

Q Given that, $f(x, y) = 3x^2 + 1$, $x_0 = 1$, $y_0 = 2$ & $h = 0.5$
 $x_1 = x_0 + h = 1 + 0.5 = 1.5$, $x_2 = x_0 + 2h = 1 + 2 \times 0.5 = 2$
 $x_3 = x_0 + 3$.

By Euler's Formula, $y_n = y(x_n) = y_{n-1} + hf(x_{n-1}, y_{n-1})$
 $n=1$, $y_1 = y(x_1) = y(1.5) = y_0 + hf(x_0, y_0)$
 $= y_0 + h(3x_0^2 + 1)$
 $= 2 + 0.5(3 \times 1^2 + 1)$
 $y(1.5) = 4$
 $n=2$, $y_2 = y(x_2) = y(2) = y_1 + hf(x_1, y_1)$
 $= 4 + 0.5 \times (3 \times 1.5^2 + 1)$
 $y(2) = 7.875$

When $h = 0.25$, $x_1 = x_0 + h = 1 + 0.25 = 1.25$
 $x_2 = x_0 + 2h = 1 + 2 \times 0.25 = 1.5$
 $x_3 = x_0 + 3h = 1 + 3 \times 0.25 = 1.75$
 $x_4 = x_0 + 4h = 1 + 4 \times 0.25 = 2$.

$n=1$, $y_1 = y(x_1) = y(1.25) = y_0 + h(3x_0^2 + 1) = 2 + 0.25 \times (3 \times 1^2 + 1)$
 $y_1 = y(1.25) = 3$
 $n=2$, $y_2 = y(x_2) = y(1.5) = y_1 + h(3x_1^2 + 1) = 3 + 0.25 \times (3 \times 1.25^2 + 1)$
 $y_2 = y(1.5) = 4.421875$
 $n=3$, $y_3 = y(x_3) = y(1.75) = y_2 + h(3x_2^2 + 1) = 4.421875 + 0.25 \times (3 \times 1.5^2 + 1)$
 $y_3 = y(1.75) = 6.359375$
 $n=4$, $y_4 = y(x_4) = y(2) = y_3 + h(3x_3^2 + 1) = 6.359375 + 0.25 \times (3 \times 1.75^2 + 1)$
 $y_4 = y(2) = 8.90625$.

Compare $y(2)$ in 1st and 2nd,

$$y(2) = 8.90625 - 7.875 = 1.03125$$

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