CBET lolol

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Declaration

I hereby certify that the material of this thesis, which I now submit for the award of Doctor of Philosophy, is entirely my own work unless otherwise cited or acknowledged within the body of text.

Philip Moloney

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Abstract

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Contents

List of Acronyms

Rad-MHD Radiative Magnetohydrodynamics

HEDP High Energy Density Physics

LPIs Laser-Plasma Instabilities

CBET Cross-Beam Energy Transfer

ICF Interial Confinement Fusion

PiC Particle in Cell

GO Geometric Optics

IB Inverse-Bremmstrahlung

List of Tables

List of Figures

1 SOLAS, A 3-D Laser Ray Trace and Cross-Beam Energy Transfer Model

This chapter will describe the SOLAS code, a 3-D Laser ray tracing module implemented in the Radiative Magnetohydrodynamics (Rad-MHD) code CHIMERA. The chapter begins with a discussion of why ray tracing is frequenctly used to model 'long-pulse' lasers for High Energy Density Physics (HEDP) experiments and why the standard framework is inadequate to model Laser-Plasma Instabilities (LPIs). It will then go on to describe the ray-trajectory solver, electric-field reconstruction and Cross-Beam Energy Transfer (CBET) components of the model in detail. Discussion of the validity of the model components will be included. The numerical methods will also be presented alongside an extensive set validation problems to verify the implementation.

1.1 Ray Tracing for Hydrodynamic Simulations of Fusion Plasmas

Nano-second length ('long-pulse') lasers are often used as an external energy source in the field of HEDP, for example in laboratory-astrophysics experiments or Interial Confinement Fusion (ICF) implosions. Experimental design and analysis for these experiments must often be supported with fluid Rad-MHD simulations. The laser must therefore be described in these codes by a theoretical framework that is both valid to the problem and computationally tracatable. The physical processes by which lasers interact with plasma is a result of microscopic couplings between the laser field and particles or plasma waves. The detailed microphysics of these interactions are often studied using Particle in Cell (PiC) codes or wave-based solvers, typically for scales and durations of tens of micrometres and hundreds of picoseconds. Coupling these tools directly to multi-dimensional hydrodynamic simulations, which are often used for millimetre and nanosecond scales, would usually be computationally intractable.

The Geometric Optics (GO) assumptions are often widely applicable for HEDP laser-plasma interactions (validitiy discussed in detail for ICF plasmas in section 1.5.8) and therefore ray-tracing offers a computationally tractable approach to modelling lasers in these experiments. By assuming static hydrodynamic profiles (which is normally valid for the propagation time of light through the computational domain) a laser beam can be discretised into a bundle of rays and the ray equations can then be integrated along their path to solve for the trajectory of the light, assuming that refraction dominates over diffraction. A discrete amount of power can also be given to each ray. If there is a

suitable model for the power-absorption rate, this can also be integrated along the ray to provide an energy source for the plasma. In many laser-driven HEDP experiemnts, frequency-doubled or -tripled lasers and long scale-length plasmas mean that Inverse-Bremmstrahlung (IB) is the dominant deposition process. There are well established models for IB that are suitable for implementation in ray-tracing codes, because they only require knowledge of the local plasma conditions, which are easily accesible via interpolation from the hydrodynamic grid to rays. The combination of the ray equations and IB deposition therefore is the basis for the vast majority of laser-modules coupled to hydrodynamic codes.

In laser-driven ICF experiments however, another class of interaction, LPIs are vitally important to the energetics of the implosion. For example CBET leads to a zeroth-order correction to the energy deposited in direct-drive experiments at the OMEGA laser facility, reducing coupled power late in the implosion by $\sim 50\%$. They cannot be included in the simple framework described above because they are non-linear[1] and rely on knowledge of the electric field or intensity of the light. Implementation in a tracing code therefore necessitates a method by which the seperate light waves can 'talk' to eachother. For example, the CBET code described in this chapter stores information for seperate components of laser beams on a common grid which can then interact via the 'pump-depletion iterations,' described in section 1.5.7. Additionally, the knowledge of electric field or intensity is problematic because this is not an attribute which standard GO rays posses. Heuristically, rays have an associated power, so an area is required to obtain an intensity. The evolution of a portion of the beam front's area is governed by a first order expansion of the Helmholtz equation, rather than a zeroth order expansion, as is most commonly used in ray-tracing packages for hydrodynamic codes. The first order expansion introduces an equation for the ray amplitude which can be solved in a variety of ways and used to obtain the electric field of the light. Section 1.4 describes the approach taken to solving for the amplitude of the rays in SOLAS, which is to track the area of a triangle[2] of rays around a zeroth order GO ray.

