

貳零肆捌

組員：傅冠鈞 肖可依 陳柏豪

The 2048 Problem

- Data Structure

```
testGrid = [[['', 4, 32, 128], \
               ['', '', 128, 256], \
               ['', 4, 64, 2048], \
               [2, 16, 4, 4096]]
```

- Operations

- Up,Down,Right,Left

- Settings

- 2's probability = 0.9
- 4's probability = 0.1

	4	32	128
		128	256
	4	64	2048
2	16	4	4096

Evaluation Function

- emptyTiles()
- monotonicity() + smoothness() + emptyTiles()
- snake()

emptyTiles()

- emptyTiles() = 4

	4	32	128
		128	256
	4	64	2048
2	16	4	4096

mono()+smooth()+emptyTiles()

- $\text{mono}() = 37$

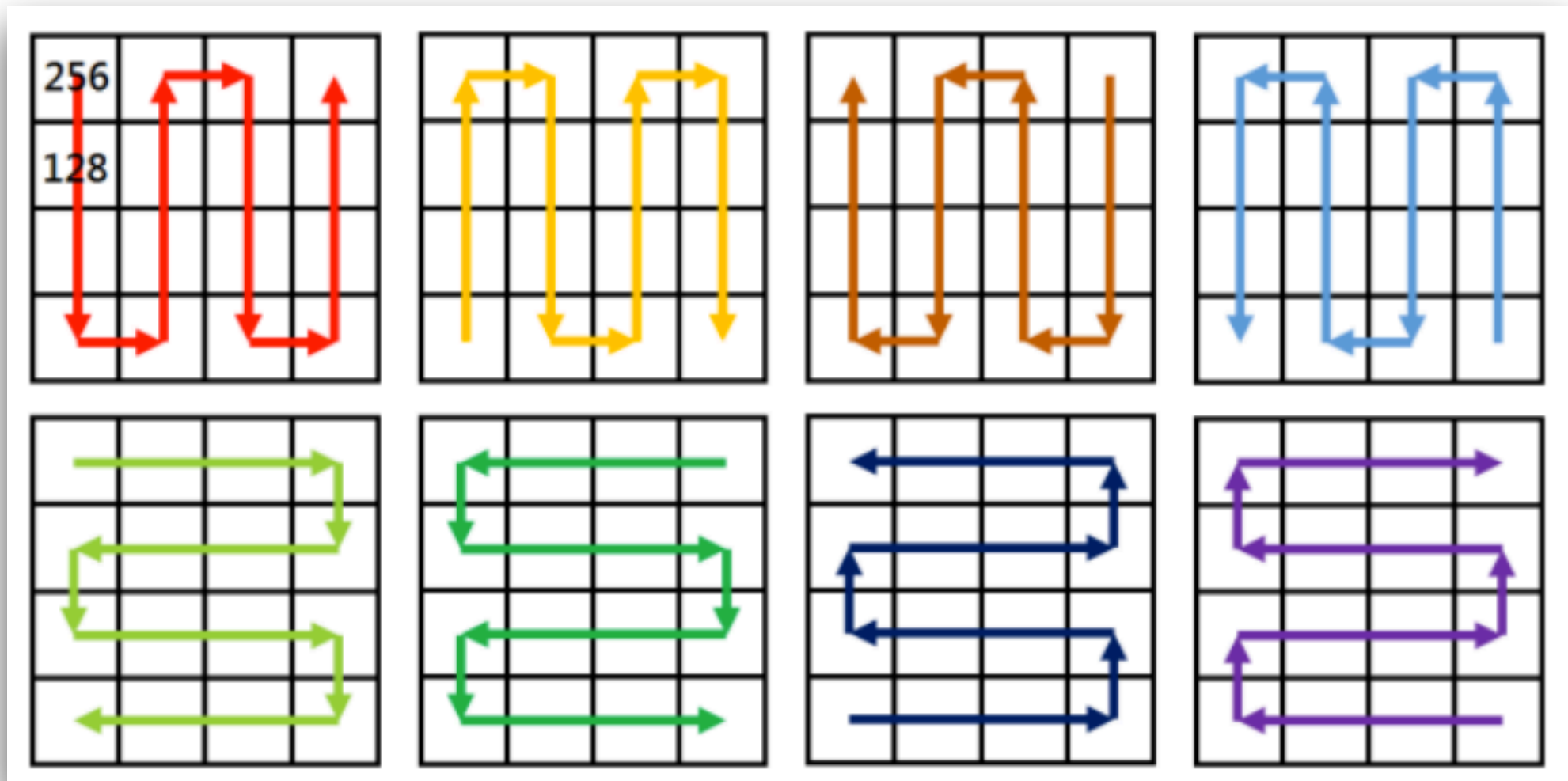
- $\text{smooth}() = 88$

- $\text{emptyTiles}() = 4$

	4	32	128
		128	256
	4	64	2048
2	16	4	4096

- $w1 * \text{emptyTiles}() + w2 * \text{smooth}() - w3 * \text{mono}()$

snake()



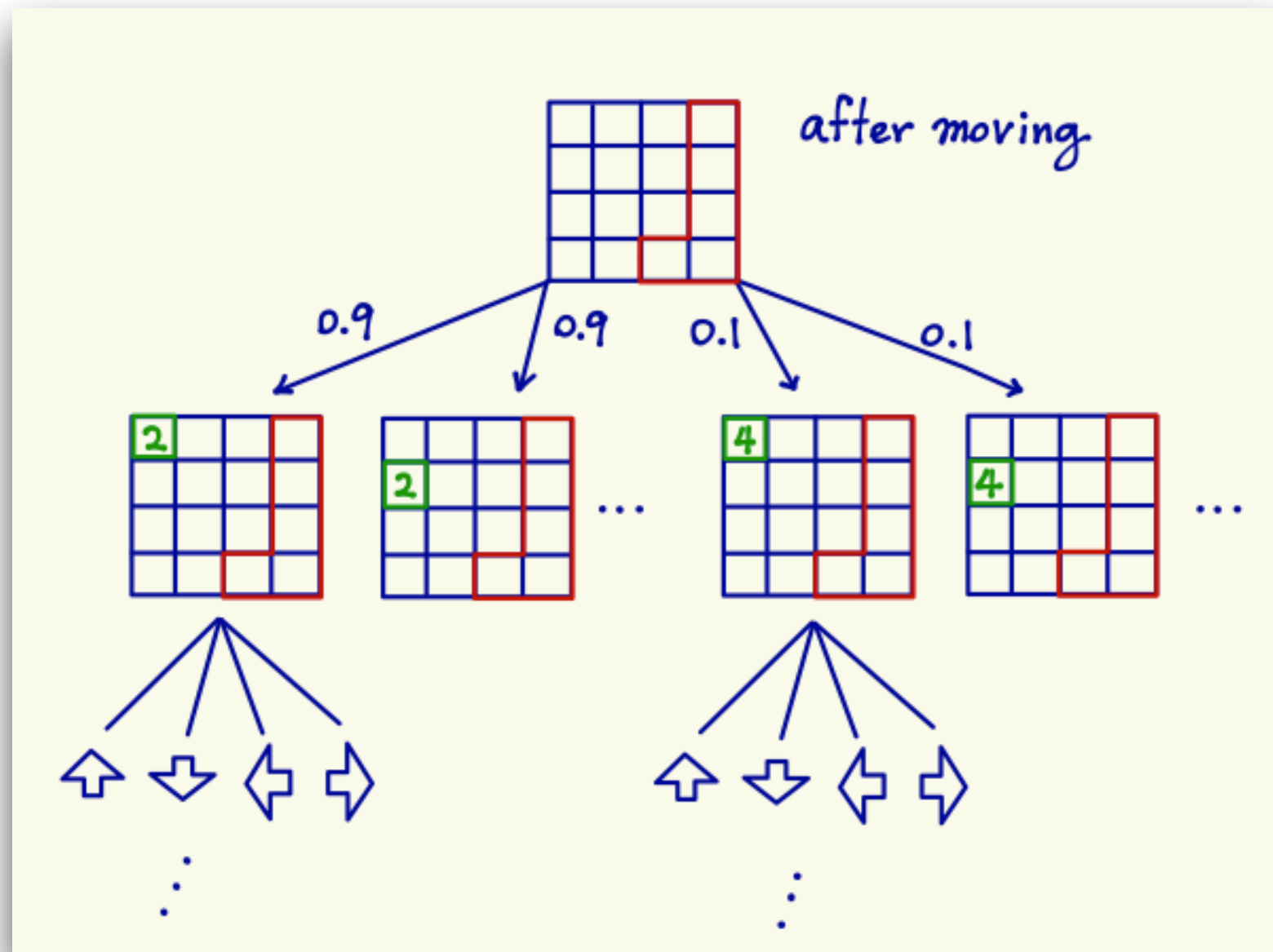
$$\text{score} = \sum \text{value}(\text{tile}(n)) * (r^n)$$

snake()

