Course Handout (Part II)

Date: 23/7/2016

Course No. MATH F445
Course Title Mathematical Fluid Dynamics

Instructor-in-Charge ASHISH TIWARI

1. Scope & Objective of the Course

This course is an introduction to the field of fluid dynamics. The objective of the course is to present some of the basic ideas of fluid dynamics in a mathematically attractive manner (which does not mean "fully rigorous"); the physical background and motivation for some constructions that have been used in recent mathematical and numerical work on the Navier–Stokes equations; and to grow interest among the students in this beautiful and difficult subject.

- 2. Text Book
- i. Introduction to Mathematical Fluid Dynamics, R. E. Meyer, Dover Publisher, 2007(4th Edition),
- ii. Fluid Mechanics, P.K.Kundu & I.M.Cohen, 3rd Edition, Elsevier, 2005.
- 3. Reference Books
- *i.* Mathematical Introduction to Fluid Mechanics by Chorin, Springer-Verlag, Fourth Edition, 2000.
- ii. A Text Book of Fluid Dynamics, F. Charlton, CBC, Reprint 1998.
- *iii.* Computational Fluid Dynamics: The Basics with Applications, J.D. Anderson, Jr, McGraw Hill International Edition, 1995.
- iv. Boundary-Layer Theory, H Schlichting, K. Gersten, Springer, 1999.
- v. A Treatise on Hydrodynamics ,W. H. Besant and A. S. Ramsey, CBS Publishers, Delhi, 1988.

| Tuonsiers, Denn, 1700. | | | | | | | |
|------------------------|---|--|--|--|--|--|--|
| 4. | Course Plan | | | | | | |
| Lec. No. | Learner's Objective | Topic to be Covered | Reference (Text Book) | | | | |
| 1-6 | Introduction to the Fluid Dynamics and Fundamental Concepts , Different Approaches to Analyze Fluid Motion and Their Equivalence | Introduction, Solids, Liquids, and Gas, Lagrange and Eulerian Descriptions, Continuum hypothesis, Conservation of Mass based on Finite Control Volume Fixed in Space and Moving with the Fluid and hence their equivalence, Equation of Continuity in Cylindrical and Spherical Coordinates, | T1: 1-4 T2:1.1-4, 3.2- 3,4.1-4.3, Appendix-B1 & B3 | | | | |
| 7-13 | Potential Flows and its characteristics | Potential Flow, Laplace Equation, Streamline, Pathline and Streakline, Streamfunction, Vorticity, Line Vortex, Vortex Sheet, one, two- and three-dimensional flow, Sources and Sink, Doublet, Complex Potential of Source and Doublet, Flow and Circulation | T1:5-9, T2: 3.4, 3.12- 13, 6.2, 6.5-7 | | | | |
| 14- 17 | Conservation Laws for Inviscid Flows | Conservation of Linear Momentum, Euler's Equation in Different Coordinate Systems, Bernoulli's equation and its application, | T1: 10-12,15 T2: 4.16-17 | | | | |







| 18- 24 | Conservations of Momentum and Energy | Constitutive equations for Newtonian Fluid, Navier-Stokes Equations in different coordinate systems, First Law of Thermodynamics, Boundary Conditions, Boussinesq approximation. | T1:17- 19,33,35,38 T2: 4.10-11, 4.14, 4.18-19 | | |
|-----------|---|--|--|--|--|
| 25- 30 | Fluid of Small/High Viscosity, Laminar Flows | Reynolds number, High and Low Reynolds number Flows, Dimensional Analysis, Exact Solution of Navier-Stokes Equation: Couette-Poiseuille Flows, Stokes' Creeping Flows around a Sphere, A singular perturbation example | | | |
| 31- 33 | Boundary Layers | Introduction, Boundary Layer Approximations, Setting up the Boundary- Layer Equations, Different measure of Boundary Layer Thickness | T2:10.1-3, | | |
| 34-40 | Limiting cases of Boundary Layer Flows | 3 3 | | | |

5. Evaluation Scheme:

| Component | Duration | Weightage | Date | Remarks |
|------------------------------|----------|-----------|--------------------------|--|
| Mid Term Exam | 90 Min | 30% | 3/10 10:00 - 11:30 AM | СВ |
| Comprehensive Examination | 3 Hours | 40% | 1/12 FN | CB/OB (details will be announced in class) |
| Quizzes/Assign ments | 30 Min | 30% | *** | CB/OB |

- *** To be announced later.
- **7. Notices:** All notices regarding the course MATH F445 will be put on online notice (NALANDA) and Mathematics department notice board.
- **8. Make up Policy:** For mid-semester and comprehensive examinations, make up will be given only in genuine cases and for that prior permission has to be obtained. For quizzes/assignments, there will be no make up in any circumstances.
- **9. Chamber consultation hours:** To be announced in the class.

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