

Analyzing constraints

Max no. of consecutive 1s after replacing  
Max no. of consecutive 1s after swapping

Majority element

Row to column zero

21 Sep → 9 PM  
Thus

25 Sep → Adv  
Monday module

## Analyzing Constraints

- ① TLE
- ② Data type

- Analyze the constraints  $\rightarrow$  help you determine which data structure / algo to use for a given problem
- Look at constraints

Don't ask the interviewer constraints directly.

- ① Brute Force : TC and SC
- ② Should I optimize further?
- ③ Optimized algo

Constraints

$$n \leq 10^6$$

$$n \leq 20$$

$$n = 20$$

TC

$$O(n) / O(n \log n)$$

$$O(n!) / O(2^n)$$

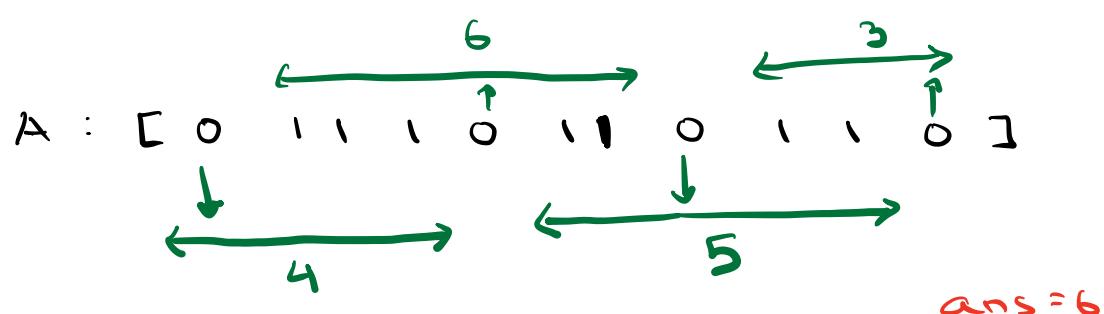
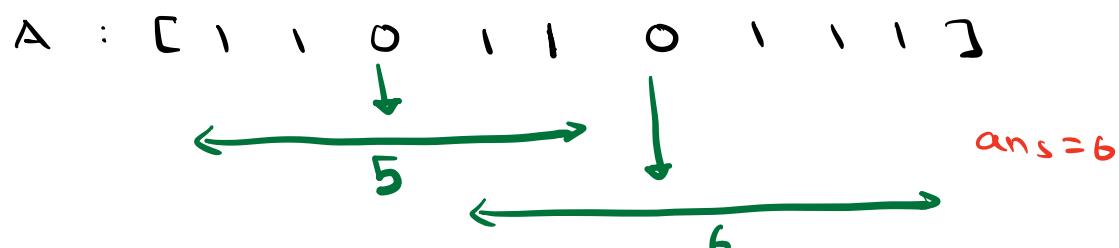
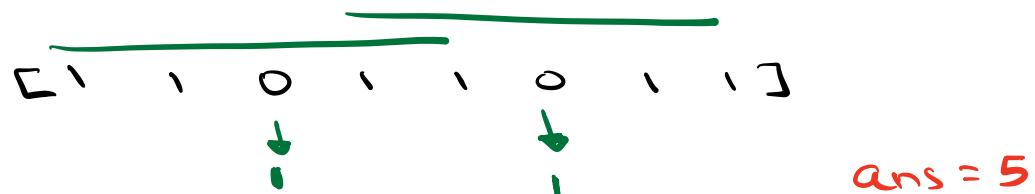
$$2^{10} \approx 10^3$$

$$2^{20} \approx 10^6$$

$$n \leq 10^{10}$$

$$O(\log n) / O(\sqrt{n})$$

1. Given an array of 1's and 0's. You're allowed to replace only one 0 with 1. Find max. no. of consecutive 1s that can be obtained after making replacement.



BF : Go to every 0 and replace it with a 1.

↓  
 Find count of 1s  
 on left side      l      r  
 Find count of 1s  
 on right side

$$\text{size of ls} = l + r + 1$$

```
int findMaxOnes (int nums[]) {  
    int n = nums.size()  
    int ans = 0 → biggest group of 1s  
    int cntonly = 0  
    for (i=0; i < n; i++) {  
        if (nums[i] == 1) cntonly++  
        if (cntonly == n) return n  
    }  
    for (i=0; i < n; i++) {  
        if (nums[i] == 0) {  
            int cntl = 0, cntr = 0  
            int j = i-1  
            while (j ≥ 0 && nums[j]==1) {  
                cntl++ j--  
            }  
            int j = i+1  
            while (j < N && nums[j]==1) {  
                cntr++ j++  
            }  
            ans = max (ans, cntl + cntr + 1)  
        }  
    }  
    return ans  
}
```

A = [ 0 0 0 0 0 ] ans = 1

A = [ 1 1 1 1 1 ] ans = 5

If all array ele are 1, ans = N

Lets count no. of times access each dc

	0	1	2	3	4	5	6	7	i
0	0	1	1	1	0	1	1	0	
=	=	=	=	=	=	=	=	=	
ctrl	0				3				outer loop
cnts	3				2				$\rightarrow i$
	$0+3+1=4$				$3+2+1=6$				$\rightarrow j \text{ left}$
									$\rightarrow j \text{ right}$

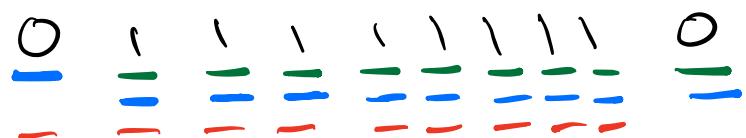
ans = 846

TC: O(3n)

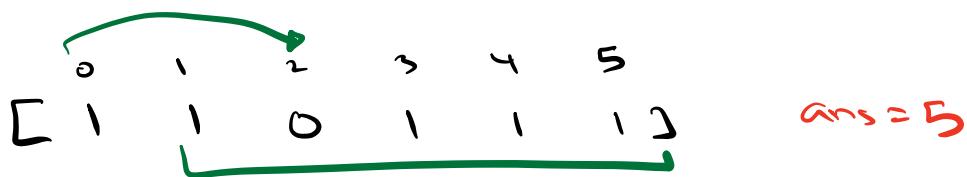
$O(n^{\frac{1}{2}})$

$N \text{ dc} \rightarrow N^2$

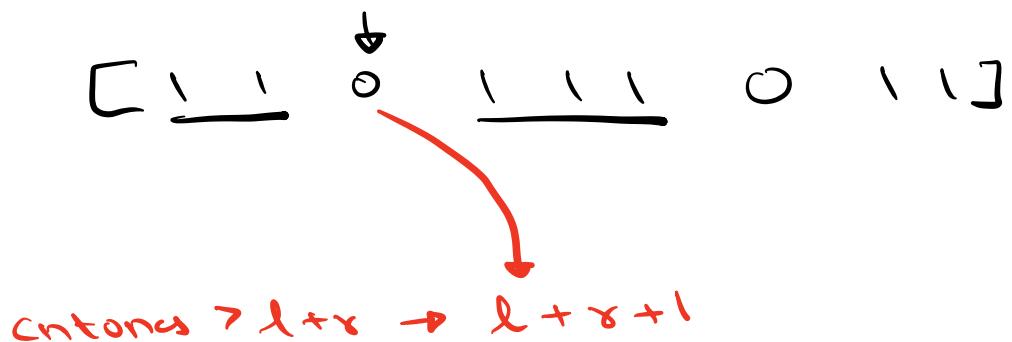
1 dc  $\rightarrow N$



2. Given an array of 1's and 0's. You're allowed to swap at max one 0 with 1. Find max. no. of consecutive 1's that can be obtained after making ~~replacement~~  
swapping.



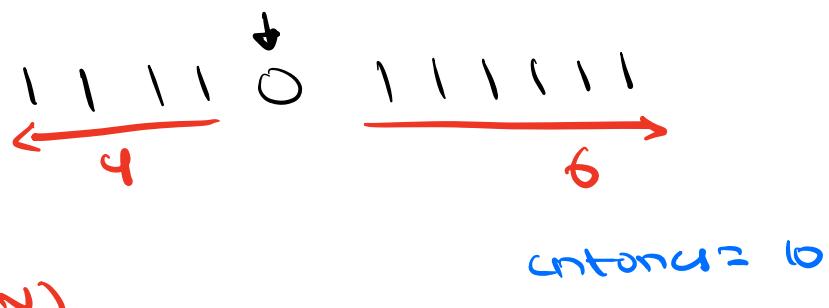
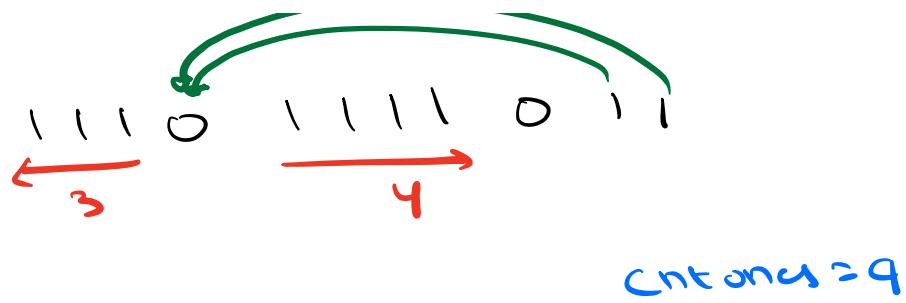
$$\text{cntones} = \ell + r \Rightarrow \ell + r$$



```

int findMaxOnes ( int nums[ ] ) {
    int n = nums.size()
    int ans = 0 → biggest group of 1s
    int cntones = 0
    for ( i = 0 ; i < n ; i++ ) {
        if ( nums[i] == 1 ) cntones++
        if ( cntones == n ) return n
    }
    for ( i = 0 ; i < n ; i++ ) {
        if ( nums[i] == 0 ) {
            int cntl = 0, cntx = 0
            int j = i - 1
            while ( j ≥ 0 && nums[j] == 1 ) {
                cntl++ j--
            }
            int j = i + 1
            while ( j < n && nums[j] == 1 ) {
                cntx++ j++
            }
            // swapped with extra 1
            if ( cntones > cntl + cntx )
                ans = max ( ans, cntl + cntx + 1 )
            else
                ans = max ( ans, cntl + cntx )
        }
    }
    return ans
}

```



TC: O(N)

SC: O(1)

10:42

3. Given N elements, find majority element.  
 Majority elements is the elements that occurs more than  $N/2$  times where N is size of array.

$\text{freq} > N/2$

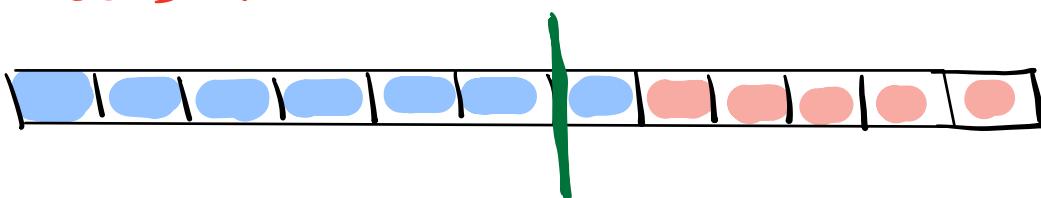
$A = [2 \ 1 \ 4]$        $\text{ans} = -1$        $\text{No majority element}$        $\text{freq} > 1$

$A = [3 \ 4 \ 3 \ 2 \ 4 \ 4 \ 4 \ 4]$        $\text{ans} = 4$        $\text{freq} > 4$

$A = [3 \ 3 \ 4 \ 2 \ 4 \ 4 \ 2 \ 4]$        $\text{ans} = -1$        $\text{No majority element}$        $\text{freq} > 4$

Q1.  $A \rightarrow [3, 4, 3, 6, 1, 3, 2, 5, 3, 3, 3]$   
 $\text{ans} = 3$        $\text{freq} > 5$        $N = 11$

