Haskell Project

Jan Lucca Thümmel - jathu21@student.sdu.dk

December 29, 2023

Contents

1   Introduction

The goal of the project is to draw fractals using L-Systems and turtle graphics in Haskell. By solving three specific tasks. These task are applying rules to a state, going to target depth and processing a fractal

2   Specification

2.1   Task 1: Applying Rules to a State

Task 1 is solved by implementing the apply function. The apply function takes a state and a list of rules and returns a state. A state is defined by a list of characters. A rule is defined by a character and a state. The apply function takes a state and rules, checking whether a character in the state has a specific rule. If a character has no rule the next character is checked. When a character has a rule the character gets replaced with the state of the rule. As an example, we have the rules: 'X' "XRYF", 'Y' "FXLY" and the state "FXRYF". In this case the apply function would replace every X with "XRYF" and every Y with "FXLY" resulting in the string "FXRYFRFXLYF".

2.2   Task 2: Going to Target Depth

Task 2 is solved by implementing the function expand. The expand function takes a state, a list of rules, a target depth in form of an integer and returns a state. The function will apply the apply function to the state until reaching the target depth and then return the result state. An example could be applying these rules: 'X' "XRYF", 'Y' "FXLY" to the state "FX" with depth two. Depth one is achieved by applying apply once, giving the string "FXRYF". Depth two is achieved by applying apply again on the new string. Resulting in the new string "FXRYFRFXLYF". This can be repeated until the target depth is reached.

2.3   Task 3: Processing a Fractal

Task 3 is solved by implementing the function process. The process function takes a fractal and produces a list of commands to draw the fractal. This is achieved by using the expand function to get the state at target depth. Then the turtle graphics commands are mapped to the state. The commands are produced by the Char→Command function, which will be used with the name charToCom in the implementation, which converts a character to a turtle command. Testing the function with the main command in GHCI should produce a white on black snowflake. A picture of the produced snowflake and all other fractals is included in the appendix (section 7.1).

3   Design

We have some predefined data types that are used by the functions apply, expand and process.

```
1
2  -- state represented by list of letters
3  type State = [Char]
4
5  -- rule represented by a letter (left-hand side) and a state (right-hand side)
6  data Rule = Rule Char State deriving Show
7
8  -- turtle graphics commands (Nop is no operation)
9  data Command = Forward | LeftTurn Int | RightTurn Int | Nop | Scale Double |
       Backward deriving Show
10
11 -- fractal represented by initial state, list of rules, mapping from letters to
       commands, target depth, initial length
12 type Fractal = (State, [Rule], Char -> Command, Int, Double)
```

We have a state which is simply defined as a list of characters. We have a Rule which consists of a Rule, a Character and a state. We also have Command which consists of turtle graphics commands. The turtle graphics commands are actions the turtle can take when drawing a fractal. They consist of forward, to move forward, LeftTurn Int to turn left with specific degrees, the same is true for RightTurn, Nop for no operation, Scale for scaling and backwards to move backwards. We have a Fractal which consists of an initial state, a list of rules, a function Char → Command that maps each character to a turtle graphics command, an int for the desired depth and a Double for the initial length.

3.1 Task 1: Design

The goal of the apply function is to apply rules to at state. Apply takes State and rule as input and returns a new State. Apply goes through the initial state and applies the first applicable rule. Characters that have no rule are just copied to the new state. This then gives a new state. Apply thus transforms the state from depth n to depth n+1.

3.2 Task 2: Design

The goal of the expand function is using apply to go to depth n. The expand function takes an initial state, a list of rules and a target depth. Using recursion the apply function is applied until the target depth is reached.

3.3 Task 3: Design

The goal of the process function is to take a fractal description and translate it to turtle graphics commands. Process uses the expand function to get the final state then it maps the function charToCom to the final state to produce the turtle graphics commands.

4 Implementation

4.1 Task 1: Implementation

```
-- go from depth n to depth n+1
apply :: State -> [Rule] -> State
apply state rule = concatMap (replace rule) state

replace :: [Rule] -> Char -> State
replace [] c = [c]
replace (Rule rc rs:xs) char = if rc == char
    then rs
    else replace xs char
```

The apply function is designed, so that it takes a state and a list of rules as input and returns a state. The result state is produced by mapping the replace function over each character in the state. For that a concatMap is used as the result should be a single list. The replace function is a helper function for the apply function. It has the logic for applying the rules. If there are no rules to apply the character stays the same. If the rule character (rc) matches with the character (char) we replace it with the state from the rule. Otherwise we recursively call the replace function again on the remaining rules(xs).

