# **Alphabetic List of Paths**

## Standard Dictionary for Path Semantics

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## Α

```
\begin{array}{l} add[(=0)] <=> \ and \\ add[(=0)] <=> \ or \\ add_{\mathbb{C},\mathbb{Q},\mathbb{R},\mathbb{Z}}[neg_{\mathbb{C},\mathbb{Q},\mathbb{R},\mathbb{Z}}] <=> \ add_{\mathbb{C},\mathbb{Q},\mathbb{R},\mathbb{Z}} \\ add_{\mathbb{N}}[even] <=> \ eq \\ add_{\mathbb{N}}[odd] <=> \ xor \\ add_{\mathbb{C},\mathbb{Q},\mathbb{R},\mathbb{Z},\mathbb{N}}[swap \rightarrow id] <=> \ add_{\mathbb{C},\mathbb{Q},\mathbb{R},\mathbb{Z},\mathbb{N}} \\ add_{\mathbb{R}}[exp] <=> \ mul_{\mathbb{R}} \\ and[not] <=> \ or \end{array}
```

### C

```
\begin{split} & concat[len] <=> \ add \\ & concat[sum] <=> \ add \\ & concat[min] <=> \ min_2 \\ & concat[max] <=> \ max_2 \\ & cos[neg \rightarrow id] <=> \ cos \\ & cross\{[vec\_dim] \ 3, [vec\_dim] \ 3\}[unit \times unit \rightarrow vec\_dim] <=> \ construct_3 \end{split}
```

## D

```
dec{(\neg=0)}[even] \le not

dec[neg] \le inc

div_{\mathbb{R}}{(\neg=0), (\neg=0)}[swap \rightarrow id] \le inv \cdot div
```

## Ε

```
eq[not] \le xor

exc[not] \le nrexc

exp_{\mathbb{R}}[ln] \le exp_{\mathbb{R}}
```

#### I

```
\begin{array}{ll} id[id] <=> id \\ id_A[id \rightarrow f] <=> f & f: A \rightarrow B \\ id_A[f] <=> id_B & f: A \rightarrow B \\ id_A[f \rightarrow id_A] <=> f^1 & f: A \rightarrow B \\ inc[even] <=> not \\ inc[inc] <=> inc \\ inc[neg] <=> dec \end{array}
```

#### L

 $ln[exp_{\mathbb{R}}] \leq > ln$ 

## M

```
\begin{split} & \text{mat\_id[id} \rightarrow \text{trace}] <=> \text{id} \\ & \text{mat\_inv}\{[\text{det}] \ (\neg=0)\}[\text{id} \rightarrow \text{mat\_inv}] <=> \text{id} \\ & \text{mat\_mul[det}] <=> \text{mul} \\ & \text{mat\_mul[fst} \cdot \text{dim} \times \text{snd} \cdot \text{dim} \rightarrow \text{dim}] <=> \text{id} \\ & \text{mul}_{\mathbb{N}}[(=0)] <=> \text{or} \\ & \text{mul}_{\mathbb{N}}[(=0)] <=> \text{and} \\ & \text{mul}_{\mathbb{N}}\{(>=0), (>=0)\}[(>=0)] <=> \text{true}_1 \\ & \text{mul}_{\mathbb{N}}\{(>=1), (==1)\}[\text{prime}] <=> \text{false}_1 \\ & \text{mul}_{\mathbb{N}}[(\% \ k: (==0))] <=> (\% \ k) \cdot \text{mul}_{\mathbb{N}} \\ & \text{mul}_{\mathbb{N}}[\text{even}] <=> \text{or} \\ & \text{mul}_{\mathbb{N}}[\text{odd}] <=> \text{and} \\ & \text{mul}_{\mathbb{R}}[\text{neg} \rightarrow \text{id}] <=> \text{mul}_{\mathbb{N}} \\ & \text{mul}_{\mathbb{C},\mathbb{Q},\mathbb{R},\mathbb{Z},\mathbb{N}}[\text{swap} \rightarrow \text{id}] <=> \text{mul}_{\mathbb{C},\mathbb{Q},\mathbb{R},\mathbb{Z},\mathbb{N}} \end{split}
```

## N

nand[not] <=> nor
nexc[not] <=> rexc
nor[not] <=> nand
not[not] <=> not
nrexc[not] <=> exc

## 0

or[not] <=> and not[not] <=> not

#### P

```
\begin{array}{l} push[len \times unit \rightarrow len] <=> inc \\ push[sum \times id \rightarrow sum] <=> add \\ push[max \times id \rightarrow max] <=> max_2 \\ push[min \times id \rightarrow min] <=> min_2 \\ pop\{[len] (\neg= 0)\}[len \rightarrow len \cdot fst] <=> dec \\ pop\{[len] (\neg= 0)\}[(sum, snd \cdot pop) \rightarrow sum \cdot fst] <=> sub \\ pop\{[len] (\neg= 0)\}[(sum, fst \cdot pop) \rightarrow sum \cdot snd] <=> sub \\ \end{array}
```

## R

rexc[not] <=> nexc

## S

```
\begin{split} & sin[neg] <=> sin \\ & sort_f[unit \rightarrow sorted_f] <=> true_1 \\ & split(\_)[id \rightarrow join] <=> id \\ & sub_{\mathbb{R}}[swap \rightarrow id] <=> neg \cdot sub_{\mathbb{R}} \end{split}
```

#### T

transpose[el(i, j)  $\rightarrow$  el(j, i)] <=> id transpose[dim] <=> swap

## U

unit[unit] <=> unit

## X

xor[not] <=> eq