```
In[1]:= cnd[z_] := (1 + Erf[z / Sqrt[2]]) / 2;
         d1[V0_{-}, K_{-}, T_{-}, r_{-}, \sigma_{-}] := \frac{\left(Log\left[\frac{V0}{K}\right] + \left(r + \frac{\sigma^{2}}{2}\right)T\right)}{\sigma^{2}\sqrt{T}};
         {\tt d2[V0\_,\,K\_,\,T\_,\,r\_,\,\sigma\_]} := {\tt d1[V0,\,K,\,T,\,r,\,\sigma]} - \sigma\,\sqrt{{\tt T}}\;;
 \ln[4] = \text{BSCall}[V0_, K_, T_, r_, \sigma_] := V0 \text{ end}[d1[V0, K, T, r, \sigma]] - K \text{Exp}[-r T] \text{ end}[d2[V0, K, T, r, \sigma]]
 In[5]:= BSCall[100, 100, 1, 0.05, 0.20]
Out[5] = 10.4506
 \ln[6] = Adl[AO_, D_, T_, r_, \sigma_] := \frac{\left(Log\left(\frac{AO}{D}\right) + \left(r + \frac{\sigma^2}{2}\right)T\right)}{\sigma \sqrt{T}};
 _{\text{ln[7]:=}} Ad2[A0_, D_, T_, r_, \sigma_] := Ad1[A0, D, T, r, \sigma] - \sigma \sqrt{\text{T}};
  ln[8]:= EquityMerton[A0_, D_, T_, r_, \sigma_] :=
           A0 cnd [Ad1 [A0, D, T, r, \sigma]] - D Exp[-rT] cnd [Ad2 [A0, D, T, r, \sigma]]
 In[9]:= EquityMerton[100, 70, 4, 0.05, 0.20]
Out[9]= 43.8038
In[10]:= Ad1[100, 70, 4, 0.05, 0.20]
Out[10]= 1.59169
ln[11]:= Ad2[100, 70, 4, 0.05, 0.20]
Out[11]= 1.19169
In[12]:= cnd[Ad1[100, 70, 4, 0.05, 0.20]]
Out[12]= 0.944273
In[13]:= cnd[Ad2[100, 70, 4, 0.05, 0.20]]
Out[13]= 0.883308
\texttt{D} \texttt{Exp}[-\texttt{r}\,\texttt{T}] - (\texttt{D}\,\texttt{Exp}[-\texttt{r}\,\texttt{T}]\,\texttt{cnd}\,[-\texttt{Ad2}[\texttt{A0}\,,\,\texttt{D}\,,\,\texttt{T}\,,\,\texttt{r}\,,\,\sigma]\,] - \texttt{A0}\,\texttt{cnd}\,[-\texttt{Ad1}[\texttt{A0}\,,\,\texttt{D}\,,\,\texttt{T}\,,\,\texttt{r}\,,\,\sigma]\,])
In[15]:= cnd[-Ad1[100, 70, 4, 0.05, 0.20]]
Out[15]= 0.0557275
In[16]:= cnd[-Ad2[100, 70, 4, 0.05, 0.20]]
Out[16]= 0.116692
In[17]:= DebtMerton[100, 70, 4, 0.05, 0.20]
Out[17]= 56.1962
```

In[18]:= 100 - DebtMerton[100, 70, 4, 0.05, 0.20]

Out[18]= 43.8038

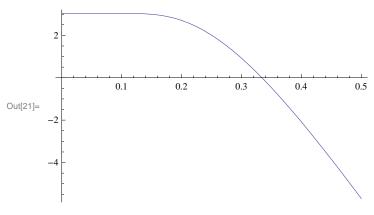
$$\ln[19] = \text{fmin}[\sigma \text{imp}] := 50 \text{ Exp}[-0.03 * 5] - \left[ 50 \text{ Exp}[-0.03 * 5] \text{ cnd} \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \left[ -\frac{\left(\text{Log}\left[\frac{100}{50}\right] + \left(0.03 + \frac{\sigma \text{imp}^2}{2}\right) 5\right)}{\sigma \text{imp} \sqrt{5}} + \sigma \text{imp} \sqrt{5} \right] - \sigma \text{imp} \sqrt{5} + \sigma \text{imp} \sqrt{5} \right] - \sigma \text{imp} \sqrt{5} + \sigma \text{imp$$

$$100 \operatorname{cnd} \left[ -\frac{\left( \operatorname{Log} \left[ \frac{100}{50} \right] + \left( 0.03 + \frac{\operatorname{\sigma imp}^2}{2} \right) 5 \right)}{\operatorname{\sigma imp} \sqrt{5}} \right] - 40$$

