

# Final Research

December 10, 2018

## 1 Forecasting Web Traffic

```
In [1]: # Importing necessary packages
import pandas as pd
import numpy as np

import seaborn as sns
import scipy.stats as ss
import pylab as pl
from statsmodels.tsa.arima_model import ARMAResults
import statsmodels.api as sm
import statsmodels.graphics.tsaplots as tsa
from statsmodels.graphics import utils
from statsmodels.tsa.stattools import acf, pacf, acovf
import statsmodels.formula.api as smf
import statsmodels.tsa.api as smt
from statsmodels.tsa.ar_model import AR

import matplotlib.pyplot as plt
import matplotlib as mpl
from IPython.display import HTML, display
import tabulate
from arch import arch_model

In [2]: # Import .csv files
# Facebook Wikipedia page
sampledata = pd.read_csv("C:/Users/Diana/Documents/University of Waterloo/" + \
                        "4th Year/ECON 423/Final Project/Facebook_Sample.csv")

sampledatasort=sampledata.sort_values(["Facebook"])
print(sampledatasort)
```

|     | Date      | Facebook |
|-----|-----------|----------|
| 40  | 8/10/2015 | 17       |
| 48  | 8/18/2015 | 17       |
| 71  | 9/10/2015 | 17       |
| 57  | 8/27/2015 | 18       |
| 127 | 11/5/2015 | 18       |

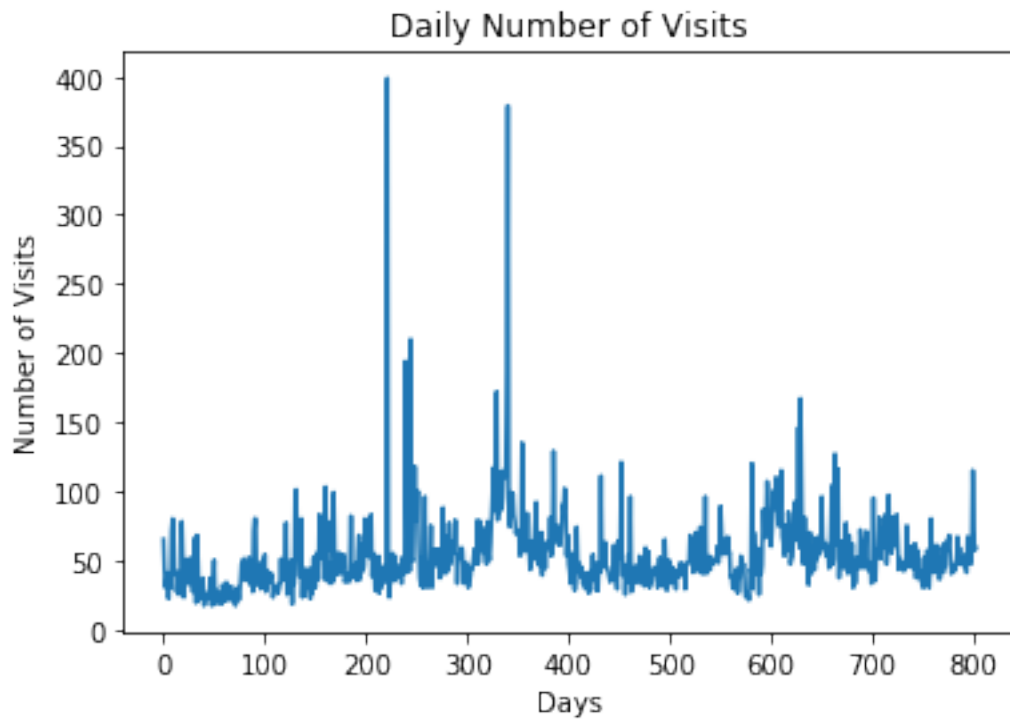
|     |            |     |
|-----|------------|-----|
| 51  | 8/21/2015  | 18  |
| 47  | 8/17/2015  | 18  |
| 32  | 8/2/2015   | 19  |
| 52  | 8/22/2015  | 20  |
| 55  | 8/25/2015  | 20  |
| 61  | 8/31/2015  | 20  |
| 578 | 1/29/2017  | 21  |
| 54  | 8/24/2015  | 21  |
| 65  | 9/4/2015   | 21  |
| 35  | 8/5/2015   | 21  |
| 68  | 9/7/2015   | 21  |
| 74  | 9/13/2015  | 21  |
| 72  | 9/11/2015  | 22  |
| 60  | 8/30/2015  | 22  |
| 38  | 8/8/2015   | 22  |
| 41  | 8/11/2015  | 22  |
| 5   | 7/6/2015   | 22  |
| 75  | 9/14/2015  | 22  |
| 56  | 8/26/2015  | 22  |
| 145 | 11/23/2015 | 22  |
| 45  | 8/15/2015  | 22  |
| 42  | 8/12/2015  | 22  |
| 575 | 1/26/2017  | 23  |
| 44  | 8/14/2015  | 23  |
| 137 | 11/15/2015 | 23  |
| ..  | ...        | ... |
| 660 | 4/21/2017  | 104 |
| 609 | 3/1/2017   | 104 |
| 327 | 5/23/2016  | 106 |
| 596 | 2/16/2017  | 107 |
| 333 | 5/29/2016  | 109 |
| 605 | 2/25/2017  | 110 |
| 337 | 6/2/2016   | 110 |
| 432 | 9/5/2016   | 111 |
| 331 | 5/27/2016  | 114 |
| 240 | 2/26/2016  | 114 |
| 610 | 3/2/2017   | 115 |
| 336 | 6/1/2016   | 115 |
| 799 | 9/7/2017   | 115 |
| 666 | 4/27/2017  | 116 |
| 338 | 6/3/2016   | 116 |
| 326 | 5/22/2016  | 117 |
| 248 | 3/5/2016   | 118 |
| 581 | 2/1/2017   | 120 |
| 452 | 9/25/2016  | 121 |
| 663 | 4/24/2017  | 127 |
| 385 | 7/20/2016  | 129 |
| 354 | 6/19/2016  | 135 |

|     |           |     |
|-----|-----------|-----|
| 627 | 3/19/2017 | 146 |
| 629 | 3/21/2017 | 167 |
| 329 | 5/25/2016 | 172 |
| 339 | 6/4/2016  | 186 |
| 239 | 2/25/2016 | 194 |
| 244 | 3/1/2016  | 210 |
| 340 | 6/5/2016  | 379 |
| 221 | 2/7/2016  | 399 |

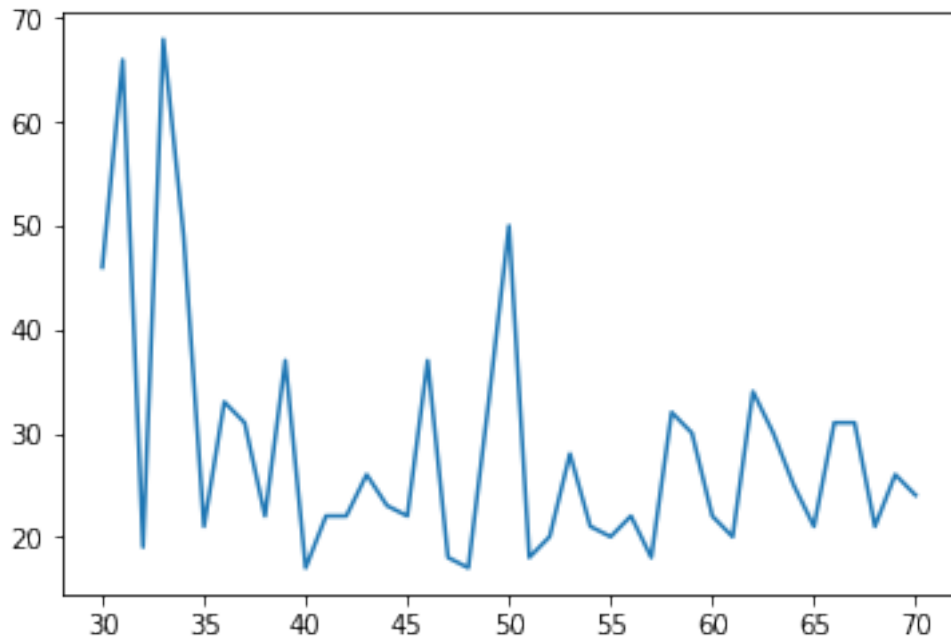
[803 rows x 2 columns]

## 1.1 Basic Data

```
In [3]: plt.plot(sampledata["Facebook"])
plt.title("Daily Number of Visits")
plt.xlabel("Days")
plt.ylabel("Number of Visits")
plt.show()
```



```
In [4]: plt.plot(sampledata["Facebook"][30:71])
plt.show()
```



Mention stuff in units and say that the actual units are not disclosed by the publisher of the code.

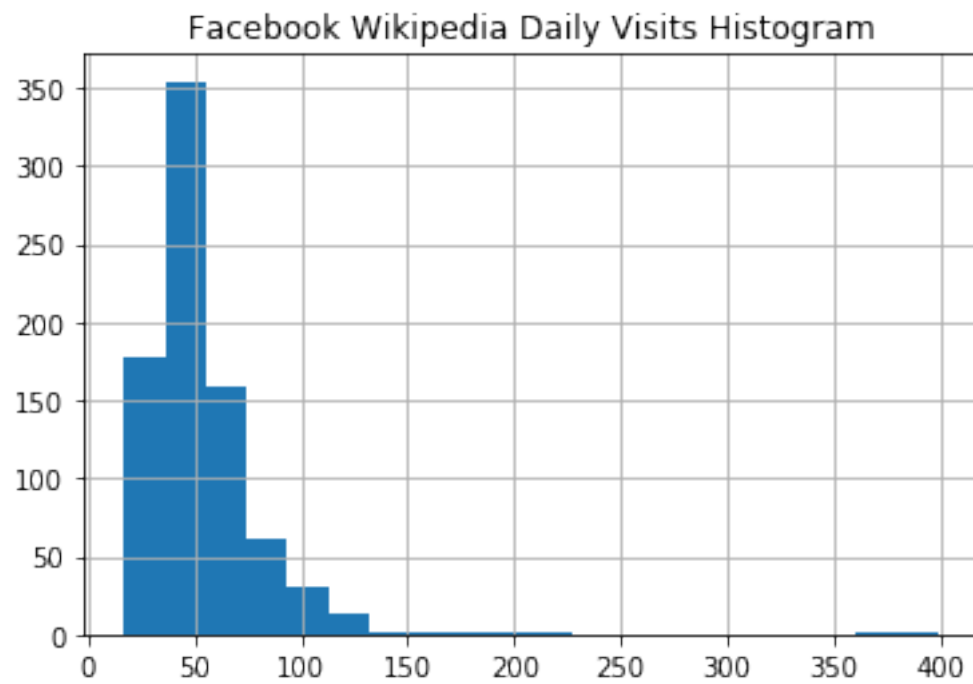
There is a weekly trend.

