

RESULT $\leftarrow R \bowtie_{\text{Ssn} = \text{Essn}} R_2 \}$ Previous
Using JOIN
condition

So, don't have to use TEMP table
part. in previous query.
This way it
will not take
more space.

NOTE: In JOIN operation, the list of operators
that are acceptable are =, >=, <=, >, <, ≠

These types of operations are called 'theta' JOIN.

When the operation is using = sign, it is
called 'equi' join.

Otherwise, all operations are called 'θ' join.
except 'equi' join.

Q Combine each project tuple with the department
tuple. Natural join

RESULT $\leftarrow \text{PROJECT} * P$ (Dname, Dnum, Mgr-ssn, Mgr-start-date) DEPARTMENT

Pname	Pnumber	Plocation	Dnum	Dname	Mgr-ssn	Mgr-start-date

The new relation will look like this.

using Natural Join.

We have made Dnumber as Dnum using operation & then
using Natural join eliminates the duplicate column

Q Retrieve the name and address of all
employees who work for Research Department.

Ans $R_1 \leftarrow \pi_{\text{Dname} = \text{'Research'}} (\text{DEPARTMENT})$

$R_2 \leftarrow R_1 \bowtie_{\text{Dnumber} = \text{Dno}} (\text{EMPLOYEE})$

RESULT $\leftarrow \pi_{\text{Fname}, \text{Address}} (R_2)$

Q Retrieve the name of all employees who
have no dependent.

Ans $R_1 \leftarrow \pi_{\text{Ssn}} (\text{EMPLOYEE})$

$R_2 \leftarrow \pi_{\text{Essn}} (\text{DEPENDENT})$

$R_3 \leftarrow R_1 - R_2$

$R_4 \leftarrow R_3 \bowtie_{\text{Ssn} = \text{Essn}} (\text{EMPLOYEE})$

RESULT $\leftarrow \pi_{\text{Fname}} (R_4)$

Division Operation (\div)

For a tuple (t) to appear in the result (T) of the division, the values in t must appear in R in combination with every tuple in S .

 R

A	B
a1	b1
a2	b1
a3	b1
a4	b1
a1	b2
a3	b2
a2	b3
a3	b3
a4	b3
a1	b4
a2	b4
a3	b4

 S

A
a1
a2
a3

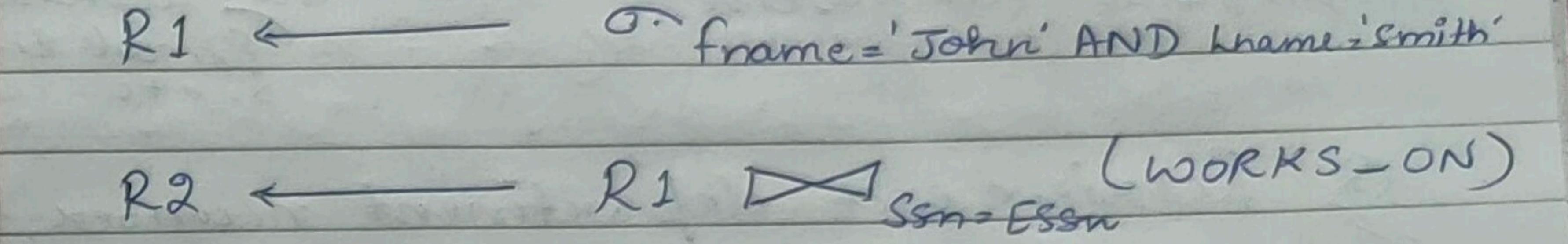
 T (Result)

b1
b4

When you see 'all' word written in the ques, just use division operation.

Q) Retrieve the ssn of employees who works on all the projects that John Smith works on.

Ans

~~Results~~ S $\leftarrow \pi_{\text{Pro}}$ $R \leftarrow \pi_{\text{ssn}, \text{Pro}}$ $T \leftarrow R \div S$

Aggregate Functions & Grouping

- Applied on numeric values.
The operation includes SUM, AVERAGE, MAXIMUM, MINIMUM & COUNT

- Grouping the tuples in a relation by the value of some of their grouping attributes and then applying aggregate functions independently on each group.

Prototype -

grouping attribute F function list

- Q Retrieve each department number, the no. of employees in the department and their average salary.

Dno F COUNT SSN, AVERAGE SALARY C EMPLOYEE)

If we skip the renname operation on this query, then the default table name will look like -

Dno	COUNT-SSN	AVERAGE-SALARY
5	10	100000
6	15	800000
7	10	700000

If we renname, then

R (Dno, no.of.employee, salary)
 $\left(\begin{array}{c} F \\ \text{Dno COUNT SSN, AVERAGE SALARY} \\ \text{(EMPLOYEE)} \end{array} \right)$

R

→ Table name

If we don't want to name a table, just remove R from query

Dno	no.of.employee	Salary
5	10	100000
6	15	800000
7	10	700000

NOTE:

1. If no grouping attribute are specified, the functions are applied to all the functions tuples in the relation.

2. Duplicates are not eliminated when an aggregate functions are applied.

3. NULL values are discarded.

If there are 5 employ in the company, & one's emp. salary is NULL, then avg salary will be divided by 4 not by 5.

Outer Join Operations

left Outer Join

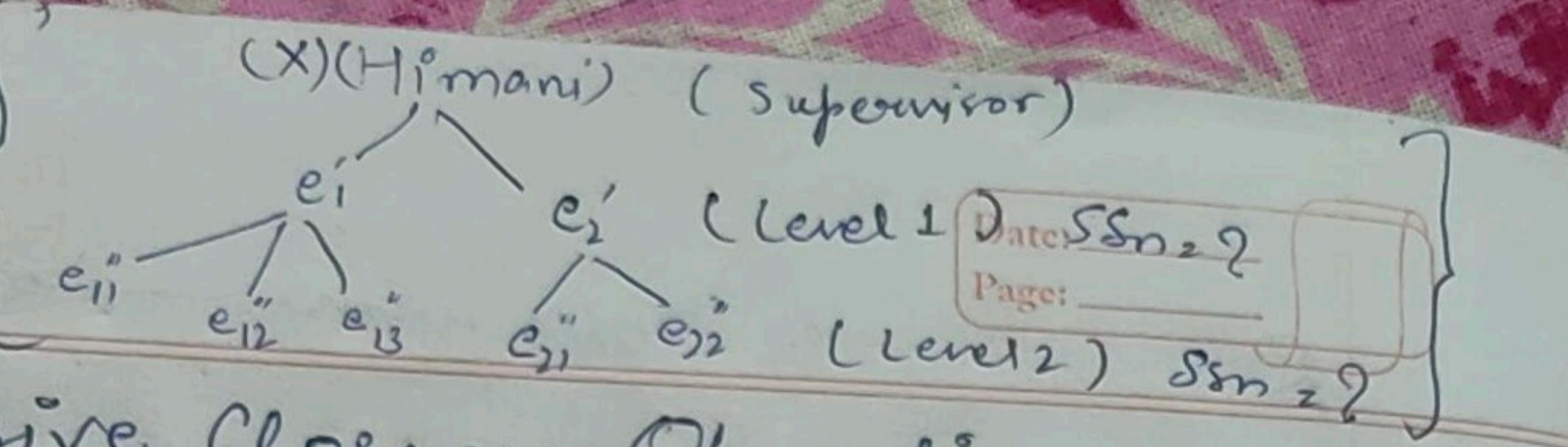
$R \Delta S$
Join condition

Right Outer Join

$R \Delta S$
Join cond.

