

# 4. Population Growth and Intraspecific Competition

Jasper Slingsby, BIO2014F

2024-04-23

# The Hutchinsonian Niche

G Evelyn Hutchinson proposed that *the niche is an n-dimensional hypervolume within which a species is able to maintain a viable population* - Hutchinson 1957

Does the occurrence of a species at a locality mean it is able to maintain a viable population there...?

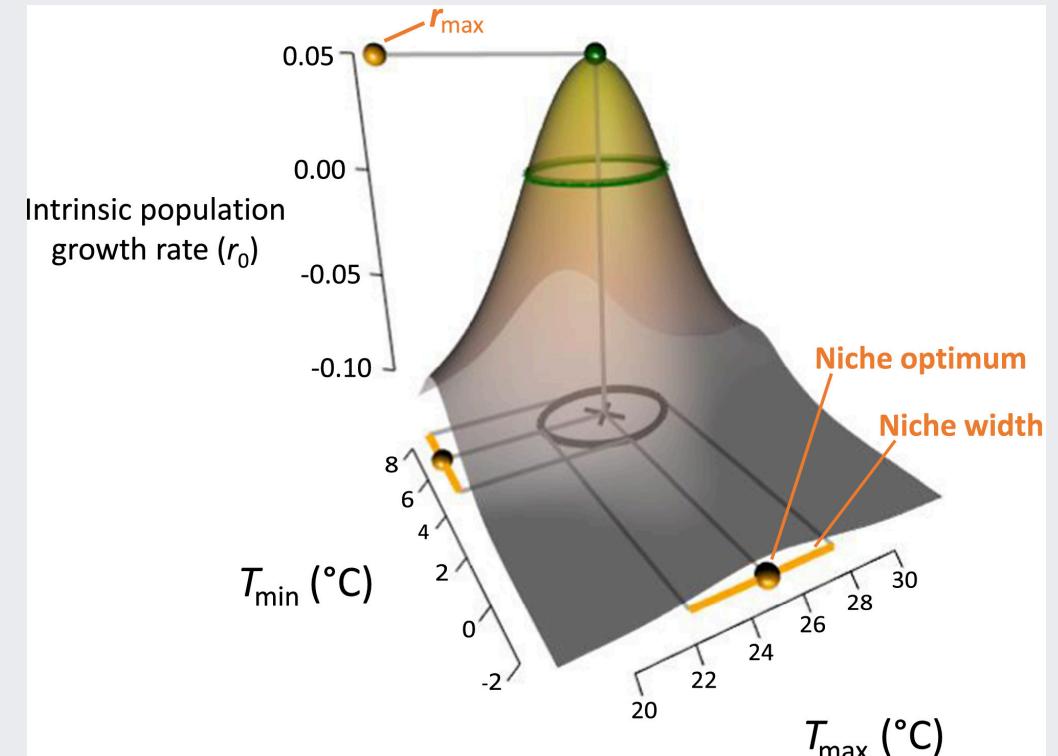


Figure from Treurnicht et al. 2020

**What does maintaining a viable population even mean?**

**It means maintaining population growth...**

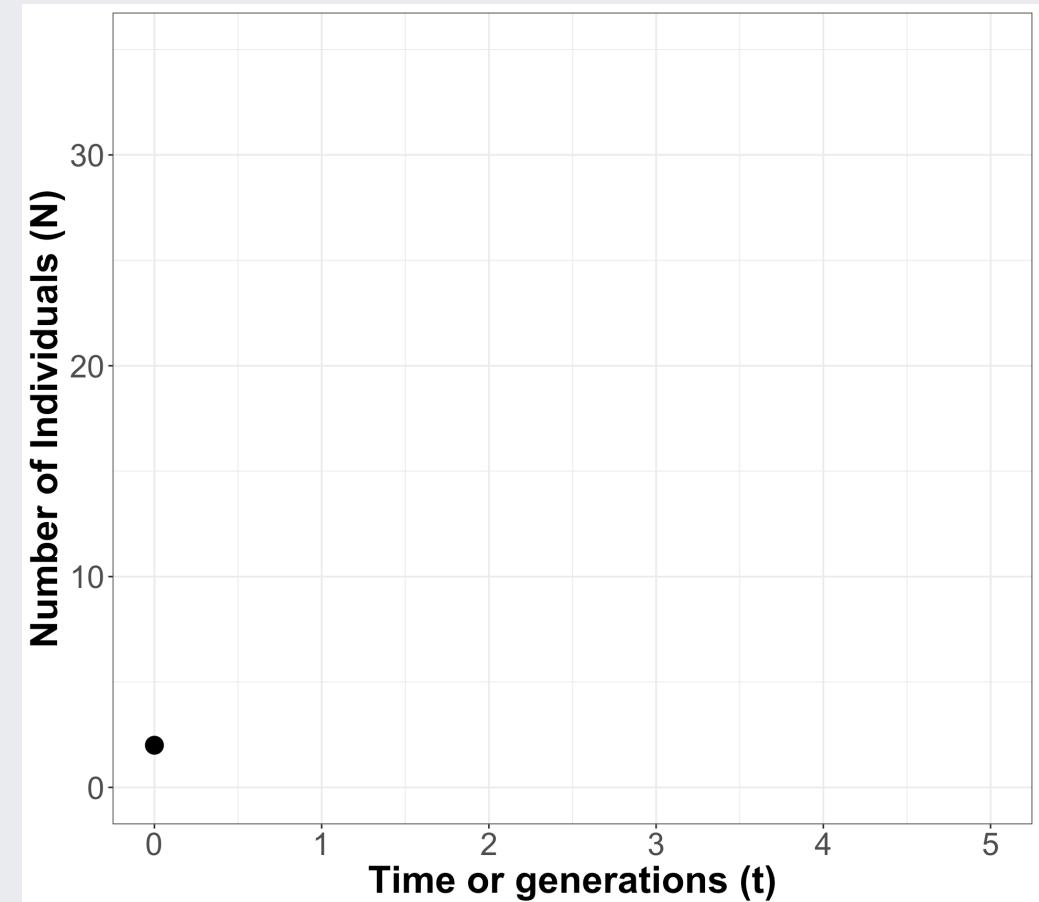
**But that's not easy...**

**Especially where there is competition for resources...**

# Population growth curve

Consider growth of a population, starting with 2 individuals at  $t = 0$ .

- Assume a per-capita reproductive rate,  $r = 2$



# Population growth curve

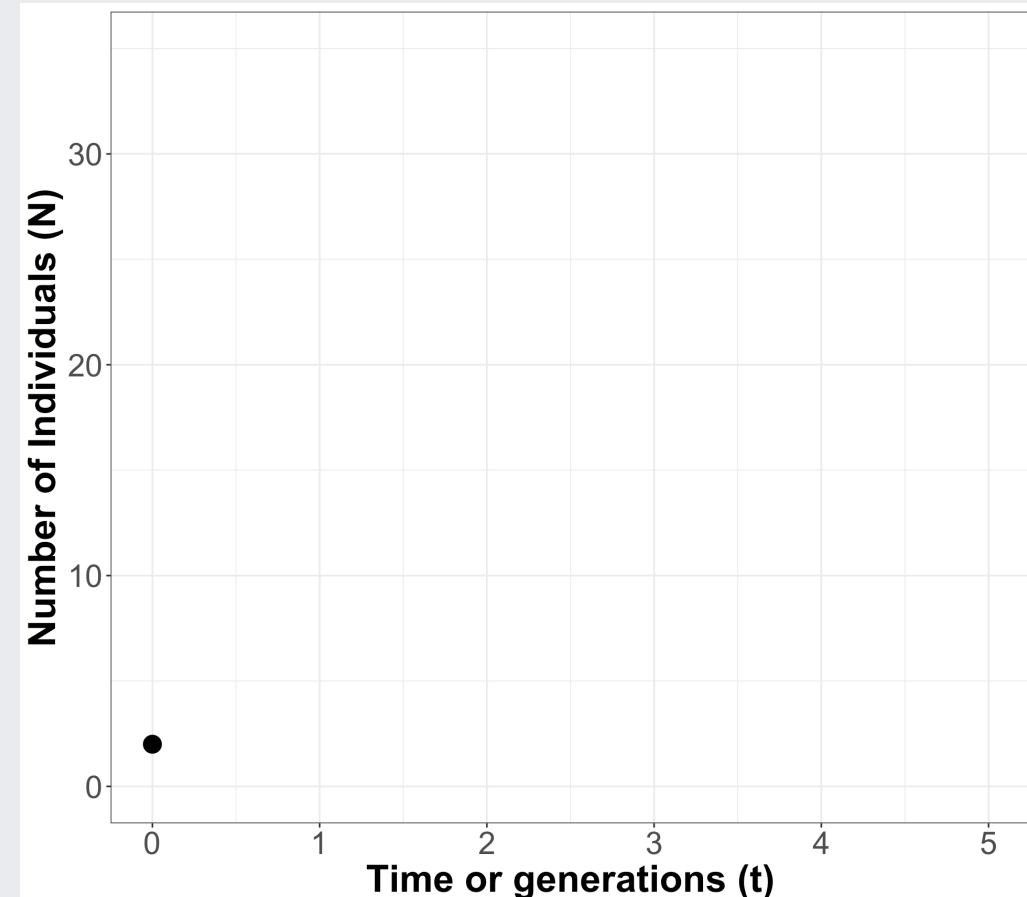
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- Assume a per-capita reproductive rate,  $r = 2$

**Note:** The per-capita reproductive rate ( $r$ ) is the number of reproductively mature individuals contributed per individual from one generation to the next.  
Population growth is positive where  $r > 0$ .

*It is a fundamental biological parameter, determined by things like the number of eggs/seeds produced, the hatching/germination success of eggs/seeds, and the success with which hatchlings/germinants survive to reproductive maturity.*

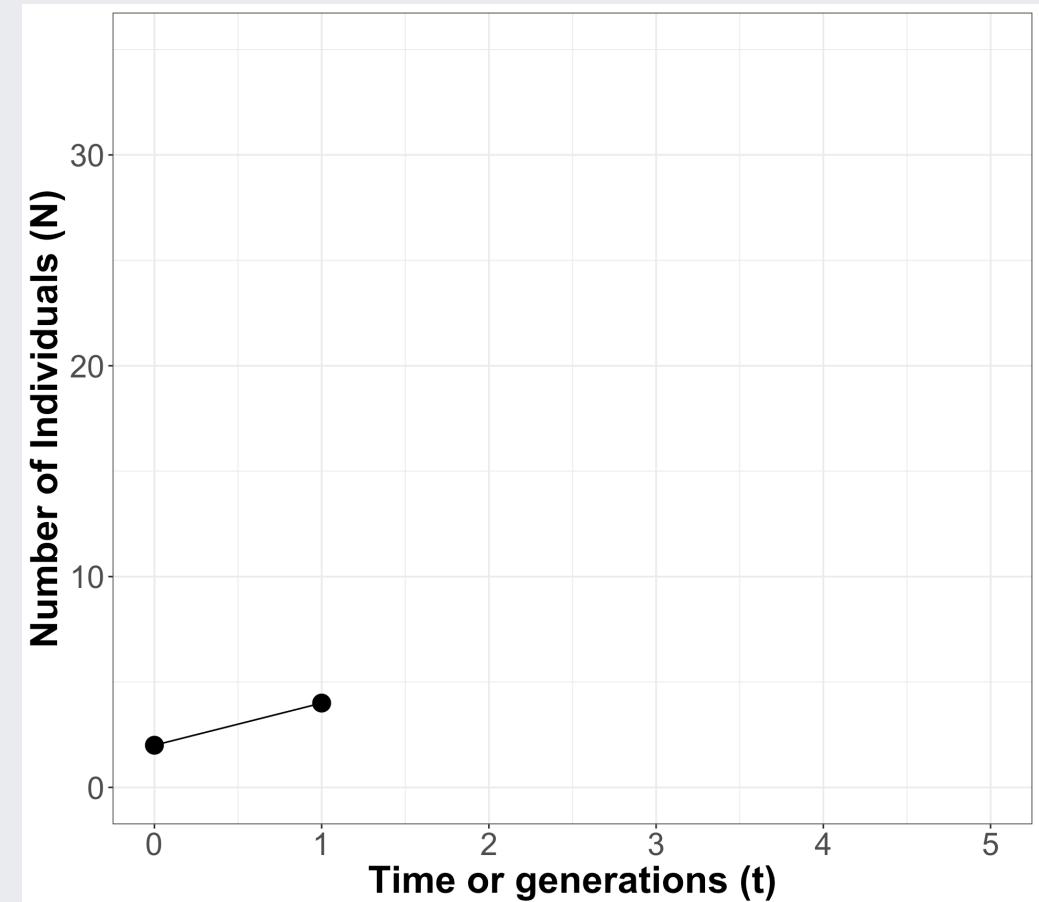
*It is the birth rate minus the death rate.*