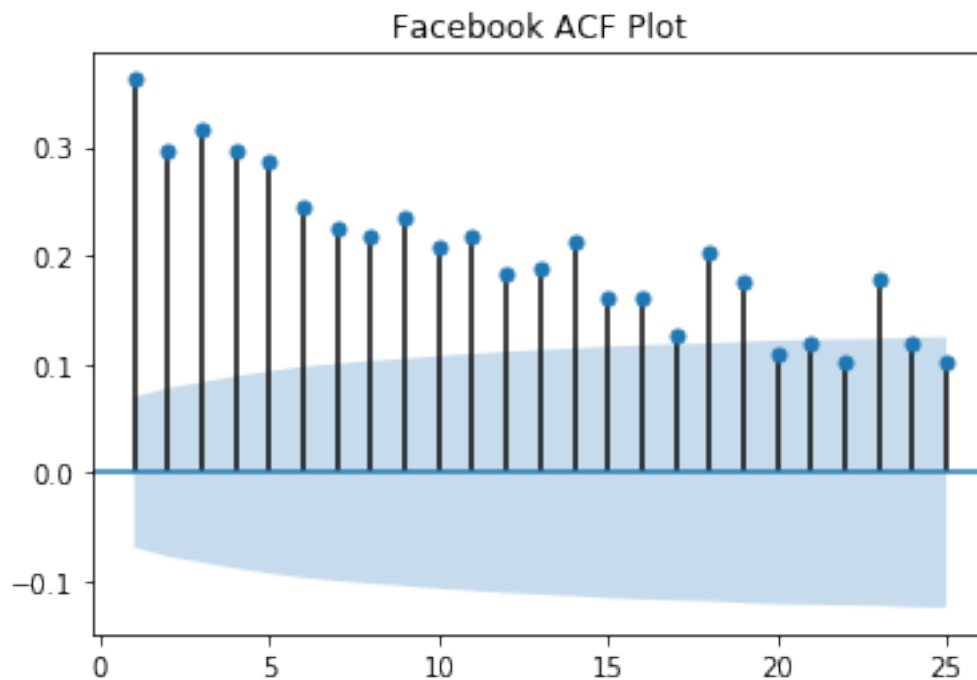
```
In [5]: def basic(df,column, histtitle,title,titlelist):
        # histogram
        df.hist(column=column, bins=20)
        pl.title(histtitle)
        # ACF plot
        data_acfplot = tsa.plot_acf(x=df[column], ax=None,
                                     lags=25, alpha=.05, use_vlines=True,
                                     unbiased=False,fft=False, title=title,
                                     zero=False, vlines_kwargs=None)

        mean_data=np.mean(df[column])
        var_data=np.var(df[column])
        skew_data=df[column].skew(skipna=True)
        kurtosis_data=df[column].kurtosis()
        print(titlelist)
        print("Mean: " + str(mean_data))
        print("Variance: " + str(var_data))
        print("Skewness(scipy): " + str(skew_data))
        print("Kurtosis: " + str(kurtosis_data))
        print("")
```

```
In [6]: basic(sampleddata,"Facebook", "Facebook Wikipedia Daily Visits Histogram",
              "Facebook ACF Plot","---Facebook Daily Visits---")
```

---Facebook Daily Visits---  
Mean: 53.612702366127024  
Variance: 820.3991910782885  
Skewness(scipy): 5.00691203231403  
Kurtosis: 48.63380282083746





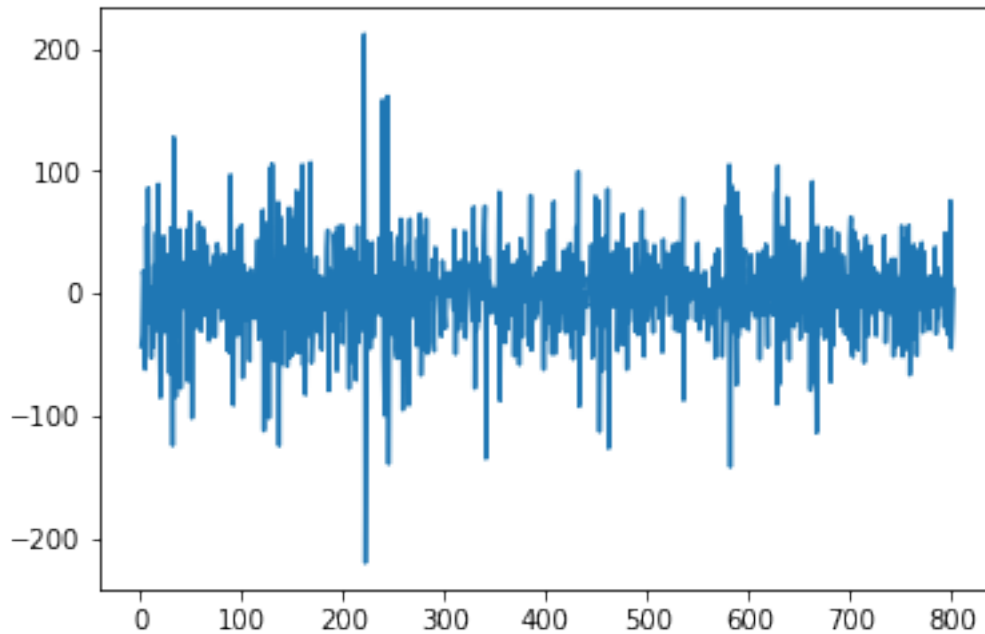
## 1.2 Change Data

```
In [7]: sampledata["FBChange"] = 100*(np.log(sampledata["Facebook"]) - \
      np.log(sampledata["Facebook"].shift(1)))
      sampledata = sampledata.iloc[1:]
      print(len(sampledata["FBChange"]))
```

802

```
In [8]: plt.plot(sampledata["FBChange"])
```

```
Out[8]: [<matplotlib.lines.Line2D at 0x27b0c6be588>]
```



```
In [9]: for i in range(1,5):
        for j in range(1,5):
            garch = arch_model(sampledata["FBChange"], p=i, q=j)
            garch_resid = garch.fit(dis='off')
            print(garch_resid.summary())
```

#### Constant Mean - GARCH Model Results

```
=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:      -0.000
Vol Model:             GARCH        Log-Likelihood:     -4063.77
Distribution:          Normal       AIC:               8135.54
Method:               Maximum Likelihood  BIC:              8154.29
                                     No. Observations:    802
Date:                 Mon, Dec 10 2018  Df Residuals:      798
Time:                 02:44:17      Df Model:          4
```

#### Mean Model

```
=====
              coef      std err          t      P>|t|  95.0% Conf. Int.
-----
mu           0.3932      1.020        0.386    0.700  [-1.606,  2.392]
```

#### Volatility Model

```
=====
              coef      std err          t      P>|t|  95.0% Conf. Int.
-----
omega        688.9091    150.450        4.579  4.672e-06  [3.940e+02,9.838e+02]
```

|          |        |           |       |           |                    |
|----------|--------|-----------|-------|-----------|--------------------|
| alpha[1] | 0.3840 | 7.056e-02 | 5.443 | 5.245e-08 | [ 0.246, 0.522]    |
| beta[1]  | 0.2263 | 9.425e-02 | 2.401 | 1.635e-02 | [4.157e-02, 0.411] |

=====

Covariance estimator: robust

Constant Mean - GARCH Model Results

=====

|                |                    |                   |          |
|----------------|--------------------|-------------------|----------|
| Dep. Variable: | FBChange           | R-squared:        | -0.000   |
| Mean Model:    | Constant Mean      | Adj. R-squared:   | -0.000   |
| Vol Model:     | GARCH              | Log-Likelihood:   | -4063.76 |
| Distribution:  | Normal             | AIC:              | 8137.52  |
| Method:        | Maximum Likelihood | BIC:              | 8160.96  |
|                |                    | No. Observations: | 802      |
| Date:          | Mon, Dec 10 2018   | Df Residuals:     | 797      |
| Time:          | 02:44:17           | Df Model:         | 5        |

Mean Model

=====

|    | coef   | std err | t     | P> t  | 95.0% Conf. Int. |
|----|--------|---------|-------|-------|------------------|
| mu | 0.3971 | 1.021   | 0.389 | 0.697 | [-1.604, 2.398]  |

Volatility Model

=====

|          | coef     | std err   | t         | P> t      | 95.0% Conf. Int.       |
|----------|----------|-----------|-----------|-----------|------------------------|
| omega    | 688.6609 | 148.924   | 4.624     | 3.760e-06 | [3.968e+02, 9.805e+02] |
| alpha[1] | 0.3855   | 7.093e-02 | 5.434     | 5.503e-08 | [ 0.246, 0.524]        |
| beta[1]  | 0.2105   | 0.254     | 0.829     | 0.407     | [-0.287, 0.708]        |
| beta[2]  | 0.0142   | 0.213     | 6.672e-02 | 0.947     | [-0.403, 0.432]        |

=====

Covariance estimator: robust

Constant Mean - GARCH Model Results

=====

|                |                    |                   |          |
|----------------|--------------------|-------------------|----------|
| Dep. Variable: | FBChange           | R-squared:        | -0.000   |
| Mean Model:    | Constant Mean      | Adj. R-squared:   | -0.000   |
| Vol Model:     | GARCH              | Log-Likelihood:   | -4063.76 |
| Distribution:  | Normal             | AIC:              | 8139.52  |
| Method:        | Maximum Likelihood | BIC:              | 8167.65  |
|                |                    | No. Observations: | 802      |
| Date:          | Mon, Dec 10 2018   | Df Residuals:     | 796      |
| Time:          | 02:44:17           | Df Model:         | 6        |

Mean Model

=====

|    | coef   | std err | t     | P> t  | 95.0% Conf. Int. |
|----|--------|---------|-------|-------|------------------|
| mu | 0.3971 | 1.019   | 0.390 | 0.697 | [-1.601, 2.395]  |

Volatility Model



|          | coef       | std err   | t         | P> t      | 95.0% Conf. Int.       |
|----------|------------|-----------|-----------|-----------|------------------------|
| omega    | 688.6269   | 206.419   | 3.336     | 8.497e-04 | [2.841e+02, 1.093e+03] |
| alpha[1] | 0.3855     | 8.230e-02 | 4.684     | 2.814e-06 | [ 0.224, 0.547]        |
| beta[1]  | 0.2106     | 0.265     | 0.796     | 0.426     | [ -0.308, 0.729]       |
| beta[2]  | 0.0141     | 0.227     | 6.218e-02 | 0.950     | [ -0.431, 0.459]       |
| beta[3]  | 2.1866e-14 | 0.103     | 2.130e-13 | 1.000     | [ -0.201, 0.201]       |

