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**INFO 6205 - Fall 2021**

**Assignment No : 3**

**Task :**

- To implement height-weighted Quick Union with Path Compression and check that the unit tests for this class all work.
- Using the implementation of UF\_HWQUPC, develop a UF client that takes an integer value  $n$  from the command line to determine the number of connections.
- To determine the relationship between the number of objects ( $n$ ) and the number of pairs ( $m$ ) generated.

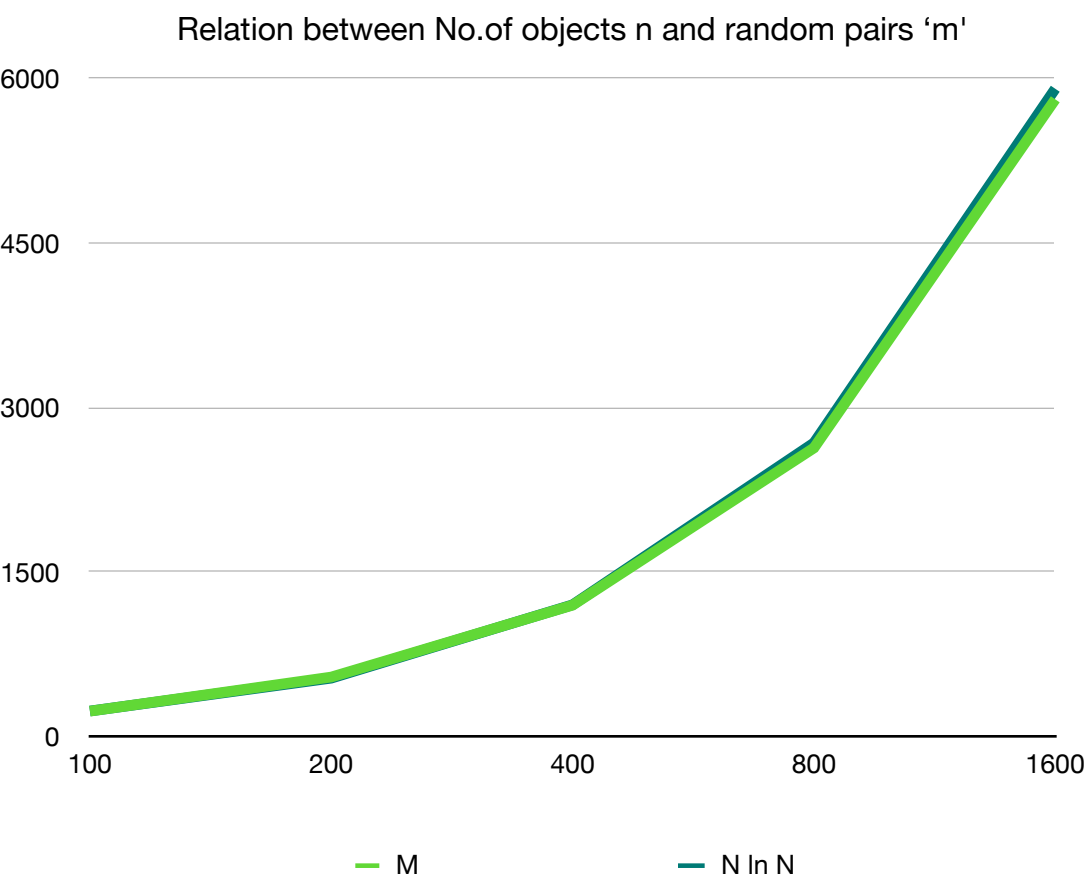
**Relationship Conclusion :** After performing a series of experiments by passing different arguments of  $N$  (100,200,400,800,1600), it can be concluded that the relation between number of random pairs generated (edges) 'M' and the number of objects 'N' is

$$M \approx 1/2 N \ln N$$

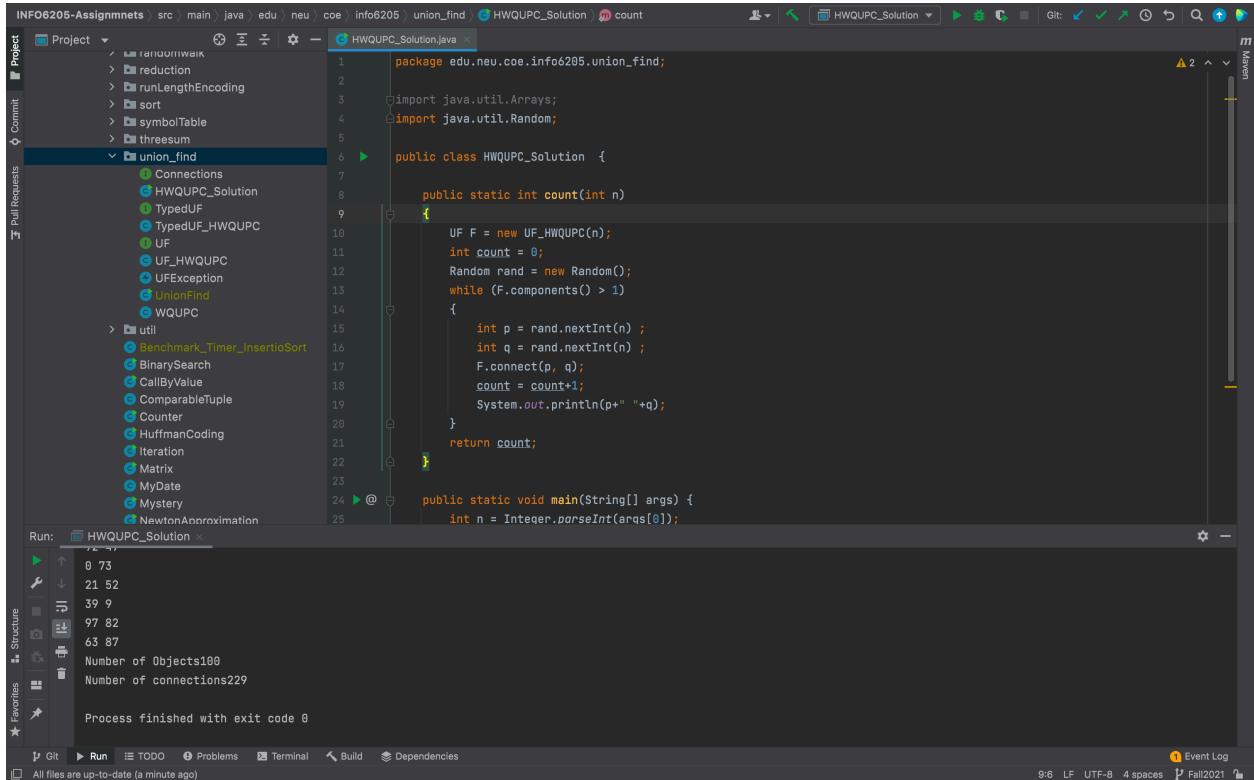
**Findings:**

For  $n = 100$ ,  $M = 229$ ,  $1/2N \ln N = 230.25$   
For  $n = 200$ ,  $M = 540$ ,  $1/2nN \ln N = 529.83$   
For  $n = 400$ ,  $M = 1195$ ,  $1/2N \ln N = 1198.29$   
For  $n = 800$ ,  $M = 2628$ ,  $1/2N \ln N = 2673.84$   
For  $n = 1600$ ,  $M = 5806$ ,  $1/2N \ln N = 5902.20$

N	M(Actual)	M = 1/2 N ln N (Expected)
10	229	230,25
200	540	529,83
400	1195	1198,29
800	2628	2673,84
1600	5806	5902,20