	4	32	128
		128	256
	4	64	2048
2	16	4	4096

$$\begin{aligned}\text{score} &= 4096 + 2048*r + 256*(r^2) + 128*(r^3) \\ &\quad + 32*(r^4) + 128*(r^5) + \dots = 6782\end{aligned}$$

Search Algorithm



`expectiminimax(grid,player,depth)`

Search Algorithm

```
def get_next_action(grid):  
    maxScore = 0  
    action = ''  
  
    if number_of_empty_cells > 3:  
        depth = 2  
    else:  
        depth = 4  
  
    for move in ['up', 'down', 'left', 'right']:  
        functions[move](grid)  
        score = expectiminimax(grid, 0, depth)  
  
        if score > maxScore:  
            maxScore = score  
            action = move  
  
    return action
```

get_next_action(grid)

Search Algorithm

```
def expectiminimax(grid, player, depth):  
    # check terminal condition  
    if depth == 0:  
        return evaluation_function(grid)  
  
    # computer's turn (consider all random conditions)  
    if player == 0:  
        alpha = 0  
  
        for x, y in get_empty_cells(grid):  
            grid[x][y] = 2  
            alpha = alpha + prob_2 * (1 / number_of_empty_cells) * expectiminimax(grid, 1, depth - 1)  
  
        for x, y in get_empty_cells(grid):  
            grid[x][y] = 4  
            alpha = alpha + prob_4 * (1 / number_of_empty_cells) * expectiminimax(grid, 1, depth - 1)  
  
    # AI's turn  
    elif player == 1:  
        alpha = 0  
  
        for move in ['up', 'down', 'left', 'right']:  
            functions[move](grid)  
            alpha = max(alpha, expectiminimax(grid, 0, depth - 1))  
  
    return alpha
```

expectiminimax(grid,player,depth)

