

HW1

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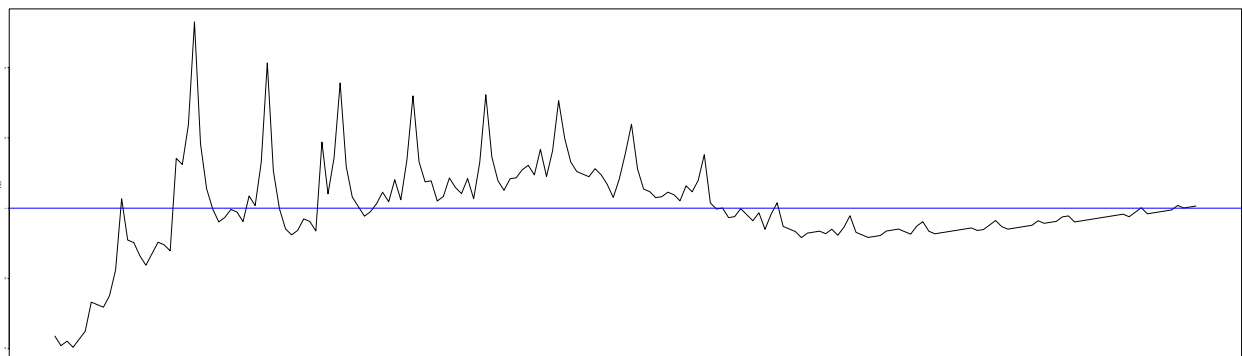
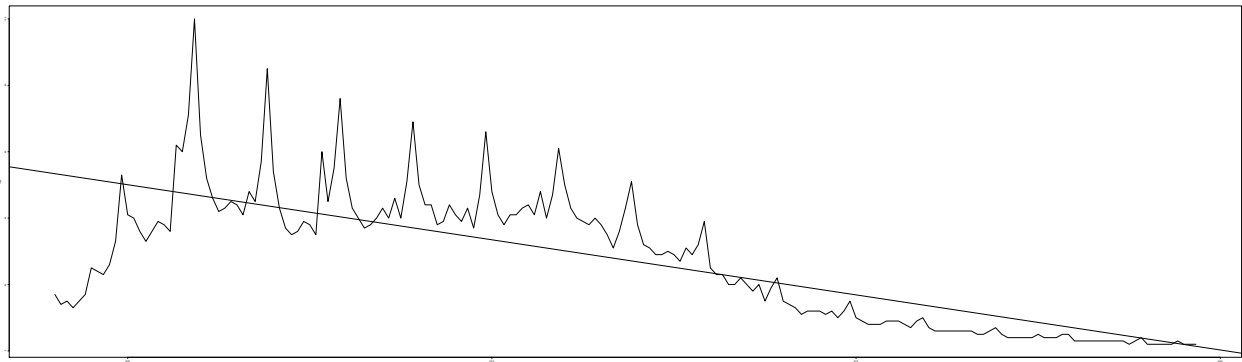
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Computer Practice

```
dataset = read.csv("/Users/li/Desktop/STAT153/iPod.csv")
iPod = ts(dataset$iPod, start = c(2004, 1), frequency = 12)
```