Full Outer Join

$R \Delta S$
Join cond.



Recursive Closure Operation

level 1

g) Retain all employee Son who are directly supervised by James. Son of James is 888665555.

Normalization

In-formal guidelines for Relational Schema

1. Making sure that the semantics of the attributes is clear in the schema.
2. Using the redundant information in tuples and update ~~the~~ anomalies.
3. Reducing null values in the tuples.
4. Disallow the generation of ~~repeated~~ spurious tuples.

Explanation
of 1:

Design a relation so that it is easy to explain.

Do not combine attributes of multiple relations into a single relation

2. (i). REDUCING THE REDUNDANT INFORMATION

The goal of schema design is to minimize the storage space used by the base relation (i.e., which exists physically)

Emp - Dept

Ename	Ssn	Bdate	Address	Dnumber	Dname	Dmgr-ssn
ABC	①					
ABC	1	X42	X42	D1	Research	NULL
PQR	2	X42	"	D2	Admin	1
RST	3	X42	"	D2	Admin	1

↓
Redundant values - repeated.

& this will not happen which will consume more space.
tables - Emp & Dept. If we make two separate

(ii) Update Anomalies

Inserction

Modification

Deletion

(a) Inserction.

Ename	Ssn	Bdate	Address	Dnumber	Dname	Dmgr-ssn
X42	1			D1	Research	1
X42	2			D2	Finance	2
ABC	3			D2	Finance	2
PQR	4			D2	Finance	3

↓
Insertion anomaly

This is the insertion mistake done by the entry operator. He/She has to remember for which Dept. the manager has its Ssn or which Dept have which dep. number

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Xamp server will not throw error but it must throw error as-

- (i) Dept. number is not same as it should be.
- (ii) the manager ssn is also different for the same department - finance.

If tables would be different, then it will throw an error.

(b) Deletion

If we delete a Employee's data, it would lead to delete some ~~inf.~~ inf. information. E.g.,

X42	D3	HR	1	X delete.
PQR	D1	Finance	2	
ABC	D1	Finance	2	

Then, if we delete X42's employee row or information, the HR department will automatically gets deleted because there is only one entry of HR.

(c) Modification

If we change Dno. of Finance, then all the rows need to be modified separately. This is modified anomaly.

If there will be separate tables, it wouldn't have happened.

Explanation

Soln → Design ~~the~~ base relation so that no update anomalies are present in the relation

3.

Emp-office Ph

/

Ssn | Ename | Office Phone .

Only department heads will get their office phone no's, so in this combined table, most of the values will be the NULL in the office phone column.

And if there will separate tables, then no NULL values will be there.

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As far as possible, reduce the NULL values in the relation.

4.

EMP-LOC

EMP-PROJ

Ename | Plocation | Ssn | Pnumber | Hrs | Pname | Plocation

EMP-PROJ

[Ssn | Pnumber | Hrs | Ename | Pname | Plocation]

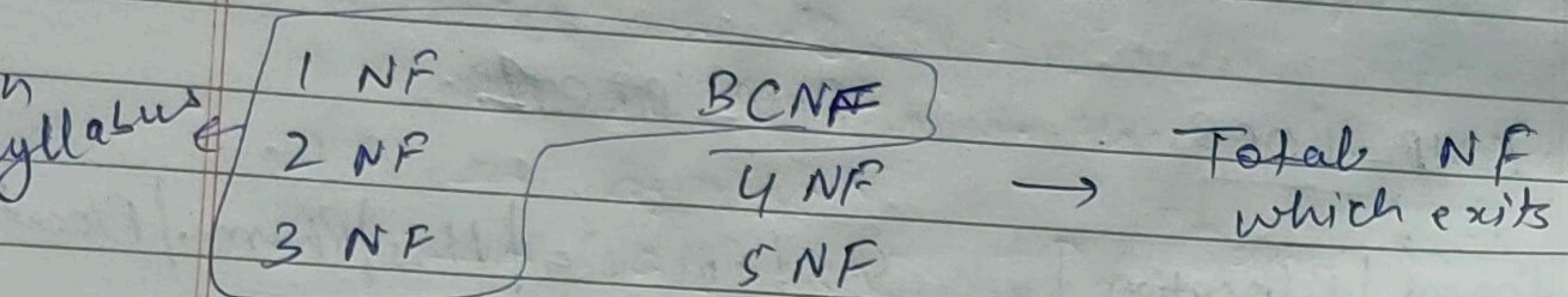
Design a relation schema so that they can be joined on attributes that are appropriately related (PK & FK) pairs in such a way that guarantees no ~~super~~ spurious tuples

In these tables, Plocation is neither a PK nor a FK, it just a simple attribute. So, there is not uniqueness & fake tuples will get generated.

P.T.O

Formal Guidelines of Normalization

NF \rightarrow Normal Forms.



• Functional Dependency (F.D) or (f.d)

F.D is denoted by $X \rightarrow Y$.

Between two sets of attributes X & Y that are subset of R specifies a constraint on the possible tuples that can form a relation state (a) of R.

$X \rightarrow Y \rightarrow$
 X goes to Y means there is a F.D from X to Y or Y is functionally dependent on X

E.g.: Given a value of Ssn, we can uniquely determine an Ename or Ename is functionally determined by Ssn.
 $Ssn \rightarrow Ename$.

E.g.: Pnumber $\rightarrow \{Pname, Place\}$
 for multiple tuples

Read \rightarrow
 Left \rightarrow Right
 Right \rightarrow Left

i) Given a relation -

A	B	C	D
a ₁	b ₁	c ₁	d ₁
a ₁	b ₂	c ₂	d ₂
a ₂	b ₂	c ₂	d ₃
a ₃	b ₃	c ₄	d ₃

Test whether the following F.D holds or not?

(i) $B \rightarrow C$

True as $(c_1, b_1), (c_2, b_2), (c_4, b_3)$.

So, it holds F.D.

If there will be suppose $(c_4, b_3), (c_4, b_1)$, then FD not holds.

(ii) $C \rightarrow B$

True as $(b_1, c_1), (b_2, c_2), (b_3, c_4)$.

