# **CS/COE 1501**

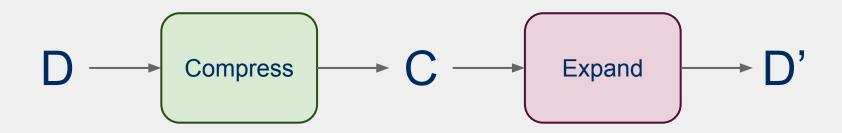
www.cs.pitt.edu/~nlf4/cs1501/

Compression

### What is compression?

- Represent the "same" data using less storage space
  - Can get more use out a disk of a given size
  - Can get more use out of memory
    - E.g., free up memory by compressing inactive sections
      - Faster than paging
      - Built in to OSX Mavericks and later
  - Can reduce the amount data transmitted
    - Faster file transfers
    - Cut power usage on mobile devices
- Two main approaches to compression...

### **Lossy Compression**



- Information is permanently lost in the compression process
- Examples:
  - MP3, H264, JPEG
- With audio/video files this typically isn't a huge problem as human users might not be able to perceive the difference

### **Lossy examples**

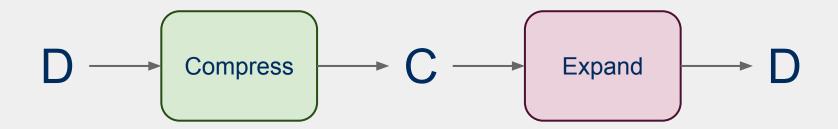
- MP3
  - "Cuts out" portions of audio that are considered beyond what most people are capable of hearing
- JPEG





40K 28K

### **Lossless Compression**



- Input can be recovered from compressed data exactly
- Examples:
  - o zip files, FLAC

### **Huffman Compression**

- Works on arbitrary bit strings, but pretty easily explained using characters
- Consider the ASCII character set
  - Essentially blocks of codes
    - In general, to fit R potential characters in a block, you need lg R bits of storage per block
      - Consequently, n bits storage blocks represent 2<sup>n</sup> characters
    - Each 8 bit code block represents one of 256 possible characters in extended ASCII
    - Easy to encode/decode

### **Considerations for compressing ASCII**

- What if we used variable length codewords instead of the constant 8? Could we store the same info in less space?
  - Different characters are represented using codes of different bit lengths
  - If all characters in the alphabet have the same usage frequency, we can't beat block storage
    - On a character by character basis...
  - What about different usage frequencies between characters?
    - In English, R, S, T, L, N, E are used much more than Q or X

### Variable length encoding

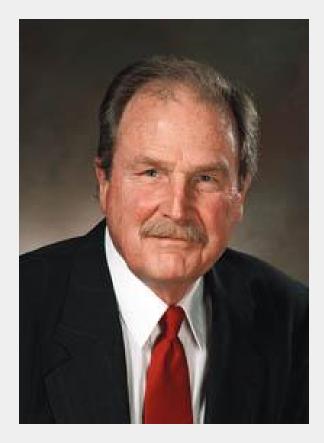
- Decoding was easy for block codes
  - Grab the next 8 bits in the bitstring
  - How can we decode a bitstring that is made of of variable length code words?
  - BAD example of variable length encoding:

1 A 00 T 01 K 001 U 100 R 101 C 10101 N

#### Variable length encoding for lossless compression

- Codes must be prefix free
  - No code can be a prefix of any other in the scheme
  - Using this, we can achieve compression by:
    - Using fewer bits to represent more common characters
    - Using longer codes to represent less common characters

### How can we create these prefix-free codes?



Huffman encoding!

### **Generating Huffman codes**

- Assume we have K characters that are used in the file to be compressed and each has a weight (its frequency of use)
- Create a forest, F, of K single-node trees, one for each character, with the single node storing that char's weight
- while |F| > 1:
  - Select T1, T2 ∈ F that have the smallest weights in F
  - Create a new tree node N whose weight is the sum of T1 and T2's weights
  - Add T1 and T2 as children (subtrees) of N
  - Remove T1 and T2 from F
  - Add the new tree rooted by N to F
- Build a tree for "ABRACADABRA!"

### **Implementation concerns**

 To encode/decode, we'll need to read in characters and output codes/read in codes and output characters

- 0 ...
- Sounds like we'll need a symbol table!
  - What implementation would be best?
    - Same for encoding and decoding?
- Note that this means we need access to the trie to expand a compressed file!