Covariance estimator: robust

#### Constant Mean - GARCH Model Results

```

=====
Dep. Variable:          FBChange      R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:     -0.000
Vol Model:             GARCH          Log-Likelihood:    -4063.74
Distribution:          Normal         AIC:              8141.48
Method:               Maximum Likelihood BIC:            8174.29
                               No. Observations:         802
Date:                 Mon, Dec 10 2018 Df Residuals:       795
Time:                 02:44:18        Df Model:          7
=====

```

#### Mean Model

|    | coef   | std err | t     | P> t  | 95.0% Conf. Int. |
|----|--------|---------|-------|-------|------------------|
| mu | 0.4041 | 1.020   | 0.396 | 0.692 | [ -1.595, 2.403] |

#### Volatility Model

|          | coef       | std err   | t         | P> t      | 95.0% Conf. Int.       |
|----------|------------|-----------|-----------|-----------|------------------------|
| omega    | 676.4021   | 216.182   | 3.129     | 1.755e-03 | [2.527e+02, 1.100e+03] |
| alpha[1] | 0.3838     | 9.634e-02 | 3.984     | 6.775e-05 | [ 0.195, 0.573]        |
| beta[1]  | 0.2177     | 0.297     | 0.734     | 0.463     | [ -0.364, 0.799]       |
| beta[2]  | 7.4322e-03 | 0.228     | 3.255e-02 | 0.974     | [ -0.440, 0.455]       |
| beta[3]  | 2.3121e-14 | 0.220     | 1.049e-13 | 1.000     | [ -0.432, 0.432]       |
| beta[4]  | 8.1214e-03 | 7.043e-02 | 0.115     | 0.908     | [ -0.130, 0.146]       |

Covariance estimator: robust

#### Constant Mean - GARCH Model Results

```

=====
Dep. Variable:          FBChange      R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:     -0.000
Vol Model:             GARCH          Log-Likelihood:    -4063.77
Distribution:          Normal         AIC:              8137.54
Method:               Maximum Likelihood BIC:            8160.97
                               No. Observations:         802
Date:                 Mon, Dec 10 2018 Df Residuals:       797
Time:                 02:44:18        Df Model:          5
=====

```

| Mean Model       |          |           |       |           |                       |
|------------------|----------|-----------|-------|-----------|-----------------------|
|                  | coef     | std err   | t     | P> t      | 95.0% Conf. Int.      |
| mu               | 0.3930   | 1.019     | 0.386 | 0.700     | [-1.605, 2.391]       |
| Volatility Model |          |           |       |           |                       |
|                  | coef     | std err   | t     | P> t      | 95.0% Conf. Int.      |
| omega            | 689.2563 | 245.728   | 2.805 | 5.032e-03 | [2.076e+02,1.171e+03] |
| alpha[1]         | 0.3840   | 7.001e-02 | 5.485 | 4.129e-08 | [ 0.247, 0.521]       |
| alpha[2]         | 0.0000   | 0.113     | 0.000 | 1.000     | [-0.221, 0.221]       |
| beta[1]          | 0.2261   | 0.236     | 0.959 | 0.338     | [-0.236, 0.688]       |

Covariance estimator: robust

#### Constant Mean - GARCH Model Results

```

=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:      -0.000
Vol Model:             GARCH         Log-Likelihood:     -4063.65
Distribution:          Normal        AIC:                8139.30
Method:               Maximum Likelihood  BIC:                8167.43
                               No. Observations:          802
Date:                 Mon, Dec 10 2018  Df Residuals:        796
Time:                 02:44:18         Df Model:            6
=====

```

| Mean Model       |            |           |           |           |                        |
|------------------|------------|-----------|-----------|-----------|------------------------|
|                  | coef       | std err   | t         | P> t      | 95.0% Conf. Int.       |
| mu               | 0.3958     | 1.023     | 0.387     | 0.699     | [-1.609, 2.401]        |
| Volatility Model |            |           |           |           |                        |
|                  | coef       | std err   | t         | P> t      | 95.0% Conf. Int.       |
| omega            | 808.5053   | 685.263   | 1.180     | 0.238     | [-5.346e+02,2.152e+03] |
| alpha[1]         | 0.3865     | 7.041e-02 | 5.489     | 4.042e-08 | [ 0.248, 0.524]        |
| alpha[2]         | 0.0714     | 0.384     | 0.186     | 0.853     | [-0.682, 0.825]        |
| beta[1]          | 5.4312e-16 | 1.000     | 5.432e-16 | 1.000     | [-1.960, 1.960]        |
| beta[2]          | 0.0839     | 0.232     | 0.362     | 0.717     | [-0.370, 0.538]        |

Covariance estimator: robust

#### Constant Mean - GARCH Model Results

```

=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:      -0.000
Vol Model:             GARCH         Log-Likelihood:     -4063.65
=====

```

Distribution: Normal AIC: 8141.30  
Method: Maximum Likelihood BIC: 8174.11  
No. Observations: 802  
Date: Mon, Dec 10 2018 Df Residuals: 795  
Time: 02:44:18 Df Model: 7

Mean Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
mu           0.3956      1.020      0.388    0.698 [ -1.603,  2.394]
```

Volatility Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
omega        808.5539    665.980      1.214    0.225 [-4.967e+02,2.114e+03]
alpha[1]      0.3865    8.213e-02     4.706  2.525e-06 [  0.226,  0.547]
alpha[2]      0.0714     0.357     0.200    0.842 [ -0.629,  0.771]
beta[1]       0.0000     0.922     0.000    1.000 [ -1.807,  1.807]
beta[2]       0.0839     0.197     0.425    0.671 [ -0.303,  0.471]
beta[3]       1.1111e-13   0.126  8.804e-13    1.000 [ -0.247,  0.247]
```

Covariance estimator: robust

Constant Mean - GARCH Model Results

```
=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:             Constant Mean  Adj. R-squared:      -0.000
Vol Model:              GARCH         Log-Likelihood:     -4063.65
Distribution:           Normal        AIC:                8143.30
Method:                 Maximum Likelihood  BIC:                8180.80
No. Observations:      802
Date:                  Mon, Dec 10 2018  Df Residuals:      794
Time:                  02:44:18         Df Model:           8
```

Mean Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
mu           0.3968      1.020      0.389    0.697 [ -1.603,  2.396]
```

Volatility Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
omega        806.0572    544.122      1.481    0.139 [-2.604e+02,1.873e+03]
alpha[1]      0.3864    8.219e-02     4.701  2.588e-06 [  0.225,  0.547]
alpha[2]      0.0714     0.274     0.261    0.794 [ -0.466,  0.608]
beta[1]       0.0000     0.685     0.000    1.000 [ -1.343,  1.343]
beta[2]       0.0835     0.137     0.611    0.541 [ -0.185,  0.352]
beta[3]       1.3035e-13   0.127  1.023e-12    1.000 [ -0.250,  0.250]
```

```
beta[4]      1.8499e-03  3.449e-02  5.364e-02      0.957 [-6.575e-02,6.945e-02]
```

```
Covariance estimator: robust
```

# Constant Mean - GARCH Model Results

```
=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:             Constant Mean  Adj. R-squared:      -0.000
Vol Model:              GARCH        Log-Likelihood:     -4063.31
Distribution:           Normal       AIC:               8138.62
Method:                Maximum Likelihood BIC:             8166.75
                               No. Observations:          802
Date:                  Mon, Dec 10 2018 Df Residuals:       796
Time:                  02:44:18      Df Model:             6
```

## Mean Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
mu           0.3633      1.020        0.356      0.722 [ -1.635,  2.362]
```

## Volatility Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
omega       878.1694     801.306        1.096      0.273 [-6.924e+02,2.449e+03]
alpha[1]     0.3821     6.970e-02        5.481  4.223e-08 [  0.245,  0.519]
alpha[2]     0.0779      0.360        0.216      0.829 [ -0.628,  0.784]
alpha[3]     0.0433      0.104        0.417      0.676 [ -0.160,  0.247]
beta[1]      0.0000      0.917        0.000      1.000 [ -1.798,  1.798]
```

```
Covariance estimator: robust
```

# Constant Mean - GARCH Model Results

```
=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:             Constant Mean  Adj. R-squared:      -0.000
Vol Model:              GARCH        Log-Likelihood:     -4063.31
Distribution:           Normal       AIC:               8140.62
Method:                Maximum Likelihood BIC:             8173.43
                               No. Observations:          802
Date:                  Mon, Dec 10 2018 Df Residuals:       795
Time:                  02:44:18      Df Model:             7
```

## Mean Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
mu           0.3634      1.046        0.347      0.728 [ -1.687,  2.413]
```

## Volatility Model

|          | coef       | std err   | t         | P> t      | 95.0% Conf. Int.        |
|----------|------------|-----------|-----------|-----------|-------------------------|
| omega    | 878.1579   | 1190.113  | 0.738     | 0.461     | [-1.454e+03, 3.211e+03] |
| alpha[1] | 0.3821     | 6.914e-02 | 5.526     | 3.270e-08 | [ 0.247, 0.518]         |
| alpha[2] | 0.0779     | 0.402     | 0.194     | 0.846     | [ -0.709, 0.865]        |
| alpha[3] | 0.0433     | 0.599     | 7.232e-02 | 0.942     | [ -1.130, 1.216]        |
| beta[1]  | 0.0000     | 1.286     | 0.000     | 1.000     | [ -2.521, 2.521]        |
| beta[2]  | 1.5146e-15 | 1.805     | 8.391e-16 | 1.000     | [ -3.538, 3.538]        |

Covariance estimator: robust

#### Constant Mean - GARCH Model Results

```

=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:      -0.000
Vol Model:             GARCH         Log-Likelihood:     -4063.31
Distribution:          Normal        AIC:               8142.62
Method:               Maximum Likelihood  BIC:              8180.12
                               No. Observations:          802
Date:                 Mon, Dec 10 2018  Df Residuals:       794
Time:                 02:44:18         Df Model:           8
=====

```

#### Mean Model

|    | coef   | std err | t     | P> t  | 95.0% Conf. Int. |
|----|--------|---------|-------|-------|------------------|
| mu | 0.3643 | 1.017   | 0.358 | 0.720 | [ -1.628, 2.357] |

#### Volatility Model

|          | coef       | std err   | t         | P> t      | 95.0% Conf. Int.        |
|----------|------------|-----------|-----------|-----------|-------------------------|
| omega    | 878.3289   | 666.678   | 1.317     | 0.188     | [-4.283e+02, 2.185e+03] |
| alpha[1] | 0.3819     | 8.442e-02 | 4.524     | 6.073e-06 | [ 0.216, 0.547]         |
| alpha[2] | 0.0778     | 0.410     | 0.190     | 0.849     | [ -0.725, 0.881]        |
| alpha[3] | 0.0432     | 0.450     | 9.606e-02 | 0.923     | [ -0.839, 0.925]        |
| beta[1]  | 3.8960e-13 | 1.318     | 2.956e-13 | 1.000     | [ -2.583, 2.583]        |
| beta[2]  | 1.0220e-13 | 1.503     | 6.802e-14 | 1.000     | [ -2.945, 2.945]        |
| beta[3]  | 7.9815e-14 | 0.198     | 4.027e-13 | 1.000     | [ -0.388, 0.388]        |

Covariance estimator: robust

#### Constant Mean - GARCH Model Results