4.2 Task 2: Implementation

```
-- expand to target depth
expand :: State -> [Rule] -> Int -> State
expand state rule 0 = state
expand state rule d = expand (apply state rule) rule (d-1)
```

The expand function takes an initial state a list of rules and a target depth. Using recursion it applies the apply function until the target depth is reached. "expand state rule 0 = state" is the base case. If the target depth is zero we just return the current state as the state is unchanged. If the depth is greater than zero expand looks like this "expand state rule d = expand (apply state rule) rule (d-1)". Because this is a recursive implementation the expand function is called until the depth reaches zero and there by achieving the base case, returning the final state with depth n.

4.3 Task 3: Implementation

```
1  -- convert fractal into sequence of turtle graphics commands
2  process :: Fractal -> [Command]
3  process (state, rule, charToCom, depth, scale) =
4      let finalState = expand state rule depth
5      in map charToCom finalState
```

The process function takes a fractal as input. It translates the fractal to turtle graphics commands so the fractal can be drawn. We obtain the final state by using the expand function with the desired depth. Then we map the function, charToCom onto the final state to get the commands. The function charToCom uses pattern matching to decide which command should be chosen based on the input character. For example if the character is F the function chooses Forward. If a character doesn't match the predefined commands it gets matched with Nop(no operation).

5 Testing

The implementation was tested by testing the functions apply, expand and process. The apply function was tested by this command in GHCI: "apply "FXRYF" [Rule 'X' "XRYF", Rule 'Y' "FXLY"]", and then checking if the function returned the desired out put. Which in this case would be "FXRYFRFXLYF". The expand function was tested in a similar way by using this command: "expand "FX" [Rule 'X' "XRYF", Rule 'Y' "FXLY"] 2". The desired output in this case would be "FXRYFRFXLYF". The function process was tested by drawing the different fractals and checking if the output is as desired. This also test apply and expand as these functions, have to be implemented the right way to draw the desired fractals. By looking at the fractals we can see if the implementation is correct. All of the example fractals are provided in the appendix (section 7.1).

