

## Kick Start 2019 - Round D

# X or What?

### Problem

Steven has an array of  $N$  non-negative integers. The  $i$ -th integer (indexed starting from 0) in the array is  $A_i$ .

Steven really likes subintervals of  $A$  that are *xor-even*. Formally, a subinterval of  $A$  is a pair of indices  $(L, R)$ , denoting the elements  $A_L, A_{L+1}, \dots, A_{R-1}, A_R$ . The xor-sum of this subinterval is  $A_L \text{ xor } A_{L+1} \text{ xor } \dots \text{ xor } A_{R-1} \text{ xor } A_R$ , where xor is the [bitwise exclusive or](#).

A subinterval is *xor-even* if its xor-sum has an even number of set bits in its binary representation.

Steven would like to make  $Q$  modifications to the array. The  $i$ -th modification changes the  $P_i$ -th (indexed from 0) element to  $V_i$ . Steven would like to know, what is the size of the xor-even subinterval of  $A$  with the most elements after each modification?

### Input

The first line of the input gives the number of test cases,  $T$ .  $T$  test cases follow.

Each test case starts with a line containing two integers  $N$  and  $Q$ , denoting the number of elements in Steven's array and the number of modifications, respectively.

The second line contains  $N$  integers. The  $i$ -th of them gives  $A_i$  indicating the  $i$ -th integer in Steven's array.

Then,  $Q$  lines follow, describing the modifications. The  $i$ -th line contains  $P_i$  and  $V_i$ . The  $i$ -th modification changes the  $P_i$ -th element to  $V_i$ , indicating that the  $i$ -th modification changes the  $P_i$ -th (indexed from 0) element to  $V_i$ .

### Output

For each test case, output one line containing `Case #x: y_1 y_2 ... y_Q`, where  $x$  is the test case number (starting from 1) and  $y_i$  is the number of elements in the largest xor-even subinterval of  $A$  after the  $i$ -th modification. If there are no xor-even subintervals, then output 0.

### Limits

Time limit: 40 seconds per test set.

Memory limit: 1GB.

$1 \leq T \leq 100$ .

$0 \leq A_i < 1024$ .

$0 \leq P_i < N$ .

$0 \leq V_i < 1024$ .

### Test set 1 (Visible)

$1 \leq N \leq 100.$   
 $1 \leq Q \leq 100.$

### Test set 2 (Hidden)

$1 \leq N \leq 10^5.$   
 $1 \leq Q \leq 10^5.$

### Sample

Sample Input	Sample Output
2 4 3 10 21 3 7 1 13 0 32 2 22 5 1 14 1 15 20 26 4 26	Case #1: 4 3 4 Case #2: 4

In Sample Case 1,  $N = 4$  and  $Q = 3$ .

- After the 1st modification,  $\mathbf{A}$  is [10, 13, 3, 7]. The subinterval (0, 3) has xor-sum  $10 \text{ xor } 13 \text{ xor } 3 \text{ xor } 7 = 3$ . In binary, the xor-sum is  $11_2$ , which has an even number of 1 bits, so the subinterval is xor-even. This is the largest subinterval possible, so the answer is 4.
- After the 2nd modification,  $\mathbf{A}$  is [32, 13, 3, 7]. The largest xor-even subinterval is (0, 2), which has xor-sum  $32 \text{ xor } 13 \text{ xor } 3 = 46$ . In binary, this is  $101110_2$ .
- After the 3rd modification,  $\mathbf{A}$  is [32, 13, 22, 7]. The largest xor-even subinterval is (0, 3) again, which has xor-sum  $32 \text{ xor } 13 \text{ xor } 22 \text{ xor } 7 = 60$ . In binary, this is  $111100_2$ .

In Sample Case 2,  $N = 5$  and  $Q = 1$ . After the 1st modification,  $\mathbf{A}$  is [14, 1, 15, 20, 26]. The largest xor-even subinterval is (1, 4), which has xor sum  $1 \text{ xor } 15 \text{ xor } 20 \text{ xor } 26 = 0$ . In binary, this is  $0_2$ .