It holds

(iii) $\{A, B\} \rightarrow D$

E.g.: $\begin{cases} a_1 & b_2 & d_2 \\ a_2 & b_2 & d_2 \\ a_3 & b_2 & d_2 \end{cases}$ This is a pattern.
 So, it FD holds

F.D

It holds.

because.

d_1 & d_2 are already unique. we'll focus on d_3 .

& d_3 is following the same pattern

$$d_3 \rightarrow (a_2, b_2)$$

$$d_3 \rightarrow (a_3, b_3) \rightarrow \text{Same pattern.}$$

If $d_3 \rightarrow (a_4, b_2)$, then, it violates ~~F.D.~~

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It holds.

For c_2 , there is a pattern.

$$\begin{array}{c|c|c} a_1 & b_2 & c_2 \\ a_2 & b_2 & c_2 \end{array} \rightarrow \text{Pattern.}$$

It holds:-

- (i) If there is some pattern which is being followed.
- (ii) If there is same value-pair or same data
 - e.g.: $b_2 \rightarrow c_2$
 - $b_2 \rightarrow c_2$

End of topic

Basically same data point diff.

$$(iv) B \rightarrow A$$

If violates for a_1

$$(v) D \rightarrow C$$

If violates for c_2

$$(vi) \{A, B\} \rightarrow C$$

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Normalization of data

It can be considered as a process of analyzing the given relational schema based on their F.D and Keys to achieve the desirable properties of -

1. Minimizing the redundant data.
2. Minimizing the update anomalies.

Normal Form Test (NF)

It refers to the highest normal form conditions that a relational schema can achieve.

Prime Attributes

A Prime Attribute of R if it is a member of some candidate key of R.

Non-Prime attribute

If it is not the member of any candidate key of R.

E.g WORKS_ON

Ssn	Pno	Hrs
-----	-----	-----

Ssn & Pno are the prime attributes of WORKS_ON &

Hrs is the non-prime attribute of WORKS_ON

1) 1 NF

- It states that the value of any attribute in the domain of that attribute must be atomic. E.g Non-atomic Address (Multi-valued) attributes Street City state.
- It disallows multi-valued attributes & composite attributes.

NOTE:

We will check the RHS of the F.D.

DEPARTMENT				→ Book Linen
Dname	Dnumber	Dmgrssn	Dlocation	
Day off generating	↑	↑	↑	

∴ Dnumber → {Dname, Dmgrssn, Dlocation}

↳ to solve ques, we use this reference.

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Since Dlocation is a multivalued attribute,
∴ The given relational schema is not in 1NF.

There are three ways that can be used
to decompose the relation into 1NF.

1st way → Best way

(1)

Dname	Dnumber	Dmgrssn	Dnumber	Dlocation
	1	123		New Delhi
	1	222		LONDON
Research	2	123		New Delhi
Admin	2	222		New York

∴ Dnumber + Dlocation is PK - Dnumber | Dlocation
 It's valid here that 1 is
 being repeated as it is in
 combination wise unique.

2nd way

(2)

Dname	Dnumber	Dmgrssn	Dlocation
Research	1	123	New Delhi
Research	1	123	LONDON
Admin	2	222	New Delhi
Admin	2	222	New York

Since the scheme contains the
 Disadvantage - Redundant values,
 which is not it violates the normalization
 of data test.

Dnumber is PK, so we can make
 Dlocation ^{also} a PK, so it combines to make PK

3rd way

(3)

Dname	Dnumber	Dmgrssn	Dlocation	Dloc2	Dloc3
Research	1	123	New Delhi	New York	NULL
Admin	2	222	LONDON	NULL	NULL

This design suffers from introduction of
 NULL values.

2. 2NF

It is based on Primary Key, PK.

2NF test is based on full functional
 dependency.

Full Functional Dependency

A F.D $X \rightarrow Y$ is a full F.D if
 removal of any attribute A from X
 means that the dependency ~~dependency~~ does not
 hold

Partial Dependency

A F.D $X \rightarrow Y$ is a partial dependency
 if some attribute A can be removed
 from X and the dependency still holds.

E.g. of Full F.D

$$\{ \text{Ssn}, \text{Pno} \} \rightarrow \text{Hrs}$$

It is a full F.D because

$$\text{Ssn} \rightarrow \text{Hrs}$$

$$\text{Pno} \rightarrow \text{Hrs}$$

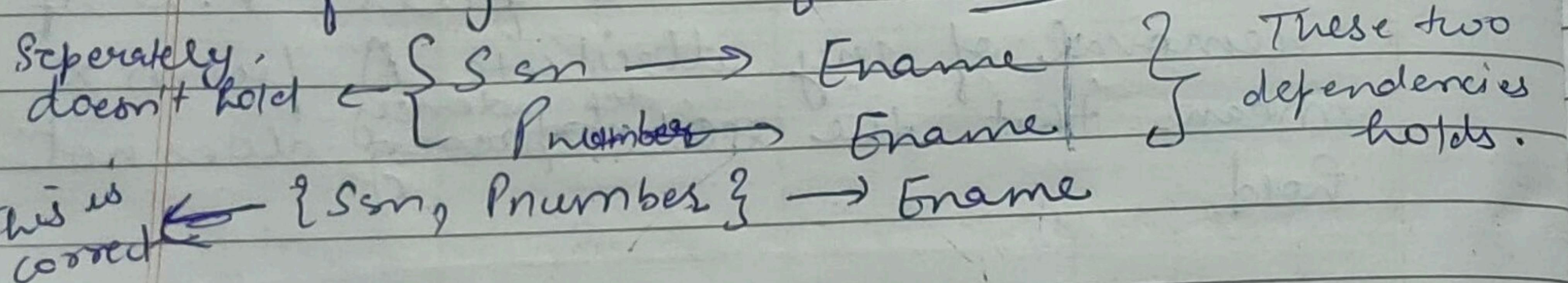
} → it does not hold.
as they separately can't determine the Hrs.

Ssn	Pno	Hrs
-----	-----	-----

E.g. of Partial F.D

$$\{ \text{Ssn}, \text{Pno} \} \rightarrow \text{Ename}$$

It is a Partial F.D because ~~non-monadic~~ of any attribute from LHS doesn't affect the dependency.



① 2NF disallows Partial Dependency

② A Relation Schema, R is in 2NF if every non prime attribute, A in R is fully functionally dependent on the PK of R.

EMP-PROJ

Ssn	Pnumbers	Hrs	Ename	Pname	Plocation
FD1					
FD2					
FD3					

FD1 is in 2NF.

FD2 is a Partial Dependency.
∴ it is not in 2 NF.

FD3 is not in 2NF because of Partial Dependency.

FD2 for FD2

(2NF)

Ssn	Pnumber	Hrs

Pnumber	Pname	Plocation

FD3 → Making it to be suitable for 2NF.

