

GUJARAT TECHNOLOGICAL UNIVERSITY**BE- SEMESTER-IV (NEW) EXAMINATION – WINTER 2020****Subject Code:3140510****Date:15/02/2021****Subject Name:Numerical Methods in Chemical Engineering****Time:02:30 PM TO 04:30 PM****Total Marks:56****Instructions:**

1. Attempt any FOUR questions out of EIGHT questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

MARKS**Q.1 (a)** Discuss bracketing methods & open methods. **03****(b)** Fit the straight line that best fits to the following data: **04**

| | | | | | |
|---|---|-----|-----|-----|-----|
| x | 0 | 1 | 2 | 3 | 4 |
| y | 1 | 1.8 | 3.3 | 4.5 | 6.3 |

(c) Fit a second degree parabola to the following data **07**

| | | | | |
|---|-----|-----|-----|-----|
| x | 1 | 2 | 3 | 4 |
| y | 1.7 | 1.8 | 2.3 | 3.2 |

Q.2 (a) Find the percentage error in the area of an ellipse when errors of 2% and 3% are made in measuring its major axes respectively. **03****(b)** Perform three iterations of the bisection method to obtain the root of the equation $2 \sin x - x = 0$, correct up to three decimal places. **04****(c)** Find the root of $x^3 - 2x - 1 = 0$ correct up to three decimal places using Secant method (starting from $x_0 = 1.5$ and $x_1 = 2$). **07****Q.3 (a)** Explain the Gauss Jordan method to solve the system of linear equations. **03****(b)** Solve the following system of equations by Gauss Elimination method: **04**

$$\begin{aligned}x + 3y + 2z &= 5 \\2x + 4y - 6z &= -4 \\x + 5y + 3z &= 10\end{aligned}$$

- (c) Find a root of the equation $x^3 + x - 1 = 0$ correct up to four decimal places by using Newton-Raphson iteration formula. **07**
- Q.4** (a) Find the largest eigen value of the matrix **03**

$$A = \begin{bmatrix} 3 & -5 \\ -2 & 4 \end{bmatrix}$$
- (b) Solve the following system of equations by Gauss Jacobi method: **04**

$$\begin{aligned} 6x + 2y - z &= 4 \\ x + 5y + z &= 3 \\ 2x + y + 4z &= 27 \end{aligned}$$
- (c) Solve the following system of equations by Gauss Siedel method: **07**

$$\begin{aligned} x + 2y + z &= 0 \\ 3x + y - z &= 0 \\ x - y + 4z &= 3 \end{aligned}$$

Starting with (1,1,1)
- Q.5** (a) Use the Euler's method to find $y(0.1)$, given that **03**
 $\frac{dy}{dx} = \frac{y-x}{y+x}$, $y(0) = 1$, Taking $h = 0.2$
- (b) Apply 4th order Runge Kutta Method to compute y for **04**
 $x = 0.1$, given that $\frac{dy}{dx} = 2x + y$, $y(0) = 1$, $h=0.1$
- (c) Evaluate $\int_0^6 \frac{dx}{1+x^2}$ by using (1) Trapezoidal rule **07**
(2) Simpson's 1/3 Rule (3) Simpson's 3/8 Rule
- Q.6** (a) Discuss in brief about boundary value problems. **03**
- (b) Using Newton's divided difference formula, evaluate **04**
 $f(8)$ from the following data:
- | | | | | | | |
|------|----|-----|-----|-----|------|------|
| x | 4 | 5 | 7 | 10 | 11 | 13 |
| f(x) | 48 | 100 | 244 | 900 | 1210 | 2028 |
- (c) Use the Taylor series method to find $y(0.2)$, given that **07**
 $\frac{dy}{dx} = 2y + 3e^x$, $y(0) = 1$. Taking $h=0.1$.

