

PGPDSE FT Mini-Project – Machine Learning Title: Car Price Prediction

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PROBLEM STATEMENT:

A Chinese automobile company Geely Auto aspires to enter the US market by setting up their manufacturing unit there and producing cars locally to give competition to their US and European counterparts. They have contracted an automobile consulting company to understand the factor on which the price of cars depends. Specifically, they want to understand the factors affecting the pricing of cars in the American market, since those may be very different from the Chinese market.

The company wants to know:

- Which variables are significant in predicting the price of a car.
- How well those variables describe the price of a car.

Based on various market surveys, the consulting firm has gathered a large dataset of different types of cars across the American market

ATTRIBUTES:

- Car_ID Unique ID for each observation.
- Symboling Its assigned insurance risk rating, value +3 indicates that the auto is risky,
 3 that it is pretty safe.
- carCompany Name of company.
- fueltype Car fuel type.
- aspiration Aspiration used in car.
- doornumber Number of doors in a car.
- carbody body of car.
- drivewheel type of drive wheel.



- enginelocation location of car engine
- wheelbase Wheelbase of car.
- carlength length of car.
- carwidth width of car.
- carheight height of car.
- curbweight The weight of a car without occupants or luggage.
- enginetype type of engine.
- cylindernumber cylinder placed in the car.
- enginesize size of car.
- fuelsystem Fuel system of car.
- boreratio Boreratio of car.
- stroke Stroke or volume inside the engine.
- compression ratio compression ratio of car.
- horsepower Horsepower
- peakrpm car peak rpm
- citympg Mileage in city
- highwaympg Mileage on highway

OBJECTIVES:

You are required to model the prices of cars with the available independent variables. It will be used by management to understand how exactly the prices vary with the independent variables. They can accordingly manipulate the design of the cars, the business strategy etc. to meet certain price levels. Further, the model will be good for management to understand the pricing dynamics of the new market.



Step 1:

Importing the libraries:

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error
import warnings
warnings.filterwarnings('ignore')
```

Step 2:

Reading the Dataset:

```
# Importing the dataset
car_data = pd.read_csv('CarPrice_Assignment.csv')
car_data.head()
```

	car_ID	symboling	CarName	fueltype	aspiration	doornumber	carbody	drivewheel	enginelocation	wheelbase	 enginesize	fuelsystem	boreratio	st
0	1	3	alfa-romero giulia	gas	std	two	convertible	rwd	front	88.6	130	mpfi	3.47	
1	2	3	alfa-romero stelvio	gas	std	two	convertible	rwd	front	88.6	130	mpfi	3.47	
2	3	1	alfa-romero Quadrifoglio	gas	std	two	hatchback	rwd	front	94.5	 152	mpfi	2.68	
3	4	2	audi 100 ls	gas	std	four	sedan	fwd	front	99.8	 109	mpfi	3.19	
4	5	2	audi 100ls	gas	std	four	sedan	4wd	front	99.4	136	mpfi	3.19	

5 rows × 26 columns

Step 3:

Checking the dimension of the dataset:

```
# # Checking the dimensions of the dataset
print("Dimensions of the dataset: ", car_data.shape)
Dimensions of the dataset: (205, 26)
```

Checking the datatype of the columns:

```
# # Checking the data types of columns
print("\nData types of columns:\n", car_data.dtypes)
```

```
Data types of columns:
car_ID
symboling
                           int64
                          int64
CarName
                         object
fueltype
aspiration
                         object
                         object
doornumber
                         object
carbody
                         object
drivewheel
                        object
object
float64
enginelocation
wheelbase
carlength
                        float64
carwidth
carheight
                       float64
float64
curbweight
                          int64
enginetype
                         object
cylindernumber
                         object
int64
enginesize
fuelsystem
                         object
boreratio
stroke
                       float64
float64
compressionratio
horsepower
                          int64
peakrpm
                          int64
citympg
                          int64
highwaympg
                          int64
price
                       float64
dtype: object
```



Checking for missing values:

```
1 # # Checking for missing values
 print("\nMissing values:\n", car_data.isnull().sum())
Missing values:
car ID
                     0
symboling
                    0
CarName
                    0
fueltype
                    0
aspiration
                    0
doornumber
carbody
                    0
drivewheel
                    0
enginelocation
                    0
wheelbase
carlength
                    0
carwidth
                    0
carheight
                    0
curbweight
enginetype
                    0
cylindernumber
                    0
enginesize
boreratio
                    0
stroke
                    0
compressionratio
horsepower
peakrpm
                    0
citympg
                    0
highwaympg
                    0
dtype: int64
```

Getting the Descriptive Statistics of the data:

```
1 # # Descriptive statistics
    print("\nDescriptive statistics:\n", car_data.describe().T)
Descriptive statistics:
                   count
                                                 std
                                                          min
                                                                   25% \
                           103.000000
                                         59.322565
                                                        1.00
                                                                52.00
car ID
                  205.0
symboling
                  205.0
                             0.834146
                                          1.245307
                                                       -2.00
                                                                 0.00
wheelbase
                  205.0
                            98.756585
                                          6.021776
                                                       86.60
                                                                94.50
                  205.0
                           174.049268
                                         12.337289
                                                      141.10
                                                               166.30
carlength
carwidth
                            65.907805
                                          2.145204
                  205.0
carheight
                  205.0
                            53.724878
                                          2.443522
                                                       47.80
curbweight
                  205.0
                          2555.565854
                                        520.680204
                                                     1488.00
                                                             2145.00
                           126.907317
                                         41.642693
                  205.0
                                                       61.00
                                                                97.00
enginesize
                             3.329756
                                          0.270844
boreratio
                  205.0
stroke
                  205.0
                             3.255415
                                          0.313597
                                                        2.07
                                                                 3.11
compressionratio
                  205.0
                            10.142537
                                          3.972040
                                                        7.00
                                                                 8.60
                  205.0
                           104.117073
                                         39.544167
                                                       48.00
                                                                70.00
horsepower
peakrpm
                  205.0
                          5125.121951
                                        476.985643 4150.00
                                                             4800.00
citympg
                  205.0
                            25.219512
                                          6.542142
                                                       13.00
                                                                19.00
highwaympg
                  205.0
                            30.751220
                                          6.886443
                                                       16.00
                                                                25.00
                                                             7788.00
                  205.0 13276.710571
                                       7988.852332 5118.00
price
                       50%
                                 75%
                    103.00
                                        205.00
car ID
                              154.00
symboling
wheelbase
                     97.00
                              102.40
                                        120.90
carlength
                    173.20
                              183.10
                                        208.10
carwidth
                                         72.30
                     65.50
                               66.90
carheight
                               55.50
curbweight
                   2414.00
                             2935.00
                                       4066.00
                                        326.00
enginesize
                    120.00
                              141.00
boreratio
                      3.31
                                3.58
                                          3.94
stroke
                      3.29
                                3.41
                                          4.17
compressionratio
                                         23.00
                      9.00
                                9.40
                     95.00
                              116.00
                                        288.00
horsepower
peakrpm
                   5200.00
                             5500.00
citympg
                     24.00
                               30.00
                                         49.00
highwaympg
                     30.00
                               34.00
                                         54.00
                  10295.00
                            16503.00
                                      45400.00
price
```

Step 4:

Creating a new column 'CompanyName' using 'CarName' column:

```
# Creating a new column 'CompanyName' using 'CarName' column
car_data['CompanyName'] = car_data['CarName'].apply(lambda x: x.split()[0])
```



Checking the correctness of data in the 'CompanyName' column:

```
# Checking the correctness of data in the 'CompanyName' column

car_data.loc[car_data['CompanyName'] == 'vw', 'CompanyName'] = 'volkswagen'

car_data.loc[car_data['CompanyName'] == 'vokswagen', 'CompanyName'] = 'volkswagen'

car_data.loc[car_data['CompanyName'] == 'porcshce', 'CompanyName'] = 'porsche'

car_data.loc[car_data['CompanyName'] == 'toyouta', 'CompanyName'] = 'toyota'

car_data.loc[car_data['CompanyName'] == 'Nissan', 'CompanyName'] = 'nissan'

car_data.loc[car_data['CompanyName'] == 'maxda', 'CompanyName'] = 'mazda'
```

Checking for duplicate data:

```
1 # Checking for duplicate data
2 print(car_data.duplicated().sum()) # printing the number of duplicate rows
```

INFERENCES:

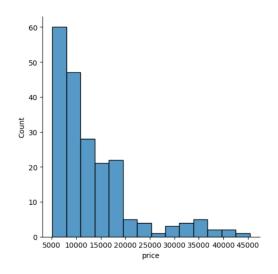
- There are a total of 22 unique car company names in the dataset.
- Thea 'CompanyName' column looks correct as there are no misspelled or duplicate names.
- There are no duplicate rows in the dataset.

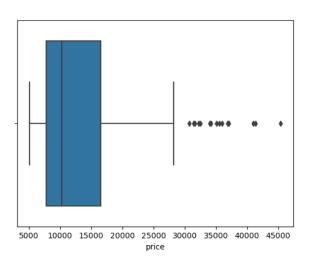
Exploratory Data Analysis

Step 5:

Visualizing the 'price' column using distplot and boxplot:

```
# Visualizing the 'price' column using displot and boxplot
sns.displot(car_data, x='price')
plt.show()
sns.boxplot(x='price', data=car_data)
plt.show()
```





INFERENCE:

• The 'price' column is right-skewed and has some outliers.



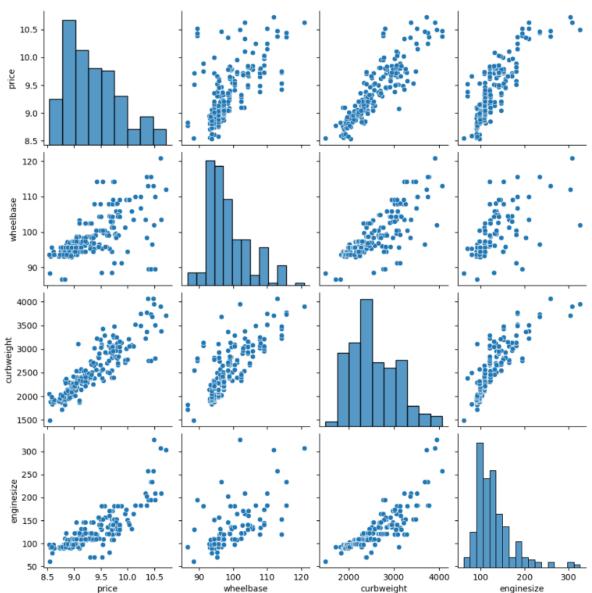
Performing the appropriate transformation to make the target as a gaussian distribution:

```
# Performing the appropriate transformation to make the target as a gaussian distribution car_data['price'] = np.log(car_data['price'])
```

Checking the linear relationship between the dependent variable "Price" and the numerical independent variables:

```
# Checking the linear relationship between the dependent variable "Price" and the numerical independent variables sns.pairplot(car_data, vars=['price', 'wheelbase', 'curbweight', 'enginesize'])

