

## Kick Start 2014 - Round B

# Parentheses Order

### Problem

An  $n$  parentheses sequence consists of  $n$  (s and  $n$  ) s.

A valid parentheses sequence is defined as the following:

*You can find a way to repeat erasing adjacent pair of parentheses ( ) until it becomes empty.*

For example, ( ( ) ) is a valid parentheses, you can erase the pair on the 2nd and 3rd position and it becomes ( ) then you can make it empty.

) ( ) ( is not a valid parentheses, after you erase the pair on the 2nd and 3rd position, it becomes ) ( and you cannot erase any more.

Now, we have all valid  $n$  parentheses sequences. Find the  $k$ -th smallest sequence in lexicographical order.

For example, here are all valid 3 parentheses sequences in lexicographical order:

```
(( ( )) )
( ( ) ( )
( ( ) ) ( )
( ) ( ( )
( ) ( ) ( )
```

### Input

The first line of the input gives the number of test cases,  $T$ .  $T$  lines follow. Each line represents a test case consisting of 2 integers,  $n$  and  $k$ .

### Output

For each test case, output one line containing "Case #x: y", where x is the test case number (starting from 1) and y is the  $k$ -th smallest parentheses sequence in all valid  $n$  parentheses sequences. Output "Doesn't Exist!" when there are less than  $k$  different  $n$  parentheses sequences.

### Limits

Time limit: 30 seconds per test set.

Memory limit: 1GB.

$1 \leq T \leq 100$ .

#### Small dataset (Test set 1 - Visible)

$1 \leq n \leq 10$ .

$1 \leq k \leq 100000$ .

#### Large dataset (Test set 2 - Hidden)

$1 \leq n \leq 100$ .  
 $1 \leq k \leq 10^{18}$ .

## Sample

### Sample Input

```
3
2 2
3 4
3 6
```

### Sample Output

```
Case #1: () ()
Case #2: () (())
Case #3: Doesn't Exist!
```