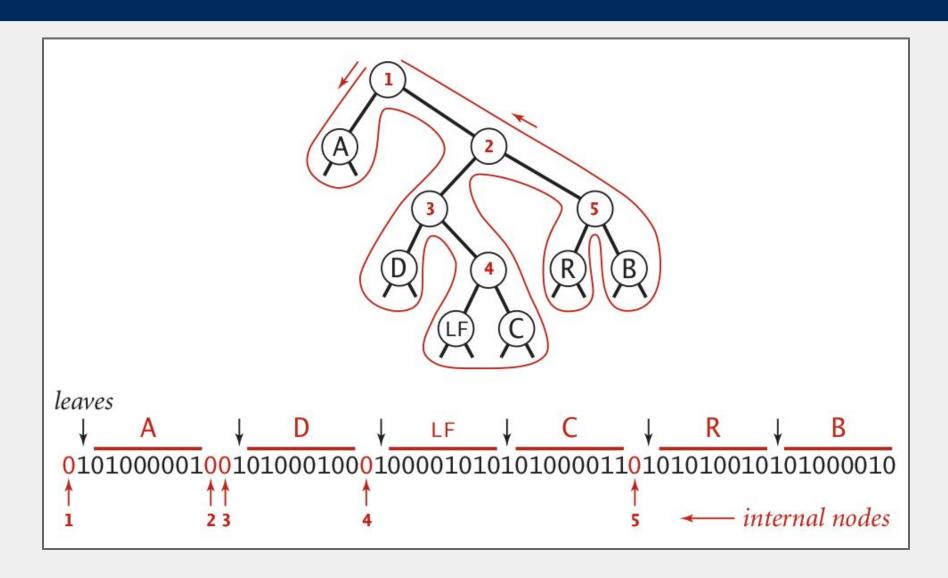
### Further implementation concerns

- Need to efficiently be able to select lowest weight trees to merge when constructing the trie
  - Can accomplish this using a priority queue
- Need to be able to read/write bitstrings!
  - Unless we pick multiples of 8 bits for our codewords, we will need to read/write fractions of bytes for our codewords
    - We're not actually going to do I/O on fraction of bytes
    - We'll maintain a buffer of bytes and perform bit processing on this buffer
    - See BinaryStdIn.java and BinaryStdOut.java

### **Binary I/O**

```
private static void writeBit(boolean bit) {
   // add bit to buffer
   buffer <<= 1;</pre>
   if (bit) buffer |= 1;
   // if buffer is full (8 bits), write out as a single byte
   N++;
   if (N == 8) clearBuffer();
writeBit(true);
writeBit(false);
                                            0000000
                                 buffer:
writeBit(true);
writeBit(false);
writeBit(false);
                                     N:
writeBit(false);
writeBit(false);
writeBit(true);
```

### Representing tries as bitstrings



### **Binary I/O**

```
private static void writeTrie(Node x){
   if (x.isLeaf()) {
       BinaryStdOut.write(true);
       BinaryStdOut.write(x.ch);
       return;
   BinaryStdOut.write(false);
   writeTrie(x.left);
   writeTrie(x.right);
}
private static Node readTrie() {
   if (BinaryStdIn.readBoolean())
       return new Node(BinaryStdIn.readChar(), 0, null, null);
   return new Node('\0', 0, readTrie(), readTrie());
```

### **Huffman pseudocode**

- Encoding approach:
  - Read input
  - Compute frequencies
  - Build trie/codeword table
  - Write out trie as a bitstring to compressed file
  - Write out character count of input
  - Use table to write out the codeword for each input character
- Decoding approach:
  - Read trie
  - Read character count
  - Use trie to decode bitstring of compressed file

### How do we determine character frequencies?

- Option 1: Preprocess the file to be compressed
  - Upside: Ensure that Huffman's algorithm will produce the best output for the given file
  - Downsides:
    - Requires two passes over the input, one to analyze frequencies/build the trie/build the code lookup table, and another to compress the file
    - Trie must be stored with the compressed file, reducing the quality of the compression
      - This especially hurts small files
      - Generally, large files are more amenable to Huffman compression
        - Just because a file is large, however, does not mean that it will compress well!

### How do we determine character frequencies?

- Option 2: Use a static trie
  - Analyze multiple sample files, build a single tree that will be used for all compressions/expansions
  - Saves on trie storage overhead…
  - But in general not a very good approach
    - Different character frequency characteristics of different files means that a code set/trie that works well for one file could work very poorly for another
      - Could even cause an increase in file size after "compression"!

### How do we determine character frequencies?

- Option 3: Adaptive Huffman coding
  - Single pass over the data to construct the codes and compress a file with no background knowledge of the source distribution
  - Not going to really focus on adaptive Huffman in the class, just pointing out that it exists...