```

=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:      -0.000
Vol Model:             GARCH         Log-Likelihood:     -4063.30
Distribution:          Normal        AIC:               8144.60
Method:               Maximum Likelihood  BIC:              8186.79
                               No. Observations:          802
=====

```

Date: Mon, Dec 10 2018 Df Residuals: 793  
Time: 02:44:18 Df Model: 9

Mean Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
mu           0.3683       1.013       0.363     0.716  [ -1.618,  2.355]
```

Volatility Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
omega        868.4047     689.416       1.260     0.208 [-4.828e+02,2.220e+03]
alpha[1]      0.3816     8.277e-02       4.610  4.019e-06  [ 0.219,  0.544]
alpha[2]      0.0777      0.229       0.339     0.735  [ -0.372,  0.527]
alpha[3]      0.0434      0.326       0.133     0.894  [ -0.596,  0.682]
beta[1]       3.7843e-13    0.603    6.279e-13     1.000  [ -1.181,  1.181]
beta[2]        0.0000      0.862       0.000     1.000  [ -1.689,  1.689]
beta[3]        0.0000      0.176       0.000     1.000  [ -0.346,  0.346]
beta[4]       6.0439e-03    5.408e-02     0.112     0.911  [-9.996e-02,  0.112]
=====
```

Covariance estimator: robust

Constant Mean - GARCH Model Results

```
=====
Dep. Variable:          FBChange      R-squared:          -0.000
Mean Model:           Constant Mean    Adj. R-squared:       -0.000
Vol Model:             GARCH          Log-Likelihood:     -4063.31
Distribution:          Normal          AIC:                8140.62
Method:               Maximum Likelihood BIC:                8173.43
                               No. Observations:          802
Date:                 Mon, Dec 10 2018 Df Residuals:        795
Time:                 02:44:18 Df Model:                    7
```

Mean Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
mu           0.3632       1.011       0.359     0.720 [ -1.619,  2.346]
```

Volatility Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
omega        878.3928     600.517       1.463     0.144 [-2.986e+02,2.055e+03]
alpha[1]      0.3820     6.941e-02       5.504  3.709e-08  [ 0.246,  0.518]
alpha[2]      0.0778      0.273       0.285     0.776  [ -0.458,  0.614]
alpha[3]      0.0433     5.449e-02       0.794     0.427  [-6.354e-02,  0.150]
alpha[4]      4.3973e-12    6.524e-02    6.740e-11     1.000  [ -0.128,  0.128]
beta[1]        0.0000      0.693       0.000     1.000  [ -1.357,  1.357]
=====
```

Covariance estimator: robust

Constant Mean - GARCH Model Results

```
=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:     -0.000
Vol Model:             GARCH        Log-Likelihood:    -4063.31
Distribution:          Normal        AIC:              8142.62
Method:               Maximum Likelihood  BIC:             8180.12
                               No. Observations:         802
Date:                 Mon, Dec 10 2018  Df Residuals:       794
Time:                 02:44:18        Df Model:           8
=====
```

Mean Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
mu           0.3636      1.025      0.355      0.723 [ -1.645,  2.372]
=====
```

Volatility Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
omega        878.3577    874.861      1.004      0.315 [-8.363e+02,2.593e+03]
alpha[1]      0.3820    6.922e-02     5.519   3.409e-08 [ 0.246,  0.518]
alpha[2]      0.0779     0.370     0.211     0.833 [ -0.647,  0.803]
alpha[3]      0.0433     0.543    7.962e-02     0.937 [ -1.022,  1.108]
alpha[4]    1.1600e-11   6.748e-02   1.719e-10     1.000 [ -0.132,  0.132]
beta[1]        0.0000     1.298     0.000     1.000 [ -2.545,  2.545]
beta[2]        0.0000     1.776     0.000     1.000 [ -3.481,  3.481]
=====
```

Covariance estimator: robust

Constant Mean - GARCH Model Results

```
=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:     -0.000
Vol Model:             GARCH        Log-Likelihood:    -4063.31
Distribution:          Normal        AIC:              8144.62
Method:               Maximum Likelihood  BIC:             8186.81
                               No. Observations:         802
Date:                 Mon, Dec 10 2018  Df Residuals:       793
Time:                 02:44:18        Df Model:           9
=====
```

Mean Model

```
=====
              coef      std err          t      P>|t|   95.0% Conf. Int.
-----
mu           0.3636      1.016      0.358      0.721 [ -1.629,  2.356]
=====
```

Volatility Model

|          | coef       | std err | t         | P> t      | 95.0% Conf. Int.        |
|----------|------------|---------|-----------|-----------|-------------------------|
| omega    | 878.0366   | 720.515 | 1.219     | 0.223     | [-5.341e+02, 2.290e+03] |
| alpha[1] | 0.3821     | 0.149   | 2.572     | 1.011e-02 | [9.091e-02, 0.673]      |
| alpha[2] | 0.0779     | 0.279   | 0.279     | 0.780     | [-0.470, 0.625]         |
| alpha[3] | 0.0434     | 0.391   | 0.111     | 0.912     | [-0.723, 0.810]         |
| alpha[4] | 3.3218e-12 | 0.184   | 1.806e-11 | 1.000     | [-0.361, 0.361]         |
| beta[1]  | 3.4890e-15 | 0.824   | 4.233e-15 | 1.000     | [-1.616, 1.616]         |
| beta[2]  | 2.6051e-14 | 1.126   | 2.314e-14 | 1.000     | [-2.207, 2.207]         |
| beta[3]  | 1.8340e-14 | 0.510   | 3.598e-14 | 1.000     | [-0.999, 0.999]         |

Covariance estimator: robust

#### Constant Mean - GARCH Model Results

```

=====
Dep. Variable:          FBChange    R-squared:          -0.000
Mean Model:            Constant Mean  Adj. R-squared:      -0.000
Vol Model:             GARCH         Log-Likelihood:     -4063.30
Distribution:          Normal        AIC:               8146.60
Method:               Maximum Likelihood  BIC:              8193.47
                                     No. Observations:    802
Date:                 Mon, Dec 10 2018  Df Residuals:       792
Time:                 02:44:18         Df Model:           10
=====

```

#### Mean Model

|    | coef   | std err | t     | P> t  | 95.0% Conf. Int. |
|----|--------|---------|-------|-------|------------------|
| mu | 0.3682 | 1.266   | 0.291 | 0.771 | [-2.113, 2.850]  |

#### Volatility Model

|          | coef       | std err  | t         | P> t  | 95.0% Conf. Int.        |
|----------|------------|----------|-----------|-------|-------------------------|
| omega    | 868.6325   | 1025.415 | 0.847     | 0.397 | [-1.141e+03, 2.878e+03] |
| alpha[1] | 0.3816     | 0.621    | 0.614     | 0.539 | [-0.836, 1.599]         |
| alpha[2] | 0.0776     | 0.747    | 0.104     | 0.917 | [-1.386, 1.541]         |
| alpha[3] | 0.0434     | 1.623    | 2.675e-02 | 0.979 | [-3.138, 3.225]         |
| alpha[4] | 0.0000     | 1.233    | 0.000     | 1.000 | [-2.416, 2.416]         |
| beta[1]  | 6.8849e-11 | 2.888    | 2.384e-11 | 1.000 | [-5.660, 5.660]         |
| beta[2]  | 3.8800e-12 | 4.802    | 8.080e-13 | 1.000 | [-9.412, 9.412]         |
| beta[3]  | 6.0379e-13 | 3.240    | 1.864e-13 | 1.000 | [-6.350, 6.350]         |
| beta[4]  | 5.9904e-03 | 0.235    | 2.551e-02 | 0.980 | [-0.454, 0.466]         |

Covariance estimator: robust

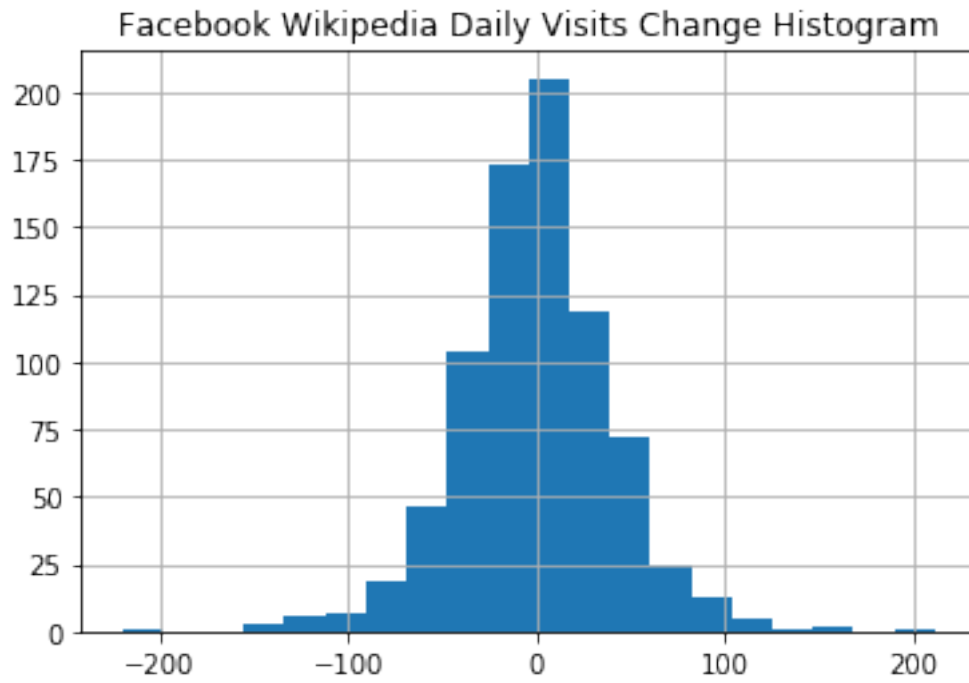
```