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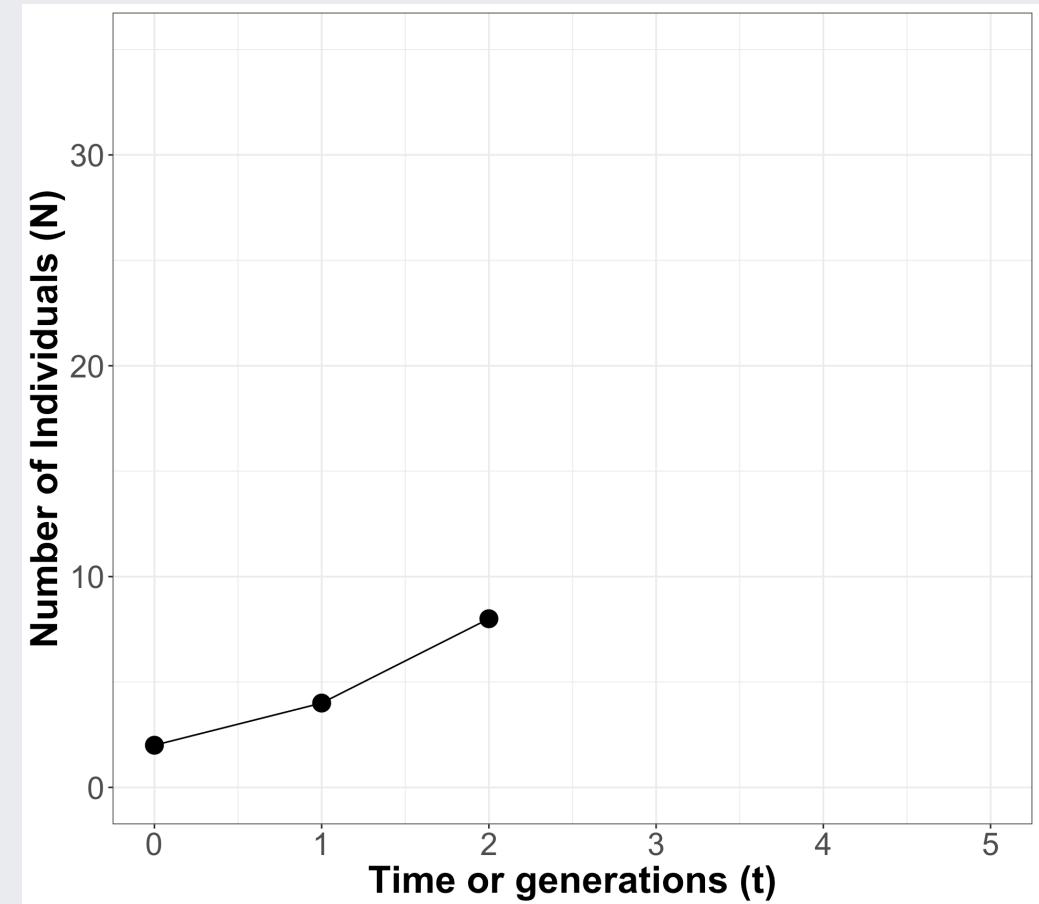
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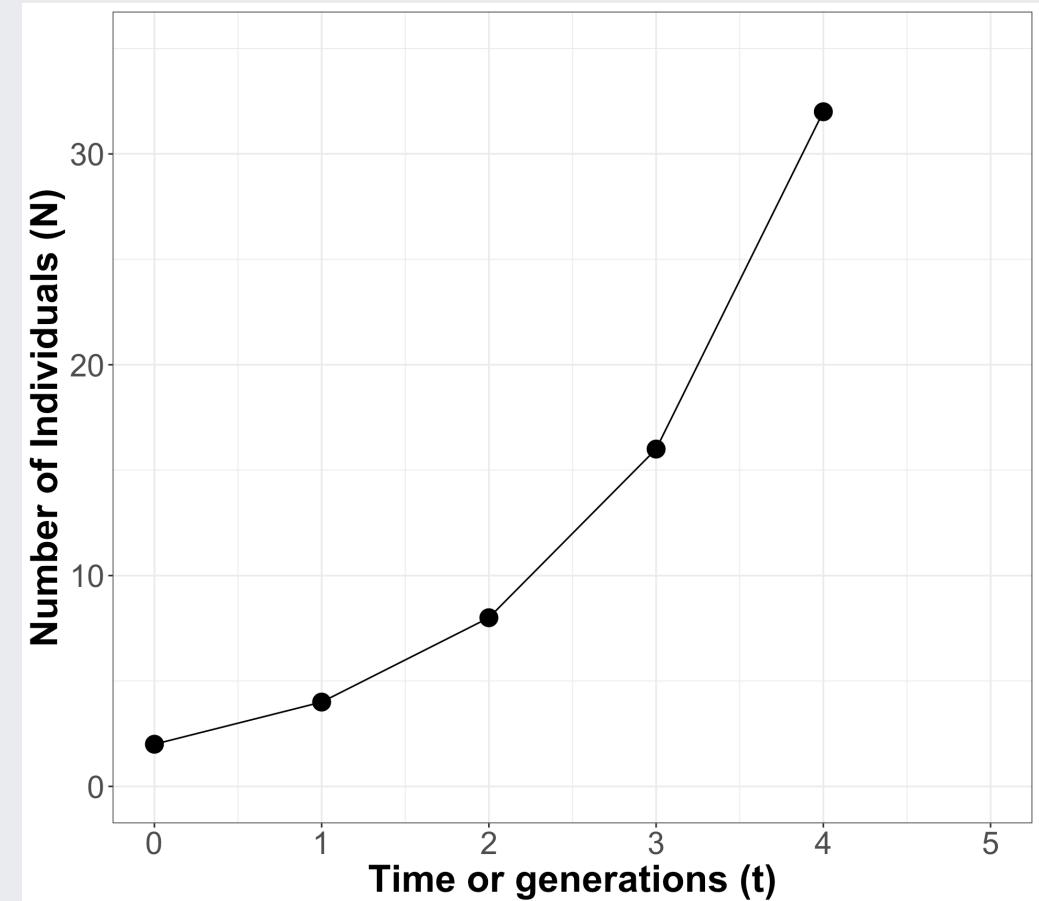


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*Growth is exponential!*



# Population growth curve

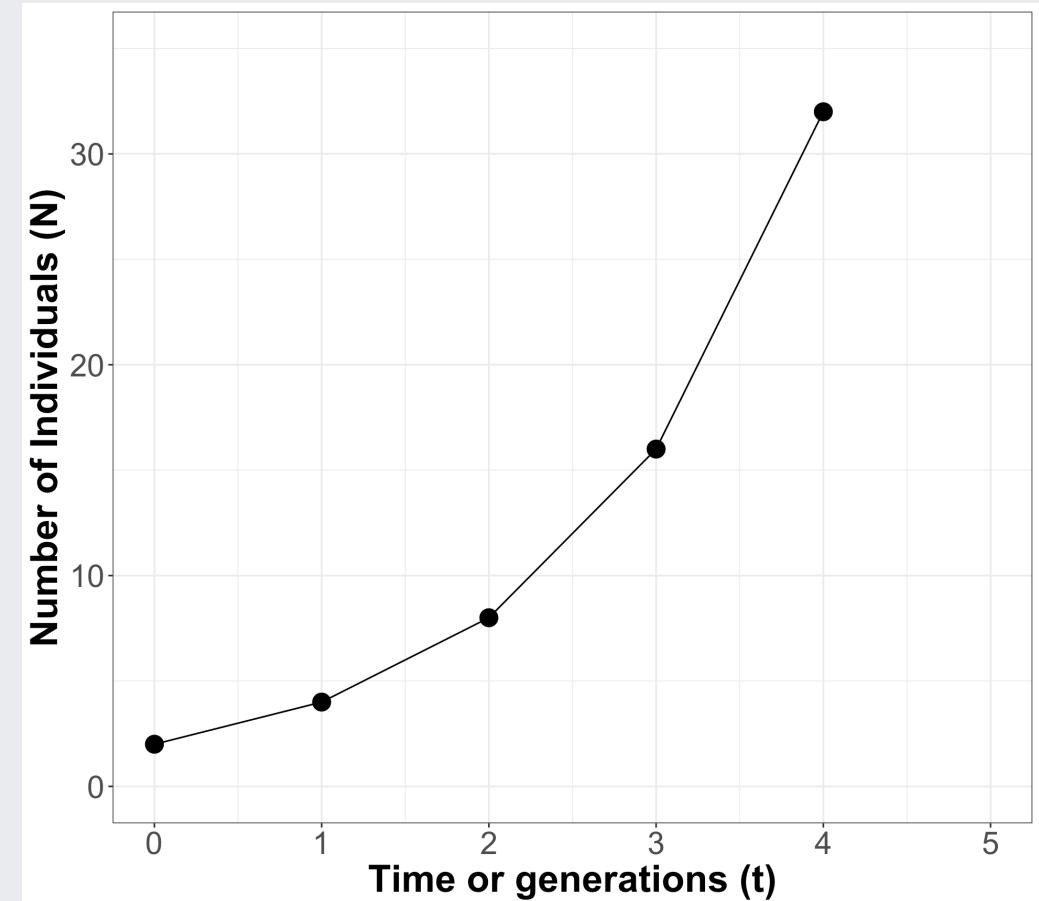
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*Growth is exponential!*

Using calculus, we can express growth as an instantaneous rate as  $dN/dt$ , the rate of change in number of organisms at a particular instant in time.

Since our example is an exponential function, the slope of this curve is given by  $dN/dt = rN$



# Is growth always exponential?

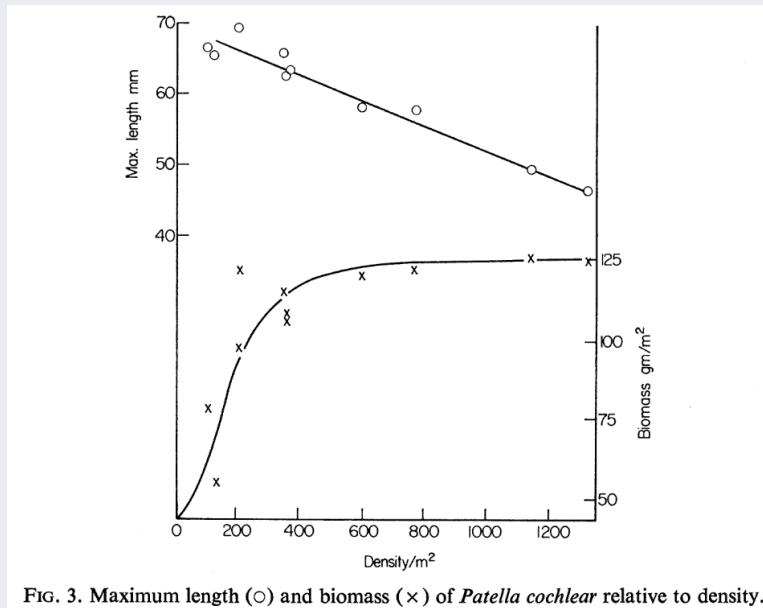


FIG. 3. Maximum length (○) and biomass (×) of *Patella cochlear* relative to density.

