# The new version of $DuMu^x$ including the modules "CRootBox" and "dumux-rosi"

**Documentation** 

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### Installation

This installation guidelines are for the new version of  $DuMu^x$ , version 3, coupled with CRootBox, in Linux systems (e.g. Ubuntu).

### Required compilers and tools

If on a recent Ubuntu system, the c++ compiler and python that come with the distribution are recent enough. Otherwise, please make sure you have a recent c++ compiler (e.g. sudo apt-get install clang), fortran compiler (sudo apt-get install gfortran) and python3 (e.g. sudo apt-get install python3.7).

```
- Install git:
```

sudo apt-get install git

- Install cmake:

sudo apt-get install cmake

- Install libboost:

sudo apt-get install libboost-all-dev

- Install pip:

sudo apt-get install python3-pip

- Install the python package numpy:

pip3 install numpy

- Install the python package scipy:

pip3 install scipy

- Install the python package matplotlib:

pip3 install matplotlib<sup>1</sup>

- Install the python package VTK:

alug pip3 install vtk

- Install the java runtime environment:

sudo apt-get install default-jre

- Install Paraview

sudo apt-get install paraview

<sup>&</sup>lt;sup>1</sup>Known bug in ubuntu 18.04: needs sudo apt-get install libfreetype6-dev libxft-dev installed before.

### DuMu<sup>x</sup> installation

```
In all dune modules we stay in version 2.6, the latest stable release version.
- Create a DuMu<sup>x</sup> working folder
mkdir DUMUX
cd DUMUX
- Download DUNE core modules:
git clone https://gitlab.dune-project.org/core/dune-common.git
cd dune-common
git checkout releases/2.6
git clone https://gitlab.dune-project.org/core/dune-geometry.git
cd dune-geometry
git checkout releases/2.6
git clone https://gitlab.dune-project.org/core/dune-grid.git
cd dune-grid
git checkout releases/2.6
cd ..
git clone https://gitlab.dune-project.org/core/dune-istl.git
cd dune-istl
git checkout releases/2.6
cd ..
git clone https://gitlab.dune-project.org/core/dune-localfunctions.git
cd dune-localfunctions
git checkout releases/2.6
- Download DUNE external modules:
git clone https://gitlab.dune-project.org/extensions/dune-foamgrid.git
cd dune-foamgrid
git checkout releases/2.6
cd ..
git clone https://gitlab.dune-project.org/extensions/dune-grid-glue.git
cd dune-grid-glue
git checkout master<sup>2</sup>
git clone https://github.com/dune-community/dune-pybindxi.git
cd dune-pybindxi
git checkout master
cd ..
```

<sup>&</sup>lt;sup>2</sup>There is no release 2.6

```
If the file 'mpicommunication.hh" in the folder dune-common/dune/common/parallel
is not downloaded automatically during cloning, create a file 'mpicommunication.hh"
in the folder and copy the code from: https://www.dune-project.org/doxygen/master/mpicommun
-Download dumux and dumux-rosi and the grid manageres alugrid, uggrid and
spgrid:
git clone https://git.iws.uni-stuttgart.de/dumux-repositories/dumux.git
cd dumux
git checkout releases/3.0
git clone https://github.com/Plant-Root-Soil-Interactions-Modelling/dumux-
rosi.git
cd dumux-rosi
git checkout master
git clone https://gitlab.dune-project.org/extensions/dune-alugrid.git
cd dune-alugrid
git checkout releases/2.6
git clone https://gitlab.dune-project.org/staging/dune-uggrid
cd dune-uggrid
git checkout releases/2.6
cd ..
git clone https://gitlab.dune-project.org/extensions/dune-spgrid
cd dune-spgrid
git checkout releases/2.6
cd ..
-Download CRootBox (only needed if root growth is used):
git clone https://github.com/Plant-Root-Soil-Interactions-Modelling/CRootBox.git
cd CRootBox
git checkout master
cd ..
To build CRootBox and its python shared library, move again into the CRootBox
folder and type into the console:
cd CRootBox
cmake .3
make
(If building CRootBox on the cluster, two lines in the file CRootBox/CMakeLists
.txt need to be outcommented before:
set(CMAKE_C_COMPILER "/usr/bin/gcc")
```

