

ICT2403 – Graphics and Image Processing

Digital Image Fundamentals 1

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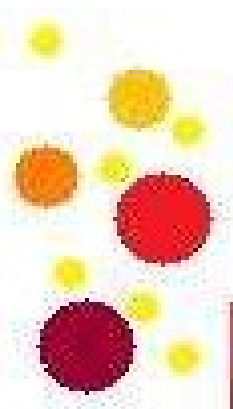
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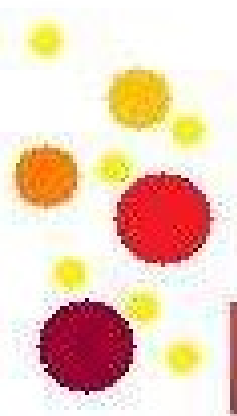
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Learning Outcomes

- At the end of this lecture, you should be able to;
 - describe the energy and the EM spectrum.
 - describe image acquisition methods.
 - discuss image formation model.
 - express sampling and quantization.
 - define dynamic range and image representation.

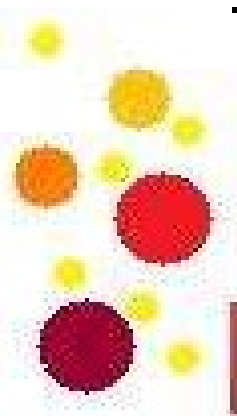


Light and the EM Spectrum

- The EM spectrum can be expressed in the terms of wavelength (λ), frequency (ν) or energy.
- Wavelength (λ) and frequency (ν) are related as;

$$\lambda = c / \nu$$

– where c is the speed of light ($2.998 * 10^8$ m/s)



Light and the EM Spectrum (Cont...)

- The energy of the various components of the EM spectrum is given by the expression;

$$E = h \nu$$

- where h is Planck's constant (6.626176×10^{-34} joule-seconds).
- Frequency is measured in Hertz (Hz), with 1Hz being equal to one cycle of a sinusoidal wave per second.
- The commonly used unit of energy is the electron-volt.



Light and the EM Spectrum (Cont...)

- Electromagnetic waves are conceptually sinusoidal and formation of different wave lengths.
- It can be thought of as a stream of massless particles, each travelling in a wave like pattern and moving at the speed of light.
- Each massless particle contains a certain amount of energy and a bundle of energy is known as photon.
- **Energy is proportional to the frequency.**
- **Therefore, for higher frequency bands in EM spectrum carries more energy per photon and lower frequency bands in EM spectrum carries lower energy per photon.**



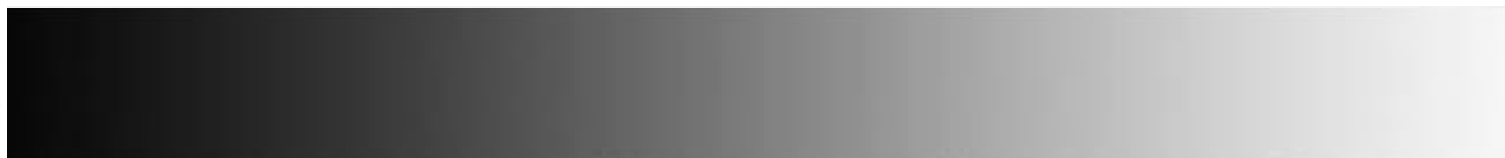
Light and the EM Spectrum - Light



- Light is the particular type of EM radiation that can be visible and sense by the human eye.
- The visible band of the EM spectrum spans the range from approximately 0.43 micrometer (violet) to about 0.79 micrometer (red).
- The color spectrum divided into six broad regions; violet, blue, green, yellow, orange and red.
- No color ends abruptly, but rather each range blends smoothly into the next.
- **The colors that human perceive in an object are determine by the nature of the light reflected from the object.**

Light and the EM Spectrum - Achromatic Light

- The light that is void of color is called **achromatic** or **monochromatic light**.
- The only attribute of such light is its intensity, or amount.
- The term **gray level** generally is used to describe monochromatic intensity because it ranges from black to gray and finally to white.



Light and the EM Spectrum - Chromatic Light

- Chromatic light spans the EM energy spectrum from approximately 0.43 to 0.79 micrometers.
- Three basic quantities are used to describe the quality of a chromatic light source; radiance, luminance and brightness.
 - **Radiance** is a total amount of energy that flows from the light source, and it is usually measured in Watts (W).
 - **Luminance** measure in lumen (lm), gives the measure of the amount of energy and observer perceives from light source.
 - **Brightness** is a subjective descriptor of light perception that is particularly impossible to measure.

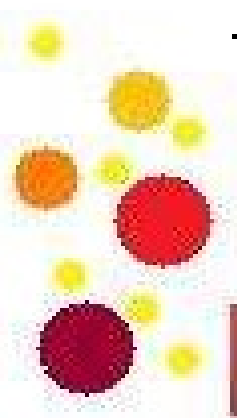


Image Sensing & Acquisition

- Most of the images are generated by the combination of an illumination source and the reflection or absorption of energy from that source by the elements of the scene being imaged.
- The illumination may originate from a source of EM energy such as radar, infrared, X-ray system or from less traditional sources, such as ultrasound or computer-generated illumination pattern.

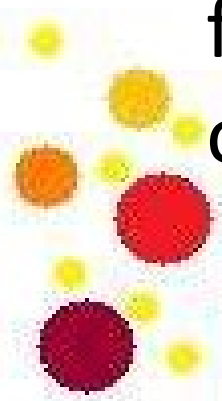


Image Sensing & Acquisition (Cont...)

- Depending on the nature of the source, illumination energy is reflected from, or transmitted through, objects.
 - As an example, we can say light reflected from planer surface and X ray transmitted through the human body to construct the images.
- In some applications, the reflected or transmitted energy is focused on to a photo converter, which **converts the energy into a visible light**.
 - Electron microscopy and some applications on Gamma imaging (single-photon emission computed tomography (SPECT)) use this approach.

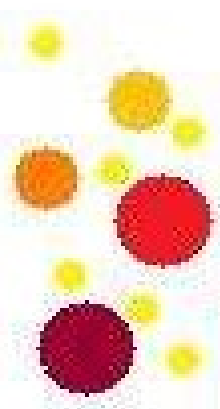


Image Sensing & Acquisition (Cont...)

- There are three principle sensor arrangements used to transform illumination energy into digital images.
 - Single imaging sensor
 - Line sensor
 - Array sensor

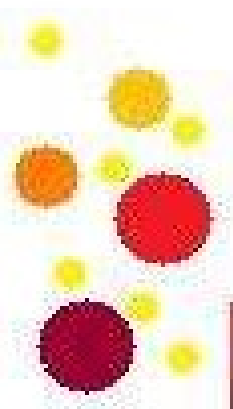
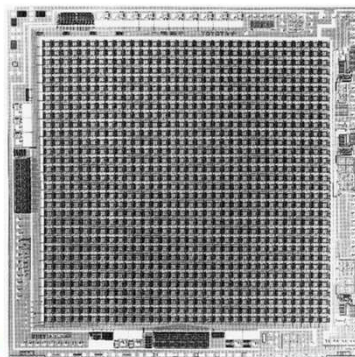


Image Sensing & Acquisition (Cont...)