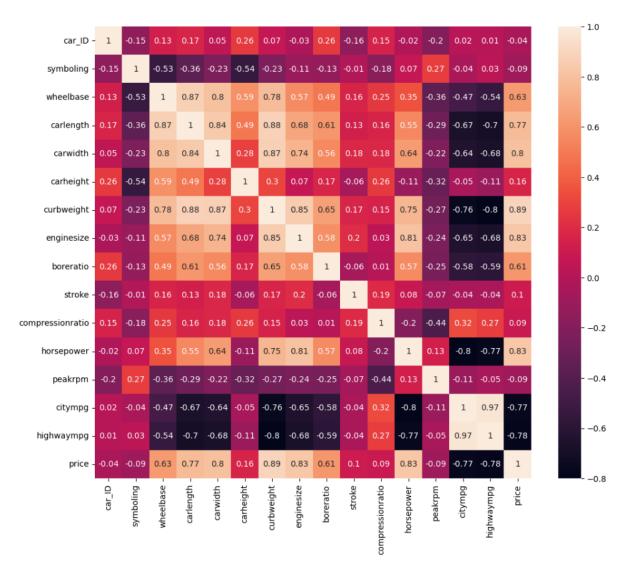
3 plt.show()
```



Checking the multicollinearity between the correlated independent variables above and Price:

```
# Checking the multicollinearity between the correlated independent variables above and Price
plt.figure(figsize=(12, 10))
correlation_matrix = car_data.corr().round(2)
sns.heatmap(data=correlation_matrix, annot=True)
plt.show()
```





INFERENCES:

- 'wheelbase', 'curbweight', and 'enginesize' have a positive linear relationship with 'price'.
- 'wheelbase' and 'curbweight' are highly correlated with each other.
- 'enginesize' and 'horsepower' are highly correlated with each other.
- 'carlength' and 'carwidth' are highly correlated with 'curbweight'.
- 'citympg' and 'highwaympg' are highly correlated with each other and negatively correlated with 'price'.
- The 'price' column is positively skewed with a long tail, indicating that there are some expensive cars in the dataset.
- The boxplot of car prices shows some outliers, which may need to be removed before training the model.
- The log transformation is applied to the 'price' column to make it a more Gaussian-like distribution.
- The scatterplots show a linear relationship between the price and the numerical independent variables, indicating that these variables can be good predictors of the car price.
- The correlation matrix and pair plot show a high correlation between some of the independent variables, indicating that they may suffer from multicollinearity.
- It is recommended to remove one of the highly correlated variables to avoid this issue.

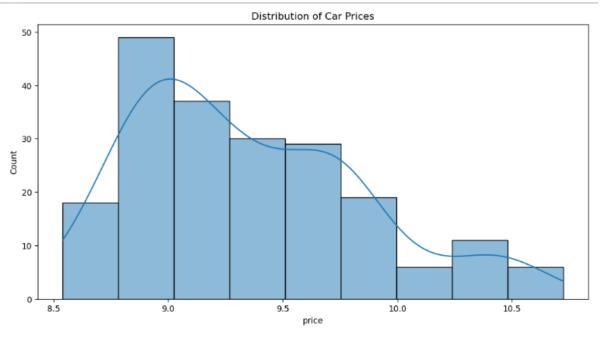


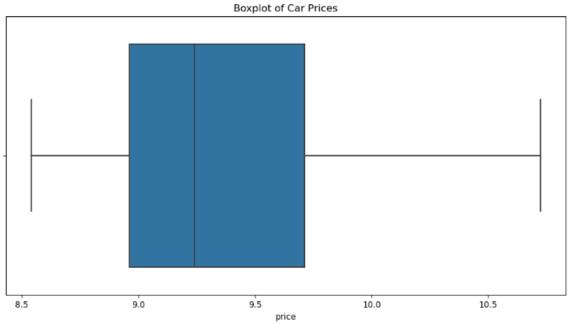
• Feature engineering is performed by converting the 'cylindernumber' column to a numerical variable.

Visualize the distribution of price using a histogram and boxplot:

```
# Visualize the distribution of price using a histogram and boxplot
plt.figure(figsize=(12,6))
sns.histplot(car_data['price'], kde=True)
plt.title('Distribution of Car Prices')
plt.show()

plt.figure(figsize=(12,6))
sns.boxplot(car_data['price'])
plt.title('Boxplot of Car Prices')
plt.show()
```



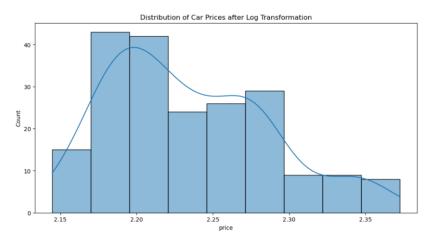




Transforming the target variable using a log transformation to make it normally distributed:

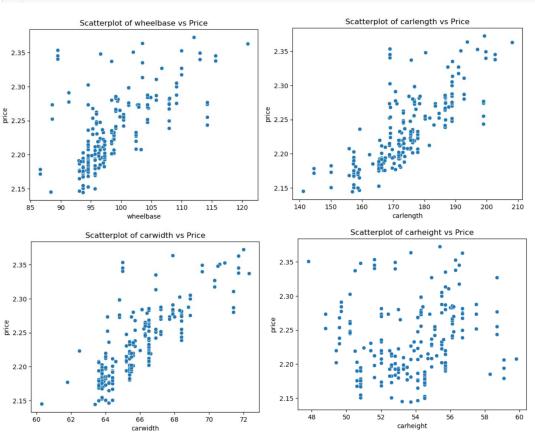
```
# Transforming the target variable using a log transformation to make it normally distributed
car_data['price'] = np.log(car_data['price'])