~~Pnumber~~

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3. 3NF Based on PK

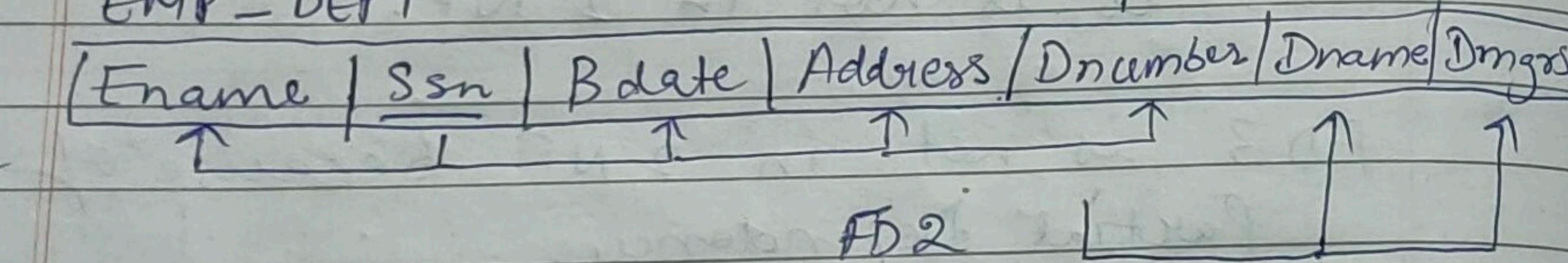
- It is based on the concept of transit dependency

Transit dependency

A F.D $X \rightarrow Y$ is transit if there exist a set of attributes Z that is neither a candidate key nor a subset of any key and both $X \rightarrow Z$ & $Z \rightarrow Y$ holds.

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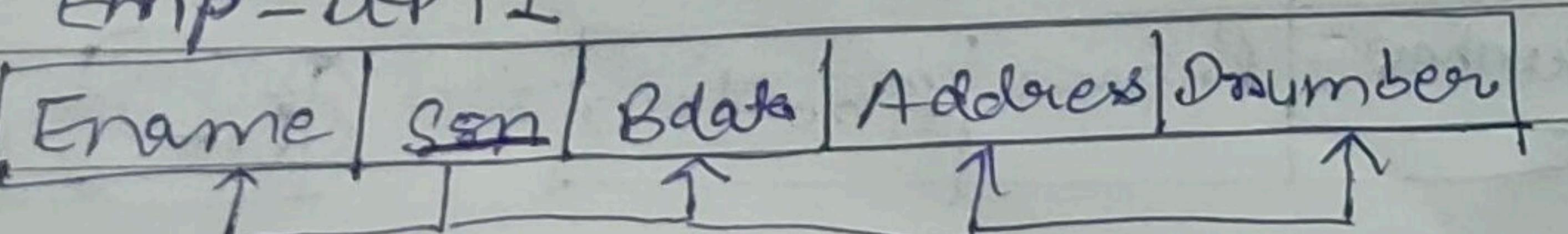
EMP - DEPT



Since the given relational scheme is not in 3NF due to transit dependency exist in Dnumber.

We will decompose ~~the~~ EMP-DEPT into 3NF

EMP - DEPT 1



EMP-DEPT 2

EMP-DEPT		
Dnumber	Dname	Dmgrssn

2NF and 3NF Based on Rebo

- o 2NF Based on Candidate key

A relational schema R is in 2NF if
every non-prime attribute A in R
is fully functionally dependent on candidate
key of R (one of the CK should be
present on the LHS of the F.D.).
CK (together can make a PK)

LO-

LOTS

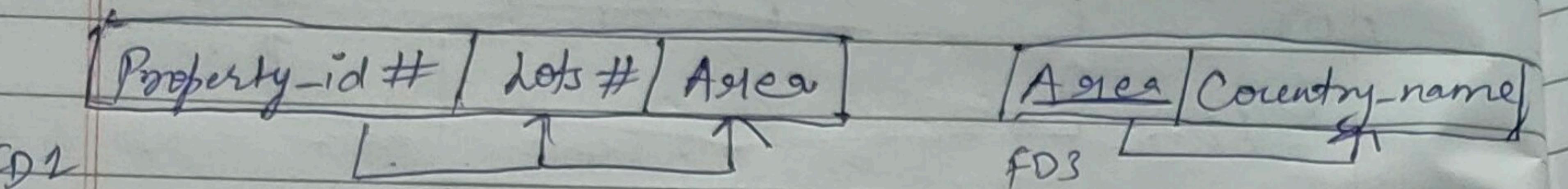
Property-id#	Country-name	Lots#	Area	Price	Tax-rate
FD1	↑	↑	↑	↑	↑
FD2	↑	↑	↑	↑	↑
FD3	↑	↑	↑	↑	↑
FD4	↑	↑	↑	↑	↑

```

    graph TD
      L[LOTS] -- "FD1" --> CN[Country-name]
      L -- "FD2" --> L1[Lots#]
      L -- "FD2" --> A1[Area]
      L -- "FD2" --> P1[Price]
      L -- "FD2" --> TR1[Tax-rate]
      CN -- "FD3" --> L2[Lots#]
      CN -- "FD3" --> A2[Area]
      CN -- "FD3" --> P2[Price]
      CN -- "FD3" --> TR2[Tax-rate]
      L2 -- "FD4" --> A3[Area]
      L2 -- "FD4" --> P3[Price]
      L2 -- "FD4" --> TR3[Tax-rate]
  
```

In the given relation schema, FD3 is violating the test of 2NF. Decomposing
↳ because candidate key is not in totality on LHS.

Hence decomposing the relational schema into BCNF.



FD₂ gets deleted.

Closure :-

The ~~subset~~ set of all dependencies that include F as well as all the dependencies that can be derived from F is called the closure of F and it is denoted by F^+ .

Eg Q1 . $F = \{ \text{Ssn} \rightarrow \{\text{Ename}, \text{Bdate}, \text{Address}, \text{Dnumber}\}$

$$\text{Dnumber} \rightarrow \{\text{Dname}, \text{Dmgr-ssn}\}$$

Find closure of $\{\text{Ssn}\}^+$ & closure of $\{\text{Dnumber}\}^+$ and also find the key.

Ans $\{\text{Ssn}\}^+ = \{\text{Ssn}, \text{Ename}, \text{Bdate}, \text{Address}, \text{Dnumber}, \text{Dname}, \text{Dmgr-ssn}\}$

$\{\text{Dnumber}\}^+ = \{\text{Dnumber}, \text{Dname}, \text{Dmgr-ssn}\}$

Since closure of Ssn contains all the attributes. Therefore, Ssn is the key.

Q2. $F = \{ \text{Ssn} \rightarrow \text{Ename}, \text{Pnumber} \rightarrow \{\text{Pname}, \text{Plocation}\}$

$$\{\text{Ssn}, \text{Pnumber}\} \rightarrow \{\text{Hrs}\}$$
. find key.