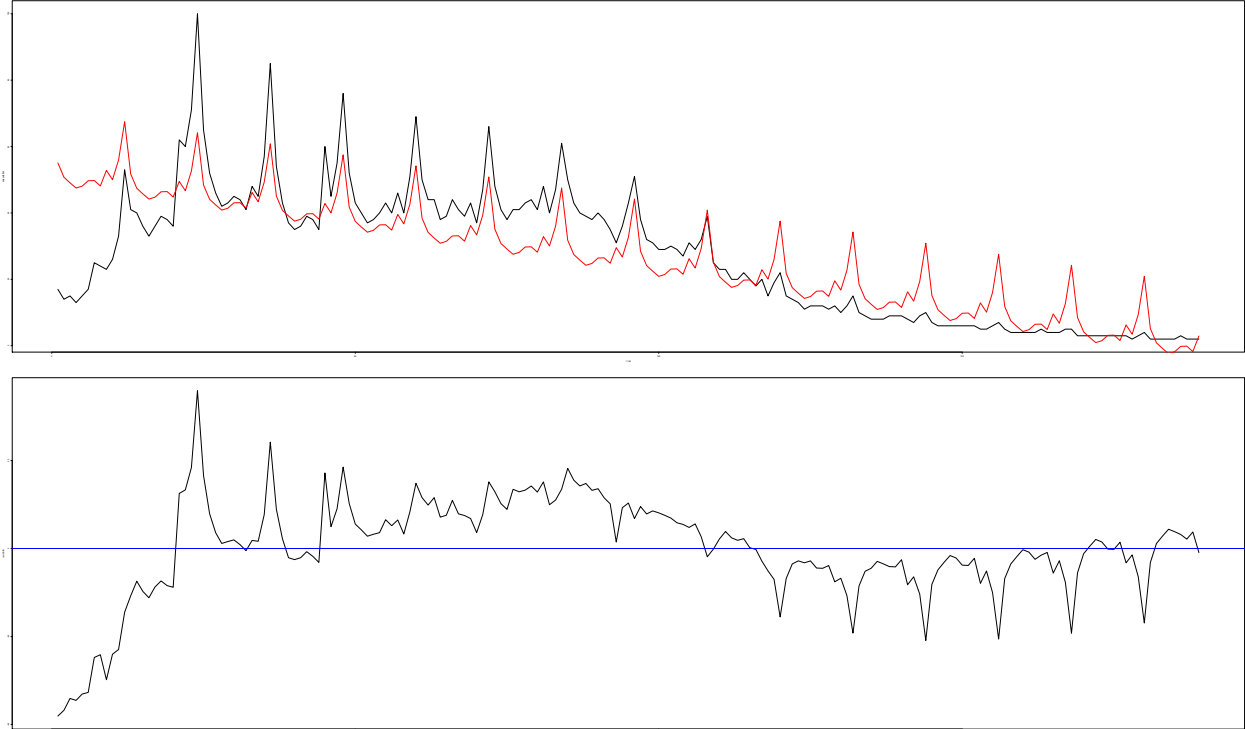
Part 1

```
##
## Call:
## lm(formula = iPod ~ time(iPod))
##
## Coefficients:
## (Intercept)    time(iPod)
##      6704.145         -3.319
```



The trend is downward, showing that iPod salesvolume is decreasing every year. The residuals has cylicity, showing that there may be a seasonality in time series.

Part 2



The trend is downward with cylicity of 12 month, showing that iPod salesvolume is decreasing every year, and have a peak every year. The residuals is not white noise, showing that there may be other factors in regression.

Part 3

The second is trustworthy because it show there is a peak season of iPad, which is in line with reality. (sorry I can't find way to show predicted fitted line. But Both two model doesn't fit well when $t = 190-204$) The reason may be the ipod has become an obsolete product line since 2019. So no more new ipod comes out and the peak doesn't exist.

Questions

$$1. P\{|r_k| \geq 1.96/\sqrt{n}\} = 5\%$$

the number is $5\%N$

$$2. P\{|r_k| \geq 1.96 \times 1.2/\sqrt{n}\} = 2 * (1 - 0.9906) = 0.0188$$

$$3. P_0 = P\{\text{none of } r_k \text{ is outside}\} = 95\%^{100} \quad P_1 = P\{\text{one of } r_k \text{ is outside}\} = 100 * 5\% * 95\%^{99} \\ P_2 = P\{\text{two of } r_k \text{ is outside}\} = 100 * 99/2 * 5\%^2 * 95\%^{98} \quad P_3 = P\{\text{three of } r_k \text{ is outside}\} = \\ 100 * 99 * 98/6 * 5\%^3 * 95\%^{97} \quad P = 1 - P_0 - P_1 - P_2 - P_3 = 0.74$$

4.

(a)

$$\text{Cov}(X_r, Y_s) = 0$$

$$E(X_t + Y_t) = E(X_t) + E(Y_t) = E(X) + E(Y) = \text{const}$$

$$\text{Cov}(X_t + Y_t, X_s + Y_s) = \text{Cov}(X_t, X_s) + \text{Cov}(X_t, Y_s) + \text{Cov}(Y_t, X_s) + \text{Cov}(Y_t, Y_s) = \text{Cov}(X_t, X_s) + \text{Cov}(Y_t, Y_s)$$

only depend on t-s

so $X_t + Y_t$ is weak-stationary

(b)

i) Yes, see prove below.

ii) No, for t even and t odd, distribution is not identical.

iii) Yes, because X is white noise, X is weak stationary

iv) No. When h = 1, X_t is not identically distribute,