Current PSP 52.04 → 60 %.

Nov23_PSP_8May
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Agenda

a) Flipkart case study

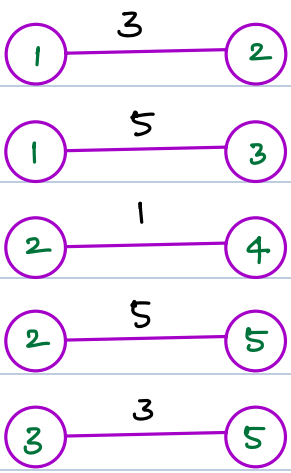
b) Prims Algorithm

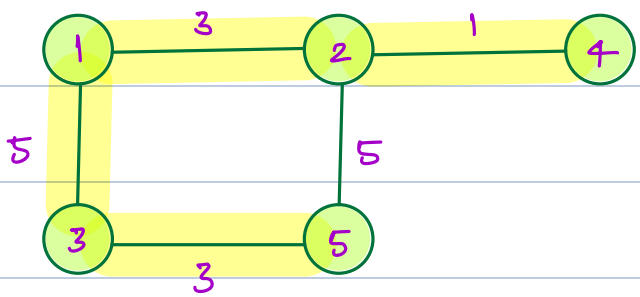
c) Dijkstra's Algorithm

Suppose Flipkart has N local distribution centers spread across a large metropolitan city. These centers need to be interconnected for efficient movement of goods. However, building and maintaining roads between these centers is costly. Flipkart's goal is to minimize these costs while ensuring every center is connected and operational.

Goal: You are given number of centers and possible connections that can be made with their cost. Find minimum cost of constructing roads between centers such that it is possible to travel from one center to any other via roads.

N = 5

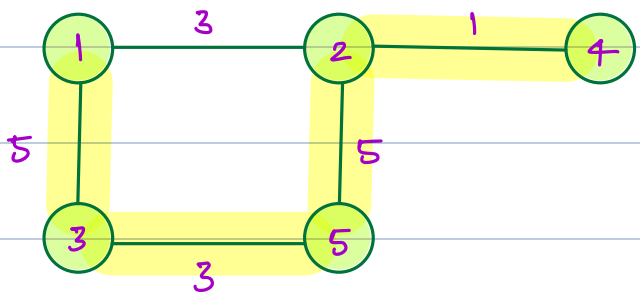




MST

If a graph is connected and has N-1 edges

→ tree



not MST

Minimum Spanning Tree (MST)

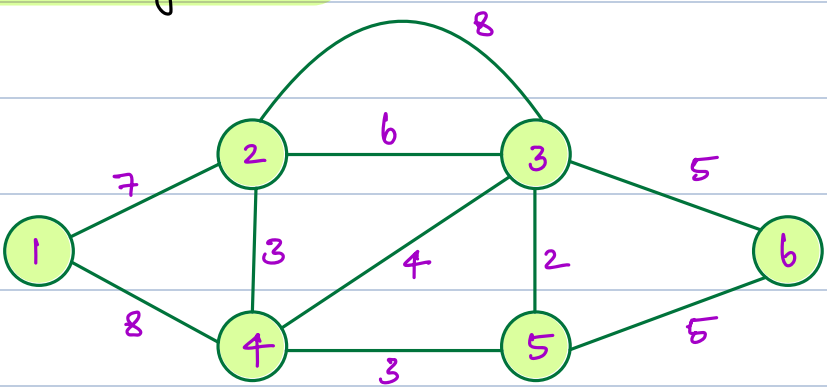
Tree generated from a connected graph, such that