## Output Screenshot:



```
package edu.neu.coe.info6205.union_find;

import java.util.Arrays;
import java.util.Random;

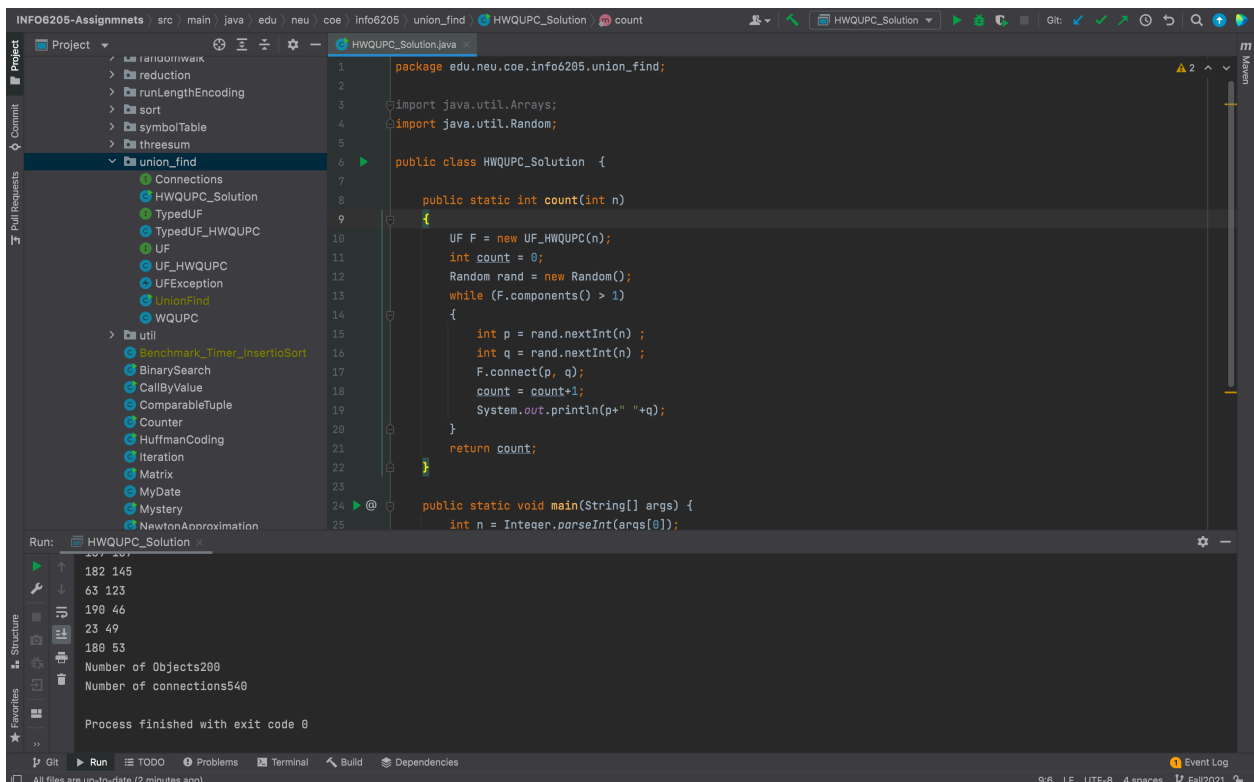
public class HWQUPC_Solution {

    public static int count(int n)
    {
        UF F = new UF_HWQUPC(n);
        int count = 0;
        Random rand = new Random();
        while (F.components() > 1)
        {
            int p = rand.nextInt(n);
            int q = rand.nextInt(n);
            F.connect(p, q);
            count = count+1;
            System.out.println(p+" "+q);
        }
        return count;
    }

    public static void main(String[] args) {
        int n = Integer.parseInt(args[0]);
    }
}
```

Run: HWQUPC\_Solution

0 73  
21 52  
39 9  
97 82  
63 87  
Number of Objects100  
Number of connections229  
Process finished with exit code 0



```
package edu.neu.coe.info6205.union_find;

import java.util.Arrays;
import java.util.Random;

public class HWQUPC_Solution {

    public static int count(int n)
    {
        UF F = new UF_HWQUPC(n);
        int count = 0;
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            int q = rand.nextInt(n);
            F.connect(p, q);
            count = count+1;
            System.out.println(p+" "+q);
        }
        return count;
    }

    public static void main(String[] args) {
        int n = Integer.parseInt(args[0]);
    }
}
```

Run: HWQUPC\_Solution

182 145  
63 123  
190 46  
23 49  
180 53  
Number of Objects200  
Number of connections540  
Process finished with exit code 0

```
package edu.neu.coe.info6205.union_find;

import java.util.Arrays;
import java.util.Random;

public class HWQUPC_Solution {

    public static int count(int n)
    {
        UF F = new UF_HWQUPC(n);
        int count = 0;
        Random rand = new Random();
        while (F.components() > 1)
        {
            int p = rand.nextInt(n);
            int q = rand.nextInt(n);
            F.connect(p, q);
            count = count+1;
            System.out.println(p+" "+q);
        }
        return count;
    }

    public static void main(String[] args) {
        int n = Integer.parseInt(args[0]);
    }
}
```

Run: HWQUPC\_Solution

318 81  
334 296  
301 46  
3 124  
221 23  
Number of Objects400  
Number of connections1195  
Process finished with exit code 0

```
package edu.neu.coe.info6205.union_find;

import java.util.Arrays;
import java.util.Random;

public class HWQUPC_Solution {

    public static int count(int n)
    {
        UF F = new UF_HWQUPC(n);
        int count = 0;
        Random rand = new Random();
        while (F.components() > 1)
        {
            int p = rand.nextInt(n);
            int q = rand.nextInt(n);
            F.connect(p, q);
            count = count+1;
            System.out.println(p+" "+q);
        }
        return count;
    }

    public static void main(String[] args) {
        int n = Integer.parseInt(args[0]);
    }
}
```

Run: HWQUPC\_Solution

278 198  
645 785  
322 37  
534 447  
504 787  
Number of Objects800  
Number of connections2628  
Process finished with exit code 0



