# **Symmetric Trees**

#### **Problem**

Given a vertex-colored tree with N nodes, can it be drawn in a 2D plane with a line of symmetry?

Formally, a tree is *line-symmetric* if each vertex can be assigned a location in the 2D plane such that:

- All locations are distinct.
- If vertex v<sub>i</sub> has color C and coordinates (x<sub>i</sub>, y<sub>i</sub>), there must also be a vertex v<sub>i</sub>' of color C located at (-x<sub>i</sub>, y<sub>i</sub>) -- Note if x<sub>i</sub> is 0, v<sub>i</sub> and v<sub>i</sub>' are the same vertex.
- For each edge (v<sub>i</sub>, v<sub>i</sub>), there must also exist an edge (v<sub>i</sub>', v<sub>i</sub>').
- If edges were represented by straight lines between their end vertices, no two edges would share any points except where adjacent edges touch at their endpoints.

### Input

The first line of the input gives the number of test cases, **T**. **T** test cases follow.

Each test case starts with a line containing a single integer **N**, the number of vertices in the tree.

**N** lines then follow, each containing a single uppercase letter. The i-th line represents the color of the i-th node.

**N**-1 lines then follow, each line containing two integers i and j ( $1 \le i < j \le N$ ). This denotes that the tree has an edge from the i-th vertex to the j-th vertex. The edges will describe a connected tree.

### Output

For each test case, output one line containing "Case #x: y", where x is the case number (starting from 1) and y is "SYMMETRIC" if the tree is line-symmetric by the definition above or "NOT SYMMETRIC" if it isn't.

#### Limits

Memory limit: 1 GB.  $1 \le T \le 100$ .

#### **Small dataset**

Time limit: 60 seconds.  $2 \le \mathbb{N} \le 12$ .

#### Large dataset

Time limit: 120 seconds.  $2 \le \mathbb{N} \le 10000$ .

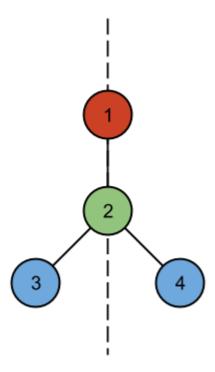
## Sample

## Sample Input 3 4 R G В В 1 2 2 3 2 4 4 R G В Y 1 2 2 3 2 4 12 Υ В Y G $\mathsf{R}$ G Υ Υ В В В R 1 3 1 9 1 10 2 3 3 7 3 8 3 11 4 8 5 7 6 7 8 12

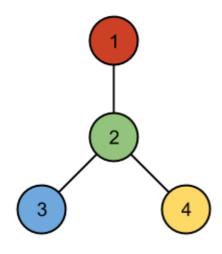
## Sample Output

Case #1: SYMMETRIC
Case #2: NOT SYMMETRIC
Case #3: SYMMETRIC

The first case can be drawn as follows:



No arrangement of the second case has a line of symmetry:



One way of drawing the third case with a symmetry line is as follows:

