

nth fibonacci number is given by:

$$f_n = f_{n-1} + f_{n-2}$$

Similarly (n+1)th fibonacci number is given by:

$$f_{n+1} = f_n + f_{n-1}$$

The first fibonacci number is 1

The second fibonacci number is 2

Third fibonacci numbe	1	+	2	=	3
	an odd number		+ an even number	=	an odd number
Fourth fibonacci number:	2	+	3	=	5
	an even number		+ an odd number	=	an odd number
Fifth fibonacci number:	3	+	5	=	8
	an odd number		+ an odd number	=	an even number

From observation, we can see that every third fibonacci number is an even number.

Let  $f_{n-2} = a(\text{odd})$  AND  $f_{n-1} = b(\text{even})$

$$f_n = f_{n-1} + f_{n-2} = a + b$$

$$f_{n+1} = f_n + f_{n-1} = a + b + b = a + 2b$$

$$f_{n+2} = f_{n+1} + f_n = a + 2b + a + b = 2a + 3b$$

Again, from observation, we can see that if  $f_{n-2} = a(\text{odd})$  AND  $f_{n-1} = b(\text{even})$ ,  
then  $f_{n+1} = a + 2b(\text{odd})$  AND  $f_{n+2} = 2a + 3b(\text{even})$

Thus, we can calculate fibonacci numbers until  $b(\text{even}) \leq 4\,000\,000$ ,  
adding b to sum on every iteration