



1. Consider the above set of processes that arrive at given times with certain priorities. The length of CPU burst time given in milliseconds.

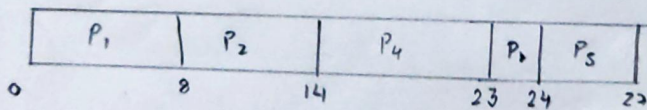
Process	Burst	Priority	Arrival Time
P <sub>1</sub>	8	4	0
P <sub>2</sub>	6	1	2
P <sub>3</sub>	1	2	2
P <sub>4</sub>	9	2	1
P <sub>5</sub>	3	3	3

Apply the following CPU scheduling to find the Average TA time, and Average Response time:

- (a) Priority Scheduling
- (b) SRTF
- (c) RR (TQ = 2 ms)

A. (a) Priority Scheduling

Gantt Chart:



$$\begin{aligned}
 \text{Avg. turnaround time} &= \frac{(8-0) + (14-2) + (23-2) + (24-23) + (27-3)}{5} \\
 &= \frac{8 + 12 + 21 + 1 + 24}{5} \\
 &= \frac{66}{5} = 13.2 \text{ ms}
 \end{aligned}$$

$$\begin{aligned}
 \text{Avg. response time} &= \frac{(0-0) + (8-2) + (14-1) + (23-2) + (27-3)}{5} \\
 &= \frac{0 + 6 + 13 + 21 + 24}{5} \\
 &= 12.8 \text{ ms}
 \end{aligned}$$

(b) Shortest Remaining Time First

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>6</sub>	
0	2	5	6	11	18	27

$$\text{Avg. Turnaround Time} = \frac{(12-0) + (18-2) + (3-2) + (24-18) + (6-3)}{5}$$

$$= \frac{12 + 16 + 1 + 6 + 3}{5}$$

$$= 8.2 \text{ ms}$$

$$\text{Avg. Response Time} = \frac{(0-0) + (12-2) + (2-2) + (18-1) + (3-3)}{5}$$

$$= \frac{10 + 17}{5} = 5.4 \text{ ms}$$

(c) Round Robin

$$\text{Time Quotient} = 2 \text{ ms}$$

P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>	P <sub>1</sub>	P <sub>2</sub>	P <sub>3</sub>	P <sub>4</sub>	P <sub>5</sub>
0	2	4	6	7	9	11	13	15	16	18	20	22	24	27

$$\text{Avg. Turnaround Time} = \frac{(24-0) + (22-2) + (7-2) + (27-1) + (16-3)}{5}$$

$$= \frac{24 + 20 + 5 + 26 + 13}{5}$$

$$= \frac{88}{5} = 17.6 \text{ ms}$$

$$\text{Avg. Response Time} = \frac{(0-0) + (4-2) + (6-2) + (11-1) + (7-3)}{5}$$

$$= \frac{2 + 4 + 4 + 10 + 4}{5} = \frac{24}{5} = 4.8 \text{ ms}$$



2. Consider the following set of processes, with the length of the CPU burst given in milliseconds:

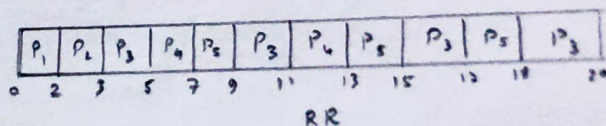
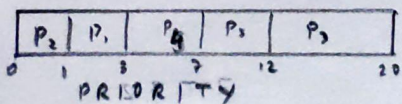
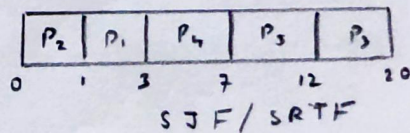
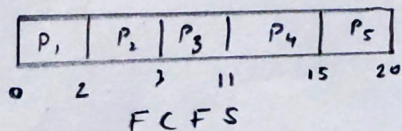
Process	Burst time	Priority
P1	2	2
P2	1	1
P3	8	4
P4	4	2
P5	5	3

The processes are assumed to have arrived in the order P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub>, P<sub>5</sub> at all time 0.

