

Analysis: Speed Typing

For better understanding, let us define some variables:

N : Length of string **I**

M : Length of string **P**

Test Set 1

All the characters in String **I** are the same, let us say that character is C . This means that **I** is made up entirely of character C occurring N times.

We need to check if **P** contains C at least N number of times (recall that N denotes the length of string **I**). This can be done by simply maintaining a count of C in **P**. If this count is greater than or equal to N , then the number of characters to be removed would be $(M - N)$, which is the number of extra characters in **P**. Else, the answer is IMPOSSIBLE.

Time and Space Complexity: All operations including counting the appearances of C in **P** can be done in $O(M)$ time, which is the overall time complexity of this solution. Extra space required would be of the order of $O(1)$.

Test Set 2

Observe that we are trying to condense **P** to **I** by deleting some characters from **P** without disturbing their order. This directly leads us to the definition of a subsequence:

A subsequence is a sequence that can be derived from another sequence by deleting some elements without changing the order of the remaining elements.

- If **I** is not a subsequence of **P**, the answer is IMPOSSIBLE. This can take place when:
 - Case 1: **P** is shorter than **I**
 - Case 2: A character in **I** is not present in **P**
 - Case 3: A character in **I** is present in **P**, but not at the right place
- If **I** is a subsequence of **P**, then **P** contains all characters of **I** in the same order along with some extra characters (possibly 0). Barbara will have to hit backspace on these extra characters to correct the string. The answer would be $(M - N)$.

Time and Space Complexity: Subsequence check can be done in $O(M)$ time using a two-pointer approach. The overall time complexity of this solution comes out to be $O(M)$ as well. Extra space required would be of the order of $O(1)$.

Pseudocode for Subsequence Check:

```
FUNCTION checkSubSequence(String I, String P) RETURNS BOOLEAN
```

```
    // Assign lengths of I and P to variables N and M
    N <- Length of I
    M <- Length of P
```

```
    // Declare pointers ptrI and ptrP to the current position in I and P respectively
    // and assign them to position 0
    ptrI <- 0
    ptrP <- 0
```

```
    // Traverse both strings, and compare current character of P with first unmatched char of I
    // While making sure the pointers do not go out of bounds of their respective strings
    WHILE ptrI is less than N AND ptrP is less than M
```

```
        // If characters at current positions match, then move ahead in both I and P
        IF I[ptrI] equals P[ptrP]
            ptrI <- ptrI + 1
            ptrP <- ptrP + 1
```

```
        // If the characters at current the positions do not match, then move ahead only in P
        ELSE
            ptrP <- ptrP + 1
```

```
    ENDIF
```

```
ENDWHILE

// If we reach past the end of I, we have successfully matched all the characters of I
// to some characters of P
// If not, some characters in I remain unmatched and it is not a subsequence of P
IF ptrI equals N
    RETURN True;

ELSE
    RETURN False;

ENDIF

ENDFUNCTION
```