Resources available to individuals typically shrink as population size and density increase.

Competition between individuals limits growth and reproductive output.

A study of the Pear Limpet, *Scutellastra cochlear*, by Branch 1975

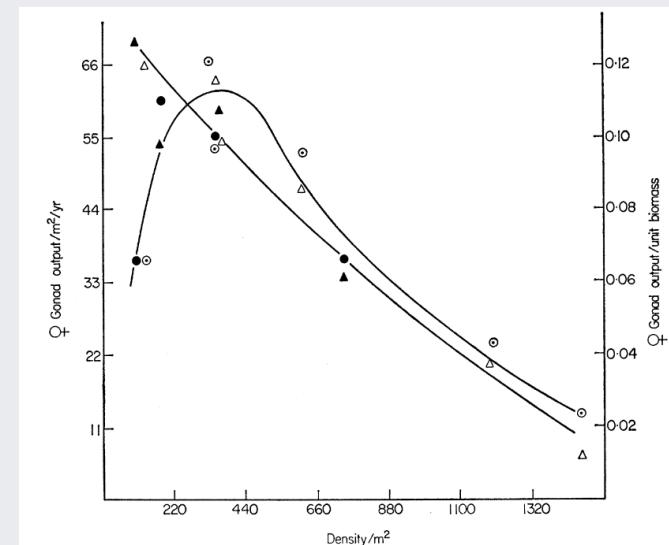
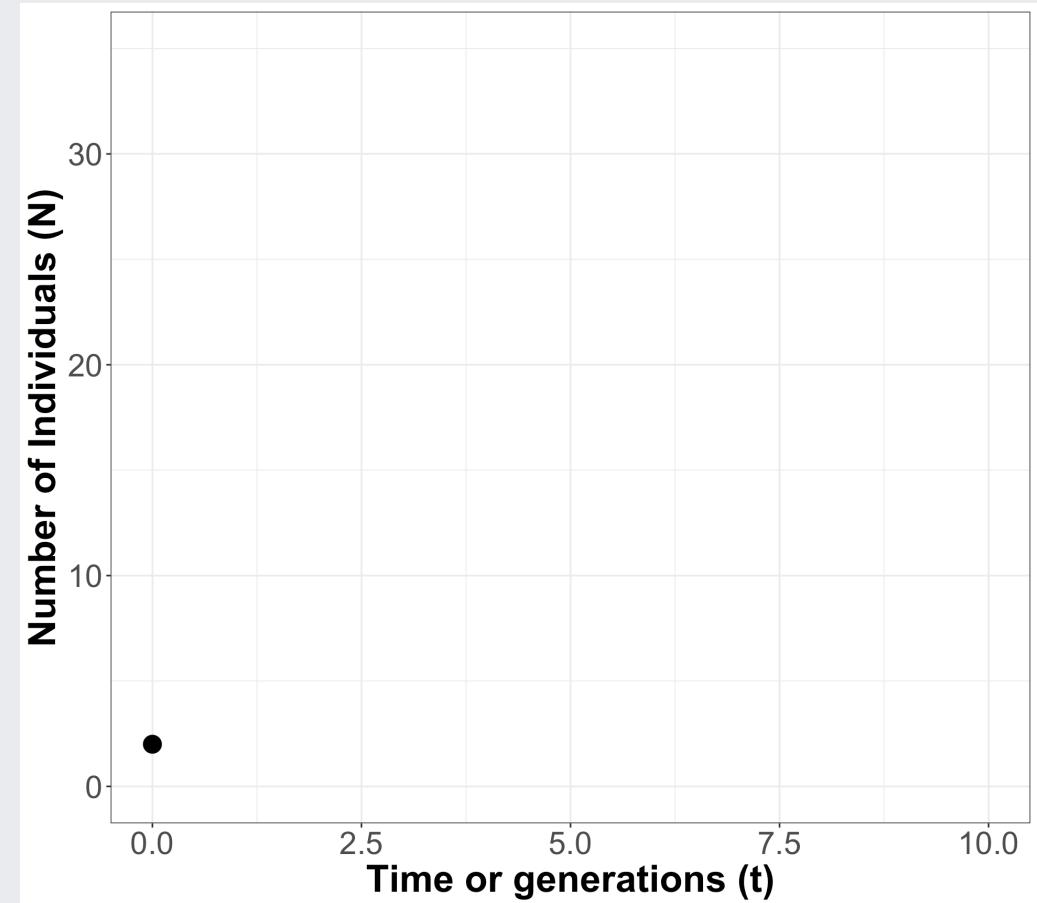


FIG. 6. Gonad output in *Patella cochlear*, relative to density. Gamete output per  $m^2$ : ●, measured; ○, calculated. Gamete output per unit biomass; ▲, measured; △, calculated.

image: Allan Ellis, iNaturalist

# Population growth curve

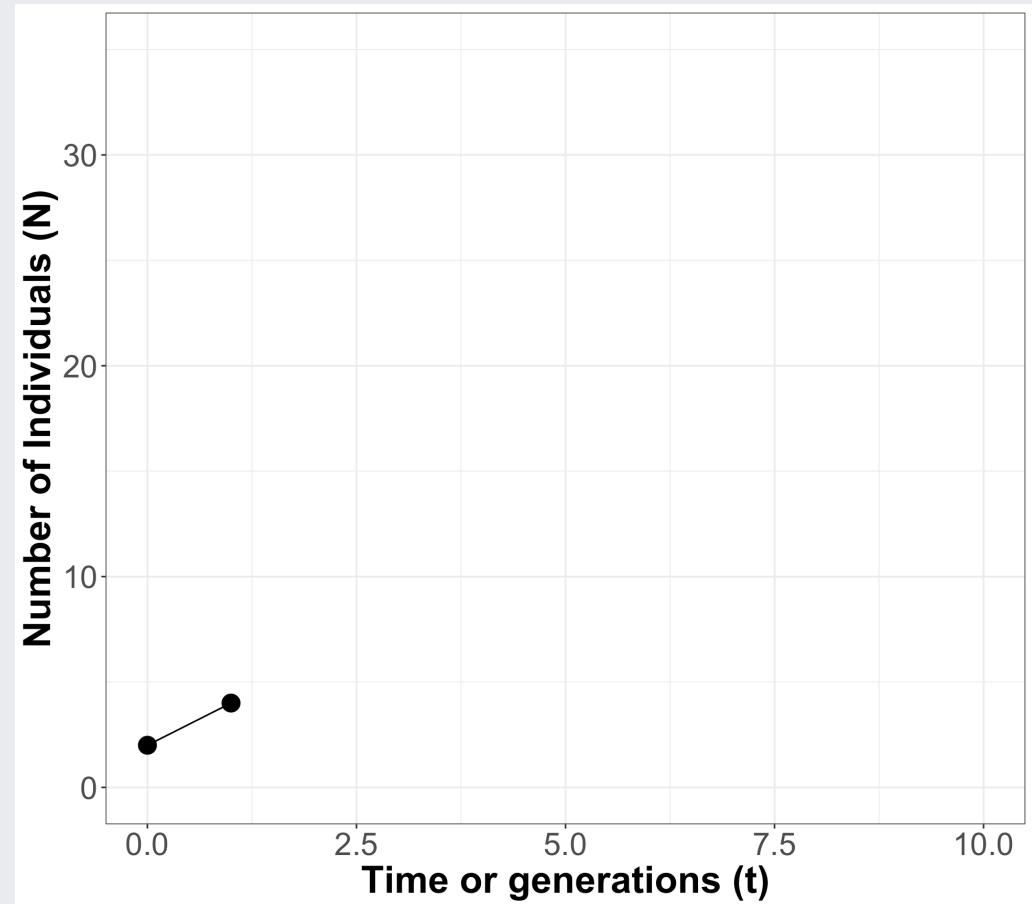
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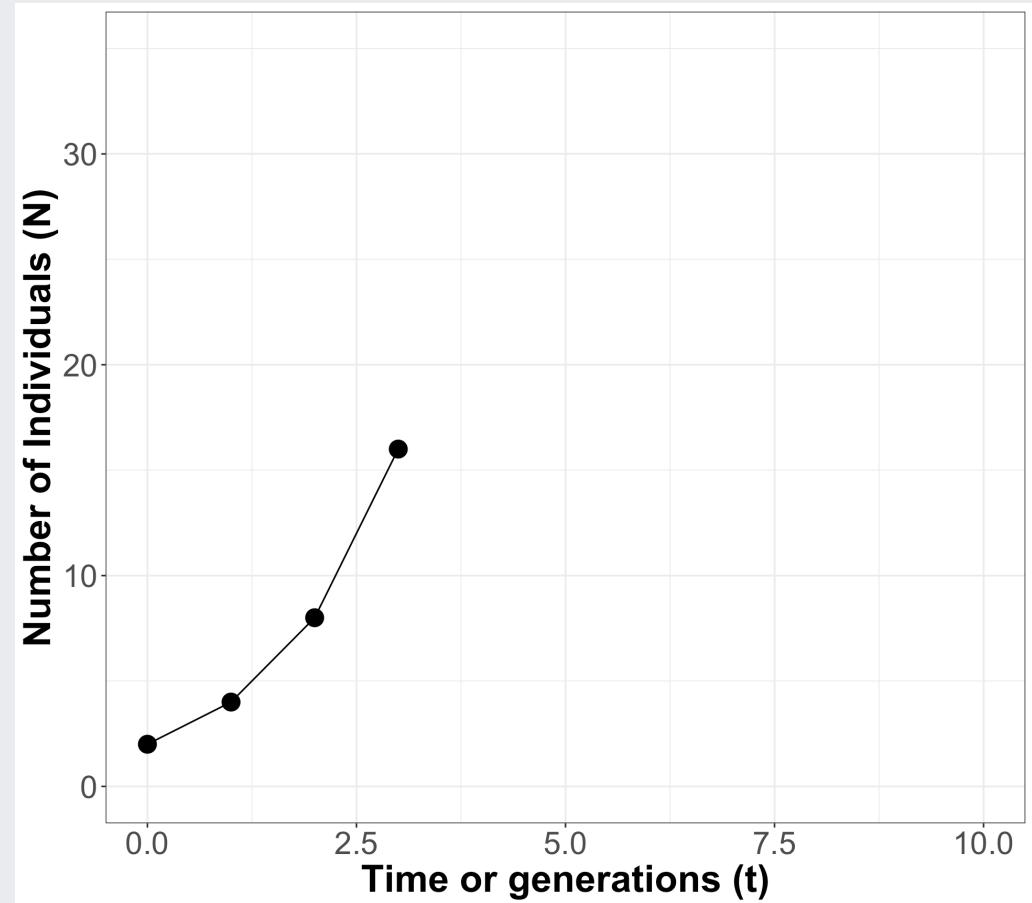
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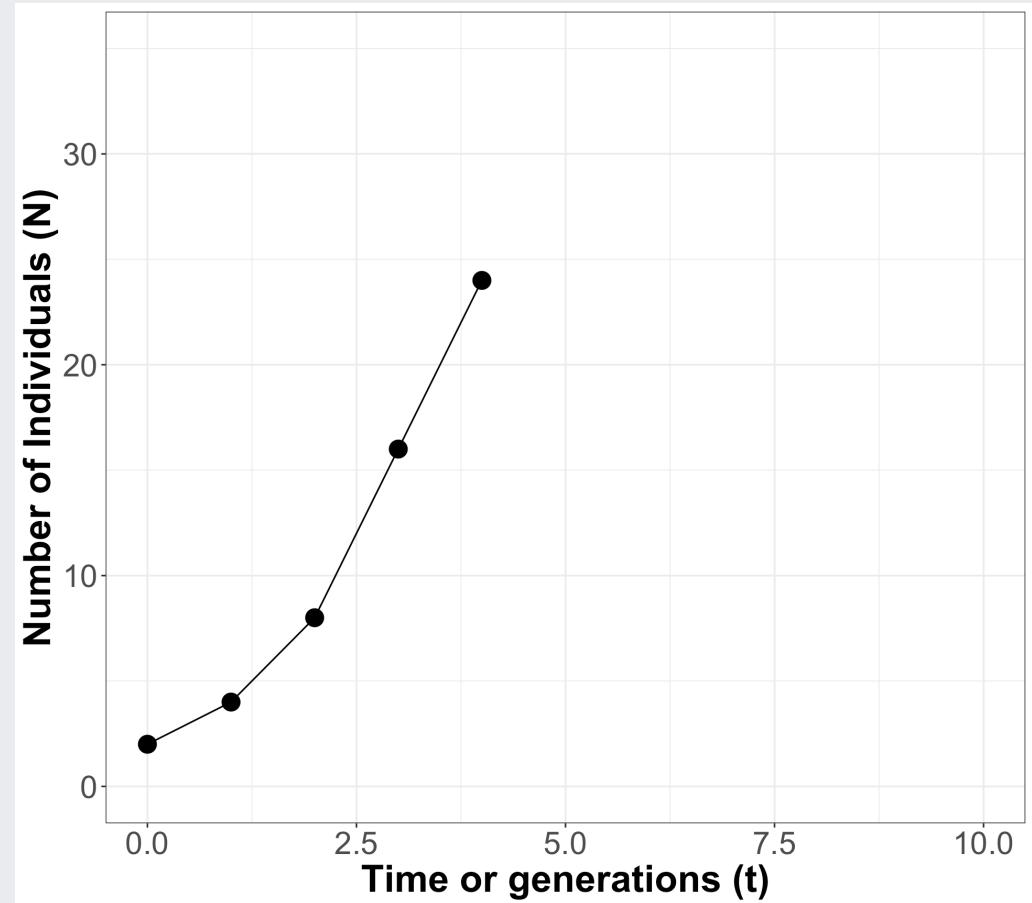
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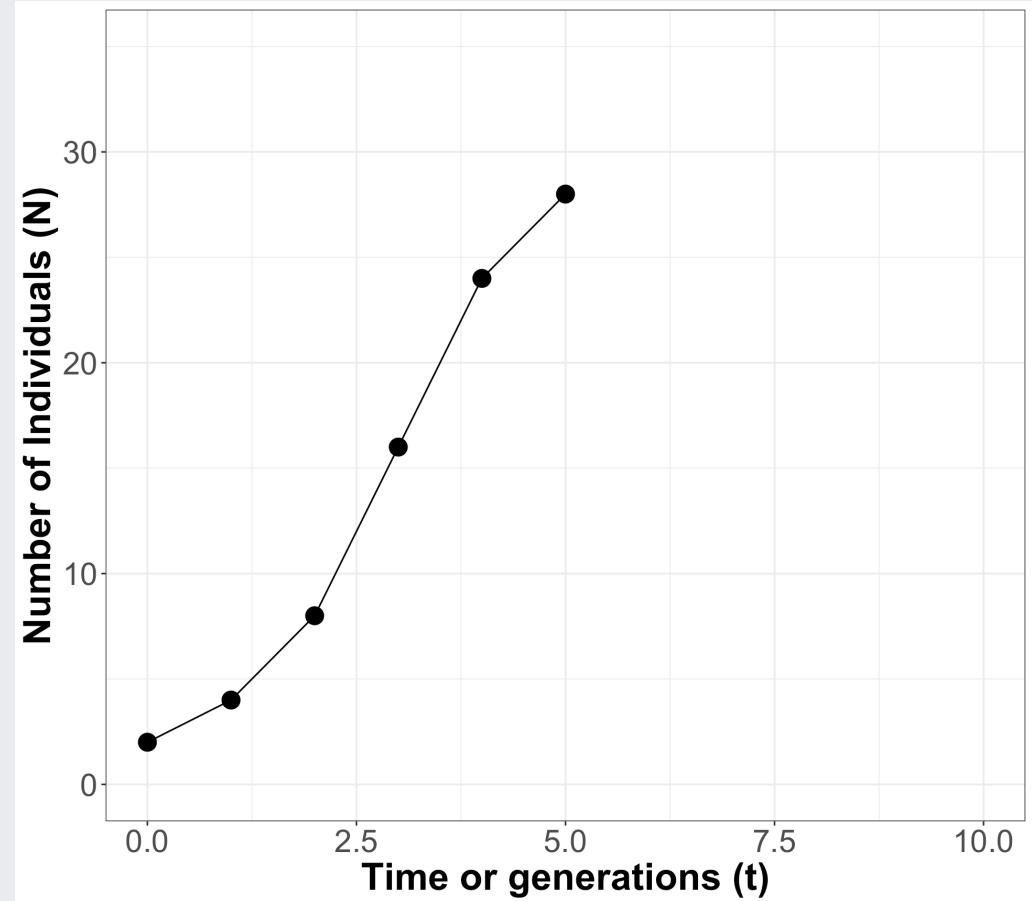