6 Conclusion

The three main tasks of implementing the functions apply, expand and process where implemented successfully. The apply function was successfully implemented to apply rules to a state. This was confirmed by testing the function. The expand function was successfully implemented, with the help of the apply function, to reach the targeted depth. This was done by recursively applying the apply function until the desired depth is reached. The correctness of the implementation was also confirmed by testing. The process function that translates a final state into turtle graphics commands was also successfully implemented. The implementation was also shown to be correct by the program drawing the correct fractals. The three implemented functions thus also work together. The current implementation meets the project requirements but future improvements may include optimizing the code or implementing the support for colours and line width to make the fractals look even better.
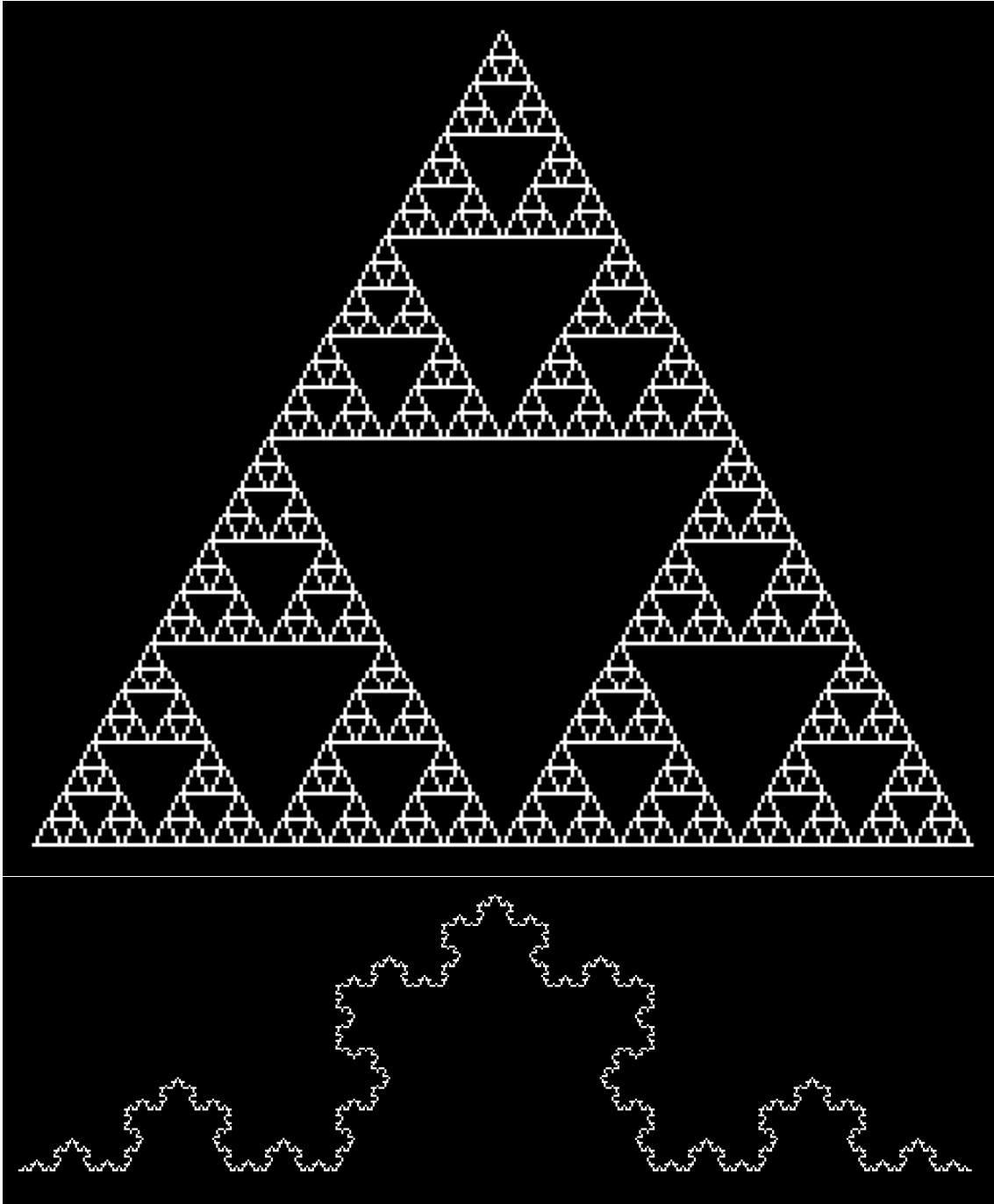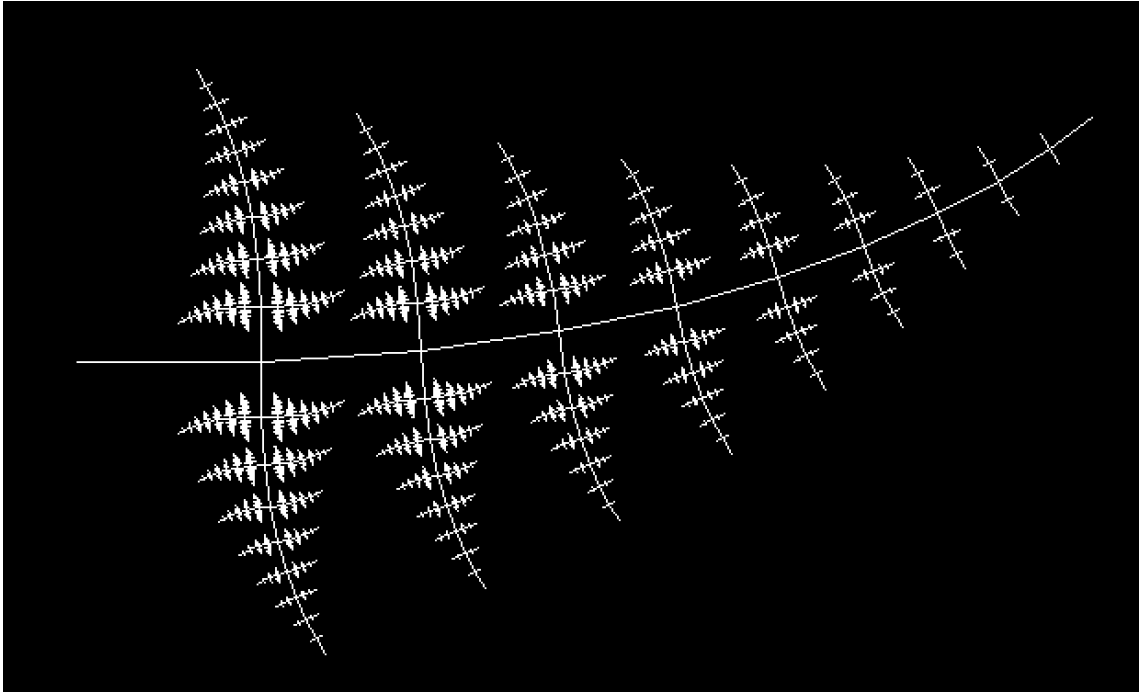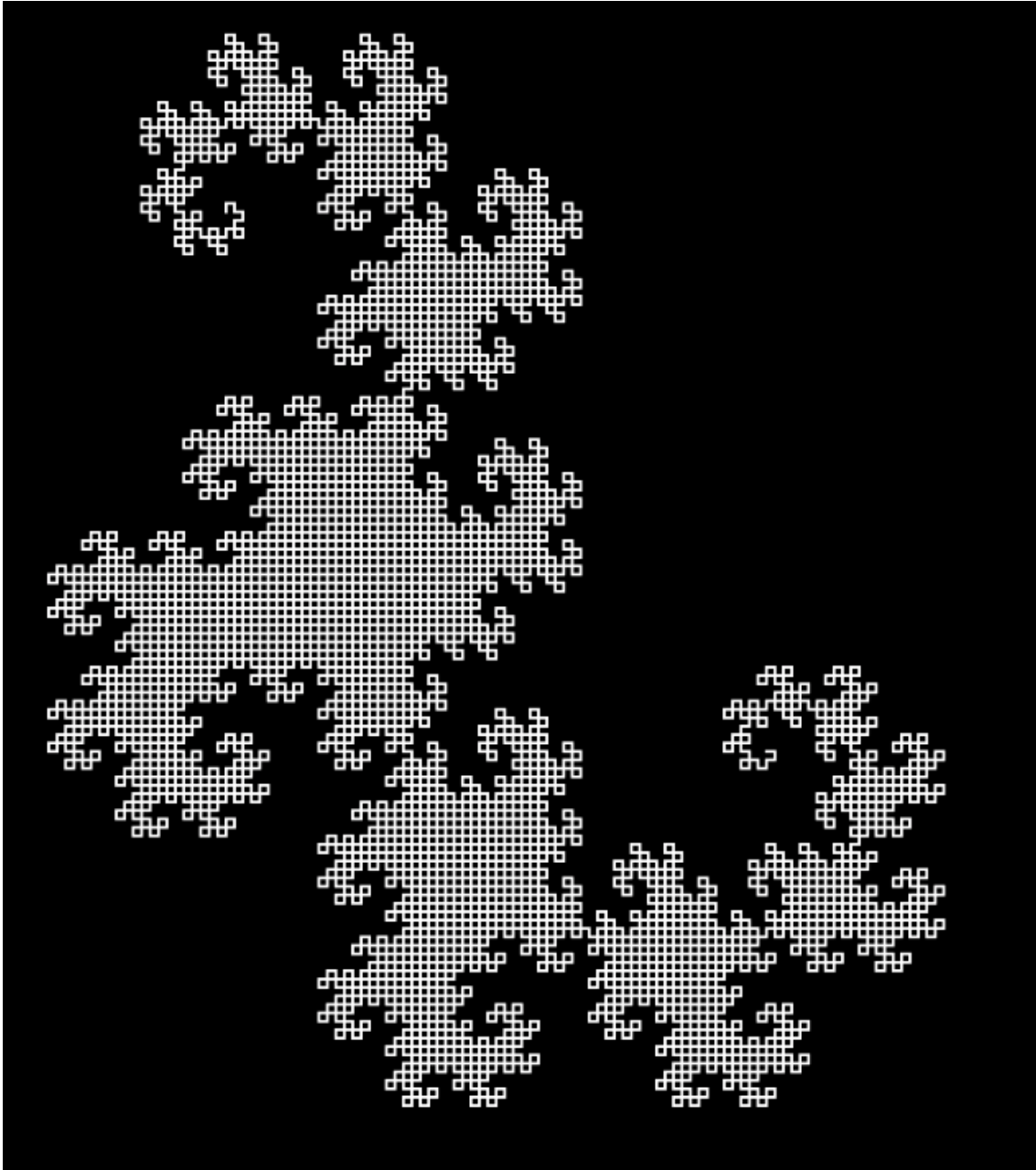
7 Appendix