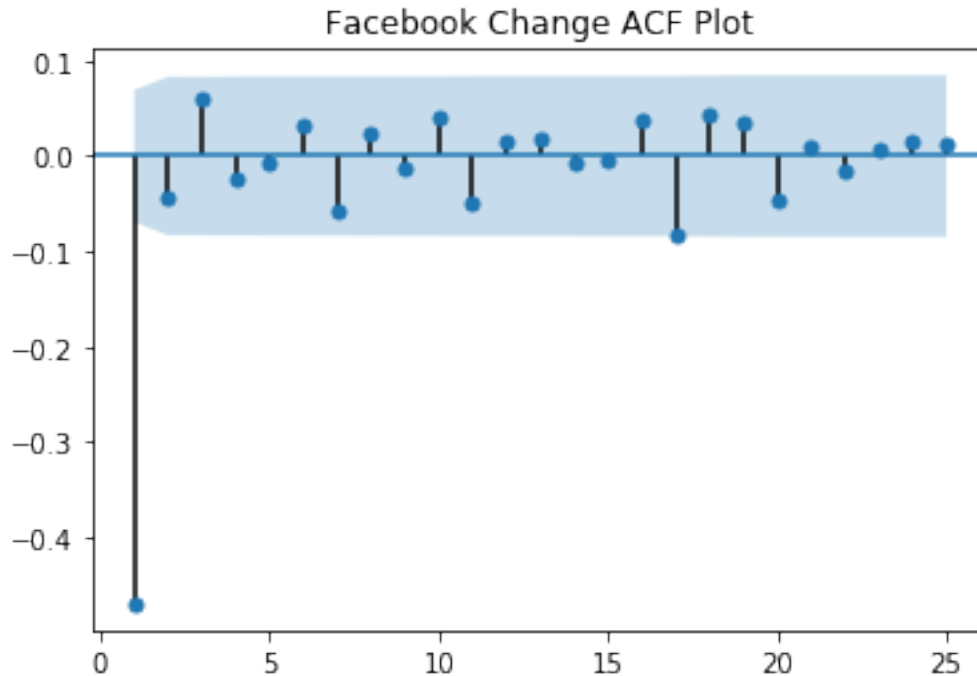
In [10]: basic(sampleddata, "FBChange", "Facebook Wikipedia Daily Visits Change Histogram", "Facebook Daily Visits")
---Facebook Daily Visits---

```



Mean: -0.01207603815335625  
Variance: 1694.9150341390537  
Skewness(scipy): -0.07505160617431292  
Kurtosis: 2.6043402578909682





Not really autocorrelated. Meaning number of visits from yesterday's data doesn't determine the number of visits of today's data. Nothing too interesting with first differenced data.

### 1.3 Stationarity

```
In [11]: result=smt.adfuller(sampledata["Facebook"])
         print('ADF Statistic: %f' % result[0])
         print('p-value: %f' % result[1])
         print('Critical Values:')
         for key, value in result[4].items():
             print('\t%s: %.3f' % (key, value))
```

ADF Statistic: -6.964697

p-value: 0.000000

Critical Values:

1%: -3.439

5%: -2.865

10%: -2.569

Data is stationary.

```
In [27]: result=smt.adfuller(sampledata["FBChange"])
         print('ADF Statistic: %f' % result[0])
         print('p-value: %s' % result[1])
         print('Critical Values:')
```

```

for key, value in result[4].items():
    print('\t%s: %.3f' % (key, value))

```

ADF Statistic: -11.812116

p-value: 8.810406134104259e-22

Critical Values:

1%: -3.439

5%: -2.865

10%: -2.569

Same with this one.

## 1.4 Model

```

In [13]: for i in range(0,11):
         for j in range(0,11):
             model = smt.ARMA(sampledata["Facebook"], order=(i,j))
             model_fit = model.fit(dis=0, method='mle', solver='nm')
             print(model_fit.summary())

```

### ARMA Model Results

```

=====
Dep. Variable:          Facebook    No. Observations:              802
Model:                ARMA(0, 0)    Log Likelihood                -3829.036
Method:                  css        S.D. of innovations              28.658
Date:                  Mon, 10 Dec 2018    AIC                          7662.071
Time:                  02:44:19          BIC                          7671.445
Sample:                0              HQIC                          7665.672
=====

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          53.5985      1.012      52.966      0.000      51.615      55.582
=====

```

### ARMA Model Results

```

=====
Dep. Variable:          Facebook    No. Observations:              802
Model:                ARMA(0, 1)    Log Likelihood                -3788.302
Method:                  mle        S.D. of innovations              27.237
Date:                  Mon, 10 Dec 2018    AIC                          7582.603
Time:                  02:44:19          BIC                          7596.665
Sample:                0              HQIC                          7588.004
=====

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          53.5979      1.229      43.603      0.000      51.189      56.007
ma.L1.Facebook    0.2784      0.030       9.281      0.000       0.220       0.337
=====

```

| Roots |         |           |         |           |
|-------|---------|-----------|---------|-----------|
|       | Real    | Imaginary | Modulus | Frequency |
| MA.1  | -3.5916 | +0.0000j  | 3.5916  | 0.5000    |

| ARMA Model Results |                  |                     |           |
|--------------------|------------------|---------------------|-----------|
| Dep. Variable:     | Facebook         | No. Observations:   | 802       |
| Model:             | ARMA(0, 2)       | Log Likelihood      | -3776.584 |
| Method:            | mle              | S.D. of innovations | 26.842    |
| Date:              | Mon, 10 Dec 2018 | AIC                 | 7561.169  |
| Time:              | 02:44:19         | BIC                 | 7579.917  |
| Sample:            | 0                | HQIC                | 7568.370  |

|                | coef    | std err | z      | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|--------|-------|--------|--------|
| const          | 53.5949 | 1.356   | 39.528 | 0.000 | 50.937 | 56.252 |
| ma.L1.Facebook | 0.2769  | 0.036   | 7.771  | 0.000 | 0.207  | 0.347  |
| ma.L2.Facebook | 0.1544  | 0.032   | 4.872  | 0.000 | 0.092  | 0.216  |

| Roots |         |           |         |           |
|-------|---------|-----------|---------|-----------|
|       | Real    | Imaginary | Modulus | Frequency |
| MA.1  | -0.8969 | -2.3820j  | 2.5452  | -0.3073   |
| MA.2  | -0.8969 | +2.3820j  | 2.5452  | 0.3073    |

| ARMA Model Results |                  |                     |           |
|--------------------|------------------|---------------------|-----------|
| Dep. Variable:     | Facebook         | No. Observations:   | 802       |
| Model:             | ARMA(0, 3)       | Log Likelihood      | -3765.003 |
| Method:            | mle              | S.D. of innovations | 26.456    |
| Date:              | Mon, 10 Dec 2018 | AIC                 | 7540.006  |
| Time:              | 02:44:19         | BIC                 | 7563.442  |
| Sample:            | 0                | HQIC                | 7549.008  |

|                | coef    | std err | z      | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|--------|-------|--------|--------|
| const          | 53.5814 | 1.472   | 36.410 | 0.000 | 50.697 | 56.466 |
| ma.L1.Facebook | 0.2614  | 0.036   | 7.199  | 0.000 | 0.190  | 0.333  |
| ma.L2.Facebook | 0.1572  | 0.032   | 4.854  | 0.000 | 0.094  | 0.221  |
| ma.L3.Facebook | 0.1579  | 0.033   | 4.845  | 0.000 | 0.094  | 0.222  |

| Roots |           |         |           |
|-------|-----------|---------|-----------|
| ===== |           |         |           |
| Real  | Imaginary | Modulus | Frequency |

|      |         |          |        |         |
|------|---------|----------|--------|---------|
| MA.1 | 0.4477  | -1.7743j | 1.8299 | -0.2107 |
| MA.2 | 0.4477  | +1.7743j | 1.8299 | 0.2107  |
| MA.3 | -1.8910 | -0.0000j | 1.8910 | -0.5000 |

-----

ARMA Model Results

=====

|                |                  |                     |           |
|----------------|------------------|---------------------|-----------|
| Dep. Variable: | Facebook         | No. Observations:   | 802       |
| Model:         | ARMA(0, 4)       | Log Likelihood      | -3756.481 |
| Method:        | mle              | S.D. of innovations | 26.176    |
| Date:          | Mon, 10 Dec 2018 | AIC                 | 7524.963  |
| Time:          | 02:44:19         | BIC                 | 7553.086  |
| Sample:        | 0                | HQIC                | 7535.765  |

=====

|                | coef    | std err | z      | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|--------|-------|--------|--------|
| const          | 53.5907 | 1.577   | 33.983 | 0.000 | 50.500 | 56.682 |
| ma.L1.Facebook | 0.2408  | 0.036   | 6.687  | 0.000 | 0.170  | 0.311  |
| ma.L2.Facebook | 0.1469  | 0.036   | 4.028  | 0.000 | 0.075  | 0.218  |
| ma.L3.Facebook | 0.1770  | 0.033   | 5.437  | 0.000 | 0.113  | 0.241  |
| ma.L4.Facebook | 0.1434  | 0.034   | 4.192  | 0.000 | 0.076  | 0.210  |

Roots

=====

|      | Real    | Imaginary | Modulus | Frequency |
|------|---------|-----------|---------|-----------|
| MA.1 | 0.7743  | -1.3020j  | 1.5148  | -0.1646   |
| MA.2 | 0.7743  | +1.3020j  | 1.5148  | 0.1646    |
| MA.3 | -1.3912 | -1.0503j  | 1.7432  | -0.3971   |
| MA.4 | -1.3912 | +1.0503j  | 1.7432  | 0.3971    |

-----

ARMA Model Results

=====

|                |                  |                     |           |
|----------------|------------------|---------------------|-----------|
| Dep. Variable: | Facebook         | No. Observations:   | 802       |
| Model:         | ARMA(0, 5)       | Log Likelihood      | -3747.465 |
| Method:        | mle              | S.D. of innovations | 25.882    |
| Date:          | Mon, 10 Dec 2018 | AIC                 | 7508.930  |
| Time:          | 02:44:19         | BIC                 | 7541.740  |
| Sample:        | 0                | HQIC                | 7521.533  |

=====

|                | coef    | std err | z      | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|--------|-------|--------|--------|
| const          | 53.5983 | 1.707   | 31.405 | 0.000 | 50.253 | 56.943 |
| ma.L1.Facebook | 0.2348  | 0.035   | 6.636  | 0.000 | 0.165  | 0.304  |
| ma.L2.Facebook | 0.1507  | 0.036   | 4.174  | 0.000 | 0.080  | 0.221  |
| ma.L3.Facebook | 0.1823  | 0.033   | 5.545  | 0.000 | 0.118  | 0.247  |
| ma.L4.Facebook | 0.1566  | 0.034   | 4.624  | 0.000 | 0.090  | 0.223  |
| ma.L5.Facebook | 0.1461  | 0.034   | 4.311  | 0.000 | 0.080  | 0.213  |

| Roots |         |           |         |           |
|-------|---------|-----------|---------|-----------|
|       | Real    | Imaginary | Modulus | Frequency |
| MA.1  | 0.8879  | -1.0253j  | 1.3563  | -0.1364   |
| MA.2  | 0.8879  | +1.0253j  | 1.3563  | 0.1364    |
| MA.3  | -1.5206 | -0.0000j  | 1.5206  | -0.5000   |
| MA.4  | -0.6635 | -1.4164j  | 1.5641  | -0.3197   |
| MA.5  | -0.6635 | +1.4164j  | 1.5641  | 0.3197    |