Q.7 (a) Derive formula for Trapezoidal Rule of numerical integration. **03**

(b) By Simpson's 3/8 rule, evaluate $\int_0^1 \frac{\sin x}{x} dx$ taking $h = \frac{1}{6}$. **04**

(c) Use Lagrange's interpolation formula to find the value of y when $x = 12$, if the values of x and y are given below: **07**

| | | | | | | |
|---|----|----|----|----|-----|-----|
| x | 11 | 13 | 14 | 18 | 20 | 23 |
| y | 25 | 47 | 68 | 82 | 102 | 124 |

Q.8 (a) Derive formula for Simpson's 1/3 Rule of numerical integration. **03**

(b) Find $\cosh(0.56)$ from the following table using Newton's forward interpolation method. **04**

| | | | | |
|---|----------|----------|----------|----------|
| x | 0.5 | 0.6 | 0.7 | 0.8 |
| y | 1.127626 | 1.185465 | 1.255169 | 1.337435 |

(c) Use Milne's predictor-corrector method to find $y(0.4)$ for $y' = x + y^2$, $y(0)=1$ with $h=0.1$ **07**

GUJARAT TECHNOLOGICAL UNIVERSITY**BE - SEMESTER-IV (NEW) EXAMINATION – WINTER 2021****Subject Code:3140510****Date:03/01/2022****Subject Name:Numerical Methods in Chemical Engineering****Time:10:30 AM TO 01:00 PM****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Simple and non-programmable scientific calculators are allowed.

- | | MARKS |
|---|-----------|
| Q.1 (a) Define following: i) Truncation error ii) Round off error iii) Absolute Error | 03 |
| (b) Find the percentage error in calculating the area of a rectangle when an error of 3% is made in measuring each of its sides. | 04 |
| (c) Derive a recurrence formula for finding Square root of N, using Newton Raphson method and hence compute square root of 10. | 07 |
| Q.2 (a) Discuss bracketing methods & open methods. | 03 |
| (b) Find a root of the equation $x^3 - 4x - 9 = 0$, using the bisection method up to fourth approximation. | 04 |
| (c) Solve the following system of equations by Gauss Siedel method: $\begin{aligned} 5x + y - z &= 10 \\ 2x + 4y + z &= 14 \\ x + y + 8z &= 20 \end{aligned}$ | 07 |
| OR | |
| (c) Using Secant Method, solve $xe^x - 1 = 0$, correct up to three decimal places between 0 and 1. | 07 |
| Q.3 (a) Derive the normal equations to fit a straight line $y = a + bx$ using least square method. | 03 |
| (b) Find a real root of the equation $3x + \sin x - e^x = 0$ by the method of false position correct to four decimal places. | 04 |
| (c) Using Gauss Elimination method solve the system of equations: $\begin{aligned} 2x + y + z &= 10 \\ 3x + 2y + 3z &= 18 \\ x + 4y + 9z &= 16 \end{aligned}$ | 07 |
| OR | |
| Q.3 (a) Find the inverse of $A = \begin{bmatrix} 2 & 6 & 6 \\ 2 & 7 & 6 \\ 2 & 7 & 7 \end{bmatrix}$ | 03 |
| (b) Fit a straight line to the following data: | 04 |

| | | | | | |
|---|---|-----|-----|-----|-----|
| x | 0 | 1 | 2 | 3 | 4 |
| y | 1 | 1.8 | 3.3 | 4.5 | 6.3 |

- (c) Use Lagrange's interpolation formula to find the value of y when $x = 10$, if the values of x and y are given below: 07

| | | | | |
|---|----|----|----|----|
| x | 5 | 6 | 9 | 11 |
| y | 12 | 13 | 14 | 16 |

- Q.4** (a) Write short note on Newton's Forward Interpolation. 03

- (b) Using Newton's divided difference formula, evaluate $f(9)$ from the following data: 04

| | | | | | |
|------|-----|-----|------|------|------|
| x | 5 | 7 | 11 | 13 | 17 |
| f(x) | 150 | 392 | 1452 | 2366 | 5202 |

- (c) Use Newton's forward interpolation formula, find the value of $f(1.6)$. 07

| | | | | |
|------|------|------|------|-----|
| x | 1 | 1.4 | 1.8 | 2.2 |
| f(x) | 3.49 | 4.82 | 5.96 | 6.5 |

OR

- Q.4** (a) Derive formula for Trapezoidal rule of numerical integration. 03

- (b) Following table shows speed in m/s and time in second of a car 04

| | | | | | | | | | | | |
|---|---|------|-------|-------|-------|-------|-------|------|------|------|------|
| t | 0 | 12 | 24 | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 |
| v | 0 | 3.60 | 10.08 | 18.90 | 21.60 | 18.54 | 10.26 | 5.40 | 4.50 | 5.40 | 9.00 |

Using Simpson's 1/3 rule find the distance travelled by the car in 120 second.