7.1 Fractals
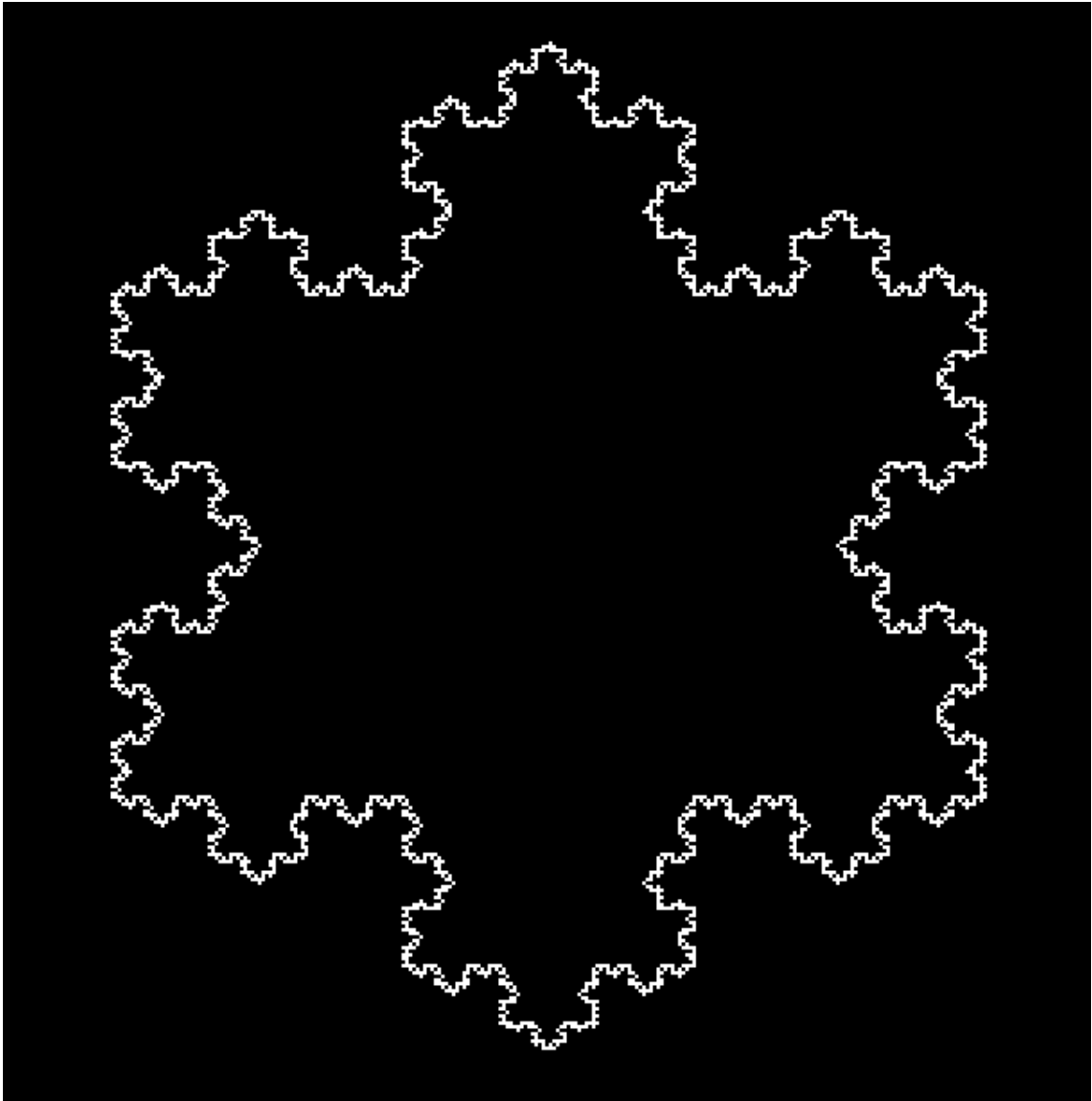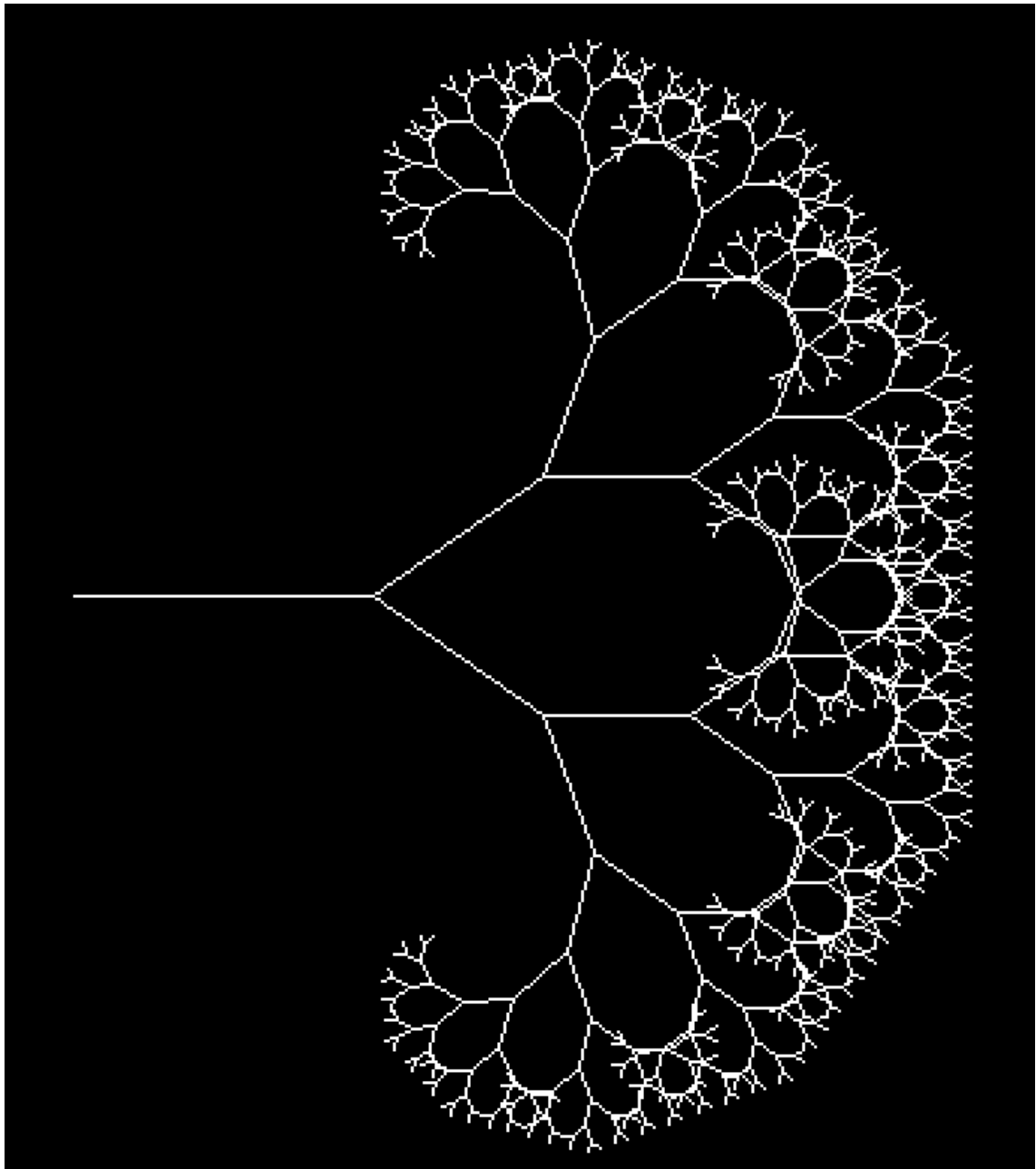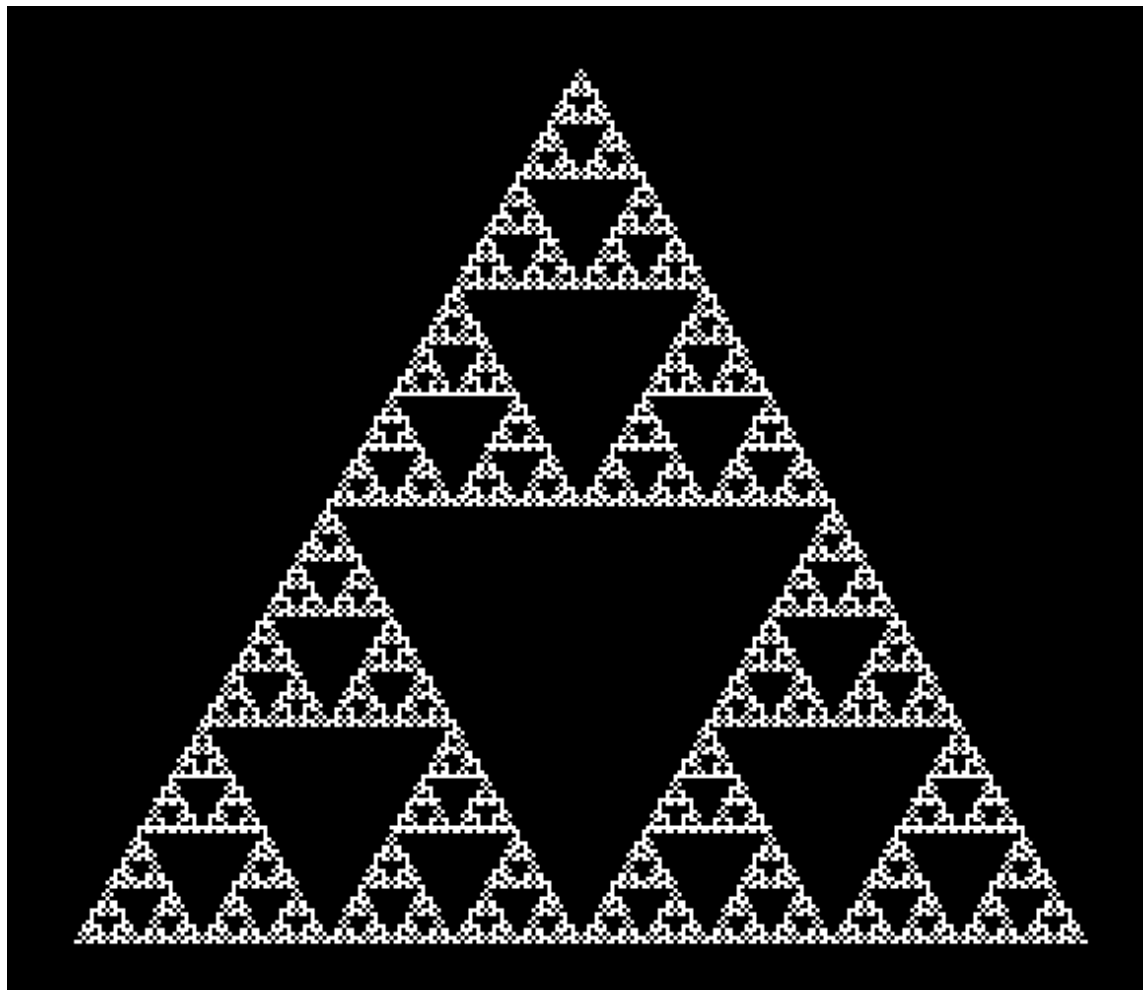
7.2 Code

```haskell
import Graphics.HGL

-- state represented by list of letters
type State = [Char]

-- rule represented by a letter (left-hand side) and a state (right-hand side)
data Rule = Rule Char State deriving Show

-- turtle graphics commands (Nop is no operation)
data Command = Forward | LeftTurn Int | RightTurn Int | Nop | Scale Double |
    Backward deriving Show

-- turtle represented by reference to window, current position, current angle,
    current length
type Turtle = (Window, Double, Double, Double, Double)

-- fractal represented by initial state, list of rules, mapping from letters to
    commands, target depth, initial length
type Fractal = (State, [Rule], Char -> Command, Int, Double)

-- examples for rule lists
rules1 = [Rule 'F' "FLFRFLF"]
```

```
20 rules2 = [Rule 'X' "XRYF", Rule 'Y' "FXLY"]
21
22 -- examples for fractals
23 fractal1 = ("F", rules1, let m 'F' = Forward; m 'L' = LeftTurn 60; m 'R' =
      RightTurn 120 in m)
24 fractal2 = ("FX", rules2, let m 'F' = Forward; m 'L' = LeftTurn 90; m 'R' =
      RightTurn 90; m _ = Nop in m)
25
26 -- go from depth n to depth n+1
27 apply :: State -> [Rule] -> State
28 apply state rule = concatMap (replace rule) state
29
30 replace :: [Rule] -> Char -> State
31 replace [] c = [c]
32 replace (Rule rc rs:xs) char = if rc == char
33     then rs
34     else replace xs char
35
36 -- expand to target depth