At max how many majority elements can be there in an array?  $\text{freq} > N/2$   
 $\text{ans} = 1$



Proof by contradiction

Let us say there are 2 ME  $\Rightarrow x, y$

$$\text{freq}(x) > N/2 \Rightarrow \text{freq}(x) = N/2 + 1$$

$$\text{freq}(y) > N/2 \Rightarrow \text{freq}(y) = N/2 + 1$$

$$\underline{\underline{\text{freq}(x) + freq(y) = N+2}}$$

BF : Check freq of each element

Hash map

TC: O(N)

SC: O(N)

Iterating in array

TC: O(N<sup>2</sup>)

SC: O(1)

## Moore's Voting Algo

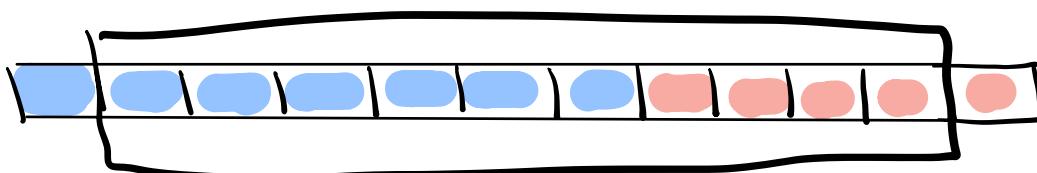
- There can only single ME
- If you remove 2 distinct ele  
then ME will remain same



Blue

$$N = 12$$

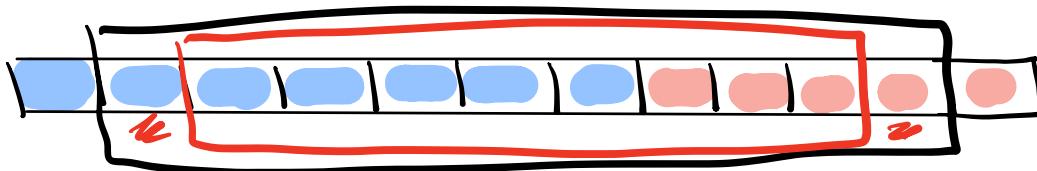
$$\text{freq} > 6$$



Blue

$$N = 10$$

$$\text{freq} > 5$$

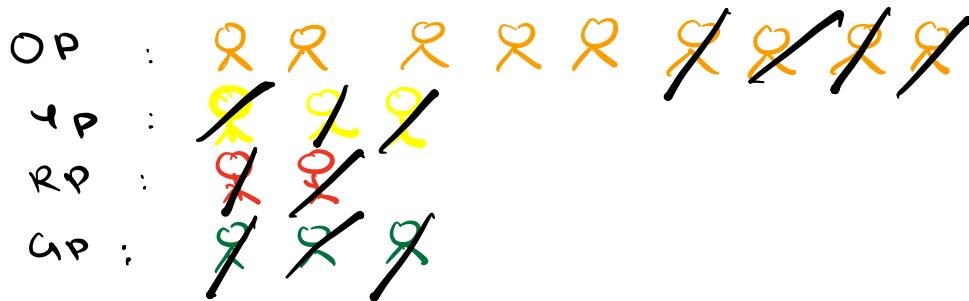


Blue

$$N = 8$$

$$\text{freq} > 4$$

4 parties in an election



OP	YP	RP	GP	Total
9	3	2	3	17

freq > 8  
min freq = 9

Remove	O	Y	R	G	Winner	Total
OP and YP	8	2	2	3	OP	15
OP and GP	7	2	2	2	OP	13
OP and RP	6	2	1	2	OP	11
YP and RP	6	1	0	2	OP	9
YP and GP	6	0	0	1	OP	7
OP and GP	5	0	0	0	OP	5