For direct-drive ICF simulations, it is also desireable to have a 3D ray trace, where rays travel and refract in 3 dimensions. In some computational direct-drive studies, particularly in 1D hydrodynamic simulations, simplified laser models are employed in which rays travel radially toward the target. This simplification is can lead to significant deviations from reality, as it neglects any refractive losses, which can be significant late in the implosion as the target converges. It also leads to deposition occuring further in radially compared to a true 3D ray trace, leading to an overestimation of the drive. The growth of LPIs also depends on vector summations of light and plasma wavevectors, so a 3D ray trace is necessary when modelling these effects. Predictive direct-drive simulations therefore necessitate a fully 3D ray-trace, even when coupled to 1D hydrodynamics.

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[1]Non-linear in this context means that the interaction involves the interaction of multiple light and plasma waves.

[2]For a 2D ray trace, a pair of rays is used rather than a triangle.

1.2 Exisiting Cross-Beam Energy Transfer Models

A non-exhaustive list will be presented here of existing codes used to model Cross-Beam Energy Transfer in ICF relevant conditions. This is provided as context for the work presented in this section.

1.2.1 Ray Based Models

Explain that only ASTER-IFRIIT can do 3D CBET+hydro LDD sims, and that uses a very different model to that presented here. Briefly describe models for hohlraum sims but don't spend much time on this. Include a discussion of methods to reconstruct field/ intensity and why mine is best lolol.

1.2.2 Wave Solvers

Explain LPSE briefly and its use as a validation code.

1.2.3 Particel in Cell Code Approaches

Explain that non-linear saturation effects may be important to CBET and how PiC is used to study this.

1.3 SOLAS 3-D Laser Ray Trace

This section will follow on from the theory section which derived the equations of ray tracing. It shall discuss 1D ray tracing and why that can be inadequate (doing CBET properly and limited to a specific use case) and compare it to 3D.

1.3.1 Equations of Rays and Adaptive Integration

Also mention here why I didn't use Kaiser solution (refraction from Snell was found to create unacceptable noise in the ray amplitude estimation). Somewhere mention that ray deposition is interpolated onto neighbrouing cells using shape functions to reduce noise. Talk about how additional quantities are integrated along ray trajectory which are described in CBET section. However, the derivatives of these other things are assumed to be constant over a single laser step and therefore are not included in the adaptive integration.

Talk about how we use adaptive RK4 to integrate rays. Mention that adaptive solvers allow large steps in flat regions and accurately resolve the turning points.

1.3.1.1 Ray Solver Validation

Quadratic trough, cylindrical helix and blast wave tests

Quadratic trough   Basic test of ray solver.

Cylindrical Helix   Test of refraction in non Cartesian coordinates and also of refraction in directions without gridding.

Blast wave   Test of inverse Bremmstrahlung absorption.

1.3.2 Ray Initialisation

Give details on random sampling, uniform and invers-projection methods explaining their relative strengths and weaknesses.

1.3.3 Solas Mesh Structure

Talk about the parallelisation method in Chimera (domain based MPI) and why a good hydro domain decomposition is not good for laser load-balancing. Mention that for direct-drive, (which drove most design philosophy for the model), laser uniformly illuminate the surface, so rays are uniformly distributed across sphere. Therefore, Ideal domain decomposition for ray trace has processors which each cover an equal area on the surface of a sphere. Therefore split the grid solid-angularly, so that even for 1D LDD problems, can load balance across sphere.