- (c) Using Taylor's series method, solve $\frac{dy}{dx} = x + y$, starting from $x = 1, y = 0$ and carry to $x = 1.2$ with $h = 0.1$ 07

- Q.5** (a) Evaluate $\int_0^1 e^{-x^2} dx$ by trapezoidal rule with $n = 10$. 03

- (b) Apply 4th order Runge Kutta Method to compute y for $x = 0.2$, given that $\frac{dy}{dx} = y - \frac{2x}{y}$, $y(0) = 1$ 04

- (c) Find $y(4.4)$ given $5xy' + y^2 - 2 = 0$ with $y(4) = 1, y(4.1) = 1.0049, y(4.2) = 1.0097, y(4.3) = 1.0143$. 07

OR

- Q.5** (a) Explain the method of finite difference approximations to partial derivatives. 03

- (b) By Simpson's 3/8 rule, evaluate $\int_0^1 \frac{\sin x}{x} dx$ taking $h = \frac{1}{6}$ 04

- (c) Write the general linear partial differential equation of the second order in two independent variables. Also determine whether the following partial differential equations are elliptic, parabolic or hyperbolic? 07

$$1. \frac{\partial^2 u}{\partial x^2} + 4 \frac{\partial^2 u}{\partial x \partial y} + 4 \frac{\partial^2 u}{\partial y^2} - \frac{\partial u}{\partial x} + 2 \frac{\partial u}{\partial y} = 0$$

$$2. (1 + x^2) \frac{\partial^2 u}{\partial x^2} + (5 + 2x^2) \frac{\partial^2 u}{\partial x \partial t} + (4 + x^2) \frac{\partial^2 u}{\partial t^2} = 0$$

GUJARAT TECHNOLOGICAL UNIVERSITY**BE - SEMESTER-IV (NEW) EXAMINATION – SUMMER 2021****Subject Code:3140510****Date:06/09/2021****Subject Name:Numerical Methods in Chemical Engineering****Time:02:30 PM TO 05:00 PM****Total Marks:70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Simple and non-programmable scientific calculators are allowed.

MARKS

- Q.1**
- (a) Differentiate between accuracy and precision with appropriate example. **03**
- (b) Derive the relation between number of iterations and absolute error for bisection method. **04**
- (c) Derive the equation for Newton's forward difference polynomial. **07**

- Q.2**
- (a) Using Descartes rule of sign find maximum number of positive and negative roots of the following equation. **03**
- $$f(x) = 2x^7 - x^5 + 4x^3 - 5 = 0$$
- (b) Explain algorithm for finding the root of an equation using Newton-Raphson method. **04**
- (c) A chemical reaction $A \rightarrow B$ takes place in a CSTR. The following model describes the system **07**

$$\frac{C_{in} - C_A}{\tau} - \frac{k\sqrt{C_A}}{K + C_A} = 0$$

where, $k=1$, $K=0.25$, $C_{in}=1$ and $\tau=0.25$. Report C_A obtained after third iteration of Secant method. Consider $C_A=0$ and $C_A=1$ as two initial guesses for Secant method.

OR

- (c) You are designing a spherical tank to hold water for a small village in a developing country. The volume of liquid it can hold can be computed as: **07**

$$V = \pi h^2 \frac{[3R - h]}{3}$$

Where V =volume (m^3), h =depth of water in tank (m), and R = the tank radius (m). If $R=3$ m, what depth must tank be filled so that it holds $30 m^3$? Assume initial value of $h = 2$ m. Use three iterations of the Newton-Raphson method and calculate absolute error after each iteration.

- Q.3**
- (a) Discuss about the pitfalls of Gauss elimination method and techniques for improvement. **03**
- (b) Explain algorithm for finding the root of an equation using False-Position method. **04**
- (c) The relationship between stress ' τ ' and the strain ' γ ' for a pseudoplastic fluid can be expressed by the following equation: **07**

$$\tau = \mu \gamma^n$$

The following data come from a 0.5% hydroxethylcellulose in water solution. Using linear least square method, Estimate the parameters ' μ ' and ' n '.

| | | | | | |
|----------|------|------|------|------|-------|
| γ | 50 | 70 | 90 | 110 | 130 |
| τ | 6.01 | 7.48 | 8.59 | 9.19 | 10.21 |