- **Sensor process**

- Incoming energy is transformed into a voltage by the combination of input electrical power and a sensor material that is responsive to the particular type of energy being detected.
- The output voltage waveform is the response of the sensor(s), and a digital quantity is obtained from each sensor by digitizing its response.

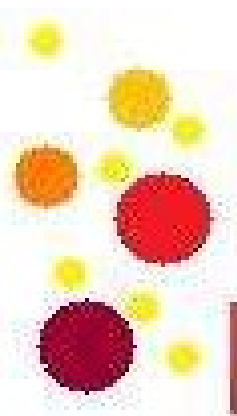


Image Sensing & Acquisition (Cont...)

- Image acquisition using a single sensor

- Most familiar sensor of this type is the photodiode, which is constructed of silicon materials and whose output voltage waveform is proportional to light.
- The use of a filter in front of a sensor improves selectivity.
- In order to generate a 2D image using a single sensor, there has to be relative displacements in both the x and y directions between the sensor and the area to be imaged.

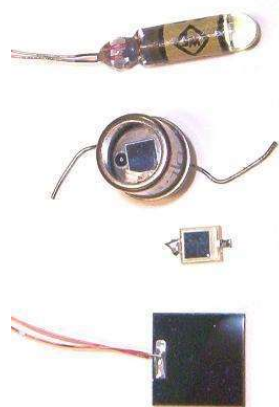
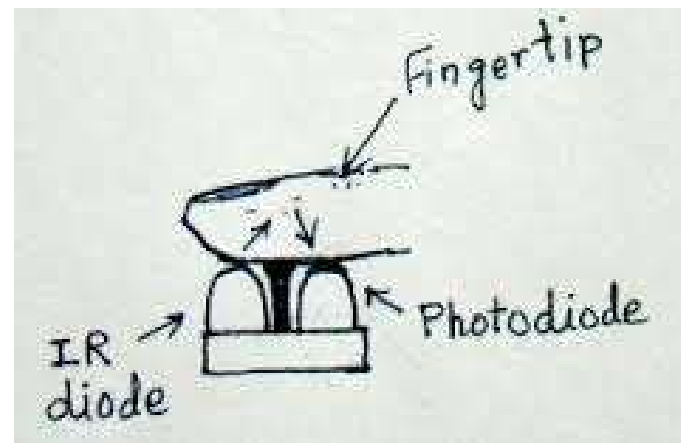
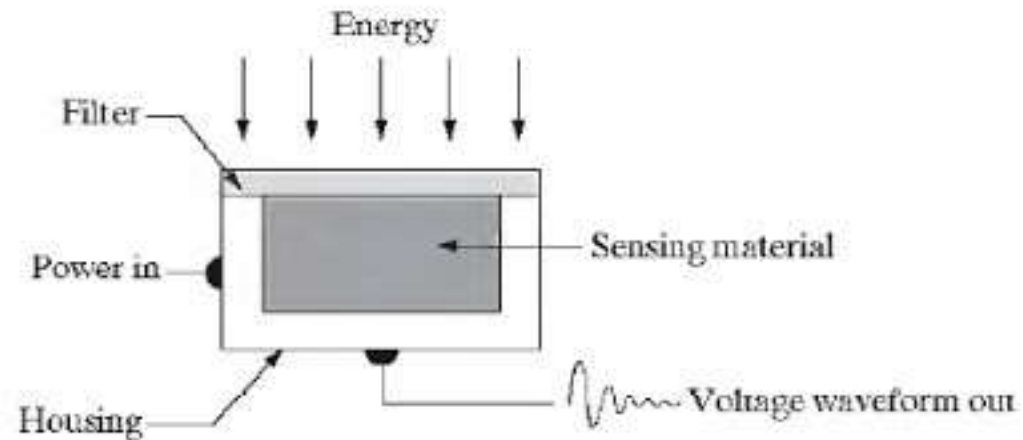


Image Sensing & Acquisition (Cont...)

- Image Acquisition using Sensor Strips
 - The sensor strip provides imaging elements in one direction.
 - Motion perpendicular to the strip provides imaging in the other direction.
 - This is the type of arrangement used in most flat bed scanners.

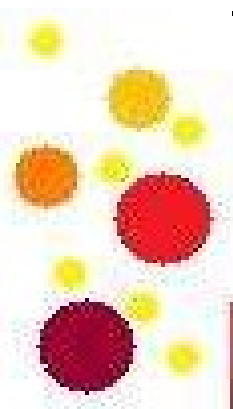
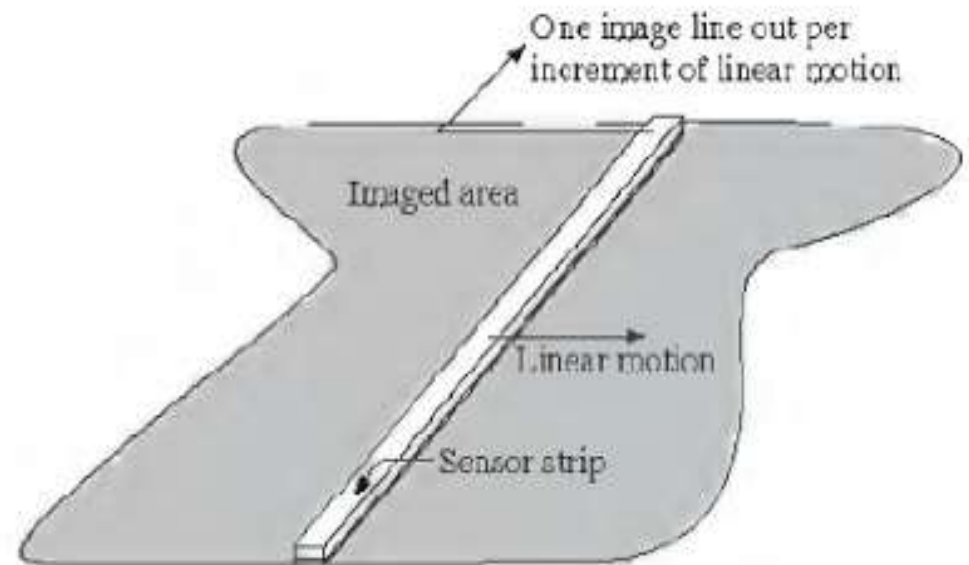


Image Sensing & Acquisition (Cont...)