37 expand :: State -> [Rule] -> Int -> State
38 expand state rule 0 = state
39 expand state rule d = expand (apply state rule) rule (d-1)
40
41 -- convert fractal into sequence of turtle graphics commands
42 process :: Fractal -> [Command]
43 process (state, rule, charToCom, depth, scale) =
44     let finalState = expand state rule depth
45     in map charToCom finalState
46
47 -- helper function to go from two floating point values to a pair of integers
48 toPoint :: Double -> Double -> Point
49 toPoint x y = (round x, round y)
50
51 -- main turtle graphics drawing function
52 drawIt :: Turtle -> [Command] -> IO ()
53 drawIt _                        []                      = return ()
54 drawIt turtle              (Nop:xs)              = drawIt turtle xs
55 drawIt (w, x, y, angle, len) (Forward:xs)         = let
56   x' = x+len*(cos angle)
57   y' = y-len*(sin angle)
58   in do
59     drawInWindow w (line (toPoint x y) (toPoint x' y'))
60     drawIt (w, x', y', angle, len) xs
61 drawIt (w, x, y, angle, len) (Backward:xs)           = let
62   x' = x-len*(cos angle)
63   y' = y+len*(sin angle)
64   in do
65     drawInWindow w (line (toPoint x y) (toPoint x' y'))
66     drawIt (w, x', y', angle, len) xs
67 drawIt (w, x, y, angle, len) (LeftTurn degree:xs)  = let angle' = angle+(
      fromIntegral degree)*pi/180 in
68     drawIt (w, x, y, angle', len) xs
69 drawIt (w, x, y, angle, len) (RightTurn degree:xs) = let angle' = angle-(
      fromIntegral degree)*pi/180 in
