

Pixelated Circle

Problem

Typical computer images are matrices of pixels, with each pixel being a small square of a specific color. Drawing lines that are not perfectly parallel to the axes of the pixel matrix results in imperfections. Drawing circles is an extreme example where those imperfections arise.

Suppose we have a picture consisting of $2R + 1$ by $2R + 1$ pixels, and we number the rows and columns of pixels between $-R$ and R , such that the center pixel is at row 0 and column 0. Initially, all pixels are white. Then, a circle of radius R and centered in the picture can be drawn in black by the following pseudocode, where `set_pixel_to_black(x, y)` makes the pixel at row x and column y be colored black.

```
draw_circle_perimeter(R):
  for x between -R and R, inclusive {
    y = round(sqrt(R * R - x * x)) # round to nearest integer, breaking ties towards zero
    set_pixel_to_black(x, y)
    set_pixel_to_black(x, -y)
    set_pixel_to_black(y, x)
    set_pixel_to_black(-y, x)
  }
```

Notice that some pixels may be set to black more than once by the code, but the operation is idempotent (that is, calling `set_pixel_to_black` on a pixel that is already black changes nothing).

The following is pseudocode for a function to draw a filled circle (starting from an all-white picture).

```
draw_circle_filled(R):
  for x between -R and R, inclusive {
    for y between -R and R, inclusive {
      if round(sqrt(x * x + y * y)) <= R:
        set_pixel_to_black(x, y)
    }
  }
```

And finally, the following is pseudocode to incorrectly draw a filled circle:

```
draw_circle_filled_wrong(R):
  for r between 0 and R, inclusive {
    draw_circle_perimeter(r)
  }
```

Given R , calculate the number of pixels that would have different colors between a picture in which `draw_circle_filled(R)` is called and another one in which `draw_circle_filled_wrong(R)` is called.

Input

The first line of the input gives the number of test cases, T . T test cases follow. Each test case is described in a single line containing a single integer R , the radius of the circle to draw.

Output

For each test case, output one line containing `Case #x: y`, where x is the test case number (starting from 1) and y is the number of pixels that would have different colors between a picture in which `draw_circle_filled(R)` is called and another one in which `draw_circle_filled_wrong(R)` is called.

Limits

Memory limit: 1 GB.
 $1 \leq T \leq 100$.

Test Set 1 (Visible Verdict)

Time limit: 10 seconds.
 $1 \leq R \leq 100$.

Test Set 2 (Hidden Verdict)

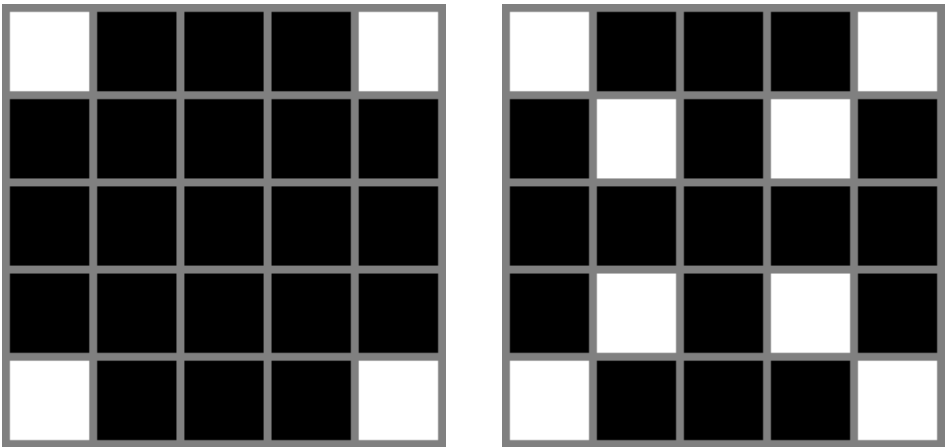
Time limit: 15 seconds.

$1 \leq R \leq 10^5$.

Sample

Sample Input	Sample Output
3 2 8 50	Case #1: 4 Case #2: 24 Case #3: 812

In Sample Case #1, 21 pixels are drawn in black by calling `draw_circle_filled(2)` (shown in the left picture). 17 pixels are drawn in black by calling `draw_circle_filled_wrong(2)` (shown in the right picture). Four pixels would have different colors between the two pictures: $(-1, -1)$, $(-1, 1)$, $(1, -1)$, and $(1, 1)$, where (x, y) represents the pixel at row x and column y , with the rows and columns numbered as described in the statement.



In Sample Case #2, the following pictures are the images generated by calling `draw_circle_filled(8)` (left) and `draw_circle_filled_wrong(8)` (right).

