

HW 6 Mean and Variance of Conditional Joint Probability Function

- Create R function for computing the conditional mean of Y and conditional variance of Y when $X = x$ using `matrix()` with the below data.
- Find the following conditional mean and variance values ...

$$E(Y|X=1) = ? \text{ (answer = 3.55)}$$

$$V(Y|X=1) = ? \text{ (answer = 0.7475)}$$

$$E(Y|X=2) = ?$$

$$V(Y|X=2) = ?$$

$$E(Y|X=3) = ?$$

$$V(Y|X=3) = ?$$

y = Response time(nearest second)	x = Number of Bars of Signal Strength			f(y)		
	1	2	3			
1	0.01	0.02	0.25	0.28		
2	0.02	0.03	0.20	0.25		
3	0.02	0.10	0.05	0.17		
4	0.15	0.10	0.05	0.30		
f(x)	0.20	0.25	0.55	y*f(y x=1)	y ² *f(y x=1)	
1	0.050	0.080	0.455	0.05	0.05	
2	0.100	0.120	0.364	0.20	0.40	
3	0.100	0.400	0.091	0.30	0.90	
4	0.750	0.400	0.091	3.00	12.00	
Sum of f(y x)	1.000	1.000	1.000	3.55	13.35	
					12.6025	
					0.7475	

- What should the response time (Y) be when $X = 3$? Why?

Hint:

- Joint = given discrete joint probability data
- Joint = matrix(c(0.01,0.02,0.25,0.02,0.03,0.20,0.02,0.10,0.05,0.15,0.10,0.05),nrow=4,ncol=3)
- The formulas to compute the Mean and Variance of conditional probability are ...

$$E(Y|x) = \int_y y \cdot f_{Y|x}(y) \quad \text{and} \quad V(Y|x) = \int_y (y - \mu_{Y|x})^2 \cdot f_{Y|x}(y) = \int_y y^2 \cdot f_{Y|x}(y) - \mu_{Y|x}^2$$

$$\text{when} \quad f_{Y|x}(y) = \frac{f_{XY}(x,y)}{f_X(x)} \quad \text{for } f_X(x) > 0$$

Note: summation(Σ) will be substituted \int in case of discrete data