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It starts out much the same while resources are abundant...

...but slows as resources become limiting...

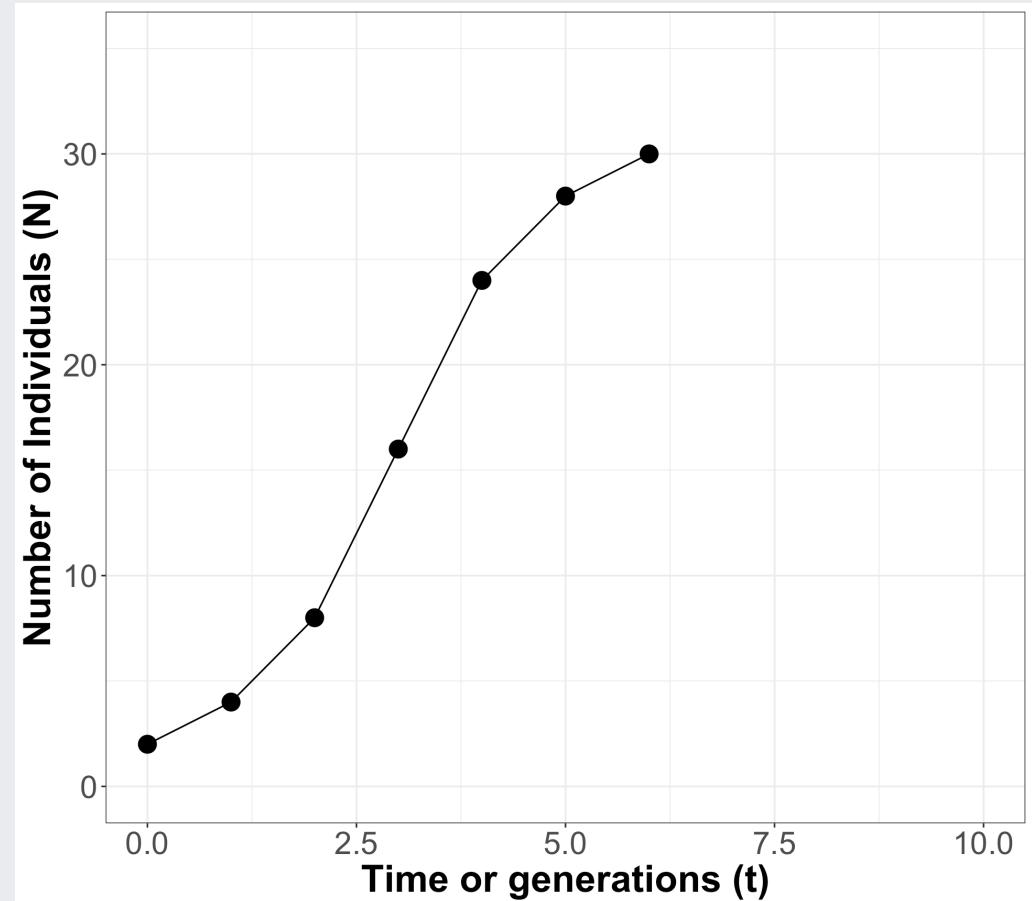


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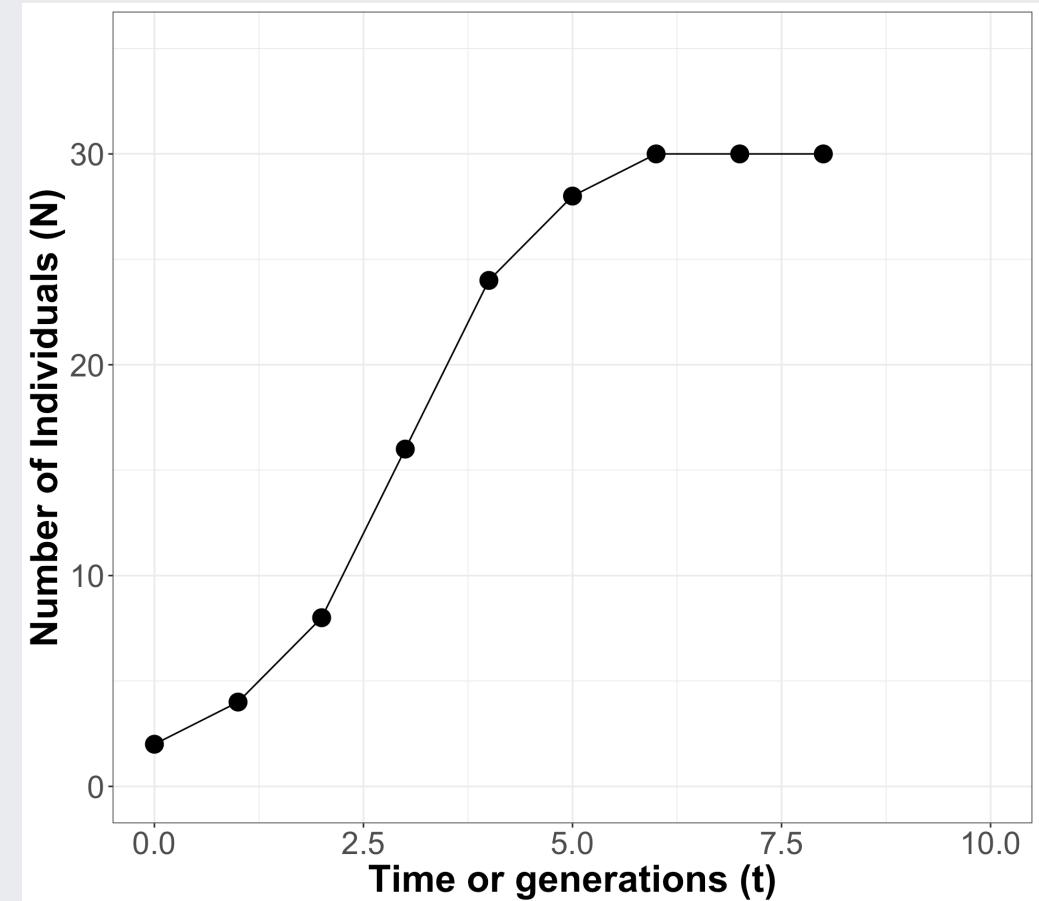
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It starts out much the same while resources are abundant...

