## Notation

```
This font is used for real scalars
                              This font is used for real column vectors
                              This font is used for real matrices
                       \boldsymbol{A}
                              This font is used for sets
                              The identity matrix
                              The zero matrix
                        0
                     oldsymbol{A}^\mathsf{T}
                              The transpose of matrix \boldsymbol{A}
                \mathbb{R}^{M\times N}
                              The vector space of real M \times N matrices
                   p(\boldsymbol{a})
                              The probability density of a
                p(\boldsymbol{a}|\boldsymbol{b})
                              The probability density of \boldsymbol{a} given \boldsymbol{b}
             \mathcal{N}(oldsymbol{\mu}, oldsymbol{\Sigma})
                              Gaussian probability density with mean \mu and covariance \Sigma
\mathcal{GP}(\boldsymbol{\mu}(t), \boldsymbol{\mathcal{K}}(t,t'))
                              Gaussian process with mean function, \mu(t), and covariance function, \mathcal{K}(t,t')
                              A posterior (estimated) quantity
                      (\check{\cdot})
                              A prior quantity
                     (\cdot)_k
                              The value of a quantity at timestep k
                              The set of values of a quantity from timestep k_1 to timestep k_2, inclusive
                (\cdot)_{k_1:k_2}
                              L1 norm \|\boldsymbol{x}\|_1 = \sum |x_i|
L2 norm \|\boldsymbol{x}\|_2 = \sqrt{\sum x_i^2}
                    \left\| \cdot \right\|_1
                    \left\| \cdot \right\|_2
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- General Notation -

2 Notation

- 3D Geometry Notation -

 $\mathcal{F}^a$  A reference frame in three dimensions

 $oldsymbol{v}^a$  The coordinates of a vector in frame  $\mathcal{F}^a$ 

 $\mathbf{R}_a^b$  A 3 × 3 rotation matrix (member of SO(3)) that takes points expressed in  $\mathcal{F}^a$  and re-expresses them in (purely rotated)  $\mathcal{F}^b$ :  $\mathbf{v}^b = \mathbf{R}_a^b \mathbf{v}^a$ 

 $t_a^b$  The three-dimensional position of the origin of frame  $\mathcal{F}^a$  expressed in  $\mathcal{F}^b$ 

$$egin{aligned} oldsymbol{v}^a &= egin{bmatrix} oldsymbol{v}^a \ oldsymbol{1} \end{bmatrix} \ oldsymbol{T}_a^b &= egin{bmatrix} oldsymbol{R}_a^b & oldsymbol{t}_a^b \ oldsymbol{0} & 1 \end{bmatrix}$$

A  $4 \times 1$  homogeneous point expressed in  $\mathcal{F}^a$ A  $4 \times 4$  transformation matrix (member of SE(3)) that takes homogeneous points

expressed in  $\mathcal{F}^a$  and re-expresses them in (rotated and translated)  $\mathcal{F}^b$ :  $\tilde{\boldsymbol{v}}^b = \boldsymbol{T}_a^b \tilde{\boldsymbol{v}}^a$ 

SO(3) The special orthogonal group, a matrix Lie group used to represent rotations

so(3) The Lie algebra associated with SO(3)

SE(3) The special Euclidean group, a matrix Lie group used to represent poses

se(3) The Lie algebra associated with SE(3)

(·)^ An operator mapping a vector in  $\mathbb{R}^3$  (resp.  $\mathbb{R}^6$ ) to an element of the Lie algebra for rotations (resp. poses); implements the cross product for three-dimensional quantities, *i.e.*, for two vectors  $\boldsymbol{u}, \boldsymbol{v} \in \mathbb{R}^3$ ,  $\boldsymbol{u}^{\wedge} \boldsymbol{v} = \boldsymbol{u} \times \boldsymbol{v}$ 

 $(\cdot)^{\vee}$  An operator mapping an element of the Lie algebra for rotations (resp. poses) to a vector in  $\mathbb{R}^3$  (resp.  $\mathbb{R}^6$ )