<sup>&</sup>lt;sup>3</sup>It may be necessary on your installation to check the CRootBox/src/CMakeLists.txt file regarding required python version and out-commenting line 34.

```
set(CMAKE_CXX_COMPILER "/usr/bin/g++"))
```

Now add the systems path of CPlantBox to your Python scripts so they can find the python shared library of CPlantBox. Alternatively, copy the shared library (a file with a name similar to "plantbox.cpython-38-x86 $_64-linux-gnu.so$ )tothefolder"/dumux-rosi/rosi\_benchmarking/python\_solver/solvers")\\ Now build DuMu^x with the CRootBox module:

-The configuration file cmake.opts is stored in the dumux folder. Move a copy of this file to your  $DuMu^x$  working folder (one level up, DUMUX)

- To build all downloaded modules and check whether all dependencies and prerequisites are met, run dunecontrol:

./dune-common/bin/dunecontrol --opts=cmake.opts all

Installation done! Good luck!

### Running an example

```
cd dumux-rosi/build-cmake/rosi_benchmarking/soil
make richards1d  # outcomment if executable is already available
./richards1d /input/b1a_1d.input  # run executable with specific input
parameter file
```

### Installing and running an example on the agrocluster

- Before installing or running  $\operatorname{DuMu}^x$  on the agrocluster, it is required to type the command module load dumux into the console. This sets the compiler versions and other tools to more recent versions than the standard versions of the agrocluster.
- On the cluster, another onfiguration file  $optim_cluster.opts$  is used. Copy this file to the file to your  $DuMu^x$  working folder (one level up).
- To build or run an example on the agrocluster, create a pbs file in your working folder that will put your job in the cluster queue
  For example queue\_my\_job.pbs

```
#!/bin/sh
#
#These commands set up the Grid Environment for your job:
#PBS -N DUMUX
#PBS -l nodes=1:ppn=1,walltime=200:00:00,pvmem=200gb
#PBS -q batch\\
```

```
#PBS -M a.schnepf@fz-juelich.de

#PBS -m abe

module load dumux

cd \$HOME/DUMUX/dumux-rosi/build-cmake/rosi_benchmarking/soil

make richards
./richards input/b1a.input
```

To start the job, run this file in your working folder with the command qsub queue\_my\_job.pbs

Use Filezilla to move the results to your local machine and use Paraview to visualize them.

If you need to install additional python packages (e.g. scipy) on the cluster (without root access), you may do so by using the --user command: pip3 install --user scipy

### Numerical grids

We distinguish two types of numerical grids: the 3D soil grid and the 1D, branched, root system grid (see Fig. 1).

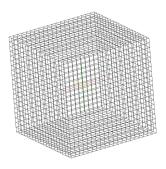




Figure 1: The 3D soil grid and the 1D, branched, grid representing the root architecture

In the example of the coupled problems, both are used simultaneously. In that case, the two grids are merged via source/sink terms in positions where root and soil grids share the same spatial coordinates. This is illustrated in Fig. 2; detailed descriptions can be found in the individual examples.

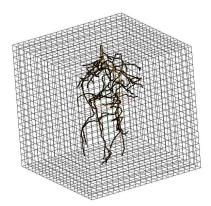


Figure 2: 3D soil grid merged with the 1D, branched, grid representing the root architecture

Grids can be created using different DUNE internal or external grid managers (see documentation of dune-grid). In the input file, the details about the numerical grids are specified in the groups [RootSystem.Grid] or [Soil.Grid].

Each folder contains a folder named ``grids" where grids can be provided in dgf format. In the dumux-rosi examples, the soil grid is usually a structured grid created by the default ``GridCreator", where corner points of the domain, spatial resolution and cell type are specified such as in the following example:

```
[ Grid ]
LowerLeft = 0 0 0
UpperRight = 1 1 1
Cells = 10 10 20
CellType = Cube # or Simplex
```

Alternatively, msh-files can be read.