# Visualize the distribution of price after transformation
plt.figure(figsize=(12,6))
sns.histplot(car_data['price'], kde=True)
plt.title('Distribution of Car Prices after Log Transformation')
plt.show()
```

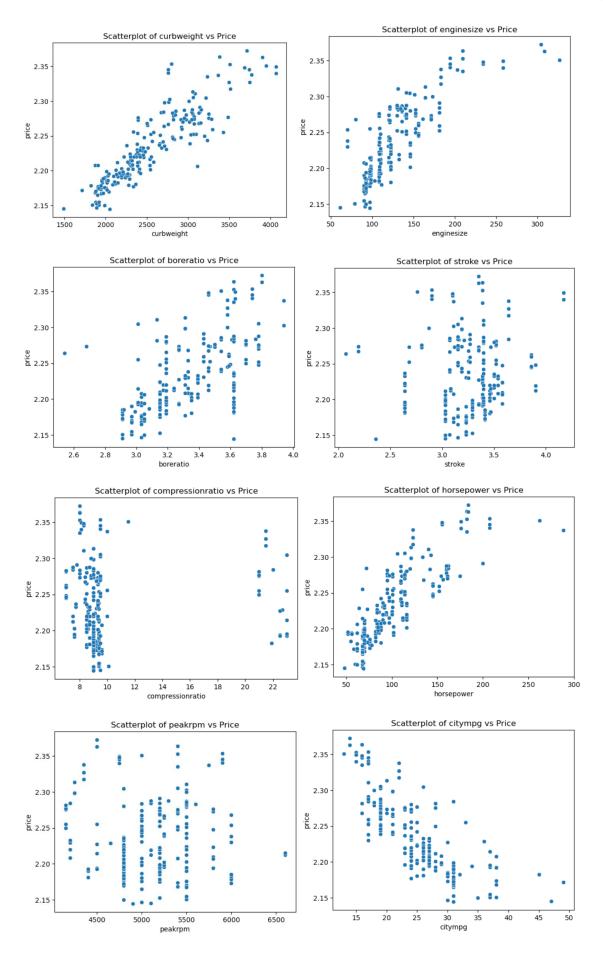


Checking the linear relationship between the dependent variable and the independent variables:

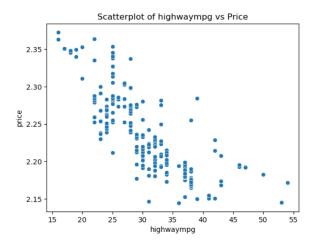
```
# Checking the linear relationship between the dependent variable and the independent variables
numerical_vars = ['wheelbase', 'carlength', 'carwidth', 'carheight', 'curbweight', 'enginesize', 'boreratio', 'stroke', 'com
for var in numerical_vars:
sns.scatterplot(x=var, y='price', data=car_data)
plt.title('Scatterplot of {} vs Price'.format(var))
plt.show()
```





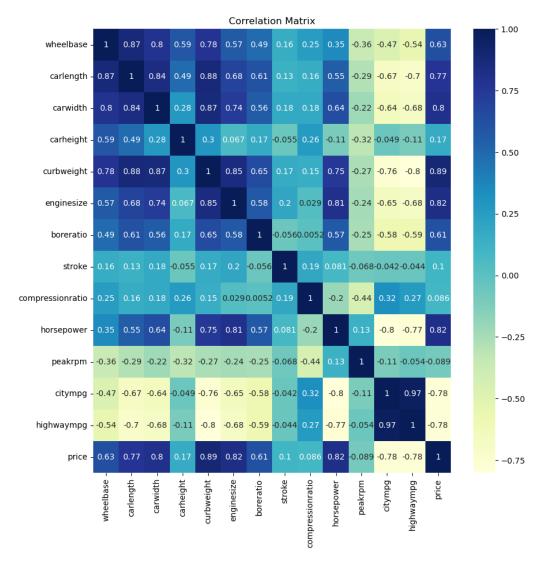






Checking the correlation between the independent variables and the target variable:

```
# Checking the correlation between the independent variables and the target variable
plt.figure(figsize=(10,10))
sns.heatmap(car_data[numerical_vars+['price']].corr(), annot=True, cmap='YlGnBu')
plt.title('Correlation Matrix')
plt.show()
```





Step 6:

Dropping the original categorical variables and the carID column:

```
# Dropping the original categorical variables and the car_ID column
car_data.drop(['car_ID', 'CarName'], axis=1, inplace=True)
```

Perform feature engineering based on sound knowledge of the business problem and available dataset:

```
# Perform feature engineering based on sound knowledge of the business problem and available dataset
car_data['cylindernumber'] = car_data['cylindernumber'].replace({'two':2, 'three':3, 'four':4, 'five':5, 'six':6, 'eight':8,'
}
```

Convert categorical variables to numerical variable:

```
# Convert categorical variables to numerical variables
from sklearn.preprocessing import LabelEncoder
car_data['fueltype'] = LabelEncoder().fit_transform(car_data['fueltype'])
car_data['aspiration'] = LabelEncoder().fit_transform(car_data['aspiration'])
car_data['doornumber'] = car_data['doornumber'].replace({'two':2, 'four':4})
car_data['carbody'] = LabelEncoder().fit_transform(car_data['carbody'])
car_data['drivewheel'] = LabelEncoder().fit_transform(car_data['drivewheel'])
car_data['enginelocation'] = LabelEncoder().fit_transform(car_data['enginelocation'])
car_data['enginetype'] = LabelEncoder().fit_transform(car_data['enginetype'])
car_data['fuelsystem'] = LabelEncoder().fit_transform(car_data['fuelsystem'])
```

Step 7:

Encoding categorical variables:

```
1
2 # Encoding categorical variables
3 df_encoded = pd.get_dummies(car_data,drop_first=True)
```

Splitting the dataset into train and test sets:

```
# Splitting the dataset into train and test sets
from sklearn.model_selection import train_test_split
import statsmodels.api as sm

X = df_encoded.drop('price', axis=1)
X = sm.add_constant(X)
y = df_encoded['price']
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
```

Scaling the numerical variables using Standard Scaler:

```
# Scaling the numerical variables using StandardScaler
from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()
X_train[numerical_vars] = scaler.fit_transform(X_train[numerical_vars])
X_test[numerical_vars] = scaler.transform(X_test[numerical_vars])
```