...but slows as resources become limiting...

...and eventually flattens out...



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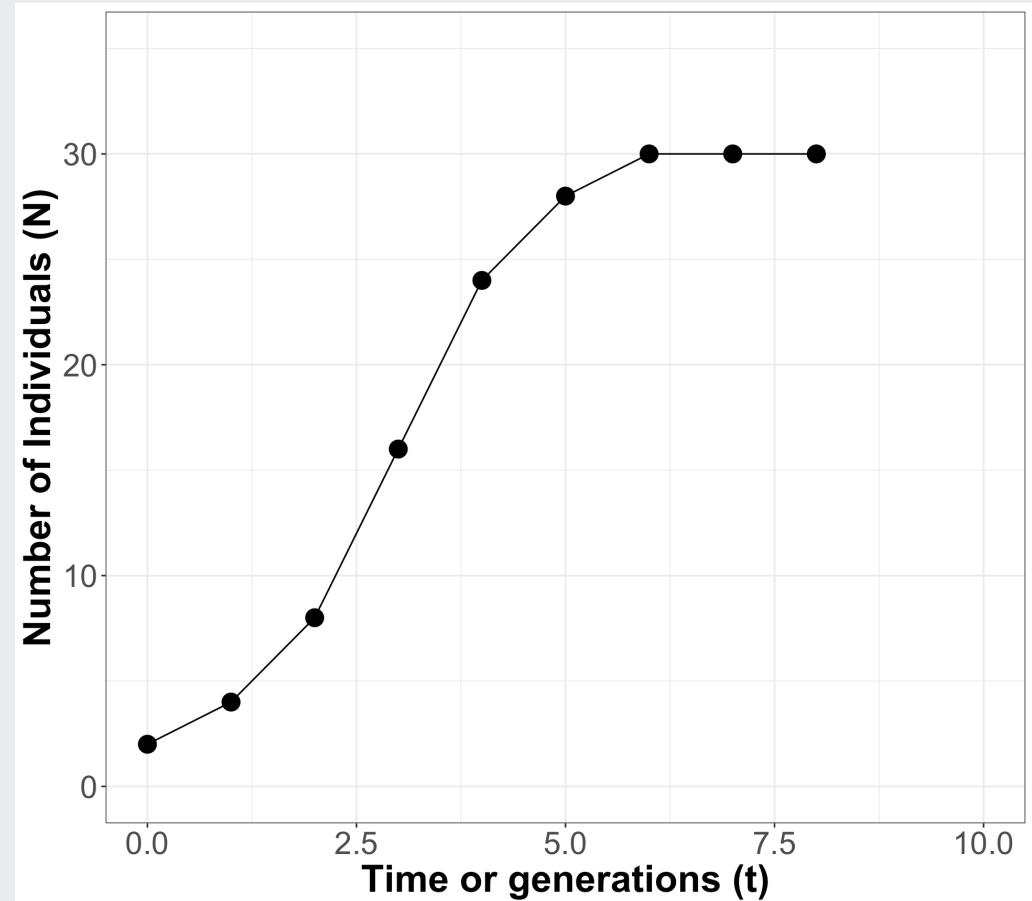
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Any thoughts on the equation to fit this curve?

$$dN/dt = ?$$



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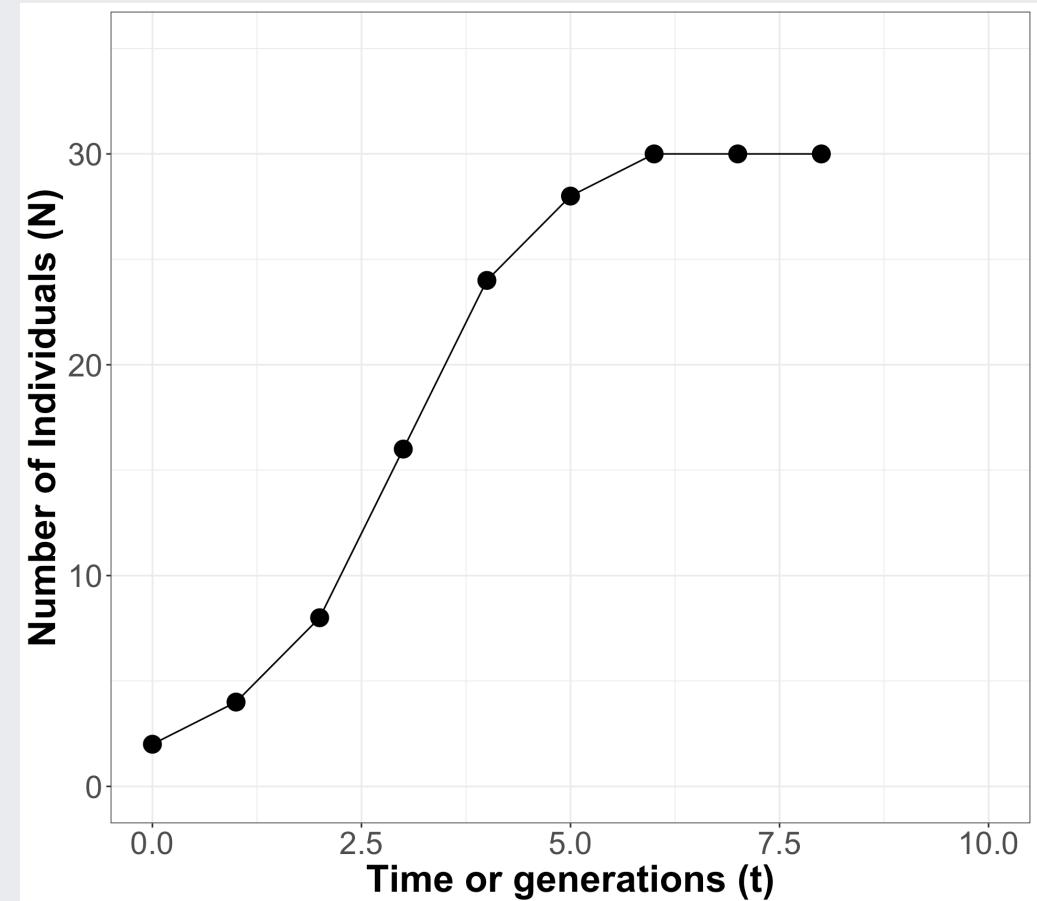
...but slows as resources become limiting...

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Any thoughts on the equation to fit this curve?

$$dN/dt = rN(K-N)/K$$

A logistic function, or what we call the logistic growth curve.

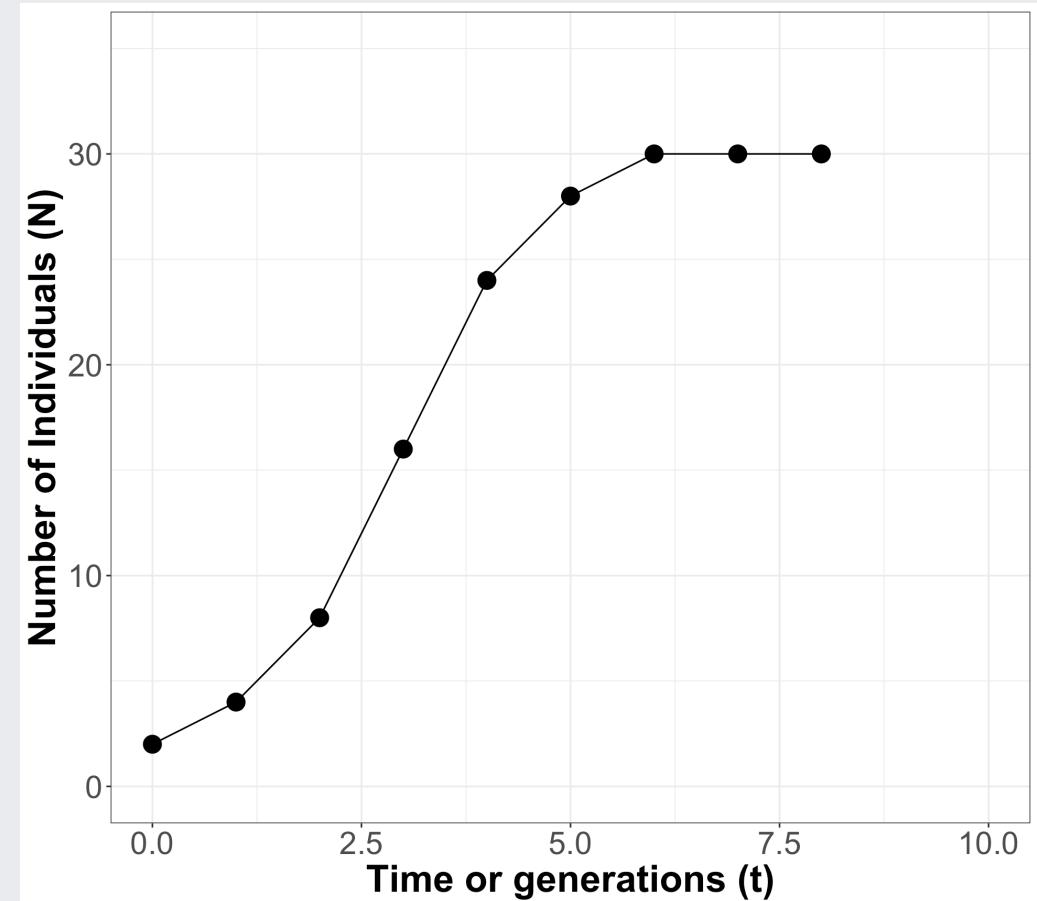


# Population growth curve

The population growth curve including **density-dependent** effects like intraspecific competition (competition among individuals of the same species) is a logistic function, flattening out as resources become limiting.

$$dN/dt = rN(K-N)/K$$

We know  $N$ ,  $t$  and  $r$ , but what is  $K$ ?