- Sensor strips mounted in a ring configuration are used in medical and industrial imaging to obtain cross sectional images of 3D objects.
- CAT, MRI and PET imaging are used this concept to produce images.
- Images are not obtained directly from the sensors by motion alone, they require extensive processing.
- A 3D digital volume consisting of stacked images is generated as the object is moved in a direction perpendicular to the sensor ring.

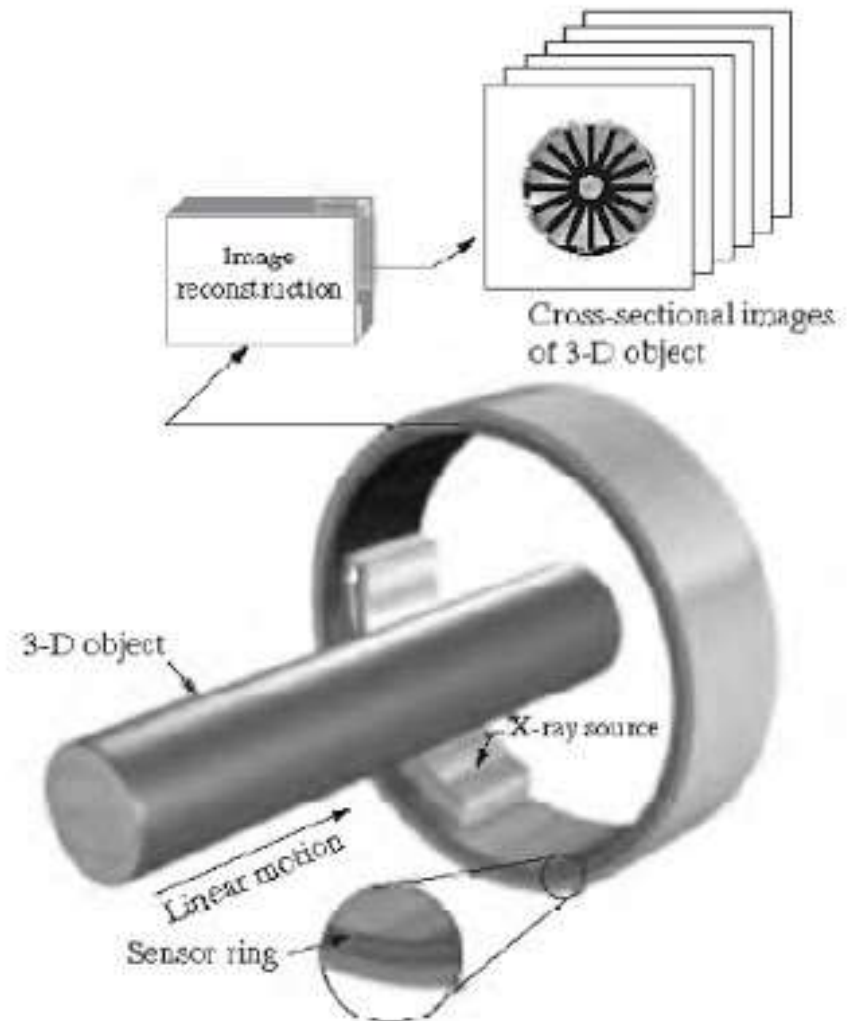


Image Sensing & Acquisition (Cont...)

- Image Acquisition using Sensor Arrays
 - Numerous electromagnetic and some ultrasonic sensing devices frequently are arranged in array format.
 - This is also found in digital cameras.
 - The response of each sensor is proportional to the **integral of the light energy** (the cumulative sum or total of the light energy) projected on to the surface of the sensor.
 - The key advantage of 2D sensor array is it can be obtained the complete image by focusing the energy pattern onto the surface of the array.
 - Motion is not necessary in this method.

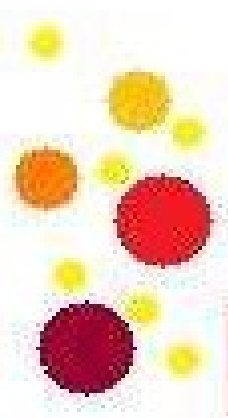


Image Sensing & Acquisition (Cont...)

