Course Handout for ME G512 Finite Element Methods

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Course Content

Introduction

- Lec. 1 Introduction to FEA, problem classification, modeling and discretisation.
- Lec. 2-3 Interpolation, elements, nodes, dof, history & applications of FEA, solving a problem using FEA.

1-D Elements

- Lec.4 Bar element, beam element, with arbitrary orientation.
- Lec.5-6 Assembly of elements, properties of stifness matrices and boundary conditions.
- Lec.7 Mechanical and thermal loads, stresses.
- Lec.8 Solved Examples

Basic Elements

- Lec.9 Interpolation and shape functions.
- Lec.10 Formulae for element matrices.
- Lec.11 Linear triangle and bilinear rectangle.
- Lec.12-14 Choice of interpolation functions, improved triangles and quadrilaterals, nodal loads.

Variational Methods

- Lec.15 Introduction to functional, strong and weak forms, principle of stationary potential energy.
- Lec. 16 Potential energy of an elastic body.
- Lec.17 Rayleigh-Ritz method.
- Lec.18 Strong and weak forms.
- Lec.19-20 Finite element form of the Rayleigh-Ritz method.

Weighted Residual Methods

- Lec.21 Galerkin method.
- Lec.22 Other methods of weighted residuals.
- Lec.23-24 Galerkin FEM in 1-D: Beam dynamics and heat ?ow in a bar.
- Lec.25 Galerkin FEM in 2-D.
- Lec.26 Mixed formulation.

Isoparametric Elements

- Lec.27 Introduction, bilinear quadrilateral.
- Lec.28 Quadrature.
- Lec.29 Quadratic quadrilaterals.
- Lec.30 Hexahedral isoparametric elements.
- Lec.31 Incompatible modes, nodeless dof.
- Lec.32 Load considerations.
- Lec.33 Stress calculations.

FEA in Structural Dynamics and Vibrations

- Lec.34 Equations, mass and damping matrices.
- Lec.35 Mass matrices: Consistent, diagonal and others.
- Lec.36 Natural frequencies and modes, damping
- Lec.37 Reduction of number of dofs.
- Lec.38 Modal methods.
- Lec.39 Ritz vectors.
- Lec.40 Component mode synthesis.

Evaluation Scheme

- Project + Assignments 35%
- Mid-term Exam 25%
- Comprehensive Exam 40%

Examination Schedule

Mid-term Exam: 7/10 8:00 - 9:30 AM

Comprehensive Exam: Afternoon 10/12 AN

Textbooks

1. Cook, Robert D., 'Concepts and applications of finite element analysis', *Wiley India Pvt. Ltd.*

Reference books

- 1. Reddy, J. N., 'Introduction to finite element method', Tata McGraw Hill.
- 2. Shames, Irving H., Dymn, Clyve L., 'Energy and finite element methods in structural analysis', *Taylor & Francis*.