- all nodes are connected
- sum of weights of all selected edges is min

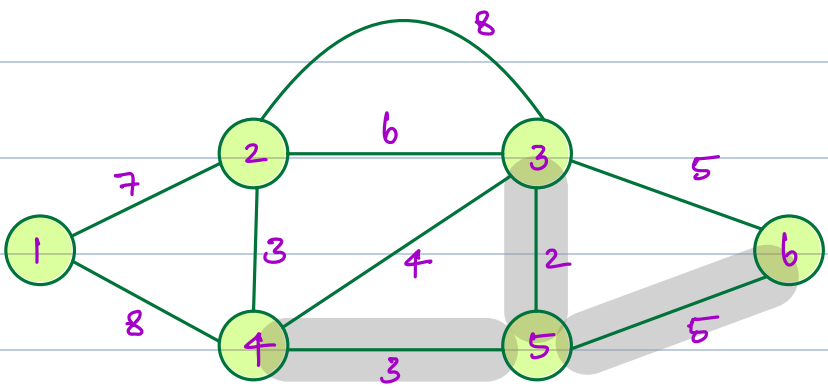
MST Algo

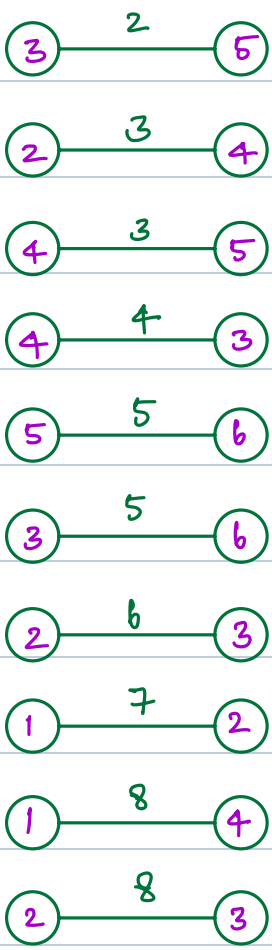
- Kruskal → DSA 4.2
- Prims

Prims Algorithm

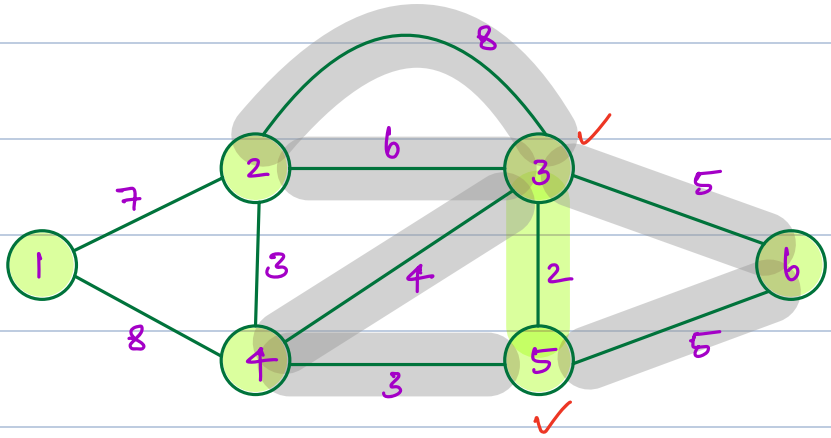


Starting at 5

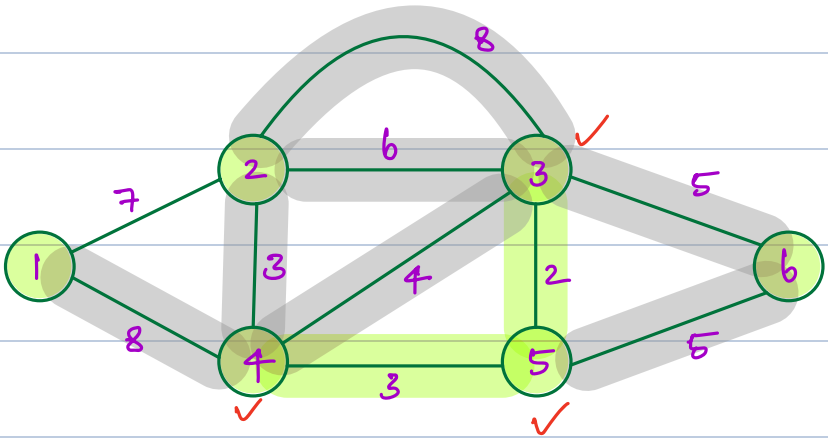




pick edge to 3 from 5

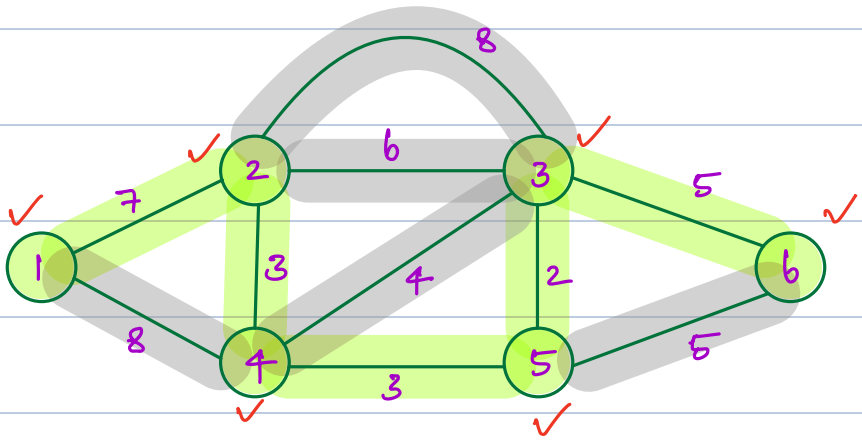


pick edge to 4 from 5



Quiz 1

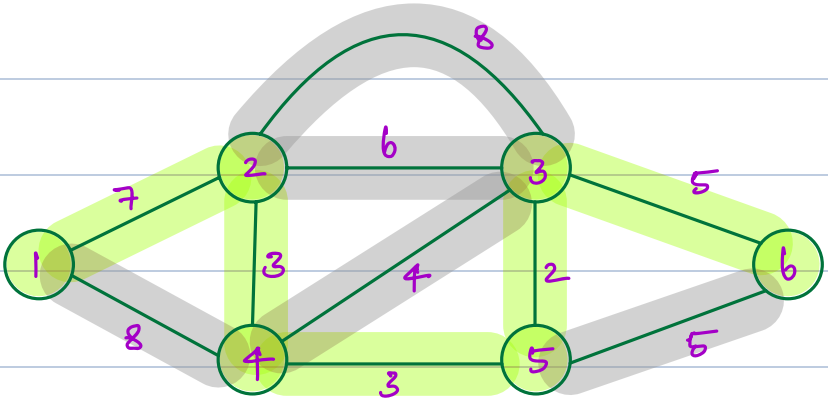
pick edge to 2 from 4



ans = 20

pick edge to 6 from 3

pick edge to 1 from 2



{ wt, nei }

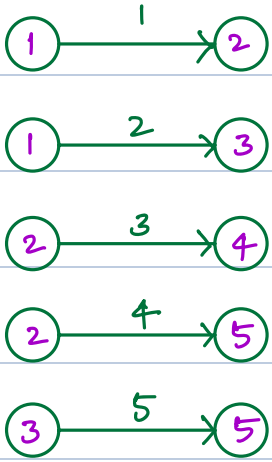
Black box

~~(6km, 2)~~	~~(8km, 2)~~	~~(4km, 4)~~
~~(2km, 5)~~	~~(5km, 6)~~	~~(3km, 4)~~
~~(5km, 6)~~	~~(3km, 2)~~	~~(8km, 1)~~
~~(7km, 1)~~		

visited array