### Choice of grid manager for the soil domain

YaspGrid: Structured grids, only non-periodic soil domains

SpGrid: Structured grids, also periodic soil domains

AluGrid: Unstructured grids, only works for  $CC_2pfa-scheme$ 

 ${\tt UGGrid}: Unstructured grids, works for both$ 

To change the grid manager, open the file dumux-rosi/rosi\_benchmarking/coupled\_1p\_richards /CMakeLists.txt. If not available, add the following lines to make the gridmanager available to build an executable. For the example of UGGrid:

```
add_executable(coupledUG EXCLUDE_FROM_ALL coupled.cc)
target compile definitions(coupledUG PUBLIC DGF GRIDTYPE=Dune:: UGrid<3>)
```

### **Grids for root systems**

There are two options to specify the root system grid. The first option is to specify it as a file in dgf-format that specifies the coordinates and connection of nodes (verteces).

```
DGF
Vertex
0 0 0 -0.03
-0.003301 -0.000687124 -0.0394144
-0.00339314 -0.00159054 -0.0473627
-0.00590116 -0.00546716 -0.0538958
-0.0115931 -0.00454388 -0.059441
-0.0105464 -0.00572357 -0.067284
-0.0100044 -0.0069212 -0.0751753
-0.00923561 -0.00814568 -0.0830435
-0.0100507 -0.00678732 -0.0908851
-0.010965 -0.00608665 -0.0962792
-0.00103059 0.000281757 -0.0413509
```

```
14 0.00284233 0.00172545 -0.0449409
15 0.00619859 0.00411514 -0.0466909
  -6.51815e-05 0.00081926 -0.041154
0.000989275 0.00146981 -0.0404847
18 -0.00013962 0.00162442 -0.0411274
19 -0.00376417 0.00152097 -0.0477906
  -0.00509243 0.00809897 -0.0472907
20
  -0.00667036 0.0130109 -0.0453872
22 -0.00784569 0.0163412 -0.0446723
23 -0.00343402 0.00160078 -0.048867
  -0.00272936 0.00153492 -0.0511603
25 -0.00257298 0.00150318 -0.0517729
26 -0.00605319 0.00128567 -0.051235
27 -0.00509341 0.00874088 -0.0479026
  -0.0051018 0.00890818 -0.0480774
  -0.0105648 -0.00490006 -0.0536398
29
30 -0.0155357 -0.00427108 -0.0535009
31 -0.0187161 -0.00393935 -0.0540514
32 -0.0129246 -0.00794987 -0.0599204
  -0.0158011 -0.0137093 -0.0604436
33
34 -0.0159531 -0.0140359 -0.0604843
35 -0.0103269 -0.00178528 -0.069703
36 -0.0097869 0.000348939 -0.071026
  -0.0101116 -0.00387942 -0.0769314
38 -0.00866863 -0.0079157 -0.0834016
39 #
40 SIMPLEX
  parameters 10 # id0, id1, order, branchId, surf[cm2], length[cm], radius[
     cm], kz[cm4 hPa-1 d-1], kr[cm hPa-1 d-1], emergence time [d], subType,
      organType
42 0 1 0 1 0.314159 1 0.05 0 0 0.253641 1 2
43 1 2 0 1 0.251327 0.8 0.05 0 0 0.461984 1 2
  2 3 0 1 0.251327 0.8 0.05 0 0 0.675409 1 2
45 3 4 0 1 0.251327 0.8 0.05 0 0 0.894171 1 2
46 4 5 0 1 0.251327 0.8 0.05 0 0 1.11854 1 2
47 5 6 0 1 0.251327 0.8 0.05 0 0 1.34882 1 2
48 6 7 0 1 0.251327 0.8 0.05 0 0 1.58532 1 2
49 7 8 0 1 0.251327 0.8 0.05 0 0 1.82839 1 2
50 8 9 0 1 0.17328 0.551569 0.05 0 0 2 1 2
51 1 10 1 2 0.0591391 0.313743 0.03 0 0 0.81929 2 2
52 10 11 1 2 0.103194 0.547463 0.03 0 0 1.36938 2 2
53 11 12 1 2 0.084377 0.447634 0.03 0 0 2 2 2
54 10 13 2 3 0.0141039 0.112236 0.02 0 0 1.88447 3 2
55 13 14 2 3 0.0176961 0.140821 0.02 0 0 2 3 2
56 13 15 3 4 0.0101666 0.080903 0.02 0 0 2 4 2
57 2 16 1 8 0.0596143 0.316264 0.03 0 0 0.976223 2 2
58 16 17 1 8 0.126845 0.672936 0.03 0 0 1.39819 2 2
59 17 18 1 8 0.103656 0.549912 0.03 0 0 1.75726 2 2
60 18 19 1 8 0.0679195 0.360324 0.03 0 0 2 2 2
61 16 20 2 9 0.0141835 0.112869 0.02 0 0 1.55953 3 2
```

```
62 20 21 2 9 0.0301593 0.24 0.02 0 0 1.81594 3 2
63 21 22 2 9 0.00795504 0.0633042 0.02 0 0 2 3 2
64 20 23 3 10 0.0445473 0.354496 0.02 0 0 2 4 2
65 17 24 2 12 0.0111449 0.088688 0.02 0 0 1.98626 3 2
66 24 25 2 12 0.00304236 0.0242104 0.02 0 0 2 3 2
67 3 26 1 16 0.088687 0.470499 0.03 0 0 1.35817 2 2
68 26 27 1 16 0.0944815 0.50124 0.03 0 0 1.74414 2 2
69 27 28 1 16 0.0611608 0.324468 0.03 0 0 2 2 2
70 4 29 1 19 0.0695225 0.368828 0.03 0 0 1.49515 2 2
71 29 30 1 19 0.121751 0.645908 0.03 0 0 1.97249 2 2
72 30 31 1 19 0.00683211 0.0362455 0.03 0 0 2 2 2
73 5 32 1 22 0.0872183 0.462707 0.03 0 0 1.79818 2 2
74 32 33 1 22 0.0484141 0.256845 0.03 0 0 2 2 2
75 6 34 1 24 0.0662369 0.351397 0.03 0 0 2 2 2
76 7 35 1 25 0.0133627 0.0708913 0.03 0 0 2 2 2
78 BOUNDARYDOMAIN
79 default 1
```

