

CQF 2009
Module 4.3
Live Lecture: April 6, 2009
Lecturer: Paul Wilmott

Calibration and Data Analysis

In this lecture:

- The theoretical yield curve and the market yield curve, should they be the same?
- How calibration works, the pros and cons
- How to analyze short-term interest rates to determine the best model
- How to analyze the slope of the yield curve to get information about the market price of interest rate risk

By the end of this lecture, you will:

- Know the meaning of ‘calibration’
- Appreciate the pros and cons of calibration
- Be able to analyze data to find a good model

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|---|----|
| Introduction..... | 3 |
| Calibration..... | 7 |
| Ho & Lee..... | 8 |
| Working forward and an inverse problem | 10 |
| Notes – knowing $\eta(t)$, can price other instruments..... | 15 |
| Another calibrated model – Extended Vasicek model of Hull & White | 16 |
| Back to Ho & Lee: Calibration in practice | 21 |
| Yield-curve fitting: For | 33 |
| Against | 34 |
| Data analysis to find the ‘best’ model..... | 36 |
| Popular one-factor spot-rate models | 37 |
| The method | 40 |
| The volatility structure | 44 |
| The drift structure | 54 |
| Advantages of working with the PDF to find the drift function | 60 |
| The slope of the yield curve and the market price of risk..... | 61 |
| The relationship between forward rates and the real spot rate..... | 72 |

Summary

- Spot interest rate models are usually calibrated to match market data, in particular the forward curve
- This calibration is in practice always inconsistent
- There are simple methods for examining interest rate data to find good models