1.3.3.1 Semi-Structured Eulerian Grid with Combined Cells

Mention that also for 3D Eulerian spherical meshes near the poles, cell volumes go to zero. At a minimum to estimate laser quantities within a cell, the requirement for total number of rays is therefore dictated by the polar region. Equivalently for a given number of rays, noise will be much worse at the poles. Therefore a novel 'semi-structured' grid was designed to circumvent this issue without giving up the advantages of an Eulerian grid (ease of implementation and interpolation between grids). Cells are combined in phi and theta to have the same dphi and dtheta as the equatorial cells on the grid, giving a roughly equal area on each raidla surface.

Also mention how cells are combined in r adaptively, which gives improved resolution in the vicinity of the caustic, where deposition, CBET and refraction are singificant. Note however that resolution is limited to the hydrodynamic resolution and the laser grid is not entirely separate. This does make interpolation between grids easier though.

1.4 Ray Based Field Reconstruction and Ray Sheets

Say that we want to find the field to get CBET. For rays this means solving the transport equation to get ray amplitude and then using amplitude to get field. Talk about the concept of ray amplitude and how it can be related to an area of adjacent rays.

1.4.1 Amplitude Estimate from Neighbour Rays

Go into detail about how the area is obtained from neighbour rays. Talk about the concept of sheets and caustics as divergence of amplitude. Also talk about 'Interpolation' from rays to cells and vice versa.

1.4.2 Caustic Field Capping

Say that since amplitude diverges in the caustic region, necessary to cap it. In reality diffraction would limit the field in this region, but standard geometric optics rays can't model diffraction. Therefore typical approach which we follow is to limit the reconstructed field to a sensible, diffraciton-limited value.

1.4.2.1 Field Limiter Approach

Say that this is the approach used throughout the thesis apart from in some validation problems where it is labelled. Caps the field to the maximum of a Airy function (ray going up linear density profile).

1.4.2.2 Etalon Integral

This is an improvement which basically allows for deviations from linearity. This is not used normally, other than when cell size « wavelength, because it needs knowledge of the other sheet from the beam which is present in caustic region. Could be implemented using linear interpolation. However, typically we don't have sufficient angular resolution in combined cell grid (at least for 1D hydro) to reliably interpolate sheet to sheet via this grid. It is generally observed however that the field limiter approach is sufficient.

1.4.3 Field Reconstruction Validation

Using Russ' paper with lovely test comparisons to LPSE. Define the electron density profile here.

1.4.3.1 1D Reflected Beam

Just a simple test of field capping compared to an analytic problem, without refraction.

1.4.3.2 2D Reflected Beam

Same as above, but now for non-normally incident rays, accounting for refraction. Show test results in both Cartesian and Cylindrical.

1.5 Ray Based CBET Model

Explain that ray based CBET uses the linear gain discussed in theory section. Say that since this assumes homogineity, effectively applies to small ray steps, which is typically

well satisfied. Also say that this homogeneity within a computational cell and nearest neighbour interpolation of field means that it is not necessary to adaptively integrate the CBET gain.

1.5.1 Power Change of Rays due to CBET

Describe how ray energy changes due to CBET from linear gain models (either fluid or kinetic). Say how when including with inv brem, the deposited power and CBET change must be got carefully (i.e. Marozas paper).

1.5.1.1 Fluid CBET Gain

Breifly discuss the fluid CBET gain and explain why it is easier to use for code validation.

1.5.1.2 Kinetic CBET Gain

Breifly discuss the kinetic CBET gain and why it is better for predictive simulations.

1.5.2 Dynamic memory structure for storing Fields and CBET Gains

Give the scaling of storing fields and gains for every beam. Say that therefore a dynamic memory structure is used which only stores the fields and gain in cells where they are present. Also state that although the ray trace module must be done in double to numerical errors (e.g. omega differences in resonance and difference between rays), gain is stored as a single which greatly reduces cost. Give an estimate for how much this reduces the overall memory requirements.

1.5.3 Doppler Shift of Frequency

Mention time dependant refractive index results in a frequency shift of light. This is small, however it is significant to include in CBET models as it can shift the resonance.