- (a) Draw four Gantt charts that illustrate the execution of these processes using the following scheduling algorithms: FCFS, SJF, SRTF, non-preemptive priority (a smaller priority number implies a higher priority) and RR (quantum = 2)
- (b) What is the average waiting time of each process for each of the scheduling algorithms in part a?
- (c) What is the average waiting time of each of these scheduling algorithms?
- (d) Which of the algorithms results in the minimum average waiting time (overall processes)?

A.

(a)



(d) (b) Avg Turn around time

$$FIFS = \frac{(2-0) + (3-0) + (11-0) + (15-0) + (20-0)}{5}$$

$$= \frac{2+3+11+15+20}{5} = \frac{51}{5} = 10.2 \text{ ms}$$

$$SJF = \frac{(3-0) + (1-0) + (2-0) + (12-0) + (20-0)}{5}$$

$$= \frac{3+1+2+12+20}{5} = \frac{43}{5} = 8.6 \text{ ms}$$

$$PRIORITY = \frac{[(3-0) + (1-0) + (2-0) + (12-0) + (20-0)]}{5}$$

$$= \frac{3+1+2+12+20}{5} = \frac{43}{5} = 8.6 \text{ ms}$$

$$RR = \frac{(2-0) + (3-0) + (20-0) + (13-0) + (18-0)}{5}$$

$$= \frac{2+3+20+13+18}{5} = \frac{66}{5} = 13.2 \text{ ms}$$

(e) (c) Avg. Waiting time

$$FIFS = \frac{(0-0) + (2-0) + (3-0) + (11-0) + (15-0)}{5}$$

$$= \frac{31}{5} = 6.2 \text{ ms}$$

$$SJF = \frac{(0-0) + (1-0) + (3-0) + (7-0) + (12-0)}{5}$$

$$= \frac{23}{5} = 4.6 \text{ ms}$$

$$PRIORITY = \frac{[(0-0) + (1-0) + (3-0) + (7-0) + (12-0)]}{5}$$

$$= \frac{23}{5} = 4.6 \text{ ms}$$

$$RR = \frac{(0-0) + (2-0) + [(3-0) + (9-5) + (15-11) + (18-17)] + [(5-0) + (11-7)] + [(7-0) + (13-9) + (12-12)]}{5}$$

$$= \frac{2 + (3+4+4+1) + (5+4) + (7+4+2) + 2 + 12 + 9 + 13}{5}$$

$$= \frac{36}{5} = 7.2 \text{ ms}$$



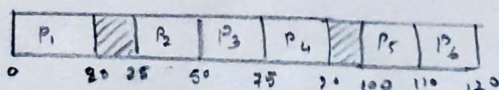
(d) 'Shortest Job First' (SJF) and Priority Scheduling had the minimum average waiting time considering overall processes.

3. Consider the following set of threads with the length of the CPU burst time given in milliseconds.

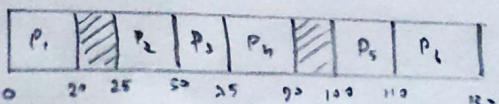
Thread	Priority	Burst	Arrival
P <sub>1</sub>	40	20	0
P <sub>2</sub>	30	25	25
P <sub>3</sub>	30	25	30
P <sub>4</sub>	35	15	60
P <sub>5</sub>	5	10	100
P <sub>6</sub>	10	10	105

- (a) Draw four Gantt charts that illustrate the execution of these processes using the following scheduling algorithms: FCFS, SJF, SRTF, non-preemptive priority and RR (quantum = 4).
- (b) What is the average turnaround time of each process for each of the scheduling algorithms in part a?
- (c) What is the average waiting time of each process for each of these scheduling algorithms?
- (d) What is the average response time for each process for each of these scheduling algorithms?
- (e) Compare the performance of all the algorithms mentioned in part a for all three metrics in parts b, c, and d with tabular expression.