### Ok, so how good is Huffman compression

- ASCII requires 8m bits to store m characters
- For a file containing c different characters
  - Given Huffman codes  $\{h_0, h_1, h_2, ..., h_{(c-1)}\}$
  - And frequencies  $\{f_0, f_1, f_2, ..., f_{(c-1)}\}$
  - $\circ$  Sum from 0 to c-1:  $|h_i| * f_i$
- Total storage depends on the differences in frequencies
  - The bigger the differences, the better the potential for compression
- Huffman is optimal for character-by-character prefix-free encodings
  - Proof in Propositions T and U of Section 5.5 of the text

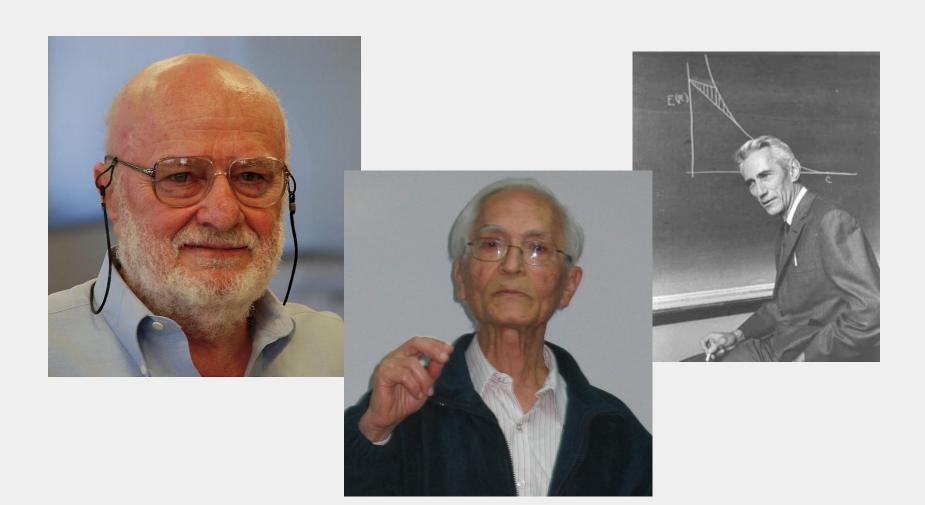
#### That seems like a bit of a caveat...

- Where does Huffman fall short?
  - What about repeated patterns of multiple characters?
    - Consider a file containing:
      - 1000 A's
      - 1000 B's
      - ...
      - 1000 of every ASCII character
    - Will this compress at all with Huffman encoding?
      - Nope!
    - But it seems like it should be compressible...

### Run length encoding

- Could represent the previously mentioned string as:
  - 1000A1000B1000C, etc.
    - Assuming we use 10 bits to represent the number of repeats, and 8 bits to represent the character...
      - 4608 bits needed to store run length encoded file
      - vs. 2048000 bits for input file
      - Huge savings!
- Note that this incredible compression performance is based on a very specific scenario...
  - Run length encoding is not generally effective for most files, as they often lack long runs of repeated characters

## What else can we do to compress files?



#### Patterns are compressible, need a general approach

- Huffman used variable-length codewords to represent fixed-length portions of the input...
  - Let's try another approach that uses fixed-length codewords to represent variable-length portions of the input
- Idea: the more characters can be represented in a single codeword, the better the compression
  - Consider "the": 24 bits in ASCII
  - Representing "the" with a single 12 bit codeword cuts the used space in half
    - Similarly, representing longer strings with a 12 bit codeword would mean even better savings!

#### How do we know that "the" will be in our file?

- Need to avoid the same problems as the use of a static trie for Huffman encoding...
- So use an adaptive algorithm and build up our patterns and codewords as we go through the file

### LZW compression

- Initialize codebook to all single characters
  - e.g., character maps to its ASCII value
- While !EOF:
  - Match longest prefix in codebook
  - Output codeword
  - Take this longest prefix, add the next character in the file, and add the result to the dictionary with a new codeword

### LZW compression example

- Compress, using 12 bit codewords:
  - TOBEORNOTTOBEORNOT

Cur	Output	Add	Т	84	TT:264
Т	84	TO:256	ТО	256	TOB:265
0	79	OB:257	BE	258	BEO:266
В	66	BE:258	OR	260	ORT:267
Е	69	EO:259	ТОВ	265	TOBE:268
0	79	OR:260	ЕО	259	EOR:269
R	82	RN:261	RN	261	RNO:270
N	78	NO:262	OT	263	
0	79	OT:263			

### LZW expansion

- Initialize codebook to all single characters
  - e.g., ASCII value maps to its character
- While !EOF:
  - Read next codeword from file
  - Lookup corresponding pattern in the codebook
  - Output that pattern
  - Add the previous pattern + the first character of the current pattern to the codebook

Note this means no codebook addition after first pattern output!

