Kick Start 2015 - Round A

gCube

Problem

Googlers are very interested in cubes, but they are bored with normal three-dimensional cubes and also want to think about other kinds of cubes! A "D-dimensional cube" has D dimensions, all of equal length. (D may be any positive integer; for example, a 1-dimensional cube is a line segment, and a 2-dimensional cube is a square, and a 4-dimensional cube is a hypercube.) A "D-dimensional cuboid" has D dimensions, but they might not all have the same lengths.

Suppose we have an **N**-dimensional cuboid. The **N** dimensions are numbered in order (0, 1, 2, ..., N-1), and each dimension has a certain length. We want to solve many subproblems of this type:

- 1. Take all consecutive dimensions between the L_i -th dimension and R_i -th dimension, inclusive.
- 2. Use those dimensions to form a D-dimensional cuboid, where $D = R_i L_i + 1$. (For example, if $L_i = 3$ and $R_i = 6$, we would form a 4-dimensional cuboid using the 3rd, 4th, 5th, and 6th dimensions of our **N**-dimensional cuboid.)
- 3. Reshape it into a D-dimensional cube that has exactly the same volume as that D-dimensional cuboid, and find the edge length of that cube.

Each test case will have **M** subproblems like this, all of which use the same original **N**-dimensional cuboid.

Input

The first line of the input gives the number of test cases, **T**. **T** test cases follow.

Each test case begins with two integers \mathbf{N} and \mathbf{M} ; \mathbf{N} is the number of dimensions and \mathbf{M} is the number of queries. Then there is one line with \mathbf{N} positive integers $\mathbf{a_i}$, which are the lengths of the dimensions, in order. Then, \mathbf{M} lines follow. In the ith line, there are two integers $\mathbf{L_i}$ and $\mathbf{R_i}$, which give the range of dimensions to use for the ith subproblem.

Output

For each test case, output one line containing "Case #x:", where x is the test case number (starting from 1). After that, output **M** lines, where the ith line has the edge length for the ith subproblem. An edge length will be considered correct if it is within an absolute error of 10^{-6} of the correct answer. See the <u>FAQ</u> for an explanation of what that means, and what formats of real numbers we accept.

Limits

Time limit: 30 seconds per test set. Memory limit: 1GB. $1 \le T \le 100$. $1 \le a_i \le 10^9$. $0 \le L_i \le R_i < N$.

Small dataset (Test Set 1 - Visible)

```
1 \le N \le 10.
1 \le M \le 10.
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Large dataset (Test Set 2 - Hidden)

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1 \le N \le 1000.
1 \le M \le 100.
```

Sample

Sample Input 2 2 2 1 4 0 0 0 1 3 2 1 2 3 0 1 1 2

Sample Output

Case #1: 1.000000000 2.000000000 Case #2: 1.414213562 2.449489743