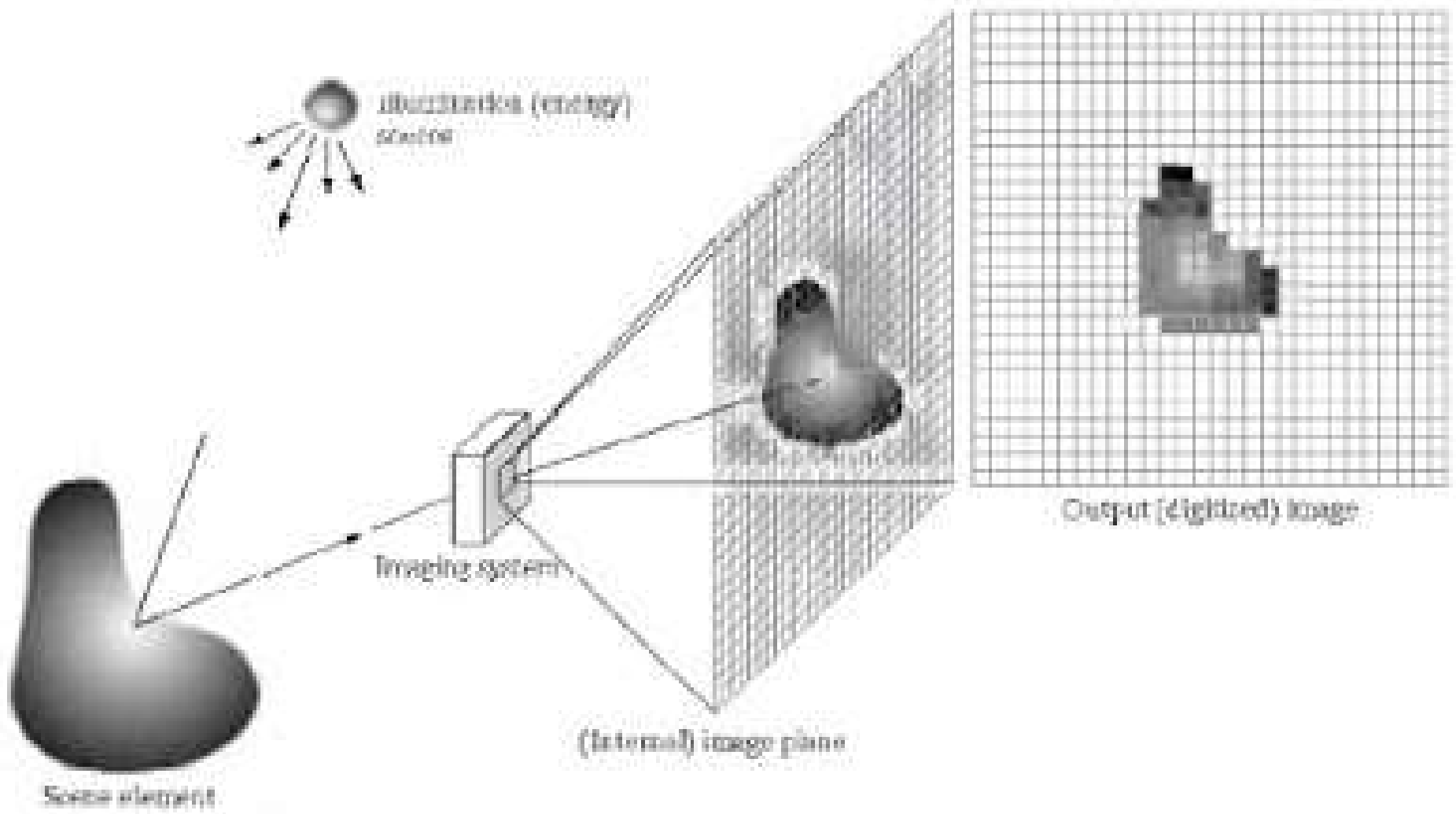


Image Formation Model

- We can denote images by two dimensional function of the form $f(x,y)$.
- The value or amplitude of the f at spatial coordinates (x,y) is a positive scalar quantity whose physical meaning is determined by the source of the image.
- When an image is generated from a physical process, its values are proportional to energy radiated by a physical source (electromagnetic waves).
- As a consequence, $f(x,y)$ must be non-zero and finite; that is, $0 < f(x,y) < \infty$

Image Formation Model (Cont...)

- The function $f(x,y)$ may be characterized by two components;
 - **Illumination** – The amount of source illumination incident on the scene being viewed - $i(x,y)$.
 - **Reflectance** – The amount of illumination reflected by the objects in the scene - $r(x,y)$.
- The two functions combine as a product to form $f(x,y)$.

$$f(x,y) = i(x,y) r(x,y)$$

Where; $0 < i(x,y) < \infty$ and $0 < r(x,y) < 1$ (0 – total absorption, 1 – total reflectance)

- The nature of $i(x,y)$ is determined by the illumination source, and $r(x,y)$ is determined by the characteristics of the imaged objects.



Image Formation Model (Cont...)

- We call the intensity of a monochrome image at any coordinates (x_n, y_n) the gray level (I) of the image at that point.
That is; $I = f(x_0, y_0)$
- It is evident that I lies in the range; $L_{min} < I < L_{max}$
- In theory, the only requirement of L_{min} is that it be positive, and on L_{max} that it be finite.
- In practice $L_{min} = i_{min} r_{min}$ and $L_{max} = i_{max} r_{max}$
- The interval $[L_{min}, L_{max}]$ is called the **GRAY SCALE**.
- Common practice is to shift this interval numerically to the interval $[0, L-1]$, where $I=0$ is considered black and $I = L-1$ is considered white on the gray scale.
- All the intermediate values are shades of gray varying from black to white.

Image Sampling & Quantization

- **Why?**

- The output of most sensors is a continuous voltage waveform whose amplitude and spatial behaviors are related to the physical phenomenon being sensed.
- To create a digital image, we need to convert the continuous sensed data into digital form.
- This involves two processes; **Sampling and Quantization**.

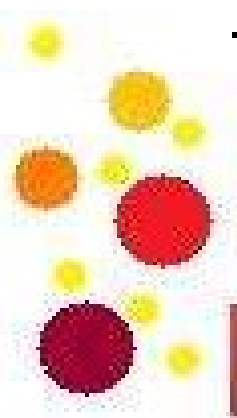


Image Sampling & Quantization

(cont...)

- An image may be continuous with respect to the x and y coordinates and also an amplitude.
- To convert image to digital form, we have to sample the function in both coordinates and in amplitude.
- Digitizing the coordinate values is called Sampling.
- Digitizing the amplitude values is called Quantization.

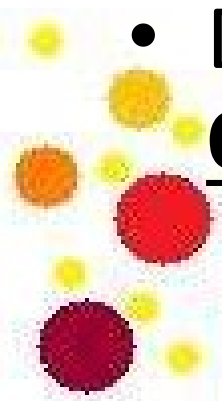


Image Sampling & Quantization (cont...)