Ans $\{\text{Ssn}, \text{Pnumber}\}^+ = \{\text{Ssn}, \text{Pnumber}, \text{Hrs}, \text{Pname}, \text{Plocation}, \text{Ename}\}$

Since closure of $\{\text{Ssn} \& \text{Pnumber}\}$ contains all the attributes. Therefore combination of Ssn & Pnumber is a PK.

Q3 Consider the relation schema R(A, B, C, D, E) with the following dependencies \Rightarrow

$$AB \rightarrow C$$

$$CD \rightarrow E$$

$$DE \rightarrow B$$

Is A B candidate key of this Relation?
If not A B D is a candidate key of this Relation?

$$\{A, B\}^+ = \{A, B, C\}$$

A, B 's closure is not a key since it does not contain all the attributes of R .

$$\{A, B, D\}^+ = \{A, B, D, E, C\}$$

Since closure of $\{ABD\}$ has all the attributes. \therefore It is a Key.

Q4. Find Key of $R (E, F, G, H, I, J, K, L, M, N)$
Given the set of dependencies \rightarrow

$$EF \rightarrow G, \quad F \rightarrow IJ, \quad EH \rightarrow KL, \\ K \rightarrow M, \quad L \rightarrow N$$

Ans $\{EFH\}$ is the Key.

$$\{EFH\}^+ = \{E, F, G, H, K, L, I, J, M, N\}$$

\therefore It is a key because its closure contains all the attributes.

Imp. 6 marks Ans)

Q5. Consider the relation $R (A, B, C, D, E, F, G, H, I, J)$ and set of FD's \rightarrow

~~for 6~~

$$F, \begin{cases} A, B \rightarrow C \\ A \rightarrow DE \\ B \rightarrow F \\ F \rightarrow GH \\ D \rightarrow IJ \end{cases}$$

What is the key of R ? Decompose R into 2NF, then 3NF.

$$\text{Ans} \quad \{AB\}^+ = \{A, B, C, D, E, F, G, H, I, J\}$$

Since, AB 's closure has all attributes.

$\therefore \{A, B\}$ is a Key.

Since ~~Q~~, we have only 1 key in the ques, therefore we'll find 2NF with taking it as PK. (Based on PK)

2 NF

Partial dependencies that are violating 2NF.

$$\{A\}^+ = \{A, D, E, I, J\}$$

$$\therefore \begin{aligned} A &\rightarrow DE \\ D &\rightarrow IJ \\ A &\rightarrow A \end{aligned} \quad (\because \text{trivial dependency})$$

$$\{B\}^+ = \{B, F, G, H\}$$

$$B \rightarrow P$$

$$F \rightarrow GH$$

$$B \rightarrow B$$

(trivial dependency)

Therefore, relations that are present in 2NF will be

$$R_1 = \{\underline{A}, D, E, I, J\}$$

$$R_2 = \{\underline{B}, F, G, H\}$$

$$R_3 = \{\underline{A}, \underline{B}, C\}$$

R_1 and R_2 has transitive dependencies, therefore relations that are present in 3NF will be - because

$$R_{11} = \{A, D, E\}$$

$$A \rightarrow D$$

$$R_{12} = \{D, I, J\}$$

$$D \rightarrow IJ$$

$$R_{21} = \{\underline{B}, F\}$$

$$B \rightarrow F$$

$$R_{22} = \{\underline{F}, G, H\}$$

$$F \rightarrow GH$$

Final set of Relations that are in 3NF are -

$R_{11}, R_{12}, R_{21}, R_{22}$ and R_3 .

6 marks ques CMA

Q. Consider the relational schema,

$R = \{A, B, C, D, E, F, G, H, I, J\}$ & FD's are

$$AB \rightarrow C$$

$$BD \rightarrow EF$$

$$A \rightarrow I$$

$$AD \rightarrow GH$$

$$H \rightarrow J$$

Find the key of R and then decompose the R into 2NF and then 3NF.

An $\{ABD\}$ is a key.

$$\{ABD\}^+ = \{A, B, D, E, F, G, H, I, J\}.$$

2 NF

Partial dependencies that are violating 2NF.

$$\{A\}^+ = \{A, I\}$$

$$A \rightarrow I \quad (\text{given})$$

$$A \rightarrow A \quad (\text{trivial dependency})$$

$$R_1 = \{\underline{A}, I\}$$

Note:
Jisko closure nikle hai,
wohi PK banta hai.

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A closure is
finished already.
 $A \rightarrow I$

$\{AB\}^+ = \{A, B, C\}$

$A, B \rightarrow C$ (given)

$A, B \rightarrow AB$ (trivial dependency)

$R_2 = \{A, B, C\}$

$\{BD\}^+ = \{B, D, E, F\}$

$B, D \rightarrow BD$ (trivial dependency)

$BD \rightarrow EF$ (given)

$R_3 = \{B, D, E, F\}$

$\{AD\}^+ = \{A, D, C, H, J\}$

$AD \rightarrow AD$ (trivial dependency)

$H \rightarrow J$ (given)

$AD \rightarrow CH$ (given)

$R_4 = \{A, D, C, H, I\}$

Relations that are present in 2NF will
be R_1, R_2, R_3, R_4 .

Now, R_4 has transitive dependency,

Decomposing R_4 into R_{41} & R_{42} .

$R_{41} = \{A, D, C, H\}$ because $[AD \rightarrow CH]$

$R_{42} = \{H, J\}$ $[H \rightarrow J]$

Other Relations that are

The final set of relations that are in 3NF
are R_1, R_2, R_3, R_{41} & R_{42} .

COVER

A ~~FD~~ set of F.D, F is said to cover
another set of F.D, E if every F.D in
E is also in F and vice-versa. (F.D's are
equivalent).

u marks ques (CMA)

Q7. For the following set of FD, check
whether ~~FD is a subset of~~ F is a subset of G

$F \subseteq G$ (u covers F)

or $G \subseteq F$ (F covers G)

or $F = G$

$F \neq G$.

$$F = \{ A \rightarrow C, AC \rightarrow D, \\ E \rightarrow AD, E \rightarrow H \}$$

$$G = \{ A \rightarrow CD, E \rightarrow AH \}$$

Ans F

A → C
AC → D
E → AD
E → H

1st Step
LHS → closure
2 FD's G ki

$$\{A\}^+ = \{A, C, D\}$$

$$\{AC\}^+ = \{A, C, D\}$$

$$\{E\}^+ = \{A, H; C, D\}$$

11th step → Check the dependencies of F in Step 1.

Since all F F.D's holds
∴ Work done by F can
also be done by G.