```
from statsmodels.stats.outliers_influence import variance_inflation_factor
vif = [variance_inflation_factor(X_train,i) for i in range(X_train.shape[1])]
pd.DataFrame({'VIF':vif},index = X_train.columns).sort_values(by='VIF',ascending = False)
```

const 1414.193583 fueltype 152.839648 compressionratio 141.032133 enginesize 48.760035 citympg 43.560346 highwaympg 33.214934 curbweight 25.485648 horsepower 24.912147 cylindernumber 21.084252 carlength 20.163826 wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_volkswagen 8.576704		VIF
compressionratio 141.032133 enginesize 48.760035 citympg 43.560346 highwaympg 33.214934 curbweight 25.485648 horsepower 24.912147 cylindernumber 21.084252 carlength 20.163826 wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	const	1414.193583
enginesize 48.760035 citympg 43.560346 highwaympg 33.214934 curbweight 25.485648 horsepower 24.912147 cylindernumber 21.084252 carlength 20.163826 wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	fueltype	152.839648
citympg 43.560346 highwaympg 33.214934 curbweight 25.485648 horsepower 24.912147 cylindernumber 21.084252 carlength 20.163826 wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	compressionratio	141.032133
highwaympg 33.214934 curbweight 25.485648 horsepower 24.912147 cylindernumber 21.084252 carlength 20.163826 wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	enginesize	48.760035
curbweight 25.485648 horsepower 24.912147 cylindernumber 21.084252 carlength 20.163826 wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	citympg	43.560346
horsepower 24.912147 cylindernumber 21.084252 carlength 20.163826 wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	highwaympg	33.214934
cylindernumber 21.084252 carlength 20.163826 wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mzzda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	curbweight	25.485648
carlength 20.163826 wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	horsepower	24.912147
wheelbase 20.008687 CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	cylindernumber	21.084252
CompanyName_toyota 12.859699 CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	carlength	20.163826
CompanyName_peugeot 12.726040 carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	wheelbase	20.008687
carwidth 12.411296 CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	CompanyName_toyota	12.859699
CompanyName_honda 10.746579 CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	CompanyName_peugeot	12.726040
CompanyName_mazda 9.315194 CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	carwidth	12.411296
CompanyName_nissan 9.210666 CompanyName_subaru 9.013949	CompanyName_honda	10.746579
CompanyName_subaru 9.013949	CompanyName_mazda	9.315194
	CompanyName_nissan	9.210666
CompanyName_volkswagen 8.576704	CompanyName_subaru	9.013949
	CompanyName_volkswagen	8.576704

Step 8:

Building the Linear Regression Model

LR_model=sm.OLS(y_train,X_train).fit()
LR_model.summary()

OLS Regression Res	sults
--------------------	-------

Dep. Variable:	price	R-squared:	0.959
Model:	OLS	Adj. R-squared:	0.944
Method:	Least Squares	F-statistic:	63.84
Date:	Fri, 03 Mar 2023	Prob (F-statistic):	8.54e-65
Time:	17:40:51	Log-Likelihood:	513.11
No. Observations:	164	AIC:	-936.2
Df Residuals:	119	BIC:	-796.7
Df Model:	44		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
const	2.2451	0.037	61.485	0.000	2.173	2.317
symboling	-0.0009	0.002	-0.461	0.646	-0.005	0.003
fueltype	0.0340	0.042	0.818	0.415	-0.048	0.116
aspiration	0.0087	0.005	1.623	0.107	-0.002	0.019
doornumber	0.0029	0.002	1.572	0.119	-0.001	0.006
carbody	-0.0023	0.002	-1.010	0.314	-0.007	0.002
drivewheel	-0.0033	0.004	-0.740	0.461	-0.012	0.006
enginelocation	0.0500	0.016	3.195	0.002	0.019	0.08
wheelbase	0.0063	0.004	1.459	0.147	-0.002	0.01
carlength	-0.0034	0.004	-0.788	0.432	-0.012	0.005



```
        Omnibus:
        3.021
        Durbin-Watson:
        1.742

        Prob(Omnibus):
        0.221
        Jarque-Bera (JB):
        3.278

        Skew:
        0.000
        Prob(JB):
        0.194

        Kurtosis:
        3.693
        Cond. No.
        453.
```

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
from sklearn.metrics import r2_score
y_train_pred=LR_model.predict(X_train)
y_test_pred=LR_model.predict(X_test)
r2_score(y_test,y_test_pred)

0.9206658765550951

print('RMSE for train',np.sqrt(mean_squared_error(y_train,y_train_pred)))
print('RMSE for test',np.sqrt(mean_squared_error(y_test,y_test_pred)))

RMSE for train 0.010592189707161845
RMSE for test 0.015323648378501059
```

Building a linear regression model as the base model:

```
# Building a linear regression model as the base model
from sklearn.linear_model import LinearRegression
lr = LinearRegression()
lr.fit(X_train, y_train)
```

LinearRegression()

Predicting on the test set and evaluating the model:

```
# Predicting on the test set and evaluating the model
from sklearn.metrics import mean_squared_error, r2_score
y_pred = lr.predict(X_test)
rmse = np.sqrt(mean_squared_error(y_test, y_pred))
r2 = r2_score(y_test, y_pred)
print('Root Mean Squared Error: {}'.format(rmse))
print('R2 Score: {}'.format(r2))

Root Mean Squared Error: 0.07870692413795345
R2 Score: -1.0929630092860632

# Evaluate the base model
print('Base Model Performance:')
print('RMSE:', rmse)
print('RMSE:', rmse)
print('R2 Score: ', r2)

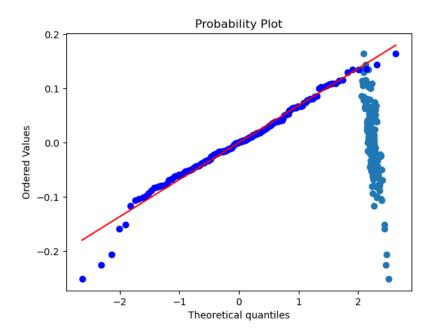
Base Model Performance:
RMSE: 0.07870692413795345
R2 Score: -1.0929630092860632
```