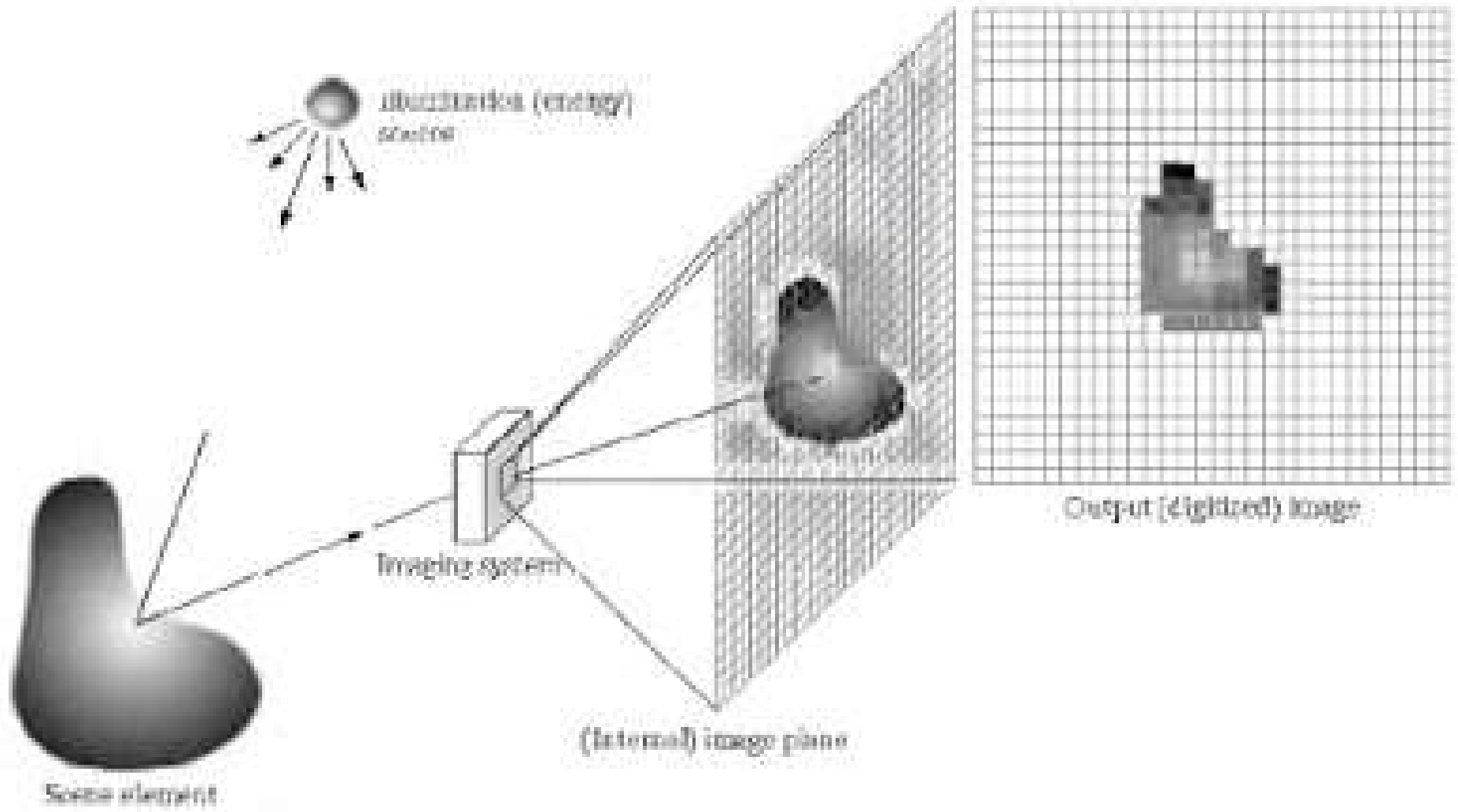
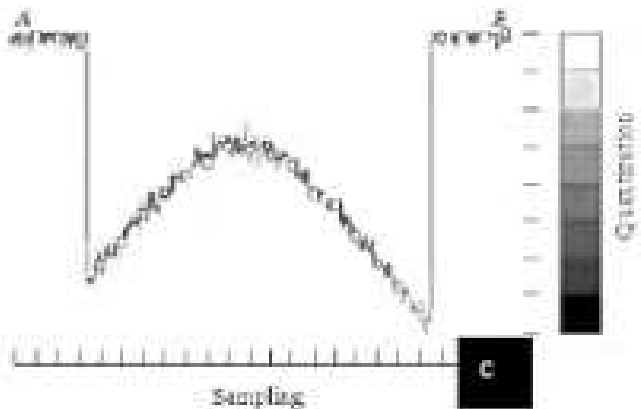
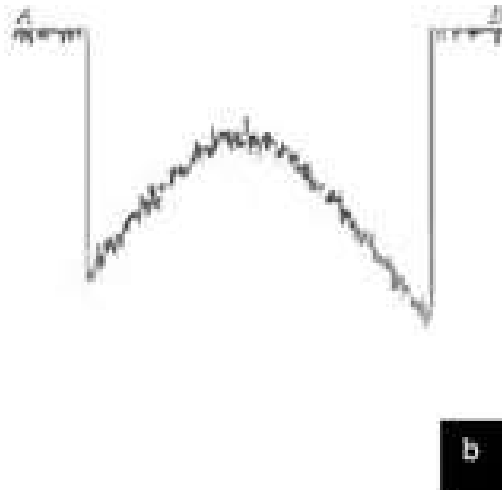
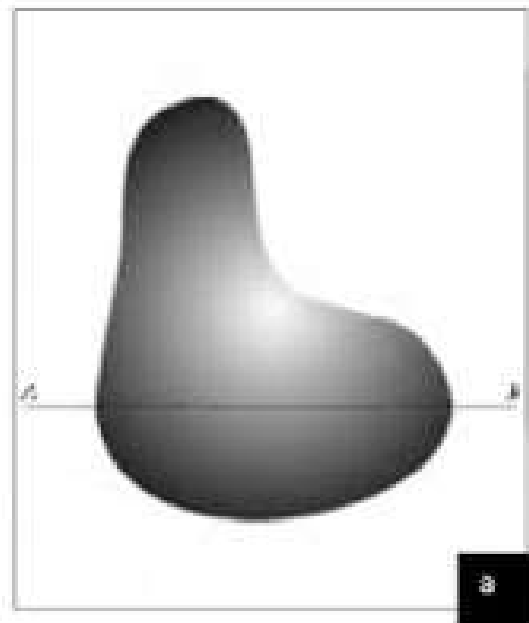


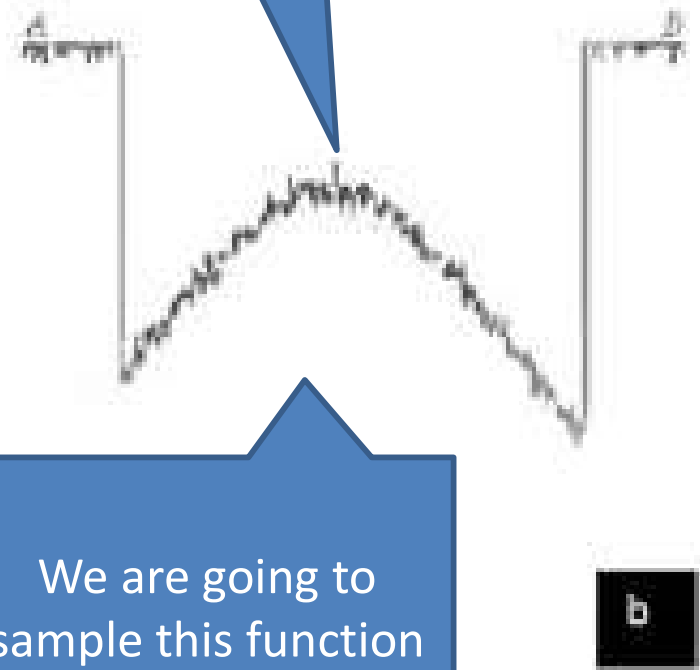
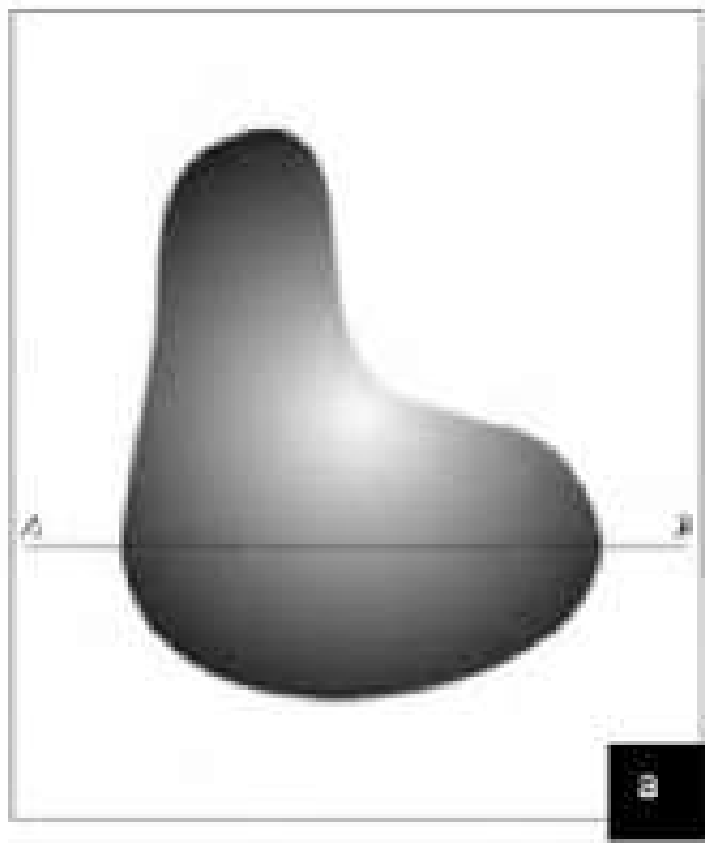
Image Sampling & Quantization (cont...)