The paragraph ``SIMPLEX" specifies 10 parameters for each root segment: node1ID, node2ID, order, branchID, surfaceIdx in cm $^2$ , length in cm , radiusIdx in cm, axialCondIdx cm $^4$  hPa $^{-1}$  d $^{-1}$ , radialCondIdx cm hPa $^{-1}$  d $^{-1}$ , emergenceTimeId $^4$  Order numbering starts with 0, i.e., primary roots have order 0. Potential artificial shoot segements have order  $^{-1}$ .

Root systems in dgf format can be computed from measured root systems as well as with the root architecture module of CPlantBox.

The second option is to provide the root architectural parameters in the input file such that the root architecture and related grid is computed by  $\mathsf{CRootBox}$  while used as a  $\mathsf{DuMu}^x$  module.

```
[RootSystem.Grid]

File = Triticum_aestivum_a_Bingham_2011

InitialT = 10 # days
```

Important to know: It is currently necessary to build the code either for option 1 or for option 2 (i.e., two executables can be built that need to be provided with the correct input at runtime).

<sup>&</sup>lt;sup>4</sup>Note: in the code we often use the term '´creation time", however, we always mean '´emergence time". Branch nodes exist twice, once in the mother branch, once as the starting node of the daughter branch. They have different emergence times but the same nodeID.

### **Numerical schemes**

### Numercical schemes available in DuMu<sup>x</sup>

#### **Box Method**

 $CC_2pfaMethod$ 

### How to switch numerical scheme in a $DuMu^x$ simulation

```
Open the main file of your application. For coupled root-soil problems, it is for example the file coupled.cc.

Change the line that specifies the numerical scheme for the soil subproblem: using SoilTypeTag = Properties::TTag::RichardsBox;

or using SoilTypeTag = Properties::TTag::RichardsCC;

Change the line that specifies the numerical scheme for the root subproblem: using RootTypeTag = Properties::TTag::RootsCCTpfa;

or using RootTypeTag = Properties::TTag::RootsBox;
```

Make sure that the relevant properties file is given (line 62 in coupled.cc).

### Python for pre- and postprocessing

We created a python layer around CRootBox and dumux-rosi for pre- and postprocessing such that the model can be run without handling the C++ code once an executable is available.

