

Kick Start 2017 - Round F

Catch Them All

Problem

After the release of **Codejamon Go**, you, like many of your friends, took to the streets of your city to catch as many of the furry little creatures as you could. The objective of the game is to catch *Codejamon* that appear around your city by going to their locations. You are wondering how long it would take for you to catch them all!

Your city consists of **N** locations numbered from 1 to **N**. You start at location 1. There are **M** bidirectional roads (numbered from 1 to **M**). The *i*-th road connects a pair of distinct locations (U_i, V_i), and it takes D_i minutes to travel on it in either direction. It is guaranteed that it is possible to reach any other location from location 1 by travelling on one or more roads.

At time 0, a *Codejamon* will appear at a uniformly random location other than your current location (which is location 1 at time 0). Uniformly random means that the probability that it will appear at each of the **N** - 1 locations other than your current location is exactly $1 / (N - 1)$. The instant that a *Codejamon* appears, you can immediately start moving towards it. When you arrive at a location containing a *Codejamon*, you instantly catch it, and then a new *Codejamon* will instantly appear at a uniformly random location other than your current location, and so on. Notice that only one *Codejamon* is present at any given time, and you must catch the existing one before the next will appear.

Given the layout of your city, calculate the expected time to catch **P** *Codejamon*, assuming that you always take the fastest possible route between any two locations.

Input

The input starts with one line containing one integer **T**: the number of test cases. **T** test cases follow.

Each test case begins with one line containing 3 integers **N**, **M** and **P**, indicating the number of locations, roads, and *Codejamon* to catch, respectively.

Then, each test case continues with **M** lines; the *i*-th of these lines contains three integers U_i , V_i and D_i , indicating that the *i*-th road is between locations U_i and V_i , and it takes D_i minutes to travel on it in either direction.

Output

For each test case, output one line containing `Case #x: y`, where *x* is the test case number (starting from 1) and *y* is the expected time in minutes to catch **P** *Codejamon*. Your answer will be considered correct if it is within an absolute or relative error of 10^{-4} of the correct answer. See the [FAQ](#) for an explanation of what that means, and what formats of real numbers we accept.

Limits

$1 \leq T \leq 100$.

Time limit: 40 seconds per test set.

Memory limit: 1GB.

$$N - 1 \leq M \leq (N * (N - 1)) / 2.$$

$$1 \leq D_i \leq 10, \text{ for all } i.$$

$$1 \leq U_i < V_i \leq N, \text{ for all } i.$$

For all i and j with $i \neq j$, $U_i \neq U_j$ and/or $V_i \neq V_j$. (There is at most one road between any two locations.)

It is guaranteed that it is possible to reach any other location from location 1 by travelling on one or more roads.

Small dataset (Test set 1 - Visible)

$$2 \leq N \leq 50.$$

$$1 \leq P \leq 200.$$

Large dataset (Test set 2 - Hidden)

$$2 \leq N \leq 100.$$

$$1 \leq P \leq 10^9.$$

Sample

Sample Input

```
4
5 4 1
1 2 1
2 3 2
1 4 2
4 5 1
2 1 200
1 2 5
5 4 2
1 2 1
2 3 2
1 4 2
4 5 1
3 3 1
1 2 3
1 3 1
2 3 1
```

Sample Output

```
Case #1: 2.250000
Case #2: 1000.000000
Case #3: 5.437500
Case #4: 1.500000
```

In Sample Case #1, there is only one Codejamon for us to catch. With equal probability, it will appear at locations 2, 3, 4, and 5, which are at distances of 1, 3, 2, and 3, respectively, from our starting location 1. So the expected time it will take is $(1 + 3 + 2 + 3) / 4 = 2.25$ minutes.

In Sample Case #2, there are only two locations connected by one road. Every time a Codejamon appears, it will be in the location other than our current one, and we will have to take the road to get there. So we take the road 200 times, taking 5 minutes each time, for a total of 1000 minutes.

Sample Case #3 uses the same map as Sample Case #1. There are 16 ordered-pair possibilities for where the two Codejamon will appear, and doing the math yields an expected $87/16 = 5.4375$ minutes.

In Sample Case #4, the one Codejamon we need to catch will appear at location 2 or location 3. If it appears at location 2, it is better for us to get there in two minutes via the 1-to-3 and 3-to-2 roads, instead of taking the more time-consuming 1-to-2 road. So the expected time taken is $(2 + 1) / 2 = 1.5$ minutes.