OR

- Q.3**
- (a) Explain the algorithm for Gauss-Jordan method. **03**
- (b) Derive formula for Trapezoidal rule for numerical integration. **04**
- (c) An investigator has reported the data tabulated below for an experiment to **07**

determine the growth rate of bacteria k (per d), as a function of oxygen concentration C (mg/L). It is known that such data can be modeled by the following equation:

$$k = \frac{k_{\max} C^2}{C_s + C^2}$$

Where C_s and k_{\max} are parameters. Use a transformation to linearize this equation. Then use linear regression to estimate C_s and k_{\max} and predict the growth rate at $C = 2$ mg/L.

| | | | | | |
|---|-----|-----|-----|-----|-----|
| C | 0.5 | 0.8 | 1.5 | 2.5 | 4 |
| k | 1.1 | 2.4 | 5.3 | 7.6 | 8.9 |

- Q.4** (a) Discuss about convergence criteria for the Gauss-Siedel method. **03**
 (b) Derive equations to fit a straight line ($y = a_0 + a_1x$) with the least square method. **04**
 (c) A nutrient is administered by diluting it with water. The flowrate, Q (ml/min) and the nutrient concentration C ($\mu\text{g/ml}$) both vary with time. The total amount of nutrient delivered in one hour is: **07**

$$m = \int_0^{60} Q(t)C(t)dt$$

The following data is given:

| | | | | | | | |
|---------------------------|-----|-----|-----|-----|-----|-----|-----|
| t (min) | 0 | 10 | 20 | 30 | 40 | 50 | 60 |
| Q(t) (ml/min) | 52 | 45 | 48 | 46 | 53 | 50 | 47 |
| C(t) ($\mu\text{g/ml}$) | 1.2 | 1.5 | 2.4 | 1.9 | 2.0 | 2.2 | 1.6 |

Using Simpson's 1/3 rule calculate total amount of nutrient introduced to water in 1 hour.

OR

- Q.4** (a) Explain about the system of ill-conditioned equations using appropriate example. **03**
 (b) Consider the following data: **04**

| | | | | |
|---|------|------|------|-----|
| x | 0.2 | 0.3 | 0.4 | 0.5 |
| y | 0.83 | 1.15 | 1.42 | 1.7 |

 Using Lagrange interpolation to compute, value of y at $x=0.325$
 (c) Find the isothermal work done on the gas as it is compressed from $V_1 = 22$ L to $V_2 = 2$ L using Simpson's 1/3 rule. **07**

$$W = \int_{V_1}^{V_2} P dV$$

Use following data for calculation purpose.

| | | | | | |
|--------|-------|------|------|------|------|
| V, L | 2 | 7 | 12 | 17 | 22 |
| P, atm | 12.20 | 3.49 | 2.04 | 1.44 | 1.11 |

- Q.5** (a) 1. List out the interpolation methods, which can be used when data points are available at unequal interval. **03**
 2. Differentiate between interpolation and regression technique.
 (b) Explain Milne's predictor-corrector method. **04**
 (c) Consider the RL circuit model is given by **07**

$$\frac{dI}{dT} = \frac{V}{L} - \frac{IR}{L}$$

Where inductance $L=2$, resistance $R=2.5$, voltage $V=5$. The initial value of current at $t=0$ is $I(0)=0$. Compute the value of I at $t=2$ using Euler's method with step size of 0.5.

OR

- Q.5** (a) Differentiate between bracketing and open methods to solve non-linear algebraic equations. **03**
- (b) Explain in brief about ordinary differential equation - boundary value problems. **04**
- (c) Hot ball is exposed to atmosphere, where it loses heat to the atmosphere and Newton's Law of Cooling gives relation between Temperature (T) and time (t): **07**

$$\frac{dT}{dt} = -0.5(T - 30)$$

Initial temperature of ball is 80 °C. Calculate ball temperature at time t=2 using RK-4 method with step size of 2.

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GUJARAT TECHNOLOGICAL UNIVERSITY**BE - SEMESTER-IV (NEW) EXAMINATION – SUMMER 2022****Subject Code:3140510****Date:29-06-2022****Subject Name:Numerical Methods in Chemical Engineering****Time:10:30 AM TO 01:00 PM****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.
4. Simple and non-programmable scientific calculators are allowed.