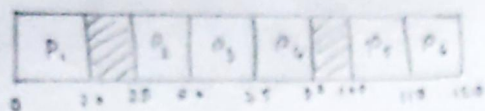
A.  
(a)



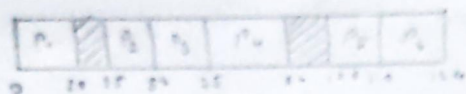
FCFS



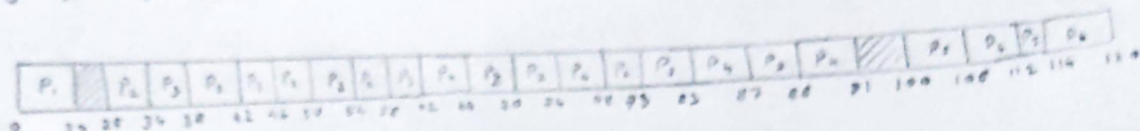
SJF



SJF



PRIORITY



ROUND ROBIN

(b) For FCFS, SJF, SRTF and PRIORITY,

$$\text{Avg. Turnaround Time} = \frac{(20-0) + (50-25) + (95-30) + (120-60) + (130-100) + (120-105)}{6}$$

$$= \frac{20 + 25 + 45 + 30 + 10 + 15}{6}$$

$$= \frac{145}{6} = 24.17 \text{ ms}$$

For RR,

$$\text{Avg. Turnaround Time} = \frac{(20-0) + (73-25) + (88-30) + (91-60) + (114-100) + (110-105)}{6}$$

$$= \frac{20 + 48 + 58 + 31 + 14 + 15}{6}$$

$$= \frac{186}{6} = 31 \text{ ms}$$

(c) For FCFS, SJF, SRTF and PRIORITY,

$$\text{Avg. Waiting Time} = \frac{(0-0) + (25-25) + (50-30) + (75-60) + (100-100) + (110-105)}{6}$$

$$= \frac{20 + 15 + 5}{6} = \frac{40}{6} = 6.67 \text{ ms}$$



For RR,

$$\begin{aligned} \text{Avg. Waiting Time} &= \frac{(0-0) + [(25-25) + (38-34) + (46-42) + (54-50) + (66-58) + (78-70) + (88-82)] + [(34-30) + (42-38) + (50-46) + (58-54) + (70-62) + (78-74) + (82-87)] + [(62-60) + (74-66) + (88-82)] + [(100-100) + (112-108)] + [(108-105) + (114-112)]}{6} \\ &= \frac{0 + [0+4+4+4+8+8] + [4+6+4+4+8+8+1] + [2+8+5+1]}{6} \\ &= \frac{0 + 28 + 33 + 16 + 4 + 5}{6} = \frac{86}{6} = 14.33 \text{ ms} \end{aligned}$$

(d) For FCFS, SJF, SRTF and PRIORITY,

$$\begin{aligned} \text{Avg. Response Time} &= \frac{(0-0) + (25-25) + (50-30) + (75-60) + (100-100) + (110-105)}{6} \\ &= \frac{20 + 15 + 5}{6} = \frac{40}{6} = 6.67 \text{ ms} \end{aligned}$$

For RR,

$$\begin{aligned} \text{Avg. Response Time} &= \frac{(0-0) + (25-25) + (34-30) + (62-60) + (100-100) + (108-105)}{6} \\ &= \frac{0 + 0 + 4 + 2 + 0 + 3}{6} = \frac{9}{6} = 1.5 \text{ ms} \end{aligned}$$

(e)

	FCFS	SJF	SRTF	PRIORITY	RR
Avg. Turnaround Time (ms)	24.17	24.17	24.17	24.17	31.0
Avg. Waiting Time (ms)	6.67	6.67	6.67	6.67	14.33
Avg. Response Time (ms)	6.67	6.67	6.67	6.67	1.5



4 Five processes are competing for resources  $R_1, R_2, R_3$  and  $R_4$  where  $(R_1, R_2, R_3, R_4) = (6, 4, 4, 2)$ . The maximum claim of these processes and the initial resources allocated to these processes, are given in the following table:

PROCESS	MAX				ALLOCATION			
	$R_1$	$R_2$	$R_3$	$R_4$	$R_1$	$R_2$	$R_3$	$R_4$
P1	3	2	1	1	2	0	1	1
P2	1	2	0	2	1	1	0	0
P3	1	1	2	0	1	1	0	0
P4	3	2	1	0	1	1	1	0
P5	2	1	0	1	0	0	0	1

(a) Determine whether the system is in deadlock state or not, with the help of Banker's algorithm.