∴ G covers F ($F \subseteq G$)

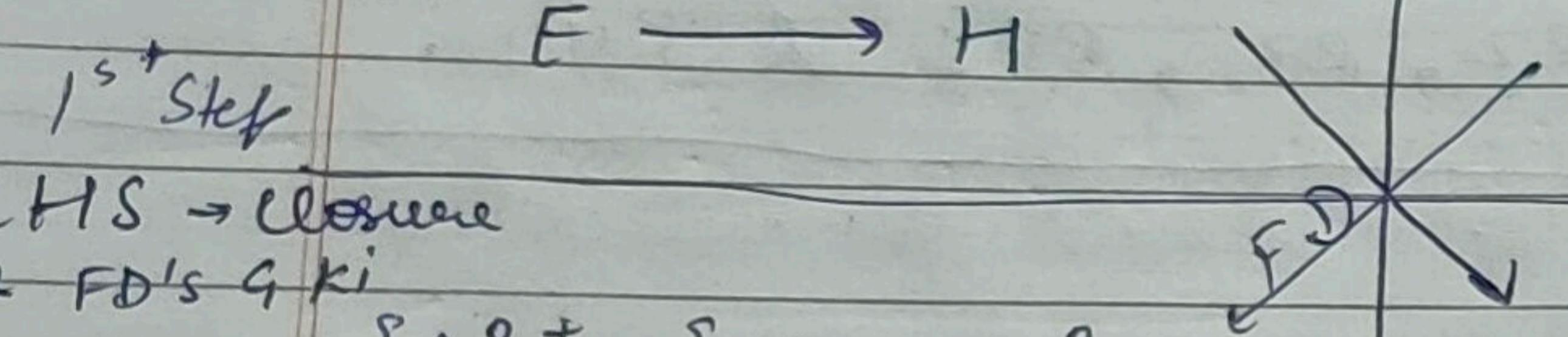
Since, F covers G & G covers F, therefore
it is equivalent.

$$G = \begin{matrix} A \rightarrow CD \\ E \rightarrow AH \end{matrix}$$

$$\{A\}^+ = \{A, C, D\}$$

$$\{E\}^+ = \{E, A, D, H, C\}$$

\vdash



$$Now, G \subseteq F$$

Q1. Find whether the two FD's ~~are~~ F & G
are equivalent or not or whether one
covers the other.

$$\text{Ans } F = \{ A \rightarrow B, \\ B \rightarrow C, \\ AB \rightarrow D \}$$

$$\text{(ii) } G = \{ A \rightarrow B, \\ B \rightarrow C, \\ A \rightarrow C, \\ A \rightarrow D \}$$

$$\text{Q2 } F = \{ A \rightarrow B, \\ B \rightarrow C, \\ A \rightarrow C \}$$

$$G = \{ A \rightarrow B, \\ B \rightarrow C, \\ A \rightarrow D \}$$

Ans (i) $F = A \rightarrow B$

A → B
B → C
AB → D

A → B
B → C
A → C
A → D

$$\{A\}^+ = \{A, C, D, B\}$$

$$\{B\}^+ = \{B, C\}$$

$$\{AB\}^+ = \{A, B, C\}$$

$$\{A\}^+ = \{A, B, C\}$$

$$\{B\}^+ = \{B, C\}$$

$$\{BC\}^+ = \{B, C\}$$

Since, F covers G & G covers F, therefore
it is equivalent.

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MINIMAL COVER

It is a set of functional dependencies, E is a minimal set of F.D's that is equivalent to E.

A minimal cover of a set of FD's, E is a minimal set of FD that is equivalent to E.

We can always find out one minimal cover.

Q

Find the minimal cover of F.

$$F: \{ A \rightarrow D \\ BC \rightarrow AD \\ C \rightarrow B \\ E \rightarrow A \\ E \rightarrow D \}$$

Step 1:- Singleton RHS

$$A \rightarrow D \\ BC \rightarrow A \quad \text{--- (1)} \\ BC \rightarrow D \\ C \rightarrow B \\ E \rightarrow A \\ E \rightarrow D$$

Step 2:- NO extra elements on LHS (on step 1)

NOTE: whenever you are making a modification, do it immediately before examine the other F.D's.

From (1),

$$\{B\}^+ = \{B\}$$

$$\{C\}^+ = \{CBA\}$$

$\{C\}^+ = \{CB\}$
 $\{C\}^+ = \{CA\}$,
then also we can eliminate B from RHS

Since (C closure) $\{C\}^+$ has B, we can eliminate B from left hand side.

The set of FD's are -

$$A \rightarrow D \quad [\because C \text{ alone can form } A \& B, \text{ therefore no need of } B]$$

 $C \rightarrow A$
 $BC \rightarrow D \quad \text{--- (2)}$

$$C \rightarrow B \\ E \rightarrow A \\ E \rightarrow D$$

$$\{B\}^+ = \{B\}$$

$$\{C\}^+ = \{C, A, B, D\}$$

Since $\{C\}^+$ has B, we can eliminate B from LHS.

Therefore, the current set of F.D's are -

$$\begin{aligned} A \rightarrow D & \quad \textcircled{1} \\ C \rightarrow A & \quad \textcircled{2} \\ C \rightarrow D & \\ C \rightarrow B & \\ E \rightarrow A & \\ E \rightarrow D & \end{aligned}$$

Step 3:- Remove redundant F.D's

NOTE: Same as in Step 2

From (1)

- $\{A\}^+ = \{A\}$

~~so~~

$\{A\}^+$ doesn't contain $\rightarrow D$, therefore we need $A \rightarrow D$ in our final set.

- From (2), $\{C\}^+ = \{C, D, B\}$

Since $\{C\}^+$ doesn't contain A , therefore we need $C \rightarrow A$ in our final set.

- From (3), $\{C\}^+ = \{C, A, B, D\}$

Since $\{C\}^+$ contains A and D , therefore we can eliminate $C \rightarrow D$.

After Modification has done -

Now, therefore the current set of FD's are -

$$\begin{aligned} A \rightarrow D & \\ C \rightarrow A & \\ C \rightarrow B & \quad \textcircled{1} \\ E \rightarrow A & \quad \textcircled{2} \\ E \rightarrow D & \quad \textcircled{3} \end{aligned}$$

From (4), $\{C\}^+ = \{C, A\}$

Since $\{C\}^+$ doesn't contain B , therefore we need $C \rightarrow B$ in our final set.

From (5), $\{E\}^+ = \{E, D\}$

Since $\{E\}^+$ doesn't contain A , therefore we need $E \rightarrow A$ in our final set.

From (6), $\{E\}^+ = \{E, A, D\}$.