70     drawIt (w, x, y, angle', len) xs
71 drawIt (w, x, y, angle, len) (Scale factor:xs)     = let len' = len*factor in
72     drawIt (w, x, y, angle, len') xs
73
74 -- draw a fractal by opening a window and using turtlegraphics
75 drawFractal fractal@(_, _, _, _, len) = runGraphics (withWindow_ "L-System using
      Turtle Graphics" (1000, 600)
76         (\ w -> do
77          drawIt (w, 500, 300, 0, len) (process fractal)
78          getKey w))
79
80 -- create a list of lists of string, where each list contains the "words" of one
      line
81 split :: String -> String -> [String] -> [[String]]
82 split []        [] []  = []
83 split ('\n':xs) [] []   = split xs [] []
84 split ('\n':xs) [] zss = split xs [] []
85 split ('\n':xs) ys zss = reverse (reverse ys : zss) : split xs [] []
86 split (' ':xs)  [] zss = split xs [] zss
87 split (' ':xs)  ys zss = split xs [] (reverse ys:zss)
88 split (x:xs)    ys zss = split xs (x : ys) zss
89
```

```haskell
90  -- interpret the list of lists as a description of initial state, rules, mapping,
        depth, and length of a fractal
91  interpret :: [[String]] -> State -> [Rule] -> (Char -> Command) -> Int -> Double ->
          Fractal
92  interpret []                    start rules m depth len = (start, rules, m, depth,
        len)
93  interpret (("rule":xs):yss)    start rules m depth len = interpret yss start (rules
          ++ [interpretRule xs]) m depth len where
94    interpretRule (l:"->":rs) = Rule (head l) (foldr (++) [] rs)
