Tulorial 6

Soll) Minimum spanning tree is a subset of the edges of a connected edger weighted undisected graph that connects all the vestions together without any cycles & with the minimal possible that edge weighted.

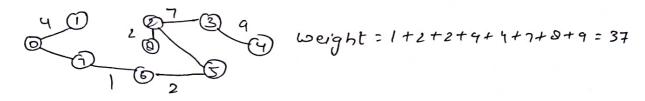
Applications -

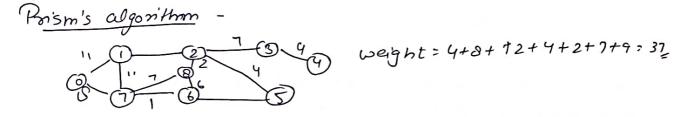
O consider n stations are to be linked using a communication network and lying of communication link between any two stethens involves a cost.

- 1 The ideal solution would be to extract a subgrouph termed as minimum Cost spanning bee.
- 3 Suppose you want to construct highways or railroads spanning several cities, then we can use the consept of minimum spanning trees.
- 1 Designing LAN
- 15 Laying pipelines connecting offshore drilling, sites, refineries & consumer markets.
- (6) Suppose you meant to apply a set of houses with-
 - -> Electric Power
 - water
 - Telephone lines
 - Sewege lines
- Sol2) Time complexity of prim's algorithm; O (IEIlog IVI) Space complexity of prim's algo : O[VI
 - -> Time complexity of Kruskal's algo : 01 \$ 109 181
 - -> Ipace complexity of Kruskal's algo; (0/V1).
 - -> Tromprof Dijkstog's algo 10(v2)
 - Sicompiof Dijkstra's algo 10 (v2)
 - -> Tramprof Bellman ford's algo 6(VE)
 - Space complexity of Beleman ford's algo O(E)

5013)

Kruskal's algorithm;





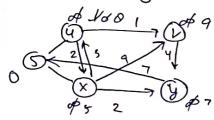
Soly i) The shortest path may change. The xavon is there may be different number of edges in different paths from 's' to 't', for eg, let shortest path bl of weight is and has edges edges.

Let there be another path with 2 edges and between weight 25.

The weight of the shortest path is increased by 5 VIo and becomes 15+50. Weight of the other path is increased by 2 VIo E becomes 25+20.50, the shortest path changes to the other path weight as 45.

(ii) If we multiply all edges weight by 60, the shoolest path doesn't change. The season is simple, weights of all paths from (3) to (t', get multiplied by some amount. The number of edges on a path doesn't matter. It was like changing units of weights.

Sols - Dijkstra Algorithm



node shortest dist from source node

u 8 n 5 v 9 7

-> Bellman food algorithm -

15+ \$\int \tilde{\tilde

graph doesn't have -ve eycle.