(b) If P2 requests two instances of  $R_1$ , one instance of  $R_3$ , and one instance of  $R_4$ , check whether the system is still in safe state. If it is, find out the safe sequence of process execution.

A.

Process	Allocation				Max				Need			
	$R_1$	$R_2$	$R_3$	$R_4$	$R_1$	$R_2$	$R_3$	$R_4$	$R_1$	$R_2$	$R_3$	$R_4$
P1	2	0	1	1	3	2	1	1	1	2	0	0
P2	1	1	0	0	1	2	0	2	0	1	0	2
P3	1	1	0	0	1	1	2	0	0	0	2	0
P4	1	1	1	0	3	2	1	0	2	1	0	0
P5	0	0	0	1	2	1	0	1	2	1	0	0

c)

Available

$$= (6, 4, 4, 2) - (5, 3, 2, 2)$$

$$= (1, 1, 2, 0)$$

$$1. \text{ Work} = \text{Available}$$

$$= (1, 1, 2, 0)$$

$$\text{Need}[3] = (0, 0, 2, 0) < \text{Work}$$

$P_3$  request granted

$$\text{Work} = \text{Work} + (1, 1, 0, 0)$$

$$= (2, 2, 2, 0)$$

$$2. \text{ Need}[4] = (2, 1, 0, 0) < \text{Work}$$

$P_4$  request granted

$$\text{Work} = \text{Work} + (1, 1, 1, 0)$$

$$= (3, 3, 3, 0)$$

$$3. \text{ Need}[5] = (2, 1, 0, 0) < \text{Work}$$

$P_5$  request granted

$$\text{Work} = \text{Work} + (0, 0, 0, 1)$$

$$= (3, 3, 3, 1)$$

$$4. \text{ Need}[1] = (1, 2, 0, 0) < \text{Work}$$

$P_1$  request granted

$$\text{Work} = \text{Work} + (2, 0, 1, 1)$$

$$= (5, 3, 4, 2)$$

$$5. \text{ Need}[2] = (0, 1, 0, 2) < \text{Work}$$

$P_2$  request granted.

$$\text{Work} = \text{Work} + (1, 1, 0, 0)$$

$$= (6, 4, 4, 2)$$

Through Banker's Algorithm, we can confirm that the system is not in deadlock with a possible safe sequence of

$$P_3 \rightarrow P_4 \rightarrow P_5 \rightarrow P_1 \rightarrow P_2$$



(b) Process P2 requests resources,

$$Req[2] = (2, 0, 1, 1)$$

By Resource Request Algorithm,

$$Available[2] = Available[2] - Req[2]$$

$$= (1, 1, 2, 0) - (2, 0, 1, 1)$$

$$= \phi$$

$\therefore$  The system will be in deadlock

5

Consider a disk queue with I/O Requests on the following cylinders in their arriving order:

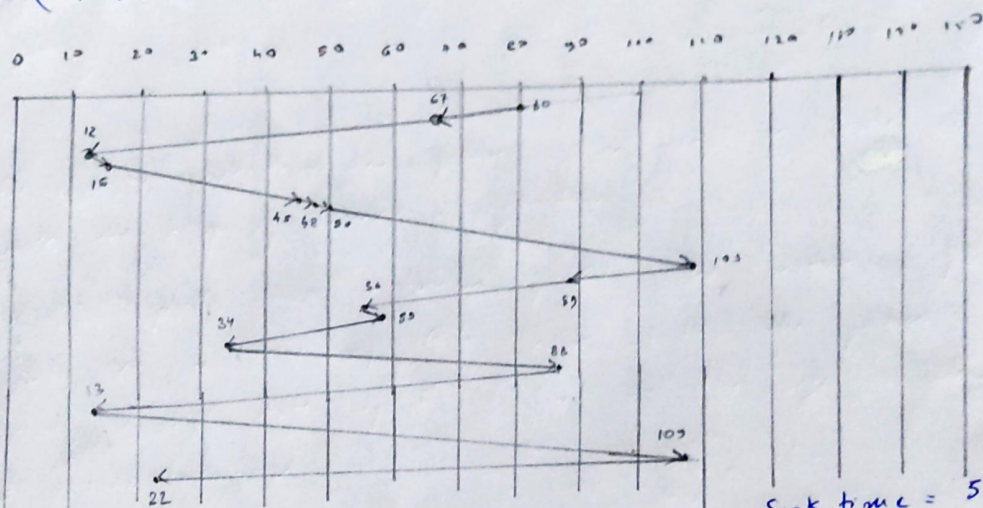
67, 12, 15, 45, 48, 50, 109, 89, 56, 59, 34, 88, 13, 103, 22

The disk head is assumed to be at cylinder 80 and the disk consists of total 150 cylinders. Compare the average seek length using FCFS, SSTF, SCAN and C-SCAN algorithm. Which one's performance is best and why?

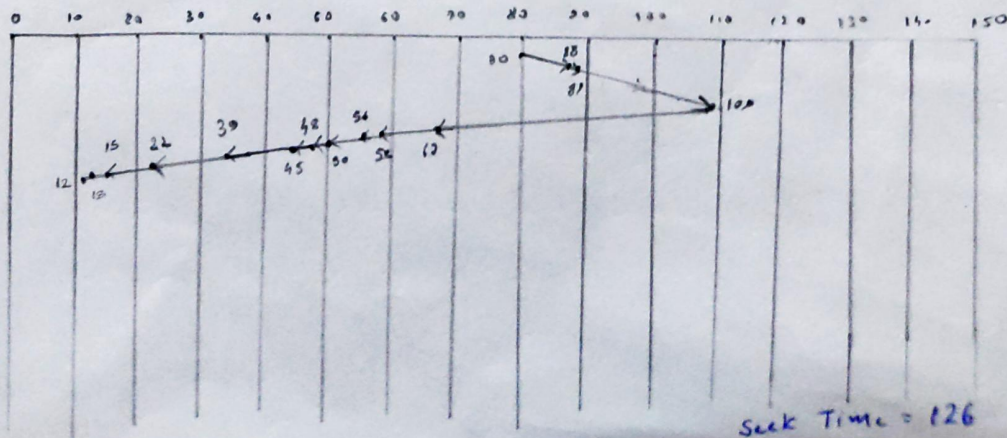
A. FCFS

Start = 80

Queue (0, 67, 12, 15, 45, 48, 50, 109, 89, 56, 59, 34, 88, 13, 103, 22, 150)

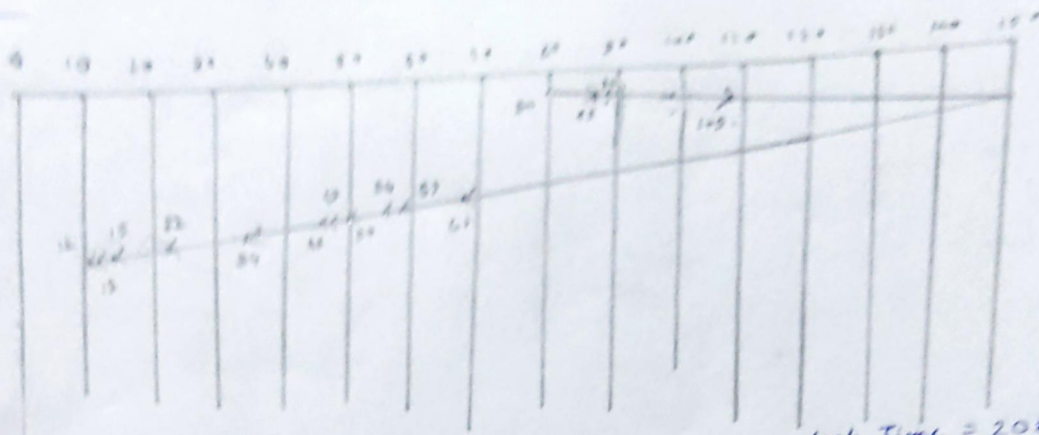


SSTF



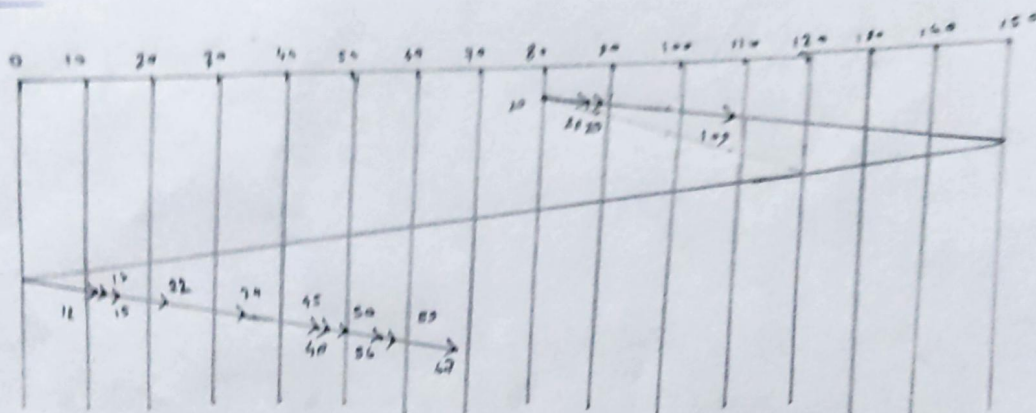


# SCAN



Seek Time = 208

# C-SCAN



Seek Time = 287

6 Consider the virtual page reference string:

5, 0, 2, 1, 0, 3, 0, 2, 4, 3, 0, 3, 2, 1, 3, 0, 1, 5, 3, 1, 2, 4, 5, 4, 0.

On a demand paged virtual memory system running on a computer system that main memory size of 3 page frames which are initially empty. Let LRU, FIFO and OPTIMAL denote the number of page faults under the corresponding page replacement policy. Examine their performance and sort them in ascending order.

A

LRU

5	0	2	1	0	3	0	2	4	3	0	3	2	1	3	0	1	5	3	1	2	4	5	4	0
5	5	5	1	1	1	1	2	2	2	0	0	0	1	1	1	1	1	1	1	1	5	5	5	5
0	0	0	0	0	0	0	0	0	3	3	3	3	3	3	3	3	5	5	5	2	2	2	2	0
2	2	2	3	3	3	3	4	4	4	4	2	2	2	0	0	0	3	3	3	4	4	4	4	4
PF:	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓

Page Faults: 18

FIFO

5	0	2	1	0	3	0	2	4	3	0	3	2	1	3	0	1	5	3	1	2	4	5	4	0
5	5	5	0	0	2	1	3	0	2	4	4	3	0	2	1	3	3	0	5	1	2	2	4	4
0	0	2	2	1	3	0	2	4	3	3	0	2	1	3	3	0	0	5	1	2	4	4	5	5
2	1	1	3	0	2	4	3	0	0	2	1	3	0	0	5	5	1	2	4	5	5	5	0	0
PF:	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓

Page Faults: 20

OPTIMAL

5	0	2	1	0	3	0	2	4	3	0	3	2	1	3	0	1	5	3	1	2	4	5	4	0
5	5	5	1	1	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	2	2	2	2	2
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	5	5	5	5	5	5	5	0
2	2	2	2	2	2	4	4	4	4	2	1	1	1	1	1	1	1	1	1	4	4	4	4	4
✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓

Page Faults: 12

Performance in Ascending Order: OPTIMAL > LRU > FIFO