1.5.4 Caustic Gain Truncation

Say that because nearest neighbour interpolation of the fields is used, there exists unphyscial interaction regions where a cell has a field but ray hasn't passed through that portion of the cell. This problem becomes particularly bad at ray turning points, where a significant amount fo CBET occurs. Therefore a method called 'CGT' is used to effectively enhance the laser grid resolution in the vicnity of caustics. In cells where a ray from a specific sheet experience a caustic, the field entry for that sheet is divided geometrically, assuming that the caustic is locally a plane. If a ray from another sheet passes through the cell and is on the 'unlit' side of the caustic plane, it will not experience CBET gain. Ray steps are also limited to the caustic plane. Other codes have shown that this approach significantly improves energy conservation.

1.5.5 Coherent Caustic Correction and Caustic Region Identification

Say how the field reconstruction assumption works everywhere apart from at caustics, where it underestimates the field. Follow what Russ says in his paper about CC correction and how it significantly improves energy conservation.

1.5.5.1 Geometric Approach to identifying the caustic region

Other codes find caustic region by phase diff and phase interpolation. We can't interpolate due to resolution issues. Therefore implemented a new, geometric approach to finding the caustic region. Talk about how location of rays is stored for each sheet, partitioned by whether they are over or under the amplitude cap. If a cell has rays from both in a cell, then a plane is found between the two to split the cell into caustic and non-caustic. If a cell has only capped rays then the whole thing is caustic. When a ray from another beam passes through, CC mult is applied if in the caustic region.

1.5.6 Energy Conservation in Ray Based CBET Models

Talk about how energy is conserved away from caustics when converged.

1.5.7 Pump Depletion Iterations

Talk about why it is necessary to iterate the ray trace. Mention that it is possible to store ray locations and avoid performing ray trace all over again, but that approach is not taken due to memory limitations. Talk about convergence parameter. Mention necessity of damping for complicated, many beam simulations.

1.5.8 Model Assumptions, Applicability and Validity to ICF

Discuss the key assumptions of the CBET model and whether it is valid to use for LDD and LID.

1.5.9 Computational Efficency and Scaling

Talk about how the CBET model is quite expensive. Give the scaling laws from Russ' paper and explain how that means for many beams, CBET is bound to be the dominant cost in the simulation. Also say how it shows that memory is a big consideration for CBET models as the gains and fields must be stored.

1.6 Coupling to Hydrodynamics and Example Use

Here present an entire explanation for the model working coupled to Hydrodynamics.

1.6.1 Power Deposition

Say that the deposited power is just added as an energy source to the electrons. If running in 1D or 2D, it is integrated over other directions first. Say that when starting from $t = 0$, often use a cold-start routine, which uniformly deposits power at the critical surface of a spherical capsule. This creates an under-dense small region in which the rays can refract and deposit energy. This is unsatisfactory for imprint simulations, where early time imprinting is important, but that is not considered for this thesis.

1.6.2 Time step limiter

Limit timstep based on the fractional electron energy change. Don't limit timestep in cells far from critical. This is usually the limitting timestep for 'cold start' simulations initially, until deposition begins to occur in hot cells.

1.6.3 Ray Trace Frequency

For many beam simulations, such as direct-drive simulations, the laser operator (especially with CBET) is typically one of the more expensive parts of the code. In the steady state of an implosion, the coronal plasma conditions don't significantly change on the global hydrodynamic timestep. Therefore the deposition also doesn't change much meaning that previously calculated Pdep can be stored and reapplied on subsequent timesteps. Especially for CBET simulations, this can reduce runtime by order of magnitude. Currently the ray trace is performed every timestep up until a pre-specified 'warm up' time has expired. Then the ray trace is performed at a pre-specified frequency by the user. Experimentation has found that for Omega scale simulations, increasing frequency of calculations doesn't significantly change the answer above ... .

Because LDD pulses often start with a low intensity and then ramp up, CBET gains are also often minimal until late in the implosion. Therefore field reconstruction and CBET iterations are only performed after a specified start time, normally when the hard-sphere intensity reaches about $1 \times 10^{14}\ Wcm^{-2}$. CBET iterations are then performed on the laser frequency.