Generating a digital image

- a:** continuous image
- b:** a scan line from A to B in the continuous image, used to illustrate the concept of sampling and quantization
- c:** Sampling and Quantization
- d:** Digital scan line

Image Sampling & Quantization (cont...)



Variations due to
noise

We are going to
sample this function

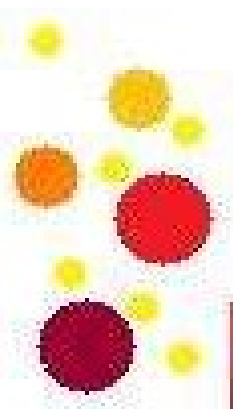


Image Sampling & Quantization (cont...)

- **Sampling**

- To sample this function, we take equally spaced samples along line AB.
- The location of each sample is given by a vertical thick mark in the bottom part of the figure.

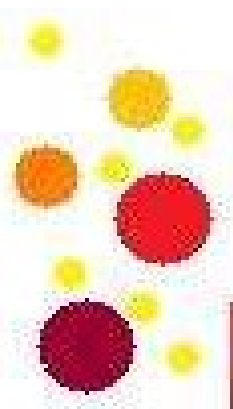
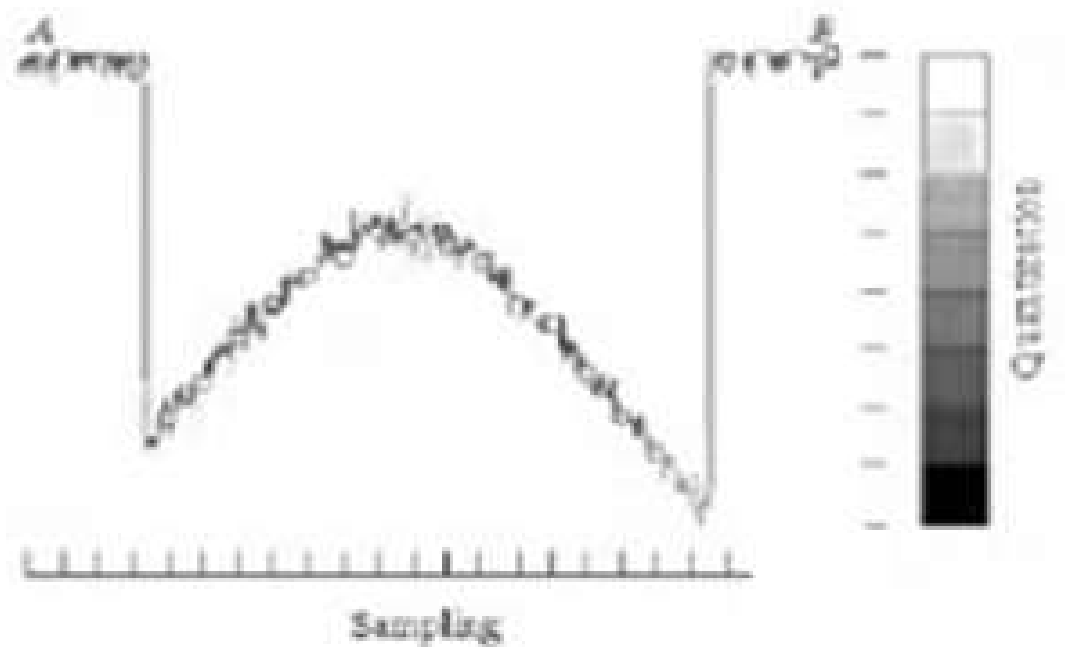


Image Sampling & Quantization

(cont...)

- The set of these discrete locations gives the sampled functions.
- However, the values of samples still span (vertically) a continuous range of gray level values.

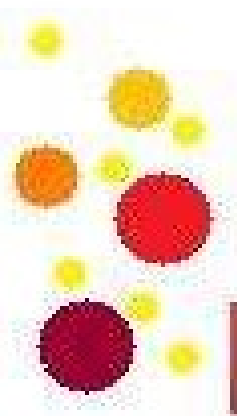


Image Sampling & Quantization (cont...)

- **Quantization**

- In order to form a digital function, the gray level values must be converted (quantized) into direct quantities.
- The right side of figure shows the gray level scale divided into eight discrete levels, ranging from black to white.
- The vertical thick marks indicate the specific values assigned to each of the eight gray levels.

