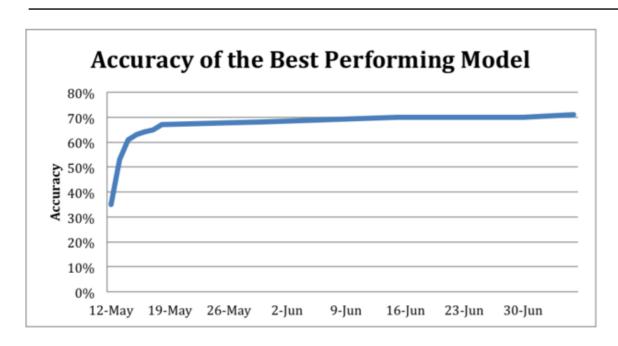


# DECISION TREES

#### **QUESTIONS FROM LAST TIME - SUPPORT VECTOR MACHINES**

- RBF!?!? What the hell is that?
- Tradeoff between slack and misclassified samples?
- Applying SVM to classify N classes
- More data preparation techniques

#### WHAT CAN YOU DO WITH AN 80% ALGORITHM?



A few months ago, my company, CrowdFlower, ran a machine learning competition on <a href="Kaggle">Kaggle</a>. It perfectly highlighted the biggest opportunity (and challenge) with machine learning: What do you do with an 80% accurate algorithm?

We uploaded data collected on our platform and Kaggle sent it out to over 1,000 data scientists, who competed to see who could build the best search model.

The simplest approach gave a baseline accuracy of 32%. Within hours a team beat that with a 35% accurate model. By the next morning, one team already had a 53% accurate model.

With Microsoft's <u>Azure ML</u> and IBM's investment in <u>Watson</u>, making models is easier than ever. Companies no longer need a Google-size R&D budget to make machine learning applicable to their business. These models aren't perfect, but they're useful. The new challenge for businesses is how to integrate an imperfect machine-learning algorithm into their existing workflow.

### **DECISION TREE AGENDA**

- I. DECISION TREES
- II. FITTING DECISION TREES
- III. OBJECTIVE FUNCTIONS
- IV. REGULARIZATION
- V. PROS/CONS & USAGE
- VI. DECISION TREE LAB
- VII. RANDOM FOREST (TIME PERMITTING)

# **DECISION TREE LEARNING OBJECTIVES**

- 1. Understand how decision trees function for classification problems
- 2. Learn the objective functions used in building decision trees
- 3. Learn the regularization process in decision tree building

# I. DECISION TREES

#### **TYPES OF ML SOLUTIONS**

# Continuous Categorical

Supervised

Regression

Classification

Unsupervised

Dimension Reduction

Clustering

Decision trees are automatically generated rules based models that can be used in both classification and regression. We will focus on classification trees due to their superior performance.

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As with any other model, we begin with a set of features  $\mathbf{X}$ , and a set of categorical response variables  $\mathbf{y}$ 

The features can be both continuous and categorical and do not require any scaling or preprocessing

At its heart, a decision tree classifier is a non-parametric hierarchical classification technique

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non-parametric: no parameters (beta), no distribution assumptions

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non-parametric: no parameters (beta), no distribution assumptions

**hierarchical:** consists of a sequence of questions which yield a class label when applied to any record

Q: How is a decision tree represented?

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- A: Using a configuration of nodes and edges.

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- A: Using a configuration of nodes and edges.

More concretely, as a multiway tree, which is a type of (directed acyclic) graph.

In a decision tree, the nodes represent questions (test conditions) and the edges are the answers to these questions.

The top node of the tree is called the **root node**. This node has 0 incoming edges, and 2+ outgoing edges.

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A **leaf node** has 1 incoming edge and, 0 outgoing edges. Leaf correspond to class labels.

#### NOTE

The nodes in our tree are connected by directed edges.

These directed edges lead from parent nodes to child nodes.

# **EXAMPLE - DATA**

**Table 4.1.** The vertebrate data set.

Name	Body	Skin	Gives	Aquatic	Aerial	Has	Hiber-	Class
	Temperature	Cover	Birth	Creature	Creature	Legs	nates	Label
human	warm-blooded	hair	yes	no	no	yes	no	mammal
python	cold-blooded	scales	no	no	no	no	yes	reptile
salmon	cold-blooded	scales	no	yes	no	no	no	fish
whale	warm-blooded	hair	yes	yes	no	no	no	mammal
frog	cold-blooded	none	no	semi	no	yes	yes	amphibian
komodo	cold-blooded	scales	no	no	no	yes	no