For that, each example folder contains a folder named ''python`` that includes several examples as well a folder that includes the corresponding input files.

### The pre-processing

Here, the path to the executable and corresponding input files is provided and the simulation is started, like in this example:

```
# go to the right place
path = os.path.dirname(os.path.realpath(__file__))
os.chdir(path)
os.chdir("../../build-cmake/rosi_benchmarking/soil")

# run dumux
os.system("./richards1d soil_richards/input/b1a_1d.input")
```

### The input file

Here is an example of an input file, /dumux-rosi/rosi\_benchmarking/soil/benchmarks\_1d/b1a.input:

```
[Problem]
Name = benchmark1d_1a

[TimeLoop]
Tend = 3153600 # 0 is steady state
DtInitial = 1 # [s]
MaxTimeStepSize = 864000 # 10 days [s]

[Soil.Grid]
UpperRight = 0
LowerLeft = -2
Cells = 199

[Soil.BC.Top]
Type = 2 # constant flux
```

```
Value = 0.5 \# [cm/d]
  [Soil.BC.Bot]
18
19 Type = 5 # free drainage
21 [Soil.IC]
P = -200 # cm pressure head (initial guess)
23
[Soil. VanGenuchten]
25 # Loam over sand
Qr = 0.08 \quad 0.045
Qs = 0.43 \ 0.43
28 Alpha = 0.04 	 0.15 	 \# [1/cm]
_{29} N = 1.6 3
_{30} Ks = 50 1000 # [cm/d]
32 [Soil.Layer]
Z = -2 -0.5 -0.5 0
34 Number = 2 2 1 1
```

Listing 1: Example input file

### The post-processing

3D simulation results are stored in form of vtk files. If not specified otherwise, vtk files are stored for the initial and the final time point of the simulation. Using the key word `CheckTimes" under the category `Time loop" in the input file, additional output times can be specified. Time series, such as transpiration flux or pressure at the root collar over time, are stored as txt files. At the moment, this is specified within the problem file of the C++ code, see for example

/dumux-rosi/rosi\_benchmarking/roots\_1p/rootsproblem.hh:

```
//! calculates transpiraton, as the sum of radial fluxes (slow but accurate) [cm^3/day]
```

Listing 2: Transpiration output

and

```
//! if true, sets bc to Dirichlet at criticalCollarPressure (false per default)
```

Listing 3: Transpiration output

Here, results are read and plotted or further analysed, like in the following example. Using the vtk\_tools is particularly helpful for creating 1D plots

such as depth profiles or time series in Python rather than using Paraview (Paraview of course is helpful for 3D visualisation).

```
# Figure 2a
s_, p_, z1_ = read1D_vtp_data("benchmark1d_1a-00001.vtp", False)
h1_ = vg.pa2head(p_)
ax1.plot(h1_, z1_ * 100, "r+")

np.savetxt("dumux1d_b1", np.vstack((z1_, h1_, z2_, h2_, z3_, h3_)),
delimiter = ",")
```

## Benchmarking example 1: Water flow in soil

Currently, benchmarks are developed to test dumux-rosi against analytical solutions and results of other numerical models. They are all described in Jupyter Notebooks at https://github.com/RSA-benchmarks/collaborative-comparison. Here, we describe the DuMu $^x$ -implementation of the 1D benchmarks of Vanderborght et al. (2005) for water flow in soil.

### The model

We solve the Richards equation for water flow in soil. Since  $\operatorname{DuMu}^x$  is developed for multi-phase flow in porous media, it uses units of absolute pressure of wetting and non-wetting phases. In the Richards equation, we assume that the non-wetting phase (air) does not change over time and has a constant pressure of  $1.0 \times 10^5$  Pa. Thus, we need to solve only the equation for the wetting phase (water). We stick to the standard  $\operatorname{DuMu}^x$  units for pressure, although in soil physics, head units are more common, in order to avoid mistakes of e.g. unconsidered hard coded constants, etc. The Richards equation thus can be written as