```

=====
                        ARMA Model Results
=====
Dep. Variable:          Facebook    No. Observations:          802
Model:                 ARMA(0, 6)  Log Likelihood             -3743.951
Method:                mle         S.D. of innovations        25.768
Date:                  Mon, 10 Dec 2018  AIC                        7503.902
Time:                  02:44:20        BIC                        7541.399
Sample:                0              HQIC                       7518.305

```

|                | coef    | std err | z      | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|--------|-------|--------|--------|
| const          | 53.5964 | 1.801   | 29.756 | 0.000 | 50.066 | 57.127 |
| ma.L1.Facebook | 0.2357  | 0.035   | 6.678  | 0.000 | 0.167  | 0.305  |
| ma.L2.Facebook | 0.1553  | 0.036   | 4.311  | 0.000 | 0.085  | 0.226  |
| ma.L3.Facebook | 0.1855  | 0.036   | 5.147  | 0.000 | 0.115  | 0.256  |
| ma.L4.Facebook | 0.1621  | 0.035   | 4.696  | 0.000 | 0.094  | 0.230  |
| ma.L5.Facebook | 0.1554  | 0.034   | 4.529  | 0.000 | 0.088  | 0.223  |
| ma.L6.Facebook | 0.0892  | 0.034   | 2.654  | 0.008 | 0.023  | 0.155  |

| Roots |         |           |         |           |
|-------|---------|-----------|---------|-----------|
|       | Real    | Imaginary | Modulus | Frequency |
| MA.1  | 0.9362  | -0.9061j  | 1.3029  | -0.1224   |
| MA.2  | 0.9362  | +0.9061j  | 1.3029  | 0.1224    |
| MA.3  | -0.2848 | -1.5182j  | 1.5447  | -0.2795   |
| MA.4  | -0.2848 | +1.5182j  | 1.5447  | 0.2795    |
| MA.5  | -1.5227 | -0.6707j  | 1.6639  | -0.4340   |
| MA.6  | -1.5227 | +0.6707j  | 1.6639  | 0.4340    |

```

C:\Users\Diana\Anaconda3\lib\site-packages\statsmodels\base\model.py:508: ConvergenceWarning: 
  "Check mle_retvals", ConvergenceWarning)

```

```

=====
                        ARMA Model Results
=====

```

```

Dep. Variable:          Facebook    No. Observations:          802
Model:                ARMA(0, 7)    Log Likelihood             -3741.873
Method:                  mle        S.D. of innovations        25.701
Date:                   Mon, 10 Dec 2018    AIC                       7501.746
Time:                   02:44:21    BIC                       7543.930
Sample:                  0        HQIC                       7517.950

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          53.5920         1.876     28.570     0.000     49.915     57.268
ma.L1.Facebook    0.2359         0.035      6.666     0.000      0.167      0.305
ma.L2.Facebook    0.1549         0.036      4.259     0.000      0.084      0.226
ma.L3.Facebook    0.1890         0.036      5.182     0.000      0.117      0.260
ma.L4.Facebook    0.1634         0.035      4.671     0.000      0.095      0.232
ma.L5.Facebook    0.1589         0.034      4.658     0.000      0.092      0.226
ma.L6.Facebook    0.1026         0.035      2.951     0.003      0.034      0.171
ma.L7.Facebook    0.0668         0.033      2.037     0.042      0.003      0.131

```

Roots

```

=====
              Real      Imaginary      Modulus      Frequency
-----
MA.1          0.9792      -0.8205j      1.2775      -0.1110
MA.2          0.9792      +0.8205j      1.2775       0.1110
MA.3          0.0812      -1.5394j      1.5416      -0.2416
MA.4          0.0812      +1.5394j      1.5416       0.2416
MA.5         -1.5011      -0.0000j      1.5011      -0.5000
MA.6         -1.0775      -1.1876j      1.6035      -0.3673
MA.7         -1.0775      +1.1876j      1.6035       0.3673

```

C:\Users\Diana\Anaconda3\lib\site-packages\statsmodels\base\model.py:508: ConvergenceWarning: I  
"Check mle\_retvals", ConvergenceWarning)

ARMA Model Results

```

=====
Dep. Variable:          Facebook    No. Observations:          802
Model:                ARMA(0, 8)    Log Likelihood             -3740.858
Method:                  mle        S.D. of innovations        25.669
Date:                   Mon, 10 Dec 2018    AIC                       7501.717
Time:                   02:44:23    BIC                       7548.588
Sample:                  0        HQIC                       7519.720

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----

```

|                |         |       |        |       |        |        |
|----------------|---------|-------|--------|-------|--------|--------|
| const          | 53.5705 | 1.924 | 27.850 | 0.000 | 49.800 | 57.341 |
| ma.L1.Facebook | 0.2304  | 0.036 | 6.449  | 0.000 | 0.160  | 0.300  |
| ma.L2.Facebook | 0.1524  | 0.037 | 4.173  | 0.000 | 0.081  | 0.224  |
| ma.L3.Facebook | 0.1876  | 0.037 | 5.127  | 0.000 | 0.116  | 0.259  |
| ma.L4.Facebook | 0.1649  | 0.037 | 4.507  | 0.000 | 0.093  | 0.237  |
| ma.L5.Facebook | 0.1645  | 0.035 | 4.754  | 0.000 | 0.097  | 0.232  |
| ma.L6.Facebook | 0.1011  | 0.035 | 2.891  | 0.004 | 0.033  | 0.170  |
| ma.L7.Facebook | 0.0763  | 0.033 | 2.288  | 0.022 | 0.011  | 0.142  |
| ma.L8.Facebook | 0.0500  | 0.035 | 1.432  | 0.153 | -0.018 | 0.119  |

#### Roots

|      | Real    | Imaginary | Modulus | Frequency |
|------|---------|-----------|---------|-----------|
| MA.1 | 1.0166  | -0.7578j  | 1.2680  | -0.1019   |
| MA.2 | 1.0166  | +0.7578j  | 1.2680  | 0.1019    |
| MA.3 | 0.3880  | -1.4624j  | 1.5130  | -0.2087   |
| MA.4 | 0.3880  | +1.4624j  | 1.5130  | 0.2087    |
| MA.5 | -0.6836 | -1.3311j  | 1.4963  | -0.3255   |
| MA.6 | -0.6836 | +1.3311j  | 1.4963  | 0.3255    |
| MA.7 | -1.4835 | -0.4737j  | 1.5573  | -0.4508   |
| MA.8 | -1.4835 | +0.4737j  | 1.5573  | 0.4508    |

C:\Users\Diana\Anaconda3\lib\site-packages\statsmodels\base\model.py:508: ConvergenceWarning:   
"Check mle\_retvals", ConvergenceWarning)

#### ARMA Model Results

|                |                  |                     |           |
|----------------|------------------|---------------------|-----------|
| Dep. Variable: | Facebook         | No. Observations:   | 802       |
| Model:         | ARMA(0, 9)       | Log Likelihood      | -3738.426 |
| Method:        | mle              | S.D. of innovations | 25.591    |
| Date:          | Mon, 10 Dec 2018 | AIC                 | 7498.853  |
| Time:          | 02:44:24         | BIC                 | 7550.411  |
| Sample:        | 0                | HQIC                | 7518.657  |

|                | coef    | std err | z      | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|--------|-------|--------|--------|
| const          | 53.6737 | 1.985   | 27.035 | 0.000 | 49.783 | 57.565 |
| ma.L1.Facebook | 0.2281  | 0.036   | 6.371  | 0.000 | 0.158  | 0.298  |
| ma.L2.Facebook | 0.1520  | 0.036   | 4.188  | 0.000 | 0.081  | 0.223  |
| ma.L3.Facebook | 0.1834  | 0.037   | 5.021  | 0.000 | 0.112  | 0.255  |
| ma.L4.Facebook | 0.1670  | 0.036   | 4.688  | 0.000 | 0.097  | 0.237  |
| ma.L5.Facebook | 0.1617  | 0.035   | 4.578  | 0.000 | 0.093  | 0.231  |
| ma.L6.Facebook | 0.1127  | 0.035   | 3.190  | 0.001 | 0.043  | 0.182  |
| ma.L7.Facebook | 0.0815  | 0.034   | 2.396  | 0.017 | 0.015  | 0.148  |



|                |        |       |       |       |        |       |
|----------------|--------|-------|-------|-------|--------|-------|
| ma.L8.Facebook | 0.0373 | 0.036 | 1.050 | 0.294 | -0.032 | 0.107 |
| ma.L9.Facebook | 0.0792 | 0.034 | 2.363 | 0.018 | 0.014  | 0.145 |

#### Roots

|      | Real    | Imaginary | Modulus | Frequency |
|------|---------|-----------|---------|-----------|
| MA.1 | 1.0653  | -0.6726j  | 1.2599  | -0.0896   |
| MA.2 | 1.0653  | +0.6726j  | 1.2599  | 0.0896    |
| MA.3 | 0.6400  | -1.2323j  | 1.3886  | -0.1738   |
| MA.4 | 0.6400  | +1.2323j  | 1.3886  | 0.1738    |
| MA.5 | -1.2876 | -0.0000j  | 1.2876  | -0.5000   |
| MA.6 | -1.0283 | -0.8458j  | 1.3314  | -0.3905   |
| MA.7 | -1.0283 | +0.8458j  | 1.3314  | 0.3905    |
| MA.8 | -0.2688 | -1.3173j  | 1.3444  | -0.2820   |
| MA.9 | -0.2688 | +1.3173j  | 1.3444  | 0.2820    |

C:\Users\Diana\Anaconda3\lib\site-packages\statsmodels\base\model.py:508: ConvergenceWarning:   
"Check mle\_retvals", ConvergenceWarning)

#### ARMA Model Results

|                |                  |                     |           |
|----------------|------------------|---------------------|-----------|
| Dep. Variable: | Facebook         | No. Observations:   | 802       |
| Model:         | ARMA(0, 10)      | Log Likelihood      | -3738.726 |
| Method:        | mle              | S.D. of innovations | 25.601    |
| Date:          | Mon, 10 Dec 2018 | AIC                 | 7501.451  |
| Time:          | 02:44:27         | BIC                 | 7557.697  |
| Sample:        | 0                | HQIC                | 7523.056  |

|                 | coef    | std err | z      | P> z  | [0.025 | 0.975] |
|-----------------|---------|---------|--------|-------|--------|--------|
| const           | 53.6545 | 1.980   | 27.093 | 0.000 | 49.773 | 57.536 |
| ma.L1.Facebook  | 0.2202  | 0.036   | 6.120  | 0.000 | 0.150  | 0.291  |
| ma.L2.Facebook  | 0.1430  | 0.037   | 3.863  | 0.000 | 0.070  | 0.216  |
| ma.L3.Facebook  | 0.1855  | 0.037   | 5.048  | 0.000 | 0.113  | 0.258  |
| ma.L4.Facebook  | 0.1645  | 0.035   | 4.683  | 0.000 | 0.096  | 0.233  |
| ma.L5.Facebook  | 0.1612  | 0.037   | 4.337  | 0.000 | 0.088  | 0.234  |
| ma.L6.Facebook  | 0.1140  | 0.035   | 3.258  | 0.001 | 0.045  | 0.183  |
| ma.L7.Facebook  | 0.0556  | 0.035   | 1.592  | 0.112 | -0.013 | 0.124  |
| ma.L8.Facebook  | 0.0180  | 0.035   | 0.516  | 0.606 | -0.050 | 0.086  |
| ma.L9.Facebook  | 0.0780  | 0.034   | 2.298  | 0.022 | 0.011  | 0.145  |
| ma.L10.Facebook | 0.0568  | 0.036   | 1.559  | 0.119 | -0.015 | 0.128  |

#### Roots

|  | Real | Imaginary | Modulus | Frequency |
|--|------|-----------|---------|-----------|
|--|------|-----------|---------|-----------|

|       |         |          |        |         |
|-------|---------|----------|--------|---------|
| MA.1  | 1.1156  | -0.6130j | 1.2729 | -0.0800 |
| MA.2  | 1.1156  | +0.6130j | 1.2729 | 0.0800  |
| MA.3  | 0.7184  | -1.0561j | 1.2773 | -0.1549 |
| MA.4  | 0.7184  | +1.0561j | 1.2773 | 0.1549  |
| MA.5  | -0.1250 | -1.2661j | 1.2723 | -0.2657 |
| MA.6  | -0.1250 | +1.2661j | 1.2723 | 0.2657  |
| MA.7  | -0.9340 | -0.9858j | 1.3581 | -0.3707 |
| MA.8  | -0.9340 | +0.9858j | 1.3581 | 0.3707  |
| MA.9  | -1.4623 | -0.3056j | 1.4939 | -0.4672 |
| MA.10 | -1.4623 | +0.3056j | 1.4939 | 0.4672  |

#### ARMA Model Results

|                |                  |                     |           |
|----------------|------------------|---------------------|-----------|
| Dep. Variable: | Facebook         | No. Observations:   | 802       |
| Model:         | ARMA(1, 0)       | Log Likelihood      | -3772.572 |
| Method:        | mle              | S.D. of innovations | 26.707    |
| Date:          | Mon, 10 Dec 2018 | AIC                 | 7551.144  |
| Time:          | 02:44:28         | BIC                 | 7565.205  |
| Sample:        | 0                | HQIC                | 7556.545  |

|                | coef    | std err | z      | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|--------|-------|--------|--------|
| const          | 53.5941 | 1.478   | 36.271 | 0.000 | 50.698 | 56.490 |
| ar.L1.Facebook | 0.3622  | 0.033   | 11.015 | 0.000 | 0.298  | 0.427  |

#### Roots

|      | Real   | Imaginary | Modulus | Frequency |
|------|--------|-----------|---------|-----------|
| AR.1 | 2.7608 | +0.0000j  | 2.7608  | 0.0000    |

#### ARMA Model Results

|                |                  |                     |           |
|----------------|------------------|---------------------|-----------|
| Dep. Variable: | Facebook         | No. Observations:   | 802       |
| Model:         | ARMA(1, 1)       | Log Likelihood      | -3728.093 |
| Method:        | mle              | S.D. of innovations | 25.260    |
| Date:          | Mon, 10 Dec 2018 | AIC                 | 7464.185  |
| Time:          | 02:44:28         | BIC                 | 7482.934  |
| Sample:        | 0                | HQIC                | 7471.387  |

|                | coef    | std err | z       | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|---------|-------|--------|--------|
| const          | 53.5391 | 3.731   | 14.351  | 0.000 | 46.227 | 60.851 |
| ar.L1.Facebook | 0.9479  | 0.018   | 52.605  | 0.000 | 0.913  | 0.983  |
| ma.L1.Facebook | -0.7782 | 0.037   | -21.076 | 0.000 | -0.851 | -0.706 |

#### Roots

|      | Real   | Imaginary | Modulus | Frequency |
|------|--------|-----------|---------|-----------|
| AR.1 | 1.0550 | +0.0000j  | 1.0550  | 0.0000    |
| MA.1 | 1.2851 | +0.0000j  | 1.2851  | 0.0000    |

#### ARMA Model Results