## LZW expansion example

Cur	Output	Add
84	Т	
79	0	256:TO
66	В	257:OB
69	Е	258:BE
79	0	259:EO
82	R	260:OR
78	N	261:RN
79	O	262:NO

84	Т	263:OT
256	TO	264:TT
258	BE	265:TOB
260	OR	266:BEO
265	ТОВ	267:ORT
259	ЕО	268:TOBE
261	RN	269:EOR
263	ОТ	270:RNO

#### How does this work out?

- Both compression and expansion construct the same codebook!
  - Compression stores character string → codeword
  - Expansion stores codeword → character string
  - They contain the same pairs in the same order
    - Hence, the codebook doesn't need to be stored with the compressed file, saving space

### Just one tiny little issue to sort out...

- Expansion can sometimes be a step ahead of compression...
  - If, during compression, the (pattern, codeword) that was just added to the dictionary is immediately used in the next step, the decompression algorithm will not yet know the codeword.
  - This is easily detected and dealt with, however

### LZW corner case example

• Compress, using 12 bit codewords: AAAAAA

Cur	Output	Add
Α	65	AA:256
AA	256	AAA:257
AAA	257	

• Expansion:

Cur	Output	Add
65	Α	
256	AA	256:AA
257	AAA	257:AAA

### LZW implementation concerns: codebook

- How to represent/store during:
  - Compression
  - Expansion
- Considerations:
  - What operations are needed?
  - How many of these operations are going to be performed?
- Discuss

### Further implementation issues: codeword size

- How long should codewords be?
  - Use fewer bits:
    - Gives better compression earlier on
    - But, leaves fewer codewords available, which will hamper compression later on
  - Use more bits:
    - Delays actual compression until longer patterns are found due to large codeword size
    - More codewords available means that greater
       compression gains can be made later on in the process

#### Variable width codewords

- This sounds eerily like variable length codewords...
  - Exactly what we set out to avoid!
- Here, we're talking about a different technique
- Example:
  - Start out using 9 bit codewords
  - When codeword 512 is inserted into the codebook, switch to outputting/grabbing 10 bit codewords
  - When codeword 1024 is inserted into the codebook, switch to outputting/grabbing 11 bit codewords...
  - o Etc.

#### Even further implementation issues: codebook size

- What happens when we run out of codewords?
  - Only 2<sup>n</sup> possible codewords for n bit codes
  - Even using variable width codewords, they can't grow arbitrarily large...
- Two primary options:
  - Stop adding new keywords, use the codebook as it stands
    - Maintains long already established patterns
    - But if the file changes, it will not be compressed as effectively
  - Throw out the codebook and start over from single characters
    - Allows new patterns to be compressed
    - Until new patterns are built up, though, compression will be minimal

### The showdown you've all been waiting for...

#### **HUFFMAN vs LZW**

- In general, LZW will give better compression
  - Also better for compression archived directories of files
    - Why?
      - Very long patterns can be built up, leading to better compression
      - Different files don't "hurt" each other as they did in Huffman
        - Remember our thoughts on using static tries?

### So lossless compression apps use LZW?

- Well, gifs can use it
  - And pdfs
- Most dedicated compression applications use other algorithms:
  - DEFLATE (combination of LZ77 and Huffman)
    - Used by PKZIP and gzip
  - Burrows-Wheeler transforms
    - Used by bzip2
  - LZMA
    - Used by 7-zip
  - brotli
    - Introduced by Google in Sept. 2015
    - Based around a " ... combination of a modern variant of the LZ77 algorithm, Huffman coding[,] and 2nd order context modeling ... "

#### **DEFLATE** et al achieve even better general compression?

- How much can they compress a file?
- Better question:
  - How much can a file be compressed by any algorithm?
- No algorithm can compress every bitstream
  - Assume we have such an algorithm
  - We can use to compress its own output!
  - And we could keep compressing its output until our compressed file is 0 bits!
    - Clearly this can't work
- Proofs in Proposition S of Section 5.5 of the text

### Can we reason about how much a file can be compressed?

Yes! Using Shannon Entropy



### Information theory in a single slide...

- Founded by Claude Shannon in his paper "A Mathematical Theory of Communication"
- Entropy is a key measure in information theory
  - Slightly different from thermodynamic entropy
  - A measure of the unpredictability of information content
  - By losslessly compressing data, we represent the same information in less space
  - Hence, 8 bits of uncompressed text has less entropy than 8 bits of compressed data

### **Entropy applied to language:**

- Translating a language into binary, the entropy is the average number of bits required to store a letter of the language
- Entropy of a message \* length of message = amount of information contained in that message
- On average, a lossless compression scheme cannot compress a message to have more than 1 bit of information per bit of compressed message
- Uncompressed, English has between 0.6 and 1.3 bits of entropy per character of the message

### A final note on compression evaluation

"Weissman scores" are a made-up metric for Silicon Valley (TV)



