

Analysis: Beauty of tree

For a given node, the $P(\text{visited by either Amadea or Bilva}) = 1 - P(\text{not visited by Amadea nor Bilva})$.

This leads to $P(\text{visited by either Amadea or Bilva}) = 1 - ((1 - P(\text{visited by Amadea})) * (1 - P(\text{visited by Bilva})))$

i.e. For a given node, note that events of visited-by-Amadea and visited-by-Bilva are [mutually independent events](#), and hence $P(\text{being visited by either Amadea or Bilva}) = P(\text{visited by Amadea}) + P(\text{visited by Bilva}) - (P(\text{visited by Amadea}) * P(\text{visited by Bilva}))$

Given the above formula, our goal now is to find out $P(\text{visited by Amadea})$ and $P(\text{visited by Bilva})$ for every node in the tree. We can use DFS in order to do this.

Firstly, let's define 2 variables `visits_a[]` and `visits_b[]` where `visits_a[i]` and `visits_b[i]` denote the number of visits to node-*i* across all paths starting from any node in the subtree of node *i* with skips **A** and **B** respectively.

Now, the first DFS run would be from node-1 to compute `visits_a[]`. As we perform this DFS, we can keep a track of the path that has been taken so far, let's say `path_taken[]`. As we enter a node-*i*, we add it to `path_taken[]` and call DFS on it's children. Once we come back to node-*i*, we remove it from the `path_taken[]` and increment `visits_a[i]` by 1. Note that this increment is for the path leading from node-*i* to itself. Next, we check if there is some node-*j* which is **A** skips behind node-*i*. Using `path_taken[]`, we check to see if such a node is present and increment the `visits_a[node-j]` by `visits_a[i]`. At the end of this DFS run, we have the total visit count for all nodes with the skip distance of **A**. Now, dividing `visits_a[]` by **N** gives us the $P(\text{visited by Amadea})$ for each node in the tree. Repeat the above process for to compute `visits_b[]` and obtain $P(\text{visited by Bilva})$ for every node in the tree.

With $P(\text{visited by Amadea})$ and $P(\text{visited by Bilva})$ computed for every node in the tree, computing and summing over $P(\text{being visited by either Amadea or Bilva})$ for each node will give us the answer. Since DFS takes linear time in the number of vertices, the time complexity of the solution is $O(N)$.