```

=====
Dep. Variable:          Facebook    No. Observations:          802
Model:                ARMA(1, 2)   Log Likelihood             -3727.359
Method:                mle         S.D. of innovations        25.237
Date:                  Mon, 10 Dec 2018   AIC                       7464.717
Time:                  02:44:28          BIC                       7488.153
Sample:                0               HQIC                      7473.719
=====

```

|                | coef    | std err | z       | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|---------|-------|--------|--------|
| const          | 53.5260 | 3.909   | 13.692  | 0.000 | 45.864 | 61.188 |
| ar.L1.Facebook | 0.9554  | 0.017   | 56.326  | 0.000 | 0.922  | 0.989  |
| ma.L1.Facebook | -0.7528 | 0.040   | -18.843 | 0.000 | -0.831 | -0.675 |
| ma.L2.Facebook | -0.0475 | 0.039   | -1.215  | 0.225 | -0.124 | 0.029  |

#### Roots

|      | Real     | Imaginary | Modulus | Frequency |
|------|----------|-----------|---------|-----------|
| AR.1 | 1.0467   | +0.0000j  | 1.0467  | 0.0000    |
| MA.1 | 1.2325   | +0.0000j  | 1.2325  | 0.0000    |
| MA.2 | -17.0977 | +0.0000j  | 17.0977 | 0.5000    |

#### ARMA Model Results

```

=====
Dep. Variable:          Facebook    No. Observations:          802
Model:                ARMA(1, 3)   Log Likelihood             -3726.939
Method:                mle         S.D. of innovations        25.223
Date:                  Mon, 10 Dec 2018   AIC                       7465.877
Time:                  02:44:29          BIC                       7494.000
Sample:                0               HQIC                      7476.679
=====

```

|                | coef    | std err | z       | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|---------|-------|--------|--------|
| const          | 53.5420 | 3.765   | 14.222  | 0.000 | 46.163 | 60.921 |
| ar.L1.Facebook | 0.9492  | 0.020   | 46.769  | 0.000 | 0.909  | 0.989  |
| ma.L1.Facebook | -0.7469 | 0.041   | -18.316 | 0.000 | -0.827 | -0.667 |
| ma.L2.Facebook | -0.0688 | 0.045   | -1.535  | 0.125 | -0.157 | 0.019  |
| ma.L3.Facebook | 0.0344  | 0.038   | 0.916   | 0.360 | -0.039 | 0.108  |

#### Roots

|      | Real    | Imaginary | Modulus | Frequency |
|------|---------|-----------|---------|-----------|
| AR.1 | 1.0535  | +0.0000j  | 1.0535  | 0.0000    |
| MA.1 | 1.2847  | +0.0000j  | 1.2847  | 0.0000    |
| MA.2 | -4.4114 | +0.0000j  | 4.4114  | 0.5000    |
| MA.3 | 5.1233  | +0.0000j  | 5.1233  | 0.0000    |

#### ARMA Model Results

```

=====
Dep. Variable:          Facebook    No. Observations:          802
Model:                ARMA(1, 4)    Log Likelihood             -3726.805
Method:                mle          S.D. of innovations         25.219
Date:                  Mon, 10 Dec 2018    AIC                        7467.610
Time:                  02:44:29          BIC                        7500.419
Sample:                0                HQIC                      7480.212
=====

```

|                | coef    | std err | z       | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|---------|-------|--------|--------|
| const          | 53.5313 | 3.845   | 13.923  | 0.000 | 45.995 | 61.067 |
| ar.L1.Facebook | 0.9529  | 0.020   | 47.334  | 0.000 | 0.913  | 0.992  |
| ma.L1.Facebook | -0.7518 | 0.041   | -18.311 | 0.000 | -0.832 | -0.671 |
| ma.L2.Facebook | -0.0693 | 0.044   | -1.573  | 0.116 | -0.156 | 0.017  |
| ma.L3.Facebook | 0.0479  | 0.046   | 1.048   | 0.295 | -0.042 | 0.138  |
| ma.L4.Facebook | -0.0192 | 0.037   | -0.517  | 0.605 | -0.092 | 0.054  |

#### Roots

|      | Real    | Imaginary | Modulus | Frequency |
|------|---------|-----------|---------|-----------|
| AR.1 | 1.0495  | +0.0000j  | 1.0495  | 0.0000    |
| MA.1 | 1.2485  | -0.0000j  | 1.2485  | -0.0000   |
| MA.2 | -2.9250 | -0.0000j  | 2.9250  | -0.5000   |
| MA.3 | 2.0851  | -3.1467j  | 3.7748  | -0.1569   |
| MA.4 | 2.0851  | +3.1467j  | 3.7748  | 0.1569    |

C:\Users\Diana\Anaconda3\lib\site-packages\statsmodels\base\model.py:508: ConvergenceWarning: I  
 "Check mle\_retvals", ConvergenceWarning)

#### ARMA Model Results

```

=====
Dep. Variable:          Facebook    No. Observations:          802
Model:                ARMA(1, 5)    Log Likelihood             -3726.674
Method:                mle          S.D. of innovations         25.215
Date:                  Mon, 10 Dec 2018    AIC                        7469.348
=====

```

Time: 02:44:30 BIC 7506.845  
Sample: 0 HQIC 7483.751

|                | coef    | std err | z       | P> z  | [0.025 | 0.975] |
|----------------|---------|---------|---------|-------|--------|--------|
| const          | 53.5241 | 3.921   | 13.652  | 0.000 | 45.840 | 61.208 |
| ar.L1.Facebook | 0.9562  | 0.020   | 48.038  | 0.000 | 0.917  | 0.995  |
| ma.L1.Facebook | -0.7564 | 0.041   | -18.341 | 0.000 | -0.837 | -0.676 |
| ma.L2.Facebook | -0.0698 | 0.044   | -1.569  | 0.117 | -0.157 | 0.017  |
| ma.L3.Facebook | 0.0494  | 0.046   | 1.068   | 0.286 | -0.041 | 0.140  |
| ma.L4.Facebook | -0.0066 | 0.045   | -0.149  | 0.882 | -0.094 | 0.081  |
| ma.L5.Facebook | -0.0196 | 0.038   | -0.511  | 0.609 | -0.095 | 0.056  |

Roots

|      | Real    | Imaginary | Modulus | Frequency |
|------|---------|-----------|---------|-----------|
| AR.1 | 1.0458  | +0.0000j  | 1.0458  | 0.0000    |
| MA.1 | 1.2150  | -0.0000j  | 1.2150  | -0.0000   |
| MA.2 | 1.5041  | -1.8192j  | 2.3605  | -0.1400   |
| MA.3 | 1.5041  | +1.8192j  | 2.3605  | 0.1400    |
| MA.4 | -2.2801 | -1.5232j  | 2.7421  | -0.4063   |
| MA.5 | -2.2801 | +1.5232j  | 2.7421  | 0.4063    |

ValueError Traceback (most recent call last)