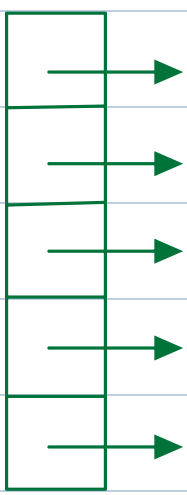
1	2	3	4	5	6
T	T	T	T	T	T

Ques 2: Min Heap for Black box



Adjacency list

{ v, w }



1 → { (2,1), (3,2) }

2 → { (4,3), (5,4) }

3 → { (5,5) }

4 →

5 →

pseudo code

```
// v ⟶ nodes    e ⟶ edges
// graph ⟶ adj. list ⟶ T.C O(v+e)
// create a min heap
// visited [N] = {F, F, ...}
// given a start node
for ( {nei, w} in graph (start)) {
    heap.add ({w, nei});
}

ans = 0;   visited [start] = True;
while (! heap.isEmpty()) {
    w, v = heap.get_min()
    if (visited [v]) continue;
    visited [v] = True;
    ans += w;
    for ( {nei_n, nei_w} in graph [v] ) {
        if (! visited [nei])
            heap.add ({nei_w, nei_n})
    }
}
```

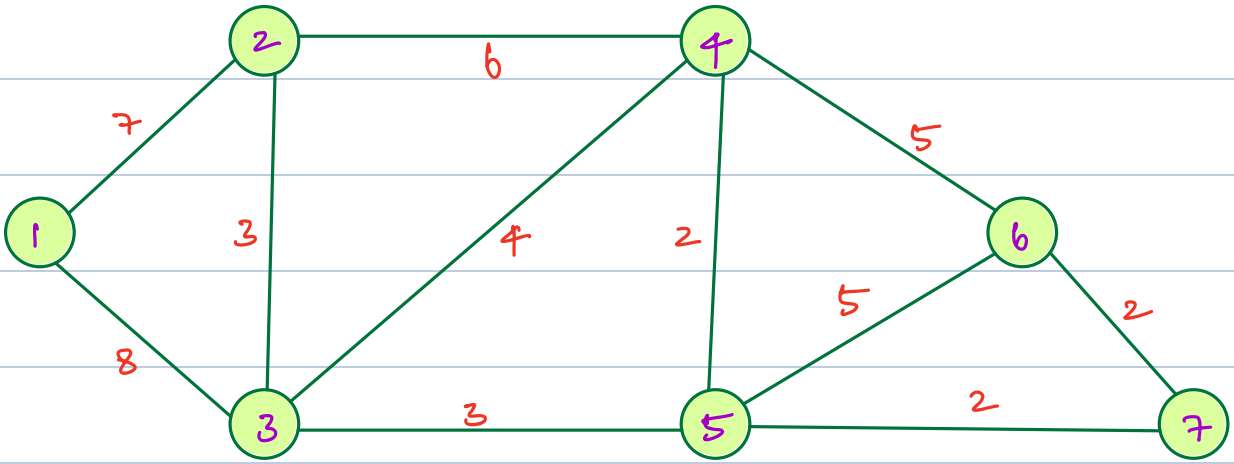
T.C = O(V+E + E log E).

10:14pm ⟶ 10:22pm

Dijkstra's Algorithm — Single Source Shortest Path

There are n cities in a country, you are living in city no. 1

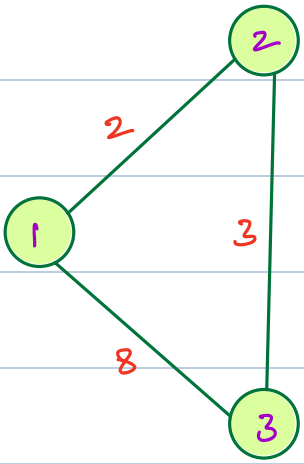
Find min distance to reach every other city from 1



Output →

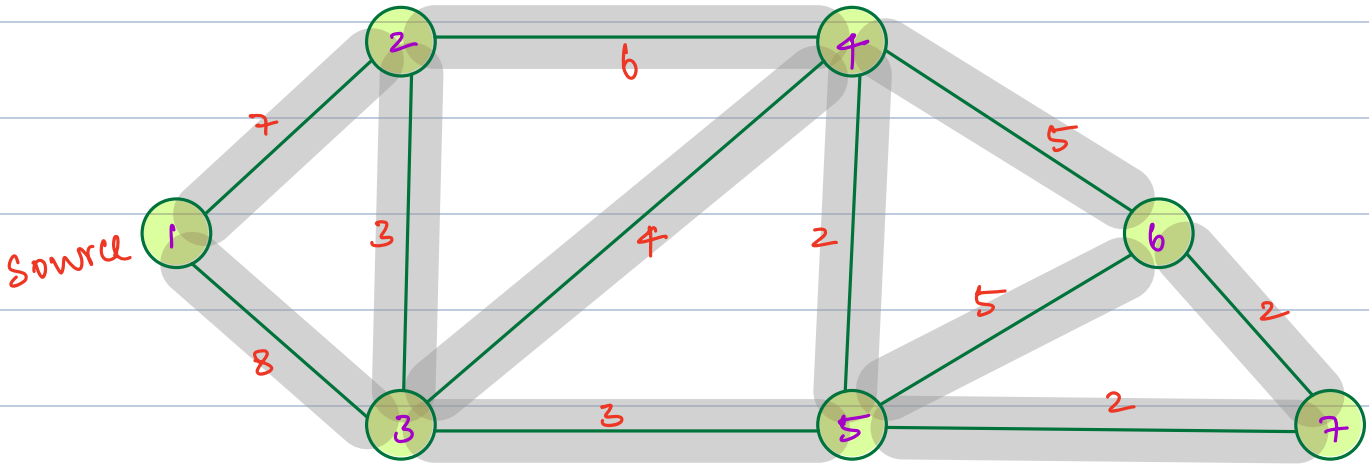
0	7	.	.	.	.	.
1	2	3	4	5	6	7

Single source shortest path = Dijkstra



$D[1-3] > D[1-2] + D[2-3]$

Dijkstra will pick through 2 different from BST



distances =

0	7	8	12	11	15	13
~~∞~~	~~∞~~	~~∞~~	~~∞~~	~~∞~~	~~∞~~	~~∞~~
1	2	3	4	5	6	7

{ d , v }

~~(0,1)~~ ~~(7,2)~~ ~~(8,3)~~ ~~(10,3)~~ ~~(13,4)~~

~~(12,4)~~ ~~(11,5)~~ ~~(13,4)~~ ~~(13,7)~~

~~(16,6)~~ ~~(17,6)~~ ~~(15,6)~~

Min Heap

Black box

Quiz 3

pseudo code

// graph ⟶ Adjacency list

// create min heap

// distance [n] = { INT_MAX , INT_MAX ... }

heap . add (0, start) ;

distance [start] = 0 ;

```
while (! heap.isEmpty()) {
    d, n = heap.getMin();
    if (d > distance[n]) continue;
    for (int nei, w : graph[n]) {
        int n_dist = distance[n] + w;
        if (n_dist < distance[nei]) {
            distance[nei] = n_dist;
            heap.add(n_dist, nei);
        }
    }
}
```

T.C = $O(E \log E)$

Quiz 4:

Announcements:

Revision Material

Brute Force / partial

Assignments (Topics you are Doubtful)