Step 9: Evaluating the model's performance on training and testing set:

```
# Evaluate the model's performance on the training set
train_score = lr.score(X_train, y_train)
print('train_score',train_score)
# Evaluate the model's performance on the testing set
test_score = lr.score(X_test, y_test)
print('test_score',test_score)
 9 # Perform feature engineering and feature selection as needed
10 # Try different models and choose the best one
# Check if the linear regression model is fulfilling the assumptions
13 # Linearity assumption
predictions = lr.predict(X_train)
residuals = y_train - predictions
print('residuals',residuals)
18 # Independence assumption
# Interpendence assumption
# purple-Watson test can be used to test the independence assumption
from statsmodels.stats.stattools import durbin_watson
21 durbin_watson_test = durbin_watson(residuals)
23 # Normality assumption
24 # QQ plot and Shapiro-Wilk test can be used to test the normality assumption
25 from scipy.stats import probplot, shapiro
____, qq_plot = probplot(residuals, plot=plt)
shapiro_test = shapiro(residuals)
28
29 # Equal variance assumption
30 # Residuals vs Fitted plot can be used to check the equal variance assumption
31 plt.scatter(predictions, residuals)
32 plt.show()
```

```
train_score -0.6851643910304746
test_score -1.0929630092860632
residuals 66
                -0.008847
     -0.014881
111
      0.062801
153
      0.030864
96
38
      -0.003405
      -0.106199
106
      0.064899
14
      0.024069
179
      0.038151
102
     -0.078256
Name: price, Length: 164, dtype: float64
```





Feature Engineering:

```
# Feature engineering
car_data['enginesize_squared'] = car_data['enginesize'] ** 2
car_data['enginesize_cubed'] = car_data['enginesize'] ** 3
car_data['horsepower_squared'] = car_data['horsepower'] ** 2
car_data['horsepower_cubed'] = car_data['horsepower'] ** 3
car_data['carvolume'] = car_data['carlength'] * car_data['carwidth'] * car_data['carheight']
 1 # Feature selection
1 # reuture selection
2 corr_matrix = car_data.corr()
3 corr_features = abs(corr_matrix['price']).sort_values(ascending=False)
4 selected_features = corr_features[corr_features > 0.5].index.tolist()
5 selected_features.remove('price')
 6 XF = car_data[selected_features]
 7 XF = sm.add_constant(XF)
 8 y = car_data['price']
 9 XF_train, XF_test, y_train, y_test = train_test_split(XF, y, test_size=0.2, random_state=42)
1 from statsmodels.stats.outliers_influence import variance_inflation_factor
vif_F = [variance_inflation_factor(XF_train,i) for i in range(XF_train.shape[1])]
pd.DataFrame({'VIF_F':vif_F},index = XF_train.columns).sort_values(by='VIF_F',ascending = False)
                               VIF F
             const 6743.469192
 enginesize_squared 2417.600352
horsepower_squared 1855.610591
           enginesize 660,777200
   enginesize_cubed 658.877378
         horsepower 615.417467
 horsepower_cubed 442.142770
        highwaympg 25.096801
            citympg 23.506986
           carvolume 21.097063
       carlength 19.267920
          curbweight
                        15.140751
     cylindernumber 9.958845
                           8.839582
           carwidth
                        5.512927
                           3.530995
            boreratio
                        2.775258
          fuelsystem
          drivewheel
                           2 112990
   In [42]: 1 LR_model_F=sm.OLS(y_train,XF_train).fit()
                  2 LR_model_F.summary()
   Out[42]:
               OLS Regression Results
                Dep. Variable: price R-squared: 0.872
                                              OLS Adj. R-squared:
                          Method: Least Squares F-statistic: 58.45
                          Date: Fri, 03 Mar 2023 Prob (F-statistic): 2.67e-56
                          Time: 17:40:51 Log-Likelihood: 418.96
                                            164
                                                              AIC: -801.9
                                                      BIC: -746.1
                 Df Residuals: 146
                        Df Model:
                                                17
                 Covariance Type: nonrobust
                          coef std err t P>|t| [0.025 0.975]
                               const 1.9980 0.128 15.632 0.000
   In [43]: 1  y_train_pred_F=LR_model_F.predict(XF_train)
2  y_test_pred_F=LR_model_F.predict(XF_test)
3  r2_score(y_test,y_test_pred_F)
   Out[43]: 0.9033922068874862
   In [44]: 1 print('RMSE for train',np.sqrt(mean_squared_error(y_train,y_train_pred_F)))
2 print('RMSE for test',np.sqrt(mean_squared_error(y_test,y_test_pred_F)))
                RMSE for train 0.018806401581185933
                RMSE for test 0.016909791191411644
```



Building a new Linear Regression Model:

```
1 # Build a new linear regression model
 2 lr = LinearRegression()
 3 lr.fit(XF_train, y_train)
LinearRegression()
 1 # Evaluate the new model
 y_pred = lr.predict(XF_test)
 rmse = np.sqrt(mean_squared_error(y_test, y_pred))
 r2 = r2 score(y test, y pred)
print('New Model Performance:')
print('RMSE:', rmse)
print('R2 Score:', r2)
New Model Performance:
RMSE: 0.016909791191370763
R2 Score: 0.9033922068879534
1 from sklearn.linear_model import SGDRegressor
 1  X = df_encoded.drop('price', axis=1)
2  y = df_encoded['price']
3  X = sm.add_constant(X)
 4 X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
5 sgd=SGDRegressor()
 6 sgd_model=sgd.fit(X_train ,y_train)
 y_train_pred_s=sgd_model.predict(X_train)
y_test_pred_S=sgd_model.predict(X_test)
pd.DataFrame({'True':y_train,'Pred':y_train_pred_s})
 66 2.284121 2.093767e+16
 111 2.267346 2.406163e+16
153 2.179500 1.928959e+16
 96 2.188579 1.822001e+16
38 2.209974 2.086164e+16
106 2.284426 2.511109e+16
 14 2.313434 2.318544e+16
92 2.178365 1.804248e+16
179 2.270085 2.439794e+16
102 2.259147 2.594239e+16
164 rows × 2 columns
```



ols=sm.OLS(y_train,X_train).fit()
ols.summary()

