

Inner and Outer Transport Theorems

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In this paper I present an inner and two outer transport theorems found in Path Semantical Logic.

The Inner Transport Theorem is a proof in Path Semantical Logic^[1]:

$$\begin{array}{l} \forall f : \{\text{and, fst, or, eq, rimply, imply, true}_2\} \{ \\ \quad (a, b, c) (A, B, C): \\ \quad \quad a(A), b(B), c(C), f(a=b, a=c) \Rightarrow f(A=B, A=C) \\ \} \end{array}$$

The Left Outer Transport Theorem is a proof:

$$\begin{array}{l} \forall f, g : \{\text{and, fst, or, eq, rimply, imply, true}_2\} \{ \\ \quad (a, b, c) (A, B, C): \\ \quad \quad a(A), b(B), c(C), f(a, b)=g(a, c) \Rightarrow f(A, B)=g(A, C) \\ \} \end{array}$$

The Right Outer Transport Theorem is a proof:

$$\begin{array}{l} \forall f, g : \{\text{and, fst, or, eq, rimply, imply, true}_2\} \{ \\ \quad (a, b, c) (A, B, C): \\ \quad \quad a(A), b(B), c(C), f(a, b)=g(b, c) \Rightarrow f(A, B)=g(B, C) \\ \} \end{array}$$

Here, the tuple `(a, b, c)` has level 1 and the tuple `(A, B, C)` has level 0.

The notation `a(A)` means `a=>A` where `A` is at a lower level.

The set `{and, fst, or, eq, rimply, imply, true}_2` are all functions that transports concretely^[2].

References:

- [1] “Path Semantical Logic”
AdvancedResearch, reading sequence on Path Semantics
https://github.com/advancedresearch/path_semantics/blob/master/sequences.md#path-semantical-logic

- [2] “Concrete and Abstract Transport”
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https://github.com/advancedresearch/path_semantics/blob/master/papers-wip/concrete-and-abstract-transport.pdf