In[20]:= **fim[1]** 

Out[20]= fim[1]

ln[21]:= Plot[fmin[ $\sigma$ imp], { $\sigma$ imp, 0, 0.5}]



In[22]:= Ad1[100, 30, 5, 0.03, 0.334]

Out[22]= 2.18634

In[23]:= Ad2[100, 30, 5, 0.03, 0.334]

Out[23] = 1.4395

In[24]:= DebtMerton[100, 30, 5, 0.03, 0.334]

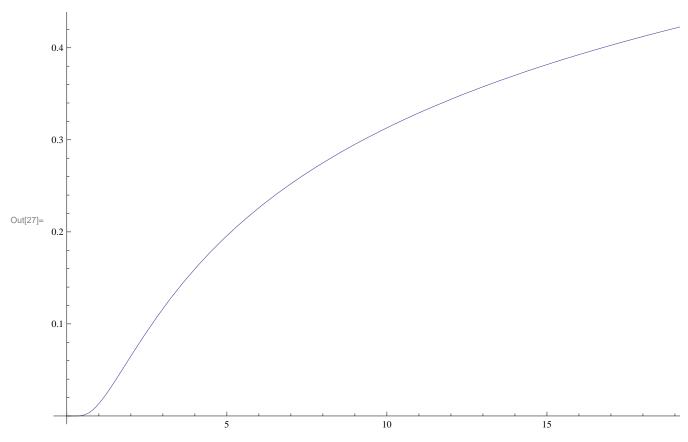
Out[24] = 25.324

ln[25]:= MertonProb[A0\_, D\_, T\_, r\_,  $\sigma_{-}$ ] := 1 - cnd[Ad2[A0, D, T, r,  $\sigma_{-}$ ]]

In[26]:= MertonProb[100, 30, 5, 0.03, 0.334]

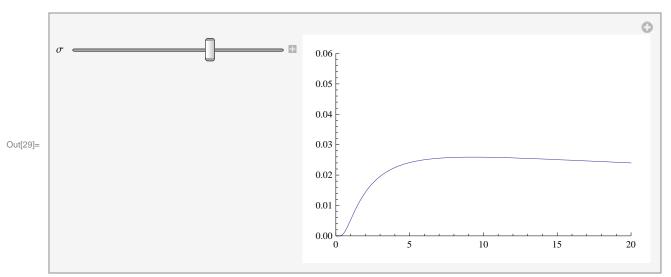
Out[26]= 0.075005

In[27]:= Plot[MertonProb[100, 40, T, 0.05, 0.40], {T, 0, 20}]

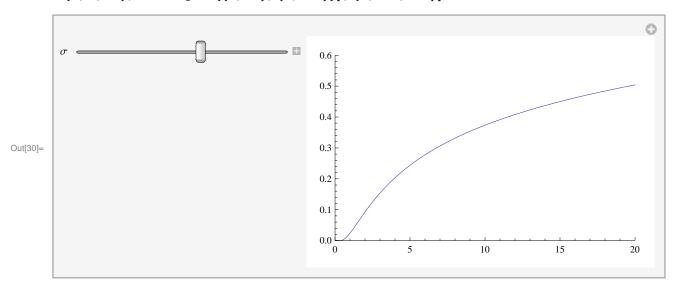


| In[28]:= MertonSpread[A0\_, D\_, T\_, r\_, σ\_] := -\frac{1}{T} Log[\frac{DebtMerton[A0, D, T, r, σ]}{D}

 $_{\text{ln[29]:=}}$  Manipulate[Plot[MertonSpread[100, 40, T, 0.05,  $\sigma]$ ,  $\{T, 0, 20\}, PlotRange \rightarrow \{\{0, 20\}, \{0, 0.06\}\}], \{\sigma, 0.2, 0.6\}]$ 



$$\begin{split} & \ln[30] := & \text{Manipulate[Plot[MertonProb[100, 40, T, 0.05, \sigma],} \\ & \qquad \qquad \left\{ \text{T, 0, 20} \right\}, & \text{PlotRange} \rightarrow \left\{ \left\{ 0, 20 \right\}, \left\{ 0, 0.6 \right\} \right], \left\{ \sigma, 0.2, 0.6 \right\} \right] \end{split}$$



 $\label{eq:loss_loss} $$ \ln[31] := $$ Plot3D[MertonSpread[100, 40, T, 0.05, \sigma], \{T, 0, 20\}, \{\sigma, 0, 0.30\}] $$ $$ $$ \end{tabular} $$$ \end{tabular} $$$ \end{tabular} $$$ \end{ta$ 