An improved approach shall soon be implemented where laser iterations occur at dt_{laser} from section 1.6.2.

1.6.4 Computational Diagnostics

Say that a variety of diagnostics can be output. Qpower with and without CBET. Geometric intensity. Electric field (from single or all beams), optionally split into inbound and reflected components, both with and without CBET.

1.6.5 Example use on Omega Shot 89224

First briefly describe the shot, showing pulse shape and target.

1.6.5.1 1-D Rad-Hydro, 3-D Ray-Trace with CBET Simulation

Describe the simulation parameters used, e.g. cell resolution, flux limiter etc. Show the absorbed power vs time and effect of CBET. Show instantaneuos radial profiles. Show integrated parameter comparison to LILAC post-shot simulation. Describe the previous method of tuning, involving a 2D scan of flux limiter and power multipliers. Say how it's great that the $flim_e = 0.06 \rightarrow 0.15$ and CBET combination now gives a predictive capability for OMEGA shots.

1.6.5.2 3-D Post Process of Absorption Non-Uniformity

Mention how the model can also be used as a postprocess. CHIMERA can restart from 1-D data into spherically symmetric 3-D profiles. Ray Trace and CBET can then be performed through these profiles to understand the absorption non-uniformity present due to CBET. Note that comparison of 1-D and 3-D simulations shows that thermal conduction does a good job of smoothing angular deviations in coronal plasma conditions. The assumption of spherically symmetric profiles for the laser is therefore deemed valid, and it is a technique typically used by post-process CBET codes.

MAYBE?? Mention how ray noise means that we can't use direct deposition. Therefore use Pdep from field estimate, which is much cleaner.

Talk about how CBET enhances angular non-uniformity. Show modal decomposition.

1.7 Future Model Extensions

Say that there is even more laser/ CBET physics that is interesting and can be implemented within the raytracing framework. Some are straightforward to implement, while others more difficult and computationally expensive.

1.7.1 Langdon Effect on Abosprtion

Describe Langdon from a kinetic perspective and why it reduces absorption. Describe how you can fit it and include as a modification to ray tracing absorption if you have the field/ intensity. Describe the magnitude of the effect for ICF like conditions. Describe breifly how it would be implemented, say it would not be difficult.

1.7.2 Langdon Effect on CBET

Describe what this is. Say that it is important for high overlapping intensities, eg hohlraum LEH. Say that it is thought to stabilise the CBET interaction in indirect drive configurations and remove the need for artificial clamps. Describe breifly how it would be implemented, say it would not be difficult.

1.7.3 Polarised CBET

Describe how ion accoustic waves are driven by beat between electric fields from light and therefore is polarisation dependent. Say how on OMEGA, RPP smoothing means that each beam is split into 2 sub-beams with linear polarisation. Say that these do not have a symmetry to the configuration about the sphere. Say that this leads to mode-1 on OMEGA. Say that you can track polarisation of rays and trace these sub-beams independently. Would make it more expensive, but definitely feasible.

1.7.4 Bandwidth for CBET Mitigation Studies

Describe how bandwidth should reduce LPI growth rates. Understanding the desired bandwidth to mitigate CBET is a key consideration for design of future laser sysytems. Fields can be modified to include discrete wavelengths to model bandwidth.

1.7.5 Additional LPIs

Could look at TPD, SBS and SRS. In theory not a difficult problem to do backscatter, but side-SRS is difficult, because additional rays would need to be launched. This could make the model more useful to indirect-drive experiments and design of ignition scale direct-drive facilities, where SRS is thought to be important energetically due to long scale lengths.

1.8 Conclusions

Say that the chapter has described the validity and implementation of Solas and validated it. Culminated in demonstrating that the model can reproduce post-shot simulations of an Omega shot from the Lilac code which includes a CBET model. This demonstrates that the Chimera code now has a predictive capability for Omega scale direct drive experiments, as no free parameter tuning was required.

Appendices

A Numerics Appendices

Bibliography

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