$$\frac{\partial}{\partial t} \left( \rho_w \Phi S \right) - \nabla \cdot \left[ \rho_w \frac{\kappa}{\mu} K \left( \nabla p_w - \rho_w \mathbf{g} \right) \right] = 0, \tag{1}$$

with t time,  $\theta$  water content, S saturation,  $\Phi$  porosity,  $S\phi=\theta$ ,  $\rho_w$  water density, K intrinsic permeability,  $\mu$  dynamic viscosity,  $\kappa$  relative permeability,  $\theta$  gravitational acceleration,  $\rho_w$  absolute pressure of wetting phase (water)<sup>5</sup>.  $\theta$  and  $h_m$  are related by the water retention curve:  $\theta:=\theta(h)$  (e.g. van Genuchten model).

Different initial and boundary conditions can be prescribed via the input file. Boundary conditions have number codes following (previous versions of) Hydrus:

 $<sup>^5</sup>p_w$  is the absolute pressure. The matric pressure  $p_m$  is defined as  $p_m = p_w - p_a$ , where  $p_a$  is the air pressure, assumed to be constant and equal to  $1.0 \times 10^5$  Pa in this Richards equation model. In order to have head units, we need to convert the water potential from energy per unit volume of water (pressure) to energy per unit weight, i.e.,  $h_m = \frac{p_m}{\rho_{w} \mathbf{g}}$ 

```
constantPressure = 1,
constantFlux = 2,
atmospheric = 4,
freeDrainage = 5.
```

### The input files

Model parameters, initial and boundary conditions can be specified via the input file such that no re-building of the code is required. Here is the listing of the input file dumux-rosi/rosi\_benchmarking/soil\_richards/input/b1a\_1d .input:

```
[Problem]
  Name = benchmark1d_1a
  [TimeLoop]
5 TEnd = 3153600 # 0 is steady state
6 DtInitial = 1 # [s]
7 MaxTimeStepSize = 864000 # 10 days [s]
9 [Soil.Grid]
10 UpperRight = 0
11 LowerLeft = -2
12 Cells = 199
[Soil.BC.Top]
Type = 2 # constant flux
_{16} Value = 0.5 # [cm/d]
17
18 [Soil.BC.Bot]
19 Type = 5 # free drainage
21 [Soil.IC]
P = -200 \# cm pressure head (initial guess)
[Soil. VanGenuchten]
25 # Loam over sand
Qr = 0.08 \quad 0.045
Qs = 0.43 \ 0.43
28 Alpha = 0.04 	 0.15 	 \# [1/cm]
_{29} N = 1.6 3
_{30} Ks = 50 1000 # [cm/d]
32 [Soil.Layer]
Z = -2 -0.5 -0.5 0
34 Number = 2 2 1 1
36 [Vtk]
```

```
AddProcessRank = "false"

AddVelocity = "false"
```

Listing 4: input file

### The DuMu<sup>x</sup> code representation of model equations

In this section, we explain where the different terms of the model equations can be found in the  $\mathrm{DuMu}^x$  code, i.e., the storage, flux and sink terms. The storage term is defined in the file

/dumux/dumux/porousmediumflow/Richards/localresidual.hh, and is computed as

```
storage[conti0EqIdx] = volVars.porosity()

volVars.density(liquidPhaseIdx)

volVars.saturation(liquidPhaseIdx);
```

Listing 5: Storage term

In this example, there is no source or sink term.

The flux term is hidden in deeper layers of the code as part of the numerical scheme. In order to see it, we have to find out the flux type of the problem in the file /dumux/dumux/porousmediumflow/richards/.... In this example, the flux type is ''darcyslaw``. Its implementation can then be found in the folder /dumux/dumux/flux, and is then different for the different numerical schemes (e.g. cell-centered finite volume scheme with two-point flux approximation (TPFA)).

