## **Avatar Zen Ladders**

by Sven Nilsen, 2021

*In this paper I introduce a list of sets which satisfy Zen language levels.* 

In the paper "Zen Languages"<sup>[1]</sup>, I introduced a simple domain specific language that resembles the philosophy of Zen<sup>[2]</sup>. However, this definition does not allow a formal mathematical object. In order to support formal mathematical objects one needs something which satisfies Zen language levels.

An Avatar Zen Ladder is a list of sets of the following property:

```
azl(s : set, x : [set]) = \forall i len(x)-1 \{ x[i+1] \in x[i] \} \land (x[0] \in pow^len(x)(s))
 x : [azl(s)] true `x` is an Avatar Zen Ladder of `s`
```

Here, 'pow' is the power set operator<sup>[3]</sup>.

The name `azl` is an abbreviation for `avatar\_zen\_ladder`.

Avatar Zen Ladders satisfy Zen language levels and makes them more intuitive. The length of the list is the Zen level and the list is a sequence of sets where each successor is a member of the predecessor.

The name "avatar" comes from Avatar Extensions<sup>[4]</sup>, due to the wrapping of successive sets. The name "ladder" comes from the story of Jacob's ladder<sup>[5]</sup>.

The set `s` is used to generate a higher power set which functions as a "context". Since the higher power set takes up a lot of space, one can use `s` instead, for reasoning about it.

## **References:**

- [1] "Zen Languages"
  Sven Nilsen, 2021
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