   $????$