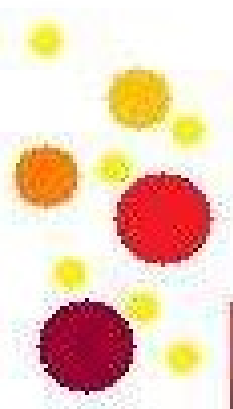
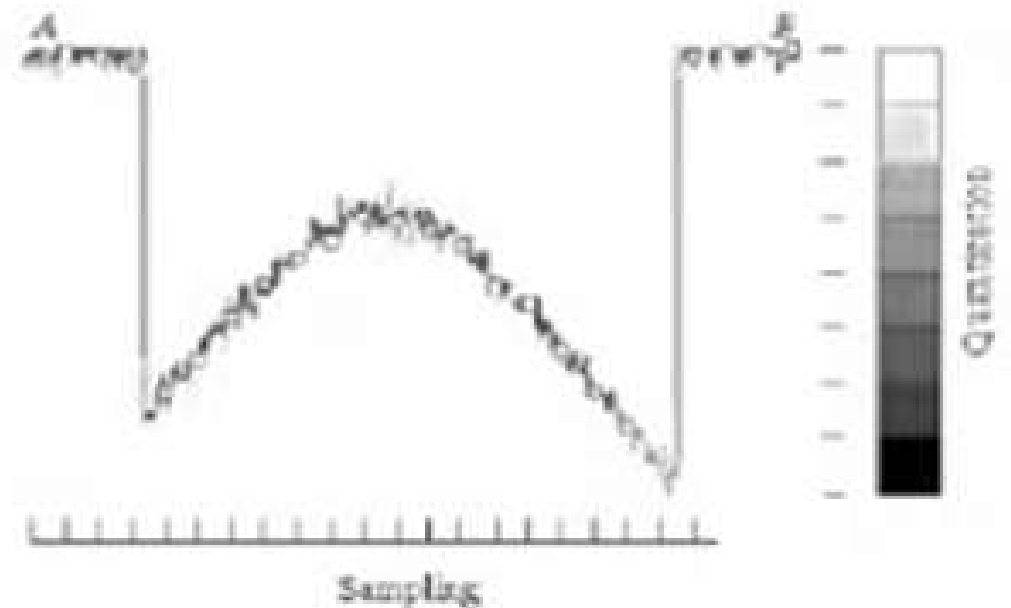
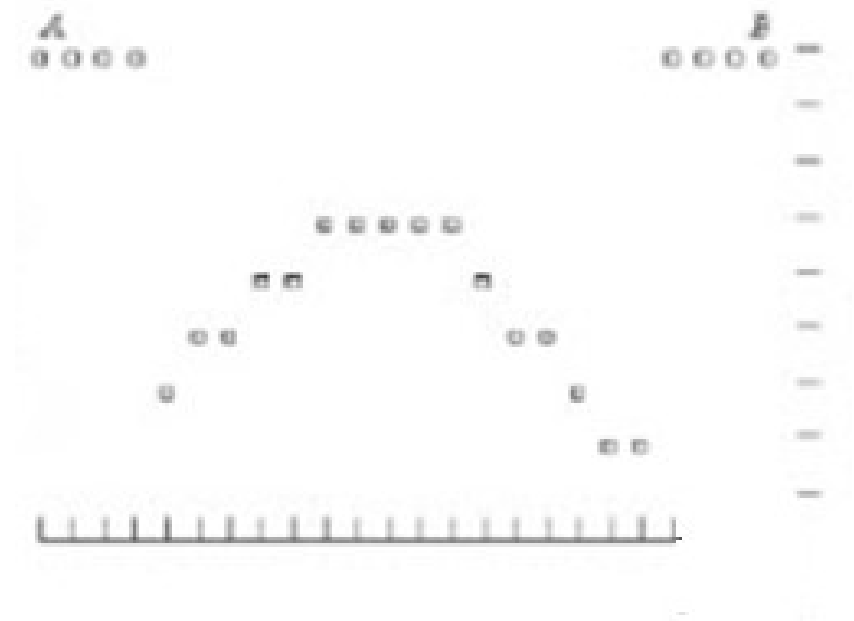


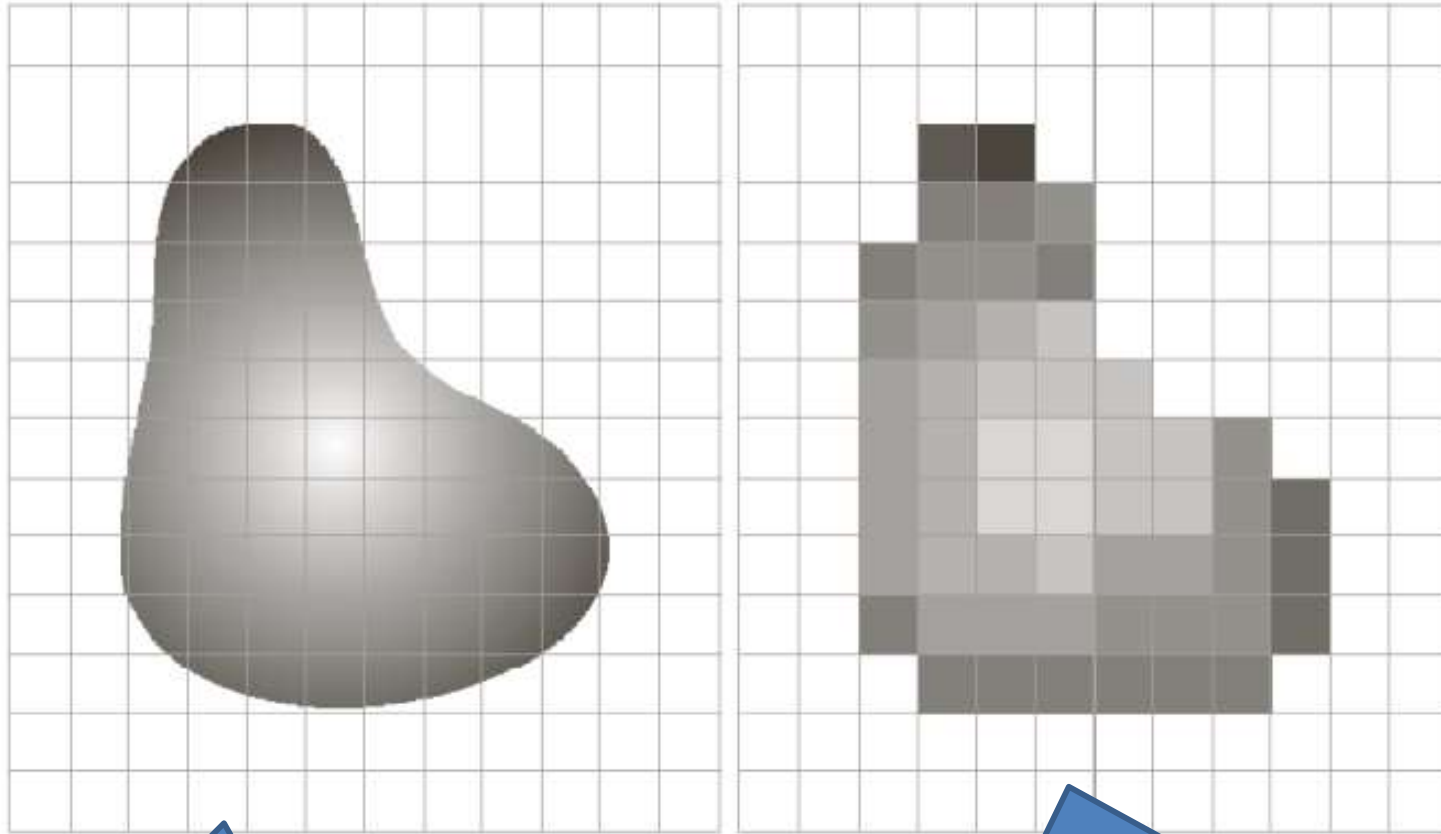
Image Sampling & Quantization (cont...)

- The continuous gray levels are quantized simply by assigning one of the eight discrete gray levels to each sample.
- The assignment is made depending on the vertical proximity of a sample to a vertical thick mark.



Starting at the top of the image and carrying out this procedure line by line produces a two dimensional digital image.

Image Sampling & Quantization (cont...)

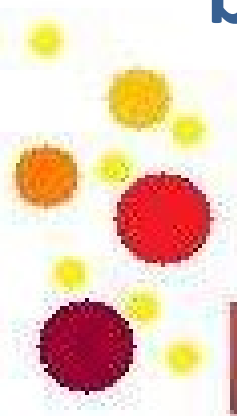


Continuous image projected
onto a sensor array.