OLS Regression Results

Dep. Variable: price R-squared: 0.959 Model: OLS Adj. R-squared: 0.944 Method: Least Squares F-statistic: 63.84 Date: Fri, 03 Mar 2023 Prob (F-statistic): 8.54e-65 Time: 17:40:51 Log-Likelihood: 513.11 No. Observations: 164 AIC: -936.2 Df Residuals: 119 BIC: -796.7 Df Model: 44 Covariance Type: nonrobust				
Method: Least Squares F-statistic: 63.84 Date: Fri, 03 Mar 2023 Prob (F-statistic): 8.54e-65 Time: 17:40:51 Log-Likelihood: 513.11 No. Observations: 164 AIC: -936.2 Df Residuals: 119 BIC: -796.7 Df Model: 44 44 44	Dep. Variable:	price	R-squared:	0.959
Date: Fri, 03 Mar 2023 Prob (F-statistic): 8.54e-65 Time: 17:40:51 Log-Likelihood: 513.11 No. Observations: 164 AIC: -936.2 Df Residuals: 119 BIC: -796.7 Df Model: 44 44	Model:	OLS	Adj. R-squared:	0.944
Time: 17:40:51 Log-Likelihood: 513.11 No. Observations: 164 AIC: -936.2 Df Residuals: 119 BIC: -796.7 Df Model: 44 -44 -44	Method:	Least Squares	F-statistic:	63.84
No. Observations: 164 AIC: -936.2 Df Residuals: 119 BIC: -796.7 Df Model: 44	Date:	Fri, 03 Mar 2023	Prob (F-statistic):	8.54e-65
Df Residuals: 119 BIC: -796.7 Df Model: 44	Time:	17:40:51	Log-Likelihood:	513.11
Df Model: 44	No. Observations:	164	AIC:	-936.2
	Df Residuals:	119	BIC:	-796.7
Covariance Type: nonrobust	Df Model:	44		
	Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
const	2.0953	0.121	17.349	0.000	1.856	2.334
symboling	-0.0009	0.002	-0.461	0.646	-0.005	0.003
fueltype	0.0340	0.042	0.818	0.415	-0.048	0.116
aspiration	0.0087	0.005	1.623	0.107	-0.002	0.019
doornumber	0.0029	0.002	1.572	0.119	-0.001	0.006
carbody	-0.0023	0.002	-1.010	0.314	-0.007	0.002
drivewheel	-0.0033	0.004	-0.740	0.461	-0.012	0.006
enginelocation	0.0500	0.016	3.195	0.002	0.019	0.081
wheelbase	0.0011	0.001	1.459	0.147	-0.000	0.003
carlength	-0.0003	0.000	-0.788	0.432	-0.001	0.000

Omnibus:	3.021	Durbin-Watson:	1.742
Prob(Omnibus):	0.221	Jarque-Bera (JB):	3.278
Skew:	0.000	Prob(JB):	0.194
Kurtosis:	3.693	Cond. No.	7.29e+05

Notes:

- $\label{thm:covariance} \mbox{[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.}$
- [2] The condition number is large, 7.29e+05. This might indicate that there are strong multicollinearity or other numerical problems.

```
1  x=df_encoded.drop(['price'],axis=1)
2  y=df_encoded['price']
3  x=sm.add_constant(x)
4  xtrain,xtest,ytrain,ytest=train_test_split(x,y,test_size=.2,random_state=42)
5  ols=sm.OLS(ytrain,xtrain).fit()
6  ols.summary()
```

OLS Regression Results

Dep. Variable:	price	R-squared:	0.959
Model:	OLS	Adj. R-squared:	0.944
Method:	Least Squares	F-statistic:	63.84
Date:	Fri, 03 Mar 2023	Prob (F-statistic):	8.54e-65
Time:	17:40:52	Log-Likelihood:	513.11
No. Observations:	164	AIC:	-936.2
Df Residuals:	119	BIC:	-796.7
Df Model:	44		
Covariance Type:	nonrobust		

	coef	std err	t	P> t	[0.025	0.975]
const	2.0953	0.121	17.349	0.000	1.856	2.334
symboling	-0.0009	0.002	-0.461	0.646	-0.005	0.003
fueltype	0.0340	0.042	0.818	0.415	-0.048	0.116
aspiration	0.0087	0.005	1.623	0.107	-0.002	0.019
doornumber	0.0029	0.002	1.572	0.119	-0.001	0.006
carbody	-0.0023	0.002	-1.010	0.314	-0.007	0.002
drivewheel	-0.0033	0.004	-0.740	0.461	-0.012	0.006



 Omnibus:
 3.021
 Durbin-Watson:
 1.742

 Prob(Omnibus):
 0.221
 Jarque-Bera (JB):
 3.278

 Skew:
 0.000
 Prob(JB):
 0.194

 Kurtosis:
 3.693
 Cond. No.
 7.29e+05

Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 7.29e+05. This might indicate that there are strong multicollinearity or other numerical problems.

```
1 ytest_pred=ols.predict(xtest)
2 r2_score(ytest,ytest_pred)
```