```
<ipython-input-13-48682322ec2a> in <module>()
      2     for j in range(0,11):
      3         model = smt.ARMA(sampleddata["Facebook"], order=(i,j))
----> 4         model_fit = model.fit(dis=0, method='mle', solver='nm')
      5         print(model_fit.summary())
```

```
~\Anaconda3\lib\site-packages\statsmodels\tsa\arima_model.py in fit(self, start_params
944     else: # estimate starting parameters
945         start_params = self._fit_start_params((k_ar, k_ma, k), method,
--> 946                                             start_ar_lags)
947
948     if transparams: # transform initial parameters to ensure invertibility
```

```
~\Anaconda3\lib\site-packages\statsmodels\tsa\arima_model.py in _fit_start_params(self
556     def _fit_start_params(self, order, method, start_ar_lags=None):
```

```

557         if method != 'css-mle': # use Hannan-Rissanen to get start params
--> 558             start_params = self._fit_start_params_hr(order, start_ar_lags)
559         else: # use CSS to get start params
560             func = lambda params: -self.loglike_css(params)

~\Anaconda3\lib\site-packages\statsmodels\tsa\arima_model.py in _fit_start_params_hr(s
539         if p and not np.all(np.abs(np.roots(np.r_[1, -start_params[k:k + p]]
540                                )) < 1):
--> 541             raise ValueError("The computed initial AR coefficients are not "
542                                "stationary\nYou should induce stationarity, "
543                                "choose a different model order, or you can\n")

```

ValueError: The computed initial AR coefficients are not stationary  
You should induce stationarity, choose a different model order, or you can  
pass your own start\_params.

```

In [14]: model = smt.ARMA(sampledata["Facebook"], order=(1,1))
         model_fit = model.fit(dis=0, method='mle', solver='nm')
         print(model_fit.summary())

         data_acfplot = tsa.plot_acf(x=model_fit.resid, ax=None,
                                    lags=25, alpha=.05, use_vlines=True,
                                     unbiased=False,fft=False, zero=False,
                                     vlines_kwargs=None)

```

#### ARMA Model Results

```

=====
Dep. Variable:          Facebook    No. Observations:              802
Model:                  ARMA(1, 1)  Log Likelihood                -3728.093
Method:                  mle        S.D. of innovations            25.260
Date:                   Mon, 10 Dec 2018    AIC                        7464.185
Time:                   02:46:03    BIC                        7482.934
Sample:                 0          HQIC                        7471.387
=====

```

```

=====
              coef      std err          z      P>|z|      [0.025      0.975]
-----
const          53.5391      3.731     14.351      0.000     46.227     60.851
ar.L1.Facebook    0.9479      0.018     52.605      0.000      0.913      0.983
ma.L1.Facebook   -0.7782      0.037    -21.076      0.000     -0.851     -0.706
=====

```

#### Roots

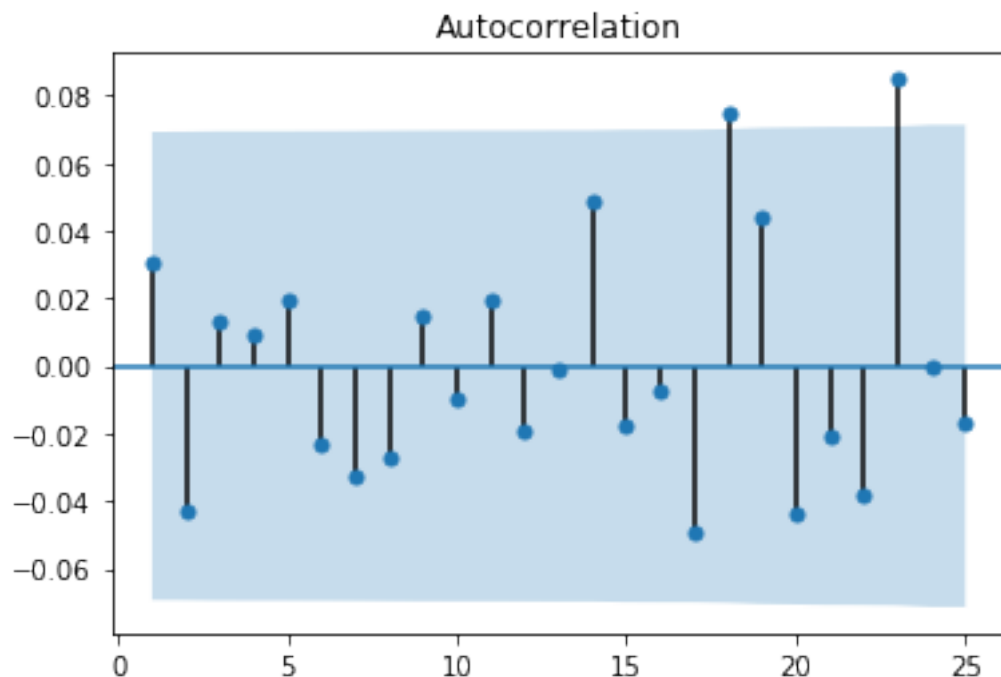
```

=====
              Real      Imaginary      Modulus      Frequency
-----
AR.1          1.0550      +0.0000j      1.0550      0.0000

```

MA.1                      1.2851                      +0.0000j                      1.2851                      0.0000

---



ARMA(1,1) is best and therefore tomorrow's data only depends on today's. Plot ACF on the residual to model check. The serial correlation is really low and no trend so it provides evidence that each residual is independent of each other.

series is adjusted to mean, the AR portion suggests that after significant spikes, the web traffic will slowly decrease overtime to the mean. You take the 95% of the first data and then 95% of that again. 95% comes from the coefficient. Can talk about how after the spike, the series goes down.

for MA with negative coefficient means that the previous day would have an opposite effect on the next day as seen in the jaggedness of the series.

```
In [15]: table = [{"Model", "AIC", "BIC"},
                  ["ARMA(0,0)", 7644.129, 7653.498],
                  ["MA(1)", 7565.164, 7579.218],
                  ["MA(2)", 7543.781, 7562.781],
                  ["MA(3)", 7522.786, 7546.209],
                  ["MA(4)", 7507.885, 7535.993],
                  ["MA(5)", 7492.126, 7524.919],
                  ["AR(1)", 7533.897, 7547.951],
                  ["AR(2)", 7506.299, 7525.037],
                  ["AR(3)", 7478.710, 7502.133],
                  ["AR(4)", 7466.529, 7494.637],
                  ["AR(5)", 7458.583, 7491.375],
                  ["ARMA(1,1)", 7447.300, 7466.039],
```

```

["ARMA(1,2)",7447.836,7471.259],
["ARMA(1,3)",7449.007,7477.114],
["ARMA(1,5)",7452.512,7489.989],
["ARMA(2,1)",7447.964,7471.387],
["ARMA(2,2)",7448.713,7476.821],
["ARMA(2,5)",7454.635,7496.796],
["ARMA(3,1)",7449.049,7477.157],
["ARMA(3,5)",7456.112,7502.958],
["ARMA(4,5)",7452.134,7503.665],
["ARMA(5,5)",7453.500,7509.716]]
display(HTML(tabulate.tabulate(table, tablefmt='html')))
```

<IPython.core.display.HTML object>

```

In [16]: facebookforecast = model_fit.forecast(steps=365)
print(facebookforecast)
plt.plot(facebookforecast[0])
plt.title("Forecasted Daily Visits")
plt.xlabel("Days")
plt.ylabel("Daily Visits")
```

```

(array([62.14503317, 61.69676194, 61.27184051, 60.86905262, 60.48724537,
        60.12532591, 59.78225831, 59.4570606 , 59.14880198, 58.8566001 ,
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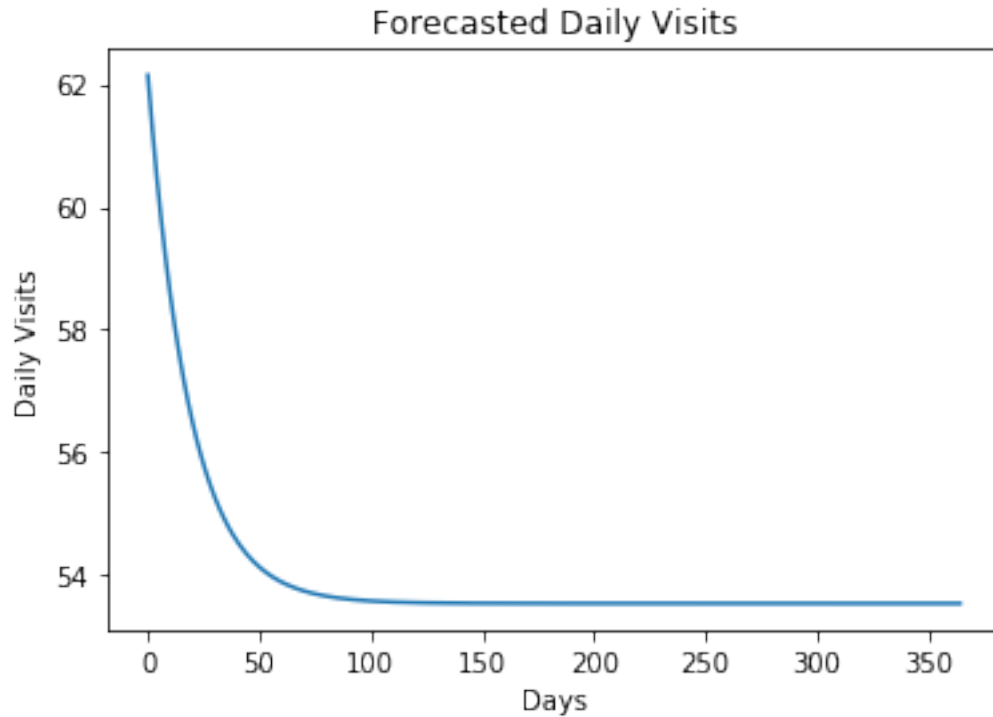


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```
Out[16]: Text(0,0.5,'Daily Visits')
```



```
In [25]: training_array = sampledata["Facebook"]
forecast, stderr, ci = model_fit.forecast(steps=10, alpha=0.1)
values_line = np.r_[training_array[-50:], forecast]
x_points = np.arange(-50, 10)
plt.plot(x_points, values_line)
# plt.fill_between(np.arange(10), ci[:,0], ci[:,1], alpha=0.3)
plt.title("Forecast for the next 10 days")
plt.xlabel("Days")
plt.ylabel("Number of Daily Visits")
plt.show()
```