The implementation of the boundary conditions specified in the input file are implemented in the file

dumux-rosi/rosi\_benchmarking/soil\_richards/richardsproblem.hh.

```
*
  * dirchlet(...) is called by the local assembler, e.g.
  BoxLocalAssembler::evalDirichletBoundaries
  */
PrimaryVariables dirichletAtPos(const GlobalPosition &globalPos) const
  {
  PrimaryVariables values;
  if (onUpperBoundary_(globalPos)) { // top bc
    switch (bcTopType_) {
    case constantPressure: values[Indices::pressureIdx] = toPa_(
    bcTopValue_); break;
  default: DUNE_THROW(Dune::InvalidStateException, "Top boundary type
    Dirichlet: unknown boundary type");
}
```

```
} else if (onLowerBoundary_(globalPos)) { // bot bc
        switch (bcBotType_) {
12
        case constantPressure: values[Indices::pressureIdx] = toPa_(
13
     bcBotValue_); break;
        default: DUNE THROW(Dune::InvalidStateException, "Bottom boundary
14
     type Dirichlet: unknown boundary type");
16
      values.setState(Indices::bothPhases);
17
      return values;
18
    }
20
     * \copydoc FVProblem::neumann // [kg/(m<sup>2</sup>*s)]
22
23
     * called by BoxLocalResidual::evalFlux,
24
     * mass flux in f [ kg / (m^2 \cdot s)] \f$
     * Negative values mean influx.
26
     */
27
    NumEqVector neumann(const Element& element,
28
        const FVElementGeometry& fvGeometry,
29
        const ElementVolumeVariables& elemVolVars,
30
        const SubControlVolumeFace& scvf) const {
31
32
      NumEqVector flux;
33
      double f = 0.; // return value
34
      GlobalPosition pos = scvf.center();
35
36
      if ( onUpperBoundary_(pos) || onLowerBoundary_(pos) ) {
```

Listing 6: Boundary conditions

```
Scalar p = MaterialLaw::pc(params, s) + pRef_; // [Pa]
        Scalar h = -toHead_(p); // cm
        GlobalPosition ePos = element.geometry().center();
        Scalar dz = 100 * std::fabs(ePos[dimWorld - 1] - pos[dimWorld - 1])
     ; // m-> cm (*2 ?)
        Scalar krw = MaterialLaw::krw(params, s);
        if (onUpperBoundary_(pos)) { // top bc
          switch (bcTopType_) {
          case constantFlux: { // with switch for maximum in- or outflow
            f = -bcTopValue_*rho_/(24.*60.*60.)/100; // cm/day -> kg/(m^2*s)
            if (f < 0.) { // inflow</pre>
              Scalar imax = rho_* * kc * ((h - 0.) / dz - gravityOn_); //
12
     maximal inflow
              // std::cout << "in:" << f <<", " << imax <<"\n";
13
              f = std::max(f, imax);
14
            } else { // outflow
```

```
Scalar omax = rho_ * kc * krw * ((h - criticalPressure_) /
     dz - gravityOn_); // maximal outflow (evaporation)
               // std::cout << "outflow " << f*1.e6 << ", " << omax*1.e6 <<
      " krw " << krw*1.e6 << "\n";
              f = std::min(f, omax);
18
            }
            break;
20
          case constantFluxCyl: { // upper = outer, with switch for maximum
22
      in- or outflow
            f = -bcTopValue_*rho_/(24.*60.*60.)/100 * pos[0]; // [cm /day]
23
       -> [kg/(m<sup>2</sup>*s)] (Eqns are multiplied by cylindrical radius)
            if (f < 0.) { // inflow</pre>
```