# Population growth curve

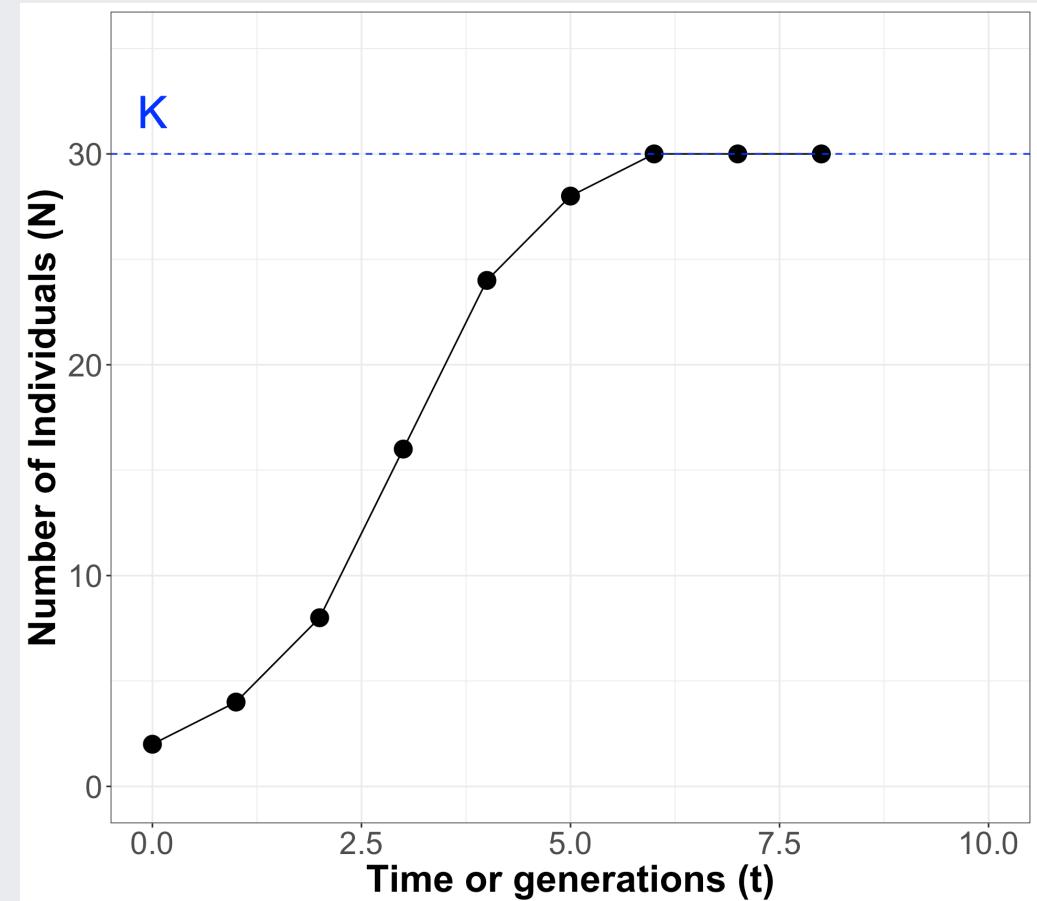
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We know  $N$ ,  $t$  and  $r$ , but what is  $K$ ?

$K$  = carrying capacity

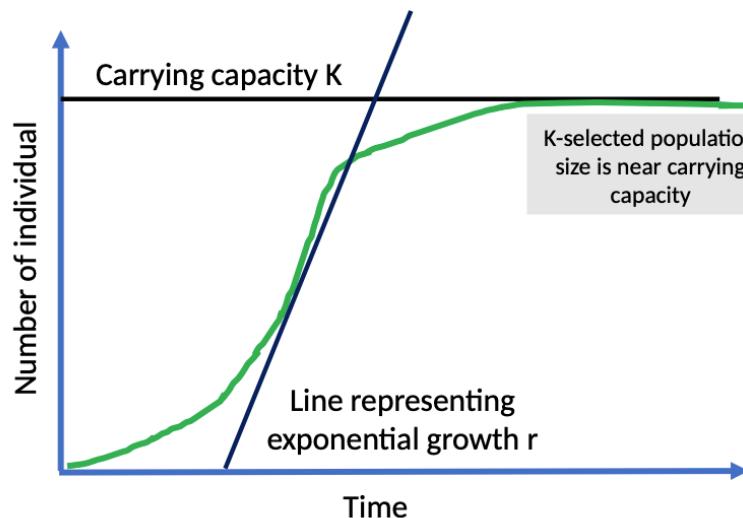
Familiar?



## *r* and *K* selection

Mac Arthur & Wilson, 1967

- **r-selected:** (*r* is for reproduction). Favoured for the ability to reproduce rapidly (high *r* - values) in *r*-selecting habitats (more unstable).
- **K-selected:** Favoured for the ability to make a large proportional contribution to a population which remains at its *carrying capacity* (*K*) in *K*-selecting habitats (more stable).



2

# Population growth curve

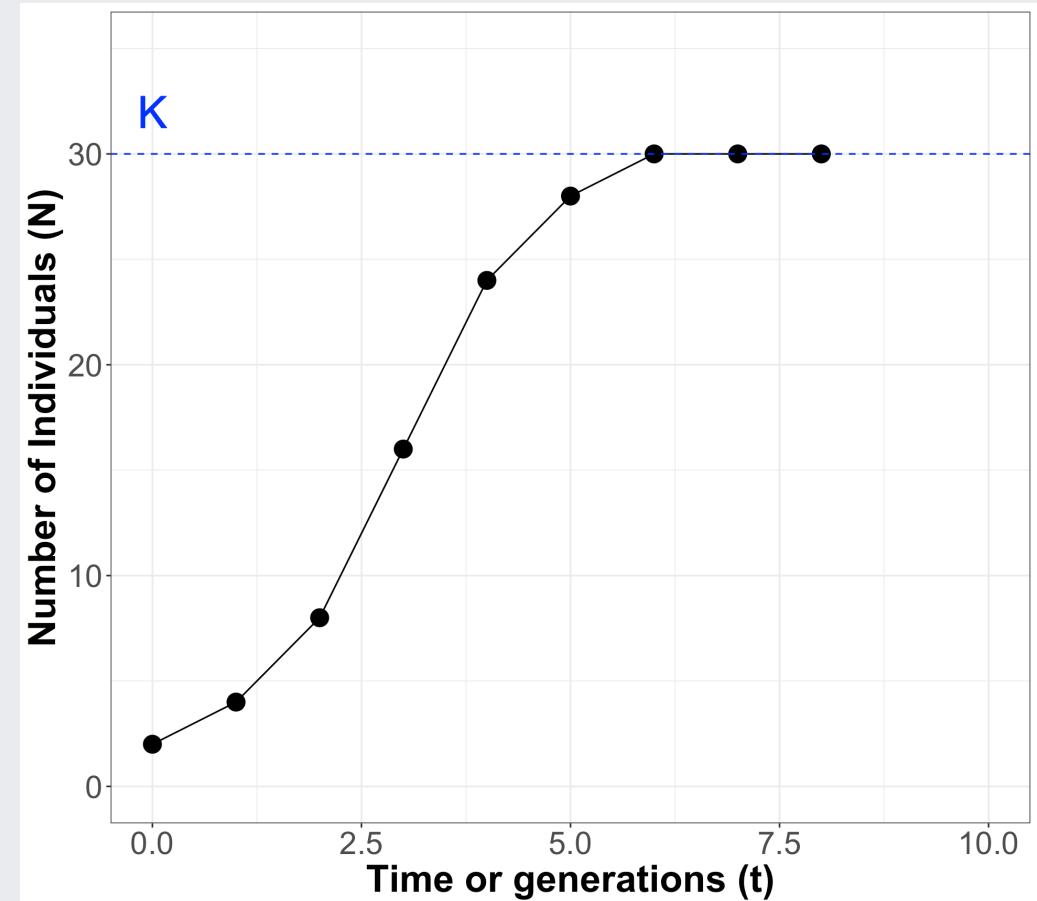
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$$dN/dt = rN(K-N)/K$$

$K$  = carrying capacity

**Note:** Where  $N$  is small, the logistic growth curve approximates the exponential growth curve ( $rN$ ), because  $(K-N)/K$  is close to 1.

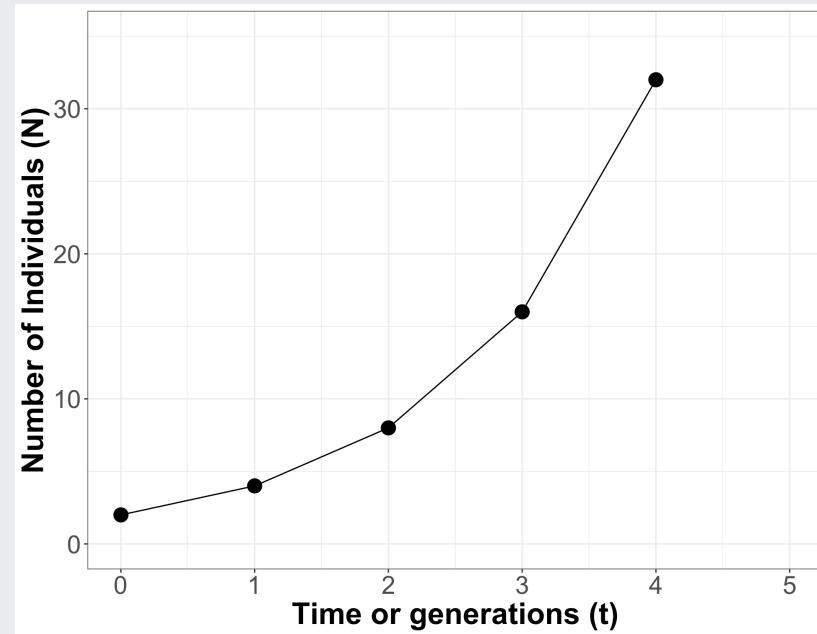
*It begins to deviate as  $N$  increases.*



# Exponential growth

$$dN/dt = rN$$

Population growth rate,  $r$ , doesn't change with population size

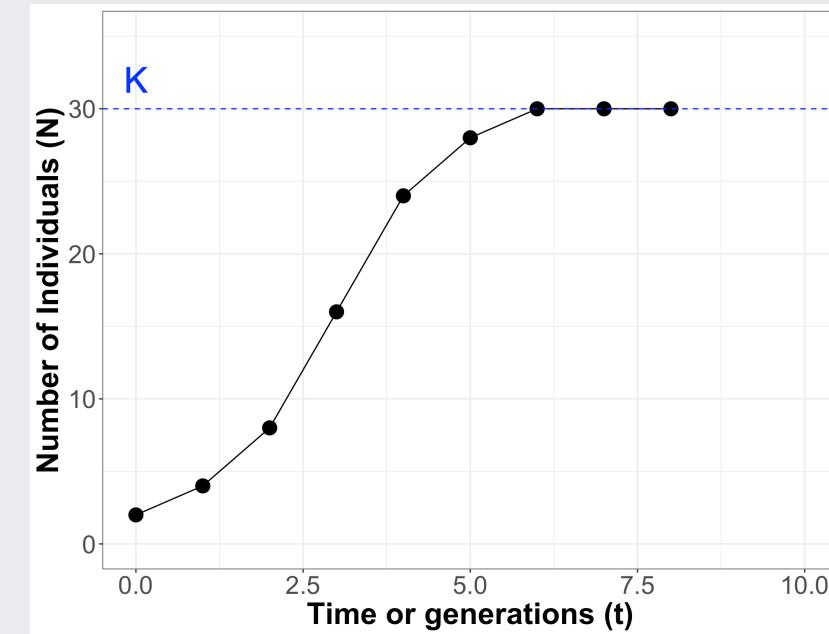


Density independent population growth

# Logistic growth

$$dN/dt = rN(K-N)/K$$

Population growth rate,  $r$ , gets small as the population approaches carrying capacity,  $K$



Density dependent population growth

**What are the implications of density-dependent growth?**

# What are the implications of density-dependent growth?

Serotinous Proteaceae are well known for extreme population density fluctuations after fire.



image: Roets et al 2006

**E**COSCIENCE

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## Fire life histories and the seeds of chaos<sup>1</sup>

William J. BOND, Kristal MAZE & Phillip DESMET, Botany Department, University of Cape Town, Private Bag, Rondebosch, 7700, South Africa, e-mail: bond@botzoo.uct.ac.za

While some of this may be exogenous, driven by external forces like climate fluctuations or variability in the fire regime, **Bond et al 1995** demonstrated that it could be endogenous, driven by internal population dynamics due to density-dependent effects.

