Statistical Inference: Part 1

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Overview

This is a part 1 for project in Statistical Inference cource by JHU. It's dedicated to exploring properties of an exponential distribution

Questions

- 1. Show the sample mean and compare it to the theoretical mean of the distribution.
- 2. Show how variable the sample is (via variance) and compare it to the theoretical variance of the distribution.
- 3. Show that the distribution is approximately normal.

Activating packages

```
library(ggplot2)
```

Simulation

```
#Setting seed for reproducibility purposes
set.seed(42)

#Simulation exponentials - 1000 simulations, 40 observations in each with a labmda of 0.2
sim_exponentials <- replicate(1000, rexp(40, 0.2))</pre>
```

Question 1

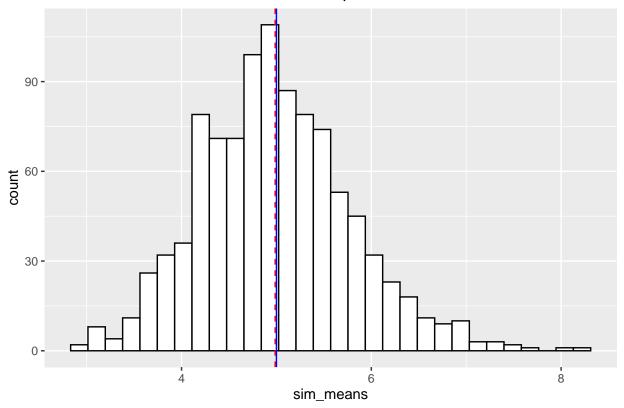
```
sim_means <- apply(sim_exponentials,2,mean)

#Calculating means
emperical_mean <- mean(sim_means)
theoretical_mean <- 1/0.2</pre>
```

```
#Visualising means
ggplot(data.frame(sim_means=sim_means),aes(x=sim_means))+
    geom_histogram(color="black",fill="white")+
    geom_vline(xintercept=emperical_mean,color="red",linetype="dashed")+
    geom_vline(xintercept=theoretical_mean,color="blue")+
    ggtitle("Mean's distribution over simulated samples")
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

Mean's distribution over simulated samples



Emperical mean is 4.9865083, theoretical mean is 5, which are quite close.

Question 2

```
#Calculating standard deviations
empirical_sd <- sd(sim_means)
theoretical_sd <- (1/0.2)/sqrt(40)

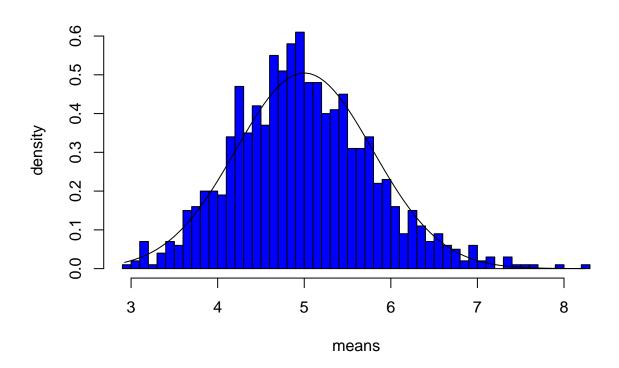
#Calculating variance
empirical_variance <- empirical_sd^2
theoretical_variance <- theoretical_sd^2</pre>
```

Emperical variance is 0.6344405, theoretical variance is 0.625, which are quite close.

Question 3

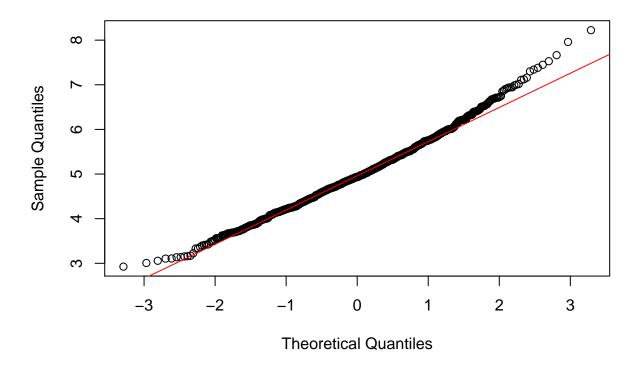
```
#Constructing a plot of means density distribution
xfit <- seq(min(sim_means), max(sim_means), length=100)
yfit <- dnorm(xfit, mean=1/0.2, sd=(1/0.2/sqrt(40)))
hist(sim_means,breaks=40,prob=T,col="blue",xlab = "means",main="Density of means",ylab="density")
lines(xfit, yfit, pch=22, col="black", lty=1)</pre>
```

Density of means



```
#Comparing distribution of averages of 40 exponentials to a normal distribution
qqnorm(sim_means)
qqline(sim_means, col = 2)
```

Normal Q-Q Plot



Due to to the central limit theorem, the distribution of averages of 40 exponentials is very close to a normal distribution.