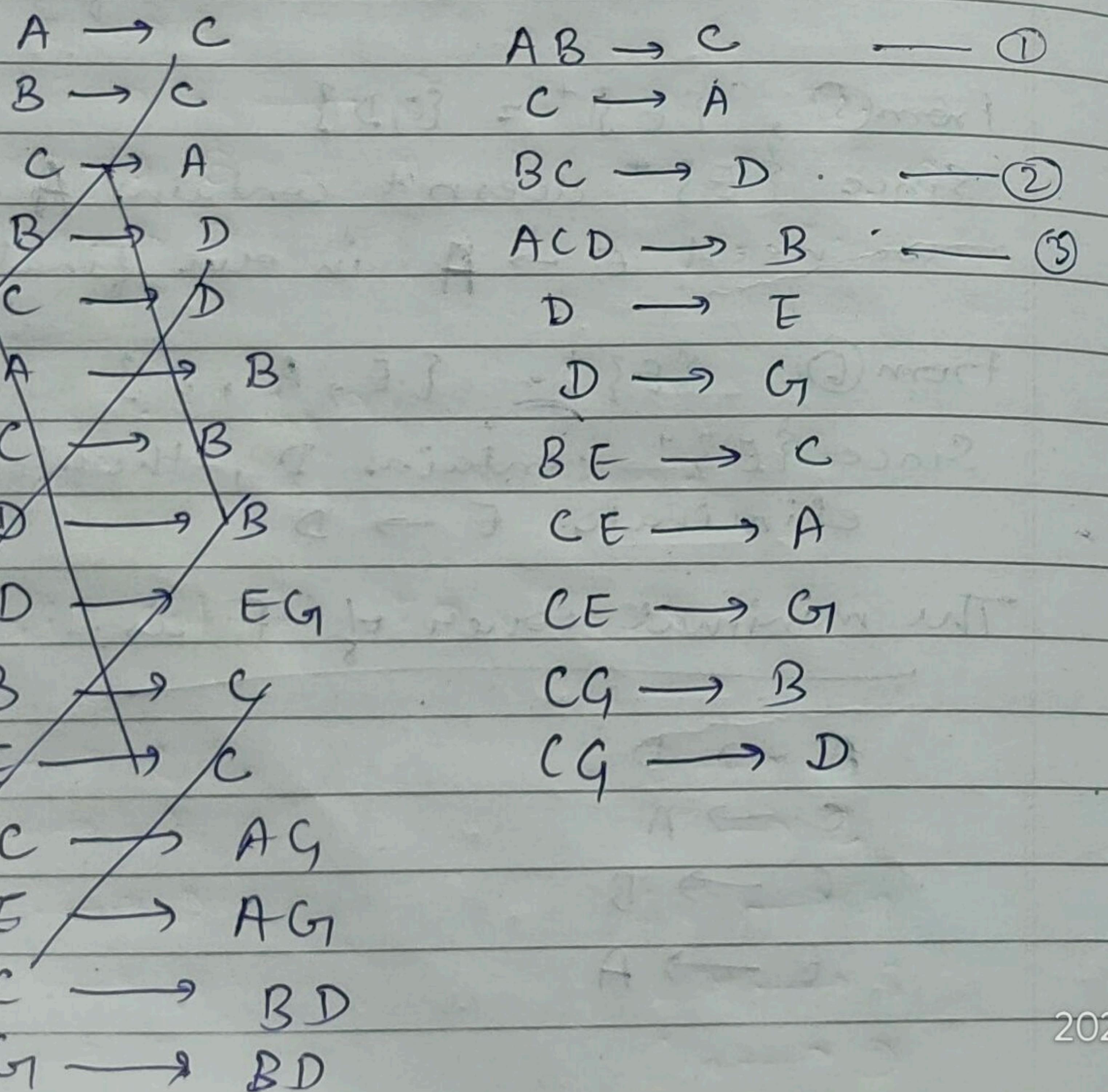
Since $\{E\}^+$ contains D , therefore we can eliminate $E \rightarrow D$.

The minimal cover of F is :-

$$\begin{aligned} A \rightarrow D & \\ C \rightarrow A & \\ C \rightarrow B & \\ E \rightarrow A & \end{aligned}$$

Q F: { AB → C
 C → A
 BC → D
 ACD → B
 D → EG
 BE → C
 CE → AG
 CG → BD }

Ans Step 1 :- Singleton RHS.



Step 2:- No extra elements on LHS

From ①,
 $\{A\}^+ = \{A\}$
 $\{B\}^+ = \{B\}$

From ②,
 $\{B\}^+ = \{B\}$
 $\{C\}^+ = \{C, A\}$

From ③,
 $\{A\}^+ = \{A\}$
 $\{C\}^+ = \{C, A\}$
 $\{D\}^+ = \{D, E, G\}$

Since $\{C\}^+$ has A, we can eliminate A from RHS.

The set of FD's are -

$AB \rightarrow C$	$BE \rightarrow C$ — ④
$C \rightarrow A$	$CE \rightarrow A$ — ⑤
$BC \rightarrow D$	$CE \rightarrow G$
$ED \rightarrow B$	$CG \rightarrow B$
$D \rightarrow E$	$CG \rightarrow D$
$D \rightarrow G$	

From ⑥

$$\{B\}^+ = \{B\}$$

$$\{E\}^+ = \{E\}$$

No changes

From ⑦

$$\{C\}^+ = \{C, A\}$$

$$\{E\}^+ = \{E\}$$

∴ Eliminate E

$$AB \rightarrow C$$

$$C \rightarrow A$$

$$BC \rightarrow D$$

$$CD \rightarrow B$$

$$D \rightarrow E$$

$$D \rightarrow G$$

$$BE \rightarrow C$$

$$C \rightarrow A$$

$$CE \rightarrow G \quad \text{--- } ⑥$$

$$CG \rightarrow B \quad \text{--- } ⑦$$

$$CG \rightarrow D \quad \text{--- } ⑧$$

From ⑥

$$\{C\}^+ = \{C, A\}$$

$$\{E\}^+ = \{E\}$$

No change

From ⑦

$$\{C\}^+ = \{C, A\}$$

$$\{G\}^+ = \{G\}$$

No change.

From ⑧

$$\{C\}^+ = \{C, A\}$$

$$\{G\}^+ = \{G\}$$

No change

Final set of FD's are -

$$AB \rightarrow C$$

$$C \rightarrow A$$

$$BC \rightarrow D$$

$$CD \rightarrow B$$

$$D \rightarrow E$$

$$D \rightarrow G$$

$$BE \rightarrow C$$

$$CE \rightarrow G$$

$$CG \rightarrow B$$

$$CG \rightarrow D$$

Chapter-17 (Indexing)

Chapter-17 (Indexing)

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- or table
- ① The file, EMPLOYEE, DEPARTMENT is referred to as Data File.
 - ② Tuple will be referred to as Data Record.
 - ③ 3 or 4 data records together is called Disc Block or Block.
 - ④ There is another file called Index file that has 2 columns -
1st column name - Index Field
2nd column name - Pointer.
 - ⑤ Index ~~file~~ Tuples are called Records.