95  interpret (("start":xs):yss)   _      rules m depth len = interpret yss (foldr (++)
        [] xs) rules m depth len
96  interpret (("cmd":xs):yss)     start rules m depth len = interpret yss start rules
        (interpretCmd xs m) depth len where
97    interpretCmd [c, "fd"]          m = \x -> if x == (head c) then Forward else m
        x
98    interpretCmd [c, "lt", deg]     m = \x -> if x == (head c) then LeftTurn (read
        deg) else m x
99    interpretCmd [c, "rt", deg]     m = \x -> if x == (head c) then RightTurn (read
         deg) else m x
100   interpretCmd [c, "nop"]         m = \x -> if x == (head c) then Nop else m x
101   interpretCmd [c, "scale", factor] m = \x -> if x == (head c) then Scale (read
        factor) else m x
102   interpretCmd [c, "bk"]          m = \x -> if x == (head c) then Backward else m
         x
103 interpret (("length":arg:xs):yss) start rules m depth _   = interpret yss start
        rules m depth (read arg)
104 interpret (("depth":arg:xs):yss)  start rules m _     len = interpret yss start
        rules m (read arg) len

105
106 -- read from given file and return a fractal
107 readFractal fileName = do
108   text <- readFile fileName
109   return (interpret (split text [] []) [] [] (\x -> error "unknown command") 0 0)

110
111 -- daw a fractal described in an .fdl file
112 drawFdl fileName = do
113   fractal <- readFractal fileName
114   drawFractal fractal

115
116 -- main function that draws the snowflake fractal
117 main :: IO ()
118 main = drawFdl "examples/dragon.fdl"
```