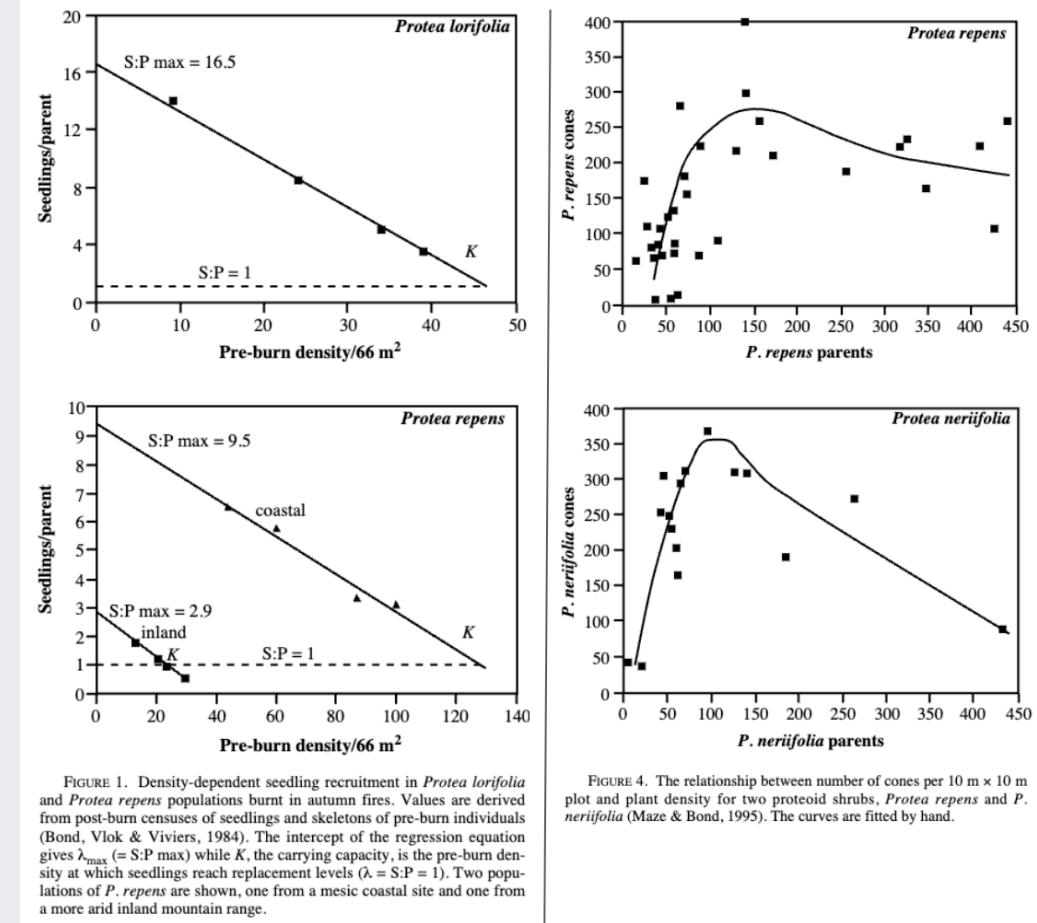
**Bond et al 1995**

# Density-dependence in serotinous Cape Proteaceae

Empirical datasets showed evidence for a negative impact of density-dependence on:

- recruitment (Figure 1)
- fecundity (Figure 4)

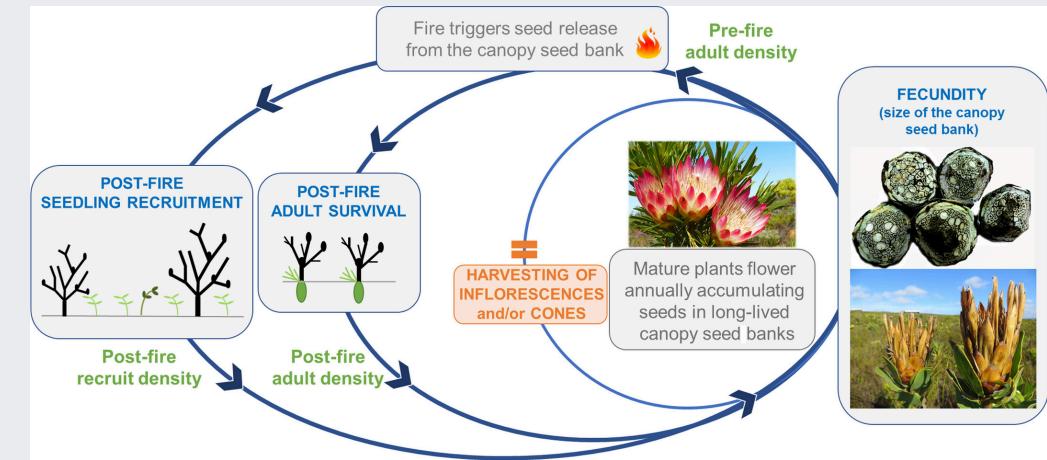
Notice the exogenous effect of aridity on *Protea repens* seedling establishment at the arid inland site (Figure 1, bottom).



# Protea density-dependence

They fed their empirical data into demographic models and projected population growth over multiple generations.

Note that generations and fires are synonymous, because serotinous Proteaceae mostly only recruit after fire.



Bond et al 1995

Figure from Treurnicht et al 2021. Ignore the harvesting...

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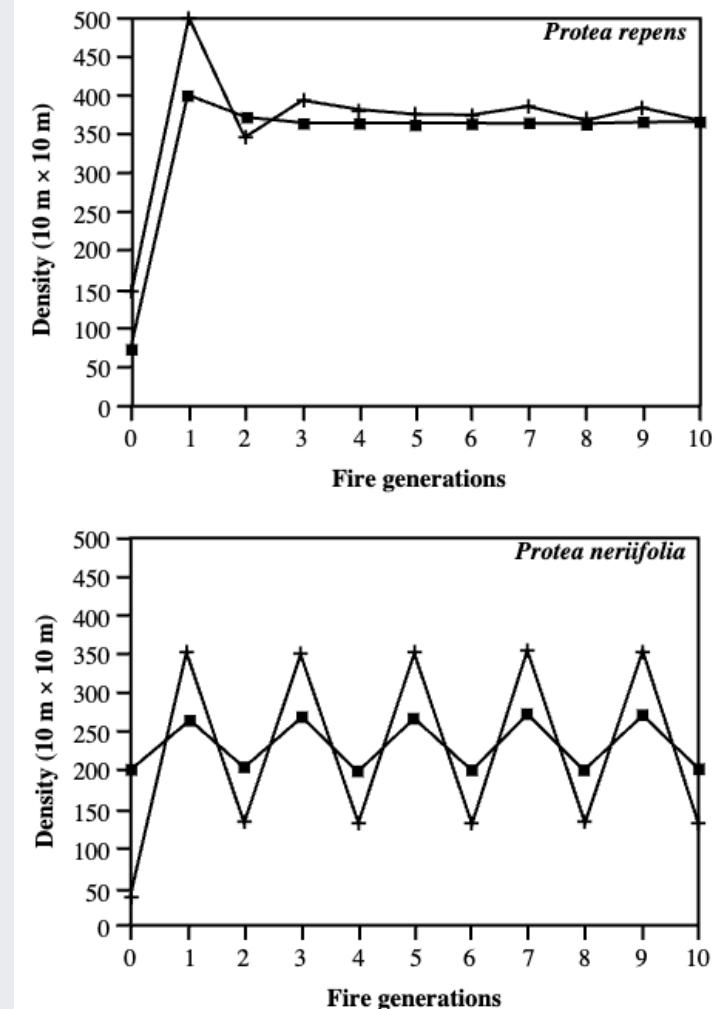


FIGURE 5. Graphic interpolation of population trajectories derived from the curves shown in Figure 4 (see Symonides, Silvertown & Andreasen, 1986 for the procedure used). The population trajectories were adjusted for seeds per cone, seed survival through fire and first dry season seedling mortality using data from Maze & Bond (1995) collected after an experimental burn. The different trajectories for each species indicate sensitivity to initial starting populations.  $N_0$  for *P. repens* = 75 (squares), 150 (crosses).  $N_0$  for *P. nerifolia* = 50 (crosses), 200 (squares).

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Note that generations and fires are synonymous, because serotinous Proteaceae mostly only recruit after fire.

Decreasing the starting population size ( $N_0$ ), which would reduce the initial effect of density on population growth, increased the amplitude of population fluctuations, creating risk of total population crashes.

This effect was stronger in *P. nerifolia*, because it had higher cone production (fecundity) and was more sensitive to population density.

Bond et al 1995

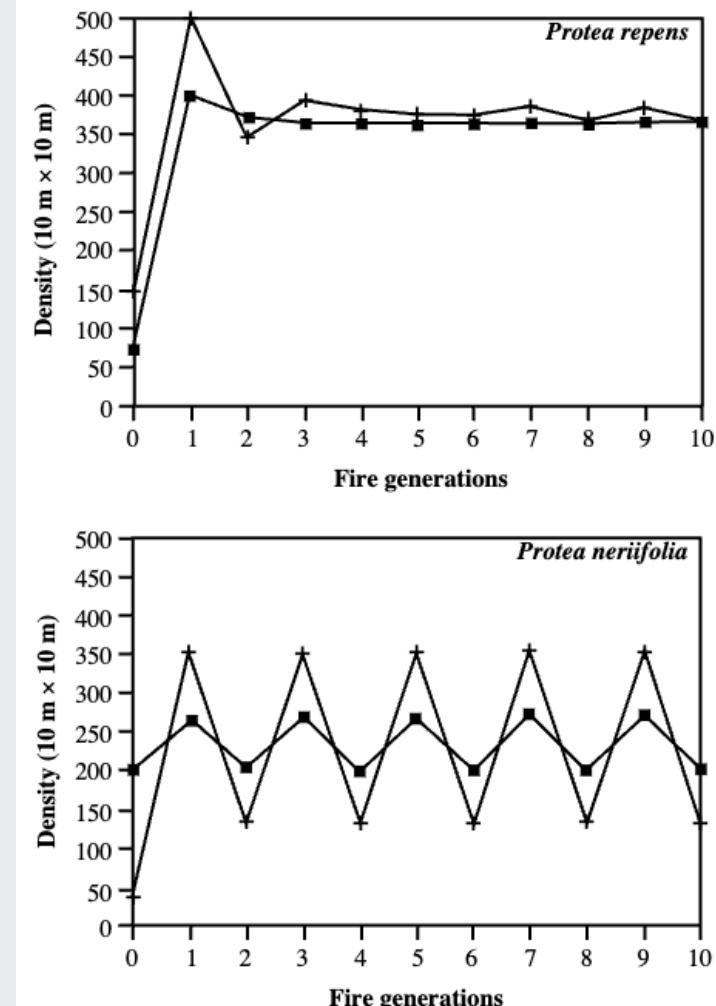


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# How does this relate to the original question at the start of the lecture?

## The Hutchinsonian Niche

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Does the occurrence of a species at a locality mean it is able to maintain a viable population there...?