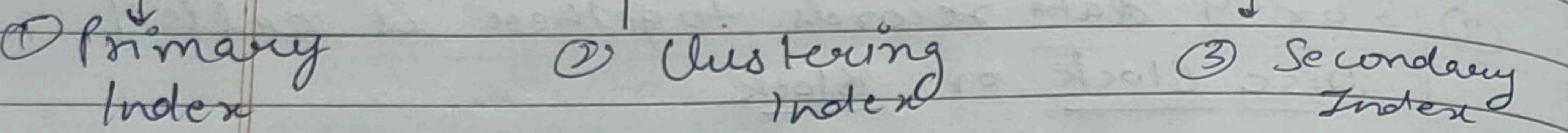
Index file is of two types -

- ① Dense Index
- ② Sparse Index
or
(non-dense index)

- ① Dense Index - It has an index entry for every search key-value (every record or data record in the data file).
- ② Sparse Index - It has index entry for only some of the search-key value. A Sparse

Index has fewer entries than the no. of records in the data file.

Types of Indexes



① Primary Index

- It is based on Key-value. (hence unique) and the data file is ordered (i.e., sorted).
- Total no. of entries in the index file is equal to $\frac{\text{no. of disc blocks or Anchor blocks.}}{\text{no. of records}}$.
- Primary Index is a Sparse Index since it includes an entry for each block rather than for every record.

Advantages -

- (1) It occupies less space.
- (2) Binary Search is performed on Index File rather than Data File. (less time)

Disadvantages

- ① In terms of Insertion & Deletion of Data Records.

② Clustering Index

NOTE: It is based on non-key. (hence, duplicates) but the Data file is ordered.

- A Clustering Index is a Sparse Index because it has an entry for every distinct value which is non key by definition & hence has duplicates.

Advantage - searching.

Disadvantage

- ① In terms of Insertion & Deletion of Data Records

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(3)

Secondary Index

Secondary Index is based on

(a) on the Key field

(b) non-key field

- (a) The data file is unordered & it is based on key-value, hence unique.

Index-File →

- It has a distinct value for every record.
- It ~~is dense~~ dense index because it has an entry for each or every record of the data file.
- Pointer points either to the block in which the record is stored or to the record itself.

Advantages

- Insertion is easy as there is no order.
- searching is also easy.

Disadvantages

If entry is deleted from Data file, it also has to be deleted from Index file.

(b) Based on non-key field

- The file is unordered and it is based on non-key value, hence duplicate.

It is a sparse index as far as an index file is concerned.

Advantages

One level of direction is there.

Disadvantages

Searching takes more time because an extra level of indirection is there.

INTRODUCTION TO TRANSACTION PROCESSING

It is a transaction because there is one database & multiple users are accessing it. E.g.: - booking of train, movie tickets, etc.

A transaction is an executing program that forms a logical unit of database processing.

A transaction can include one or more database access operations with (insertion, deletion, update, searching retrieval).

The basic database access operation are -

(1) `read-item(x)`

It reads the database item named as 'x' into a program variable also named as 'x'.

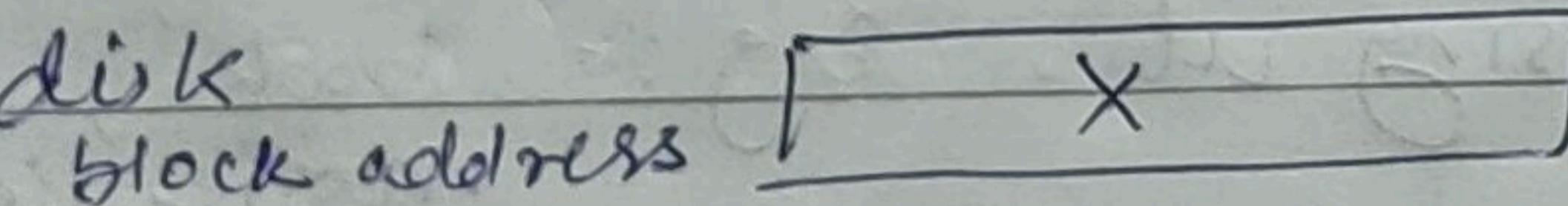
(2) `write-item(x)`

Writes the value of program variable 'x' into the data item named 'x'.

Executing a the `read-item(x)`

The command includes -

① Find out the disk block ^{address}, where the X resides



② Copy the disk block content into the main memory



③ Then copying the program variables to main memory



④ The ~~content~~ again stored to disk block (secondary) main memory.

Why concurrency control is needed?
E.g.: Flight Reservation System

There are two transactions 'T₁' and 'T₂'.

T₁

`read-item(x);`

$$x = X - N$$

`write-item(x);`

`read-item(y);`

$$y = Y + N$$

`write-item(y);`

T₂

`read-item(x);`

$$x = X + M$$

`write-item(x);`

X is the no. of reserved seats in the first flight.

Y is the no. of reserved seats in the second flight.

T₁ transfers N reservation from first flight to second flight.

T₂ reserves M seats in the second flight.

$$\begin{aligned} X &= 500 \\ Y &= 700 \\ N &= 100 \\ M &= 200 \end{aligned}$$

T_1

```
read-item(500);
X = 500 - 100
write-item(400);
read-item(700);
Y = 700 + 100
write-item(800);
```

T_2

```
read-item(400)
X = 400 + 200
write-item(600);
```

① The lost-update problem

The problem occurs when two transactions that access the same database have their operations interleaved in such a way that makes the value of some database items incorrect.

T_1

```
read-item(X);
X = X - N
```

T_2

```
read-item(X);
X = X + M
```

```
write-item(X);
read-item(Y);
```

$$\begin{aligned} Y &= Y + N \\ \text{write-item}(Y); \end{aligned}$$

write-item(X);

$$\begin{aligned} X &= 80 \\ N &= 5 \quad ; \quad M = 4 \\ Y &= 50 \end{aligned}$$

T_1

```
read-item(80);
X = 80 - 5
```

T_2

```
read-item(80);
X = 80 + 4
```

```
write-item(84);
read-item(50);
```

write-item(84);

```
Y = 50 + 5
write-item(55);
```

② Temporary update Problem (Dirty Read Problem)

This problem occurs when one transaction updates the database item and then fails.

Meanwhile, the update value is read by other transaction before it is changed back to its original value.

T_1 read-item(X);

$$X = X - N$$

write-item(X); T_2 read-item(X);

$$X = X + M$$

write-item(X);read-item(Y);

The transaction ' T_1 ' fails and must change
 the value of X back to its old value
 meanwhile ' T_2 ' reads the updated value of
 ' X '.

$$X = 80 ; N = 5 ; M = 4 ; Y = 50$$

 T_1

read-item(80);

$$X = 80 - 5$$

write-item(75);

 T_2

At this point of
 time, T_1 transaction
 fails

read-item(75);

$$X = \cancel{75} + 4$$

write-item(79);

read-item(50);