

About Option pricing

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Author	Message
stabiloboss New poster Post Number: 5	<p>Posted on Monday, 30 April, 2007 - 02:14 pm:</p> <hr/> <p>Can anyone kindly give me a guidance or help me solve in relation to the derivation of the delta(first derivate) and gamma second derivate) of digital (binary) call option?</p> <p>Pre-condition: Strike K, Maturity T, pays \$1 if S(T) greater and equal to K, and worthless if S(T)<K,</p> <p>where, Digital call(t)= $e^{-r(T-t)}N(d_2)$.....(equation 1) $d_2=d_1-STD*\sqrt{T-t}$.....(equation 2)</p> <p>Prove: Delta= $e^{-r(T-t)}N'(d_2)/STD*S(t)*\sqrt{T-t}$ Gamma- $e^{-r(T-t)}d_1*N'(d_2)/STD^2*S(t)$</p> <p>many thanks</p>
stabiloboss Poster Post Number: 6	<p>Posted on Monday, 30 April, 2007 - 04:29 pm:</p> <hr/> <p>For the above question, i forgot to add one more condition: Given: $d_1= 1/STD*\sqrt{T-t}*[ln(S(t)/k)+(r+1/2*STD^2)(T-t)]$</p> <p>Also, the Gamma should be : Gamma= $-e^{-r(T-t)}d_1*N'(d_2)/STD^2*S(t)^2(T-t)$</p> <p>Below is my attempt answer for Delta:</p> <p>STEP 1 Take Derivative of d_2 with respect to S(t)</p> <p>$d/dS(t)(d_2)=d/dS(t)1n S(t)/STD*\sqrt{T-t}=1/S(t)*STD*\sqrt{T-t}$</p> <p>STEP 2: Apply chain rule to equation (1)</p> <p>$e^{-r(T-t)}N'(d_2) d/dS(t)(d_2)= e^{-r(T-t)}N'(d_2)/STD*S(t)*\sqrt{T-t}$</p> <p>I have already give it a try for Gamma using quotient rule, however, i was not able to reach the answer as requested, could please someone help me?</p> <p>thanks a lot</p>
Andre Rzym Veteran poster Post Number: 1540	<p>Posted on Monday, 30 April, 2007 - 08:31 pm:</p> <hr/> <p>I haven't checked whether the result to be proved is actually correct, but I would start by thinking about $N'(d_2)$. Recall that $N(x)$ is an integral with an upper limit of x. What, therefore, is $N'(x)$?</p> <p>Writing this out explicitly in the expression for delta, then differentiating the lot with respect to S should get you there.</p>

If not, post your workings (and have a look at the formatting page in the instructions link below).

Andre

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