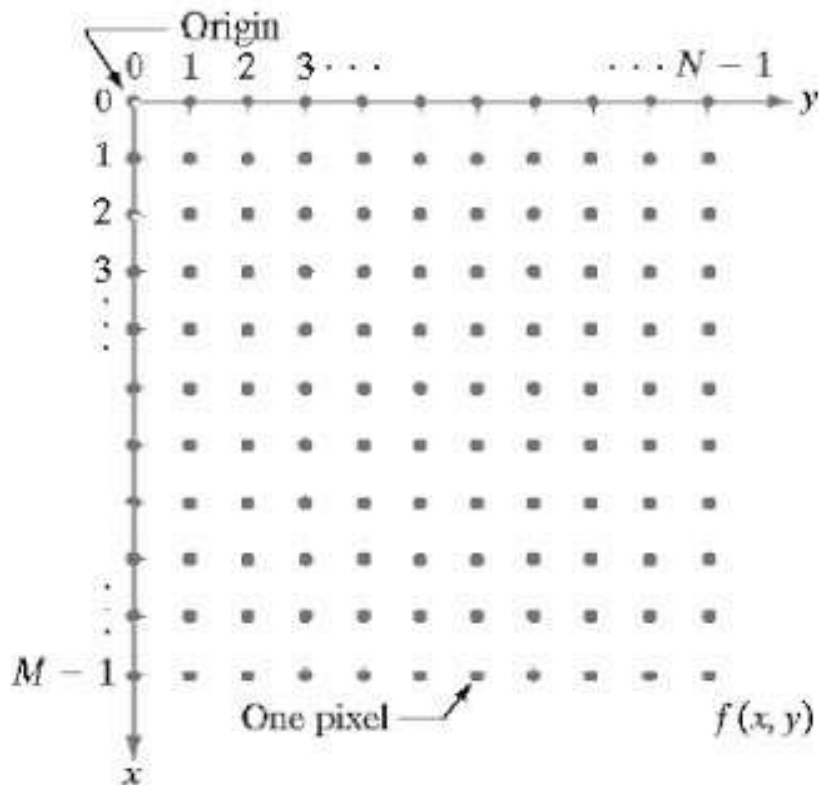
Result of image sampling and
quantization.

Representing Digital Images

- The result of sampling and quantization is a matrix of real numbers.
- Assume that an image $f(x,y)$ is sampled and so that the resulting digital image has M rows and N columns.
- The values of the coordinates (x,y) now become discrete quantities.



Representing Digital Image (cont...)

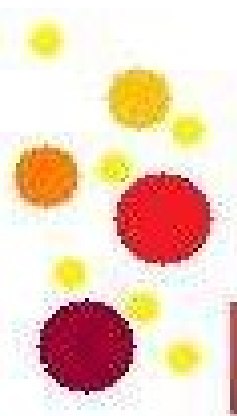


- We can denote the values of the coordinates at the origin are $(x, y) = (0, 0)$.
- It is important to keep in mind that the notation $(0, 1)$ is used to signify the first sample along the first row and so on.
- It does not mean that these are the actual values of physical coordinates when the image was sampled

Representing Digital Image (cont...)

- We can write the complete $M * N$ digital image in the following compact matrix form.

$$f(x, y) = \begin{bmatrix} f(0, 0) & f(0, 1) & \cdots & f(0, N - 1) \\ f(1, 0) & f(1, 1) & \cdots & f(1, N - 1) \\ \vdots & \vdots & & \vdots \\ f(M - 1, 0) & f(M - 1, 1) & \cdots & f(M - 1, N - 1) \end{bmatrix}.$$

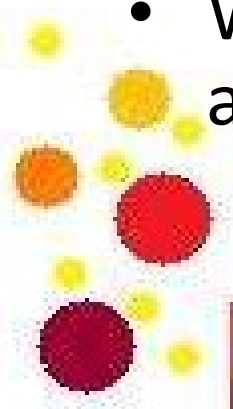


Representing Digital Image (cont...)

- The digitization process requires decisions about values for M , N and for the L number of discrete gray levels allowed for each pixel.
- M and N should be positive integers.
- However due to processing, storage and sampling hardware considerations, the number of gray levels typically is the integer power of 2 as expressed below;

$$L = 2^k$$

- We assume that the discrete levels are equally spaced and that they are integers in the interval $[0, L-1]$.



Representing Digital Image (cont...)

- The number of b of bits required to store a digitized image is

$$b = M * N * k$$

$$b = N^2 * k \text{ when } M=N$$

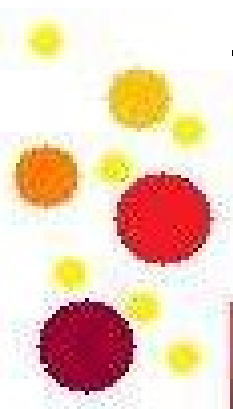
- Example: If $N = 32$ and $L = 256$, what is the value of b ?
 - If $L = 256$ then $k = 8$ because $L = 2^k$
 - Then $b = 32 * 32 * 8 = 8192$ bits
- When an image can have 2^k gray levels, it is common practice to refer to the image as a “**k bit image**”.
- For example an image with 256 possible gray level values called 8 bit image.



Representing Digital Image (cont...)

- Dynamic Range

- The lowest and highest intensity levels that a system can represent is denoted as dynamic range.
- This can be further explained as Contrast.
- When an appreciable number of pixels exhibit this property, the image will have high contrast.
- Conversely, an image with low dynamic range tends to have a dull, washed out gray look.

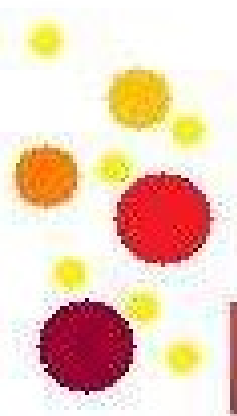


Representing Digital Image (cont...)



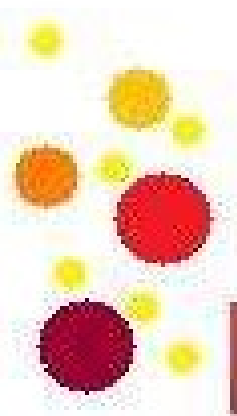
Reference

- Chapter 02 of Gonzalez, R.C., Woods, R.E., Digital Image Processing, 3rd ed. Addison-Wesley Pub.



Learning Outcomes Revisit

- Now, you should be able to;
 - describe the energy and the EM spectrum.
 - describe image acquisition methods.
 - discuss image formation model.
 - express sampling and quantization.
 - define dynamic range and image representation.



Next Lecture – Digital Image Fundamentals – II

QUESTIONS ?

