

# Multi-base happiness

## Problem

Given an integer  $N$ , replace it by the sum of the squares of its digits. A happy number is a number where, if you apply this process repeatedly, it eventually results in the number 1. For example, if you start with 82:

$$\begin{aligned} 8*8 + 2*2 &= 64 + 4 = 68, \text{ repeat:} \\ 6*6 + 8*8 &= 36 + 64 = 100, \text{ repeat:} \\ 1*1 + 0*0 + 0*0 &= 1 + 0 + 0 = 1 \text{ (happy! :)} \end{aligned}$$

Since this process resulted in 1, 82 is a happy number.

Notice that a number might be happy in some bases, but not happy in others. For instance, the base 10 number 82 is not a happy number when written in base 3 (as 10001).

You are one of the world's top number detectives. Some of the bases got together (yes, they are organized!) and hired you for an important task: find out what's the smallest integer number that's greater than 1 and is happy in all the given bases.

## Input

The first line of input gives the number of cases  $T$ .  $T$  test cases follow. Each case consists of a single line. Each line contains a space separated list of distinct integers, representing the bases. The list of bases is always in increasing order.

## Output

For each test case, output:

Case # $X$ :  $K$

where  $X$  is the test case number, starting from 1, and  $K$  is the decimal representation of the smallest integer (greater than 1) which is happy in all of the given bases.

## Limits

Time limit: 60 seconds per test set.

Memory limit: 1 GB.

$2 \leq$  all possible input bases  $\leq 10$

## Small dataset

$1 \leq T \leq 42$

$2 \leq$  number of bases on each test case  $\leq 3$

## Large dataset

$1 \leq T \leq 500$

$2 \leq \text{number of bases on each test case} \leq 9$

## Sample

### Sample Input

```
3
2 3
2 3 7
9 10
```

### Sample Output

```
Case #1: 3
Case #2: 143
Case #3: 91
```

## Important Note

Please remember that you must submit all code used to solve the problem.