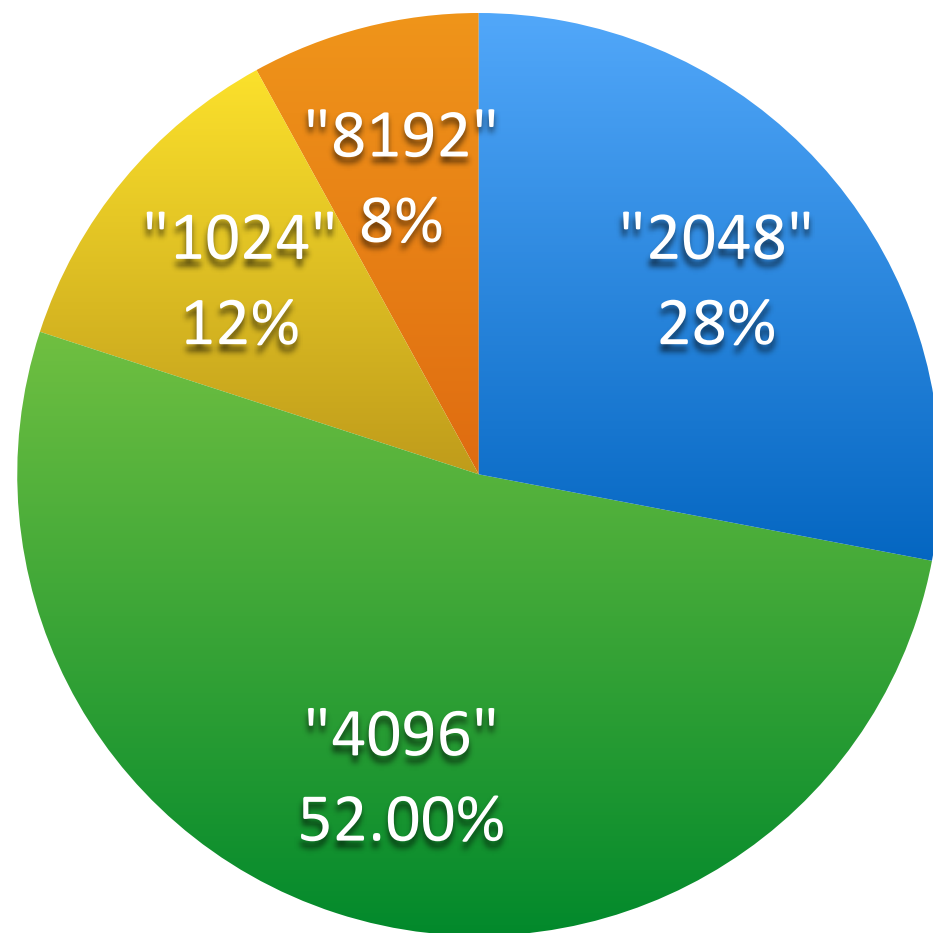
Demo

- `emptyTiles()` + `smooth()` with adaptive depth
- `snake()` with depth = 2
- `snake()` with adaptive depth (video)

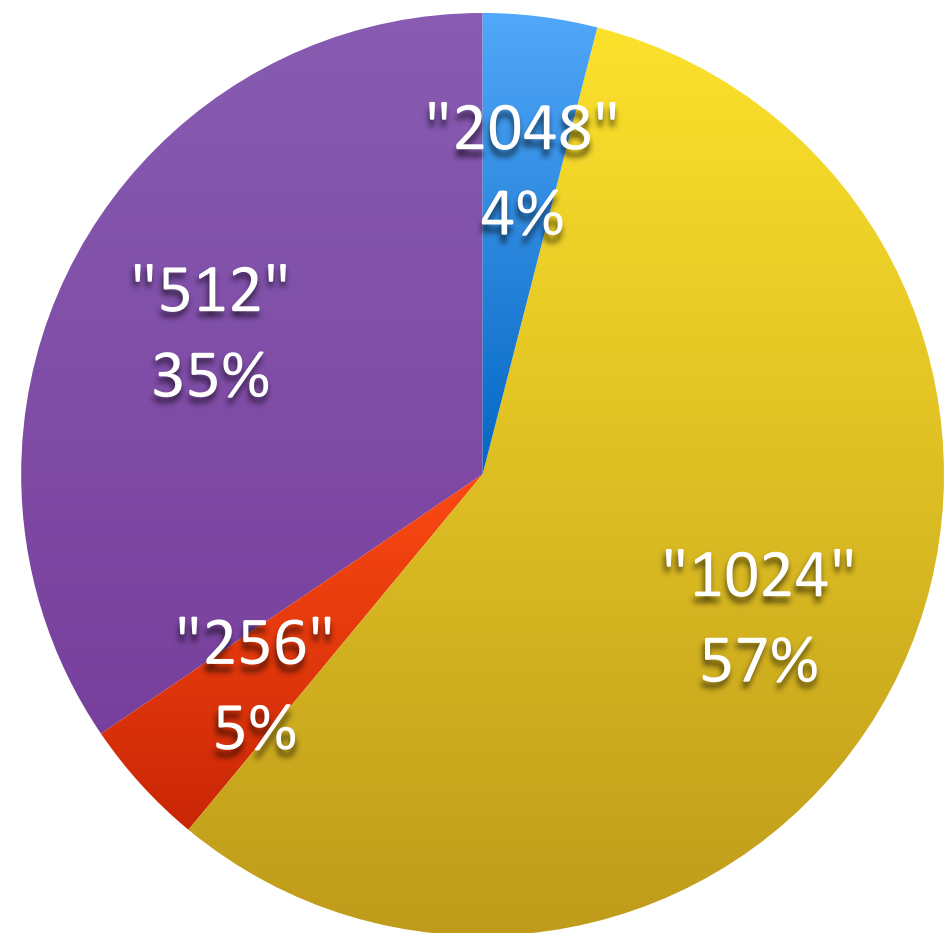
Results

- The max grid probability

snake()



emptyTiles() + smooth()



What else can be done?

- Speed up and deepen the depth by
 - encoding the grid
 - pruning

Q&A

Thanks for your attention!