Listing 7: Boundary conditions

and

```
f = std::min(f, omax);
            }
            break;
          }
          case atmospheric: { // atmospheric boundary condition (with
     surface run-off)
            Scalar prec = -precipitation_.f(time_);
            if (prec < 0.) { // precipitation</pre>
              // std::cout << "in" << "\n";
              Scalar imax = rho_ * kc * ((h - 0.) / dz - gravityOn_); //
     maximal infiltration
              f = std::max(prec, imax);
            } else { // evaporation
11
              // std::cout << "out" << ", at " << h << " cm \n";
                Scalar p2 = toPa_(-10000);
                Scalar h3 = 0.5*(h + criticalPressure_);
                Scalar p3 = toPa_(h);
15
                Scalar s2 = MaterialLaw::sw(params, -(p2- pRef_));
                           Scalar s3 = MaterialLaw::sw(params, -(p3- pRef_))
17
                // std::cout << s2 << "\n";
18
                Scalar krw2 = MaterialLaw::krw(params, s2);
                Scalar krw3 = MaterialLaw::krw(params, s3);
20
                           Scalar arithmetic = 0.5*(krw2+krw); // arithmetic
21
      currently best
                Scalar harmonic = 2*krw2*krw/(krw2+krw);
22
              Scalar emax = rho_ * kc * arithmetic *((h - criticalPressure_
23
     ) / dz + gravityOn_); // maximal evaporation KRW???
              f = std::min(prec, emax);
            }
25
            break;
26
          default: DUNE_THROW(Dune::InvalidStateException, "Top boundary
     type Neumann: unknown error");
```

```
} else if (onLowerBoundary_(pos)) { // bot bc
30
          switch (bcBotType_) {
31
          case constantFlux: { // with switch for maximum in- or outflow
32
            f = -bcBotValue *rho /(24.*60.*60.)/100.; // [cm /day] -> [kg/(
33
     m2*s)]
            if (f < 0.) { // inflow</pre>
34
               Scalar imax = rho_ * kc * ((h - 0.) / dz - gravityOn_); //
35
     maximal inflow
              imax = std::min(imax, 0.); // must stay negative
36
              f = std::max(f, imax);
37
            } else { // outflow
38
              Scalar omax = rho_ * kc * krw *((h - criticalPressure_) / dz
39
     - gravityOn_); // maximal outflow (evaporation)
              // std::cout << "outflow " << f << ", " << omax << "\n";
40
              omax = std::max(omax, 0.); // must stay positive
41
              f = std::min(f, omax);
42
            }
43
            break;
45
          case constantFluxCyl: { // lower = inner, with switch for maximum
46
      in- or outflow
            f = -bcBotValue_*rho_/(24.*60.*60.)/100. * pos[0]; // [cm /day]
47
       -> [kg/(m<sup>2</sup>*s)] (Eqns are multiplied by cylindrical radius)
            if (f < 0.) { // inflow</pre>
48
              Scalar imax = rho_* kc * ((h - (-10.)) / dz - gravityOn_)*
49
     pos[0]; // maximal inflow
              imax = std::min(imax, 0.); // must stay negative
50
              f = std::max(f, imax);
            } else { // outflow
               Scalar omax = rho_ * kc * krw *((h - criticalPressure_) / dz
      - gravityOn_)* pos[0]; // maximal outflow (evaporation)
                std::cout << " f " << f*1.e9 << ", omax "<< omax*1.e9 <<
54
      ", value " << bcBotValue_
                     << ", crit " << criticalPressure_ << ", " << pos[0] <<
  //
      ", krw " << krw <<"\n";
              omax = std::max(omax, 0.); // must stay positive
56
              f = std::min(f, omax);
57
            }
58
            break;
          case freeDrainage: {
61
            f = krw * kc * rho_; // * 1 [m]
            break;
63
          }
64
          default: DUNE_THROW(Dune::InvalidStateException, "Bottom boundary
65
      type Neumann: unknown error");
          }
66
        }
67
```

```
flux[conti0EqIdx] = f;
return flux;
}

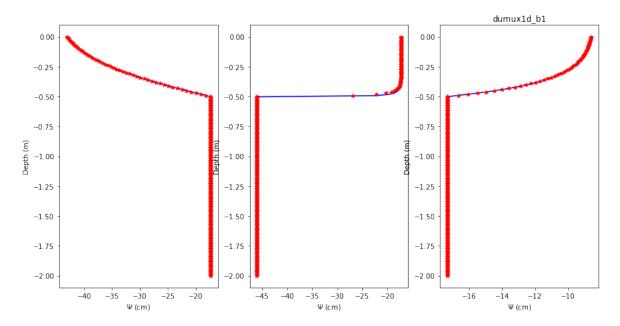
/*!
    * \copydoc FVProblem::source
    *
    called by FVLocalResidual:computeSource(...)
*
```

Listing 8: Boundary conditions

.

### Results

The vtk output of 3D simulations may be visualised using Paraview. In this case, we only have a 1D simulation, therefore, we do the visualisation after postprocessing in Python.



Results of benchmark problem 1. Blue: analytical solution, Red: numerical solution by  $\mathrm{DuMu}^x$