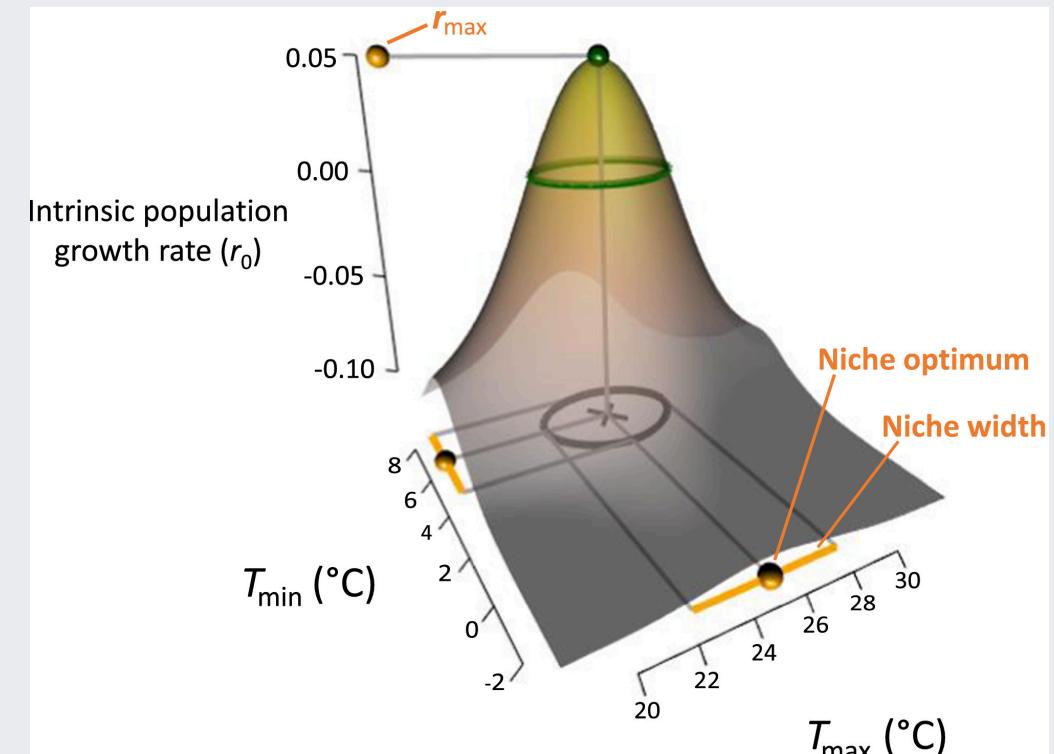


Figure from Treurnicht et al. 2020

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Does the occurrence of a species at a locality mean it is able to maintain a viable population there...?

No! We need estimates of their population growth rate ( $r$ ).

We can estimate population growth rate ( $r$ ) from demographic parameters that we can measure in the field (e.g. birth, death and dispersal rates) using demographic models.

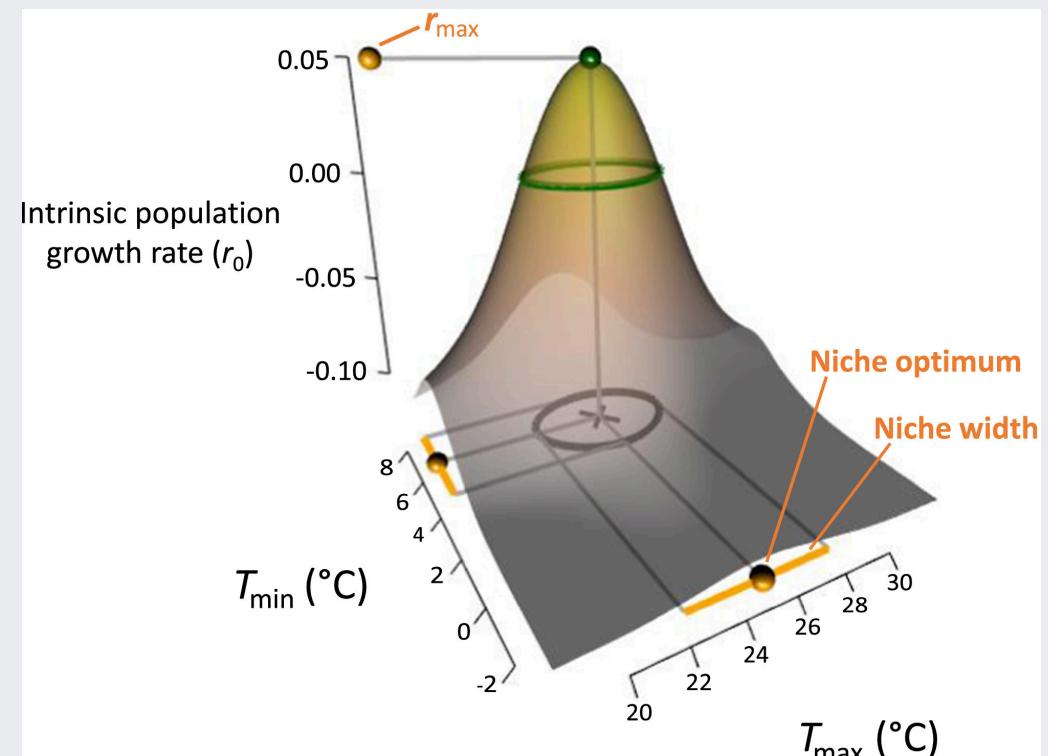


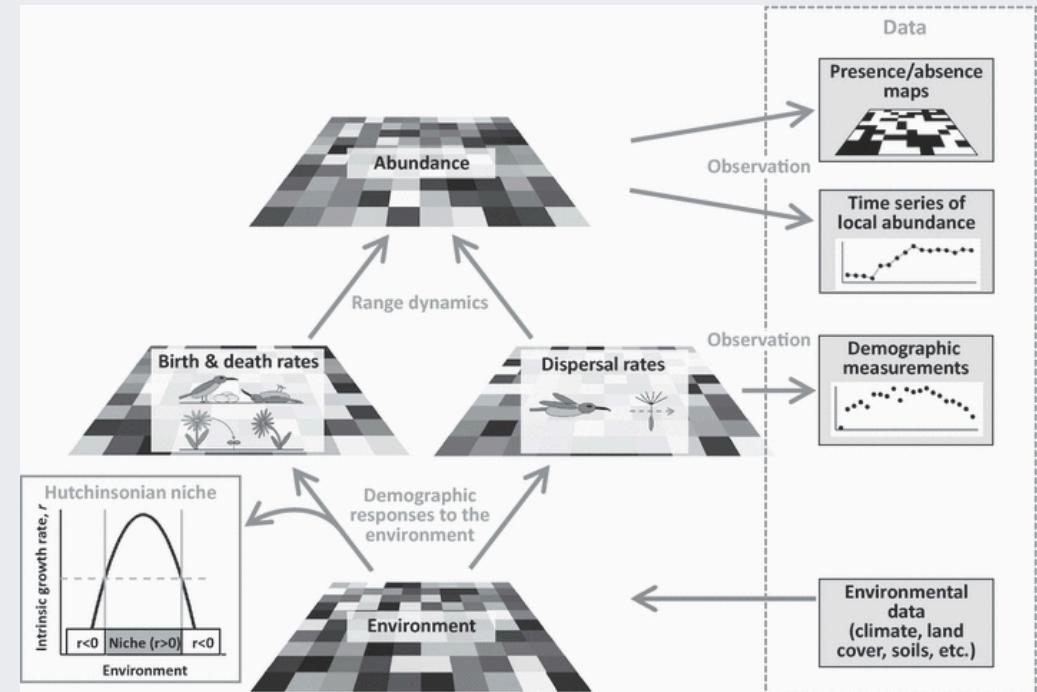
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# How does this relate to SDMs?

We can build SDMs based on demographic models that estimate population growth across different environmental conditions.



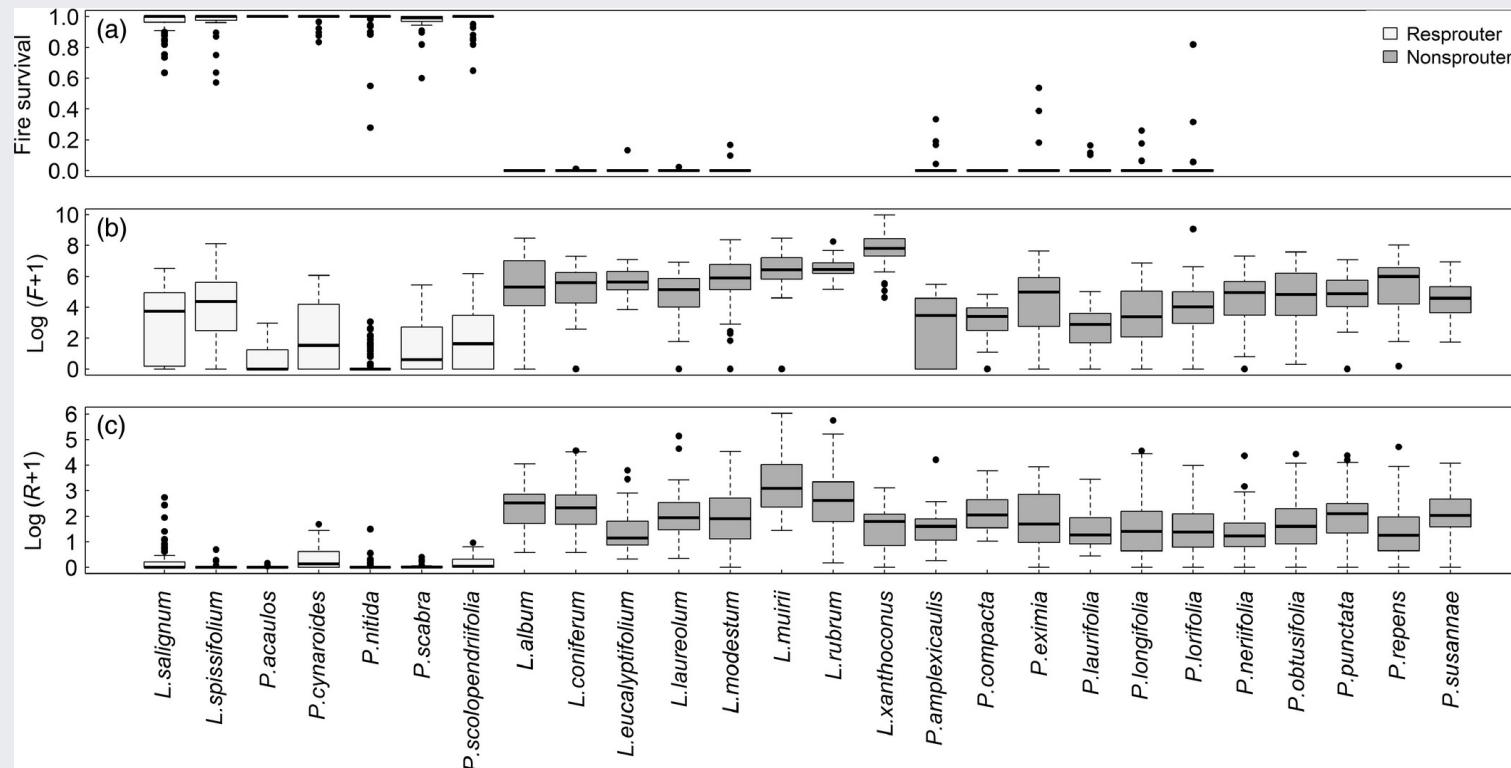
These types of SDMs are often called Demographic Distribution Models (DDMs), and can tell us where species should be able to maintain a viable population!



Schurr et al. 2012

# How does this relate to SDMs?

Interestingly, positive population growth can be maintained using very different strategies.



Here seeding vs sprouting serotinous Proteaceae show classic differentiation on the  $r$  (invest in recruitment) vs  $K$  (invest in survival) life history strategy spectrum (**Treurnicht et al. 2020**).

# Take-home

*If population growth were density-independent, it would be exponential...*

*Most species exhibit density-dependent population growth due to intraspecific competition and other density-dependent factors (e.g. disease transmission), thus self-regulating their population size.*

*Density-dependence creates an endogenous control on populations and has big implications for their size and stability.*

*One needs estimates of population growth rates to know whether populations can be maintained and define the environmental conditions of the Hutchinsonian niche. This can be done if you can estimate birth, death and dispersal rates.*

*Newer SDMs can include a demographic modelling component to map species distributions based on the Hutchinsonian niche.*

# Thanks!

Slides created via the R packages:

**xaringan**  
gadenbuie/xaringanthemer

The chakra comes from remark.js, **knitr**, and R Markdown.