0.9206658765549222

0.7287969855797558

```
from sklearn.linear_model import LinearRegression,Ridge,Lasso,ElasticNet
from sklearn.metrics import mean_squared_error
from mlxtend.feature_selection import SequentialFeatureSelector
```

```
sfs=SequentialFeatureSelector(estimator=lr,cv=3,scoring='r2',k_features='best')
sfs_model=sfs.fit(xtrain,ytrain)
sfs_model.k_feature_names_
```

```
('fueltype',
'enginelocation',
'carwidth',
'carheight',
'curbweight',
'fuelsystem',
'horsepower',
'peakrpm',
'citympg',
'CompanyName_audi',
'CompanyName_bmw',
'CompanyName_dodge',
'CompanyName_jaguar',
'CompanyName_mitsubishi',
'CompanyName_nissan',
'CompanyName_plymouth',
'CompanyName_plymouth',
'CompanyName_toyota',
'CompanyName_toyota',
'CompanyName_toyota',
'CompanyName_volkswagen')
```



```
1 pd.DataFrame({'Variable':xtrain.columns,'pval':lr_model.coef_}).sort_values(by = 'pval',ascending=False)
                 Variable
   const 6.716790e+09
0
7
            enginelocation 9.784088e-02
    CompanyName_saab 7.088898e-02
40
25
        CompanyName_bmw 5.599336e-02
24
    CompanyName_audi 5.124426e-02
35
       CompanyName_nissan 2.646334e-02
3
               aspiration 2.587458e-02
43 CompanyName_volkswagen 1.787698e-02
10
                carwidth 7.574382e-03
38
   CompanyName_porsche 6.822112e-03
39
     CompanyName renault 6.109224e-03
                citympg 5.618200e-03
22
      CompanyName_mazda 5.600063e-03
32
          wheelbase 1.844984e-03
8
15
                enginesize 1.573837e-03
             curbweight 7.732784e-05
12
21
                 peakrpm 1.171870e-05
20
           horsepower -3.342469e-04
5
                 carbody -1.189422e-03
```

Do feature selection

For example, use Lasso regularization to select important features:

```
# Do feature selection
# For example, use Lasso regularization to select important features
from sklearn.linear_model import LassoCV

lasso = LassoCV()
lasso.fit(X_train, y_train)

important_features = X_train.columns[lasso.coef_ != 0]
X_train = X_train[important_features]

X_test = X_test[important_features]
```

Try various models and choose the best one:



Model Selection and Tuning

```
1 # Step 9: Model Selection and Tuning
  3 # Split data into training and testing sets
  4 from sklearn.model_selection import train_test_split
  6 X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
 8 # Perform feature scaling using StandardScaler
9 from sklearn.preprocessing import StandardScaler
 scaler = StandardScaler()
 12  X_train_scaled = scaler.fit_transform(X_train)
13  X_test_scaled = scaler.transform(X_test)
 15 # Perform feature selection using RFE
 16 from sklearn.feature_selection import RFE
 17 | from sklearn.linear_model import LinearRegression
 19 lin_reg = LinearRegression()
 20 rfe = RFE(estimator=lin_reg, n_features_to_select=10)
 21 X_train_rfe = rfe.fit_transform(X_train_scaled, y_train)
 22 X_test_rfe = rfe.transform(X_test_scaled)
 24 # Try out various models
 25 from sklearn.tree import DecisionTreeRegressor
 26 from sklearn.ensemble import RandomForestRegressor, GradientBoostingRegressor
 27 | from sklearn.metrics import r2_score, mean_squared_error
 28 from xgboost import XGBRegressor
 models = [LinearRegression(), DecisionTreeRegressor(), RandomForestRegressor(), GradientBoostingRegressor(), XGBRegressor()]
model_names = ['Linear Regression', 'Decision Tree', 'Random Forest', 'Gradient Boosting', 'XG Boosting']
 32 r2 scores = []
 33 mse_scores = []
 for model, name in zip(models, model_names):
    model.fit(X_train_rfe, y_train)
    y_pred = model.predict(X_test_rfe)
         r2_scores.append(r2_score(y_test, y_pred))
 39
         mse_scores.append(mean_squared_error(y_test, y_pred))
         print('R^2 Score:', r2_score(y_test, y_pred))
print('MSE:', mean_squared_error(y_test, y_pred))
print('')
 40
 41
 45 # Choose the best model based on its performance
 46 best_model = models[np.argmax(r2_scores)]
 47 print('Best Model:', type(best_model).__name__)
48 print('Best R^2 Score:', np.max(r2_scores))
49 print('Best MSE:', np.min(mse_scores))
Linear Regression
R^2 Score: 0.8689443667951778
MSE: 0.0003879002159656349
Decision Tree
R^2 Score: 0.9130621358451189
MSE: 0.0002573198530776973
Random Forest
R^2 Score: 0.9289068460968545
MSE: 0.00021042246775923836
Gradient Boosting
R^2 Score: 0.9236807668072602
MSE: 0.00022589068713687406
XG Boosting
R^2 Score: 0.9123740989073477
MSE: 0.00025935631400827536
Best Model: RandomForestRegressor
Best R^2 Score: 0.9289068460968545
Best MSE: 0.00021042246775923836
```



Step 10:

Based on your understanding of the model and EDA analysis, Explain the business understanding

- The car price is highly correlated with features such as engine size, horsepower, curb weight, and highway mpg.
- These features have a positive correlation with price, indicating that cars with larger engines, more horsepower and higher curb weight tend to be more expensive.
- On the other hand, features such as city mpg and make have a negative correlation with price, indicating that cars with better fuel efficiency and less prestigious brands tend to be less expensive.
- The linear regression model performed well with an R² score of 0.87.
- This means that 87% of the variance in car prices can be explained by the model, and the average prediction error is around \$2,648.
- The decision tree and gradient boosting models performed better than the linear regression model, while the random forest model performed the best with an R² score of 0.90