X Y R P Y P 3

$M\epsilon = 3$

$M\epsilon = 1$

$\text{cnt} = \cancel{X} \cancel{Y} \cancel{Z}_0$

$M\epsilon = \cancel{Y} 3$

$\text{cnt} = \cancel{Y} 0 1$

- Iterate through each ele, keep track of ME and cnt.
- If  $i^{th}$  cur ele == ME      cnt++  
else                                cnt--
- At any point if cnt == 0  
 $i^{th}$  cur ele  $\rightarrow$  ME      cnt = 1

```

int find candidate (int a[], int n) {
    int majele = a[0]
    int cnt = 1

    for (i=1; i < n; i++) {
        if (cnt == 0) {
            majele = a[i]
            cnt = 1
        }
        else if (majele == a[i])
            cnt++
        else
            cnt--
    }
}

```

```

int countmaj = 0
for (i=0 ; i < n ; i++) {
    if (a[i] == majele)
        countmaj++
}
if (countmaj > N/2)
    return majele
else
    return -1

```

T X Z 3 P A       $N=5$   
 $\text{freq} \geq 2$

ME X 3

cnt ~~X Y Z~~,

TC: O(N)  
SC: O(1)

Y 2 3 3 4 2

1 2 7 3 A 1

4. Given a 2D +ve integer matrix. Make all elements in  $i$ th row and  $j$ th col 0 is  $A[i][j] = 0$

1	2	3	4
5	6	7	8
9	2	3	4
1	2	3	4

1	2	0	0
0	0	0	0
0	0	0	0
0	0	0	0

$$\begin{array}{ccccc}
 & 0 & 1 & 2 & 3 \\
 \rightarrow 0 & 1 & 2 & 30 & 40 \\
 \rightarrow 1 & 50 & 60 & 70 & 0 \\
 \rightarrow 2 & 9 & 20 & 0 & 40 \\
 & 0 & & &
 \end{array}$$

$$\begin{array}{ccc}
 1 & 0 & 6 \\
 1 & 5 & 8 \\
 2 & 0 & 9
 \end{array} \rightarrow \begin{array}{ccc}
 0 & 0 & 0 \\
 1 & 0 & 8 \\
 0 & 0 & 0
 \end{array}$$

$$\begin{array}{ccc}
 10 & 0 & 60 \\
 1 & 50 & 8 \\
 2 & 00 & 9
 \end{array}$$

① HashSet of rows

② HashSet of cols

	0	1	2	
0	10	0	60	Row HS
1	5	50	8	
2	20	0	90	Col HS

1. Iterate through mat  
find a cell  $\text{mat}[i][j] = 0$   
rows. insert (i)  
cols. insert (j)

2. Iterate through mat  
 $\text{mat}[i][j]$   
 $\downarrow$   
 rows. contains(i) or  
 cols. contains (j)  
 $\swarrow^r$        $\searrow^c$   
 $\text{mat}[i][j] = 0$       leave as it is

$$TC: O(NM)$$

$$SC: O(N + M)$$

Row HS + Col HS

Alternate for any cell = 0

Mark non-zero cells in row  
and col as -1

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### Doubts

freq > N/2  
freq > 0

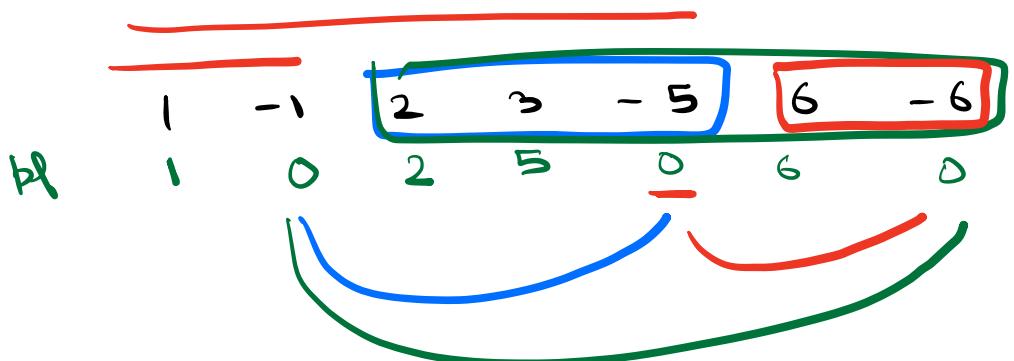
MLE → Memory Limit Exceeded

int arr [ $10^5$  -  $10^6$ ]  
↓  
 $4 \times 10^6$  Bytes

bool arr [ $10^6$ ]