- Q.1** (a) Explain following terms: 1) Significant figures, 2) Truncation Error. **03**
- (b) Define: 1) Absolute error, 2) Relative error, 3) Percentage error, 4) Inherent Error. **04**
- (c) Evaluate sum $S = \sqrt{4} + \sqrt{6} + \sqrt{8}$ to four significant digits and find absolute & relative errors. **07**

- Q.2** (a) Describe intermediate value properties. **03**
- (b) Find the root of equation $x \log_{10} x = 1.2$ correct upto four decimal places using bisection method. **04**
- (c) Enlist limitations of Newton-Raphson Method also find root of the function $x^4 - x = 10$ upto three decimal places using Newton-Raphson method. **07**

OR

- (c) Solve following equation using Newton Raphson technique starting with $x_0 = 0.5$ and $y_0 = 1.5$, carry out two iterations. **07**
- $$\sin x - y = -0.9793$$
- $$\cos y - x = -0.6703$$

- Q.3** (a) Explain Gauss elimination method with its pitfalls. **03**
- (b) Solve the system of equation using Gauss Jordan method. **04**
- $$2x + y + z = 10; 3x + 2y + 3z = 18; x + 4y + 9z = 16$$
- (c) Solve following set of equation using jacobi's iteration method correct up to three decimal places. $x_0 = y_0 = z_0 = 0$ **07**

$$20x + y - 2z = 17$$

$$3x + 20y - z = -18$$

$$2x - 3y + 20z = 25$$

OR

- Q.3** (a) Give the normal equation to fit the straight line $y = a + bx$ to n observations. **03**
- (b) Find the eigen-values and eigenvectors of the matrix **04**

$$\begin{bmatrix} 5 & 4 \\ 1 & 2 \end{bmatrix}$$

- (c) The pressure and volume of a gas are related by the equation $pV^\gamma = k$, γ and k being constants. Fit this equation to the following set of observations: **07**

| | | | | | | |
|-------------------------|------|------|------|------|------|------|
| p (kg/cm ²) | 0.5 | 1.0 | 1.5 | 2.0 | 2.5 | 3.0 |
| V (lts) | 1.62 | 1.00 | 0.75 | 0.62 | 0.52 | 0.46 |

- Q.4 (a)** Establish Newton's backward interpolation formula. **03**
- (b)** If P is pull required to lift a load W by means of a pulley block, find a linear law of form $P = mW + C$ connecting P & W, using following data. **04**

| | | | | |
|---|----|----|-----|-----|
| P | 12 | 15 | 21 | 25 |
| W | 50 | 70 | 100 | 120 |

- (c)** Obtain the density of a 26% solution of H_3PO_4 in water at 20 °C during using Lagrange's interpolation formula can we perform the same calculation using Newton's forward difference interpolation formula? Yes or No? **07**

| | | | | |
|---------------|--------|--------|--------|--------|
| y (Density) | 1.0764 | 1.1134 | 1.2160 | 1.3350 |
| x % H_3PO_4 | 14 | 20 | 35 | 50 |

OR

- Q.4 (a)** Write an algorithm for trapezoidal rule. **03**
- (b)** Using Newton's backward difference formula, construct an interpolating polynomial of degree 3 for the data: $f(-0.75) = -0.0718125$, $f(-0.5) = -0.02475$, $f(-0.25) = 0.3349375$, $f(0) = 1.10100$. **04**
- (c)** Evaluate $\int_0^{0.6} e^{-x^2}$ using the trapezoidal rule and Simpson's $1/3^{rd}$ rule, taking $h = 0.1$ **07**

- Q.5 (a)** Discuss in brief about the boundary value problem. **03**
- (b)** Compute the value of $\int_{0.2}^{1.4} (\sin x - \log x + e^x) dx$ using Simpson's $3/8$ rule. **04**
- (c)** Using Euler's method, find an approximate value of y corresponding to $x = 1$, given that $dy/dx = x + y$ and $y = 1$ when $x = 0$. **07**

OR

- Q.5 (a)** Describe Milne's predictor-corrector method. **03**
- (b)** Apply the Runge - Kutta fourth order method to find an approximate value of y when $x = 0.2$ given that $dy/dx = x + y$ and $y = 1$ when $x = 0$. **04**
- (c)** Solve by Taylor's series method the equation $\frac{dy}{dx} = \log(xy)$ for y(1.1) and y(1.2), given y(1) = 2. **07**