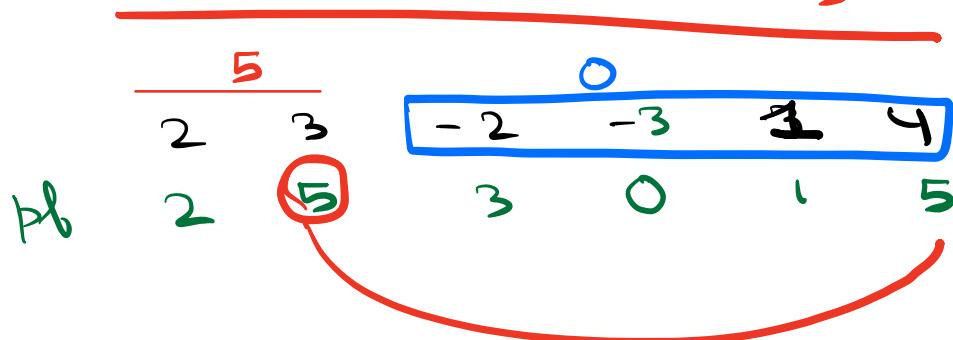
↓  
 $10^6$

subarray  
where sum = 0



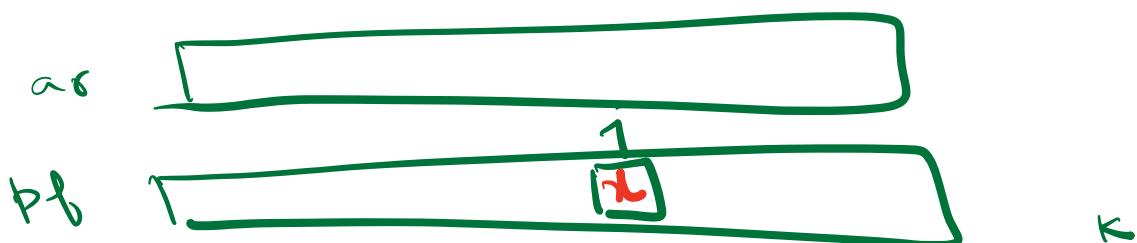
①  $\text{pf}[i] = 0$   
 $\text{cnt}++$

② cnt pair of  
 duplicates  
 in pf  
**5**



Map

pf, cnt



$$\text{pf}[i] == k$$

$\downarrow$   
 $\text{sum}(0-i)$  →  $\text{cnt}++$

$$k - (n-k) = k$$

$i < j$

$$\begin{aligned} \underline{\text{sum}(i-j)} &= k \\ \text{pf}[j] - \text{pf}[i-1] &= k \\ n - \boxed{k} &= k \end{aligned}$$

$$\text{pf}[i-1] = n-k$$

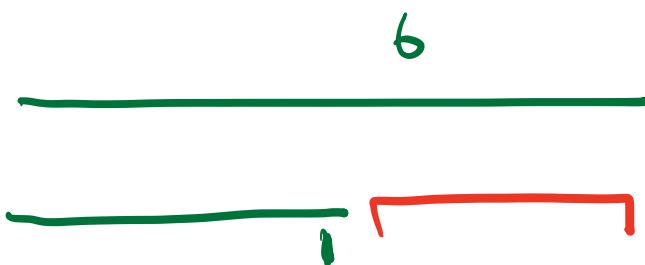
				$i$		sum = 5
0	1	2	2	3		
1	2	2	1			
bf	0	1	3	5	6	$\kappa$

$$\text{sum}(i - j) = \kappa$$

$$bf(j) - bf(i-1) = \kappa$$

$$6 - \underline{1} = 5$$

$$j = 3$$



$$\frac{bf(j) - bf(i-1)}{\kappa} = ? = \kappa$$

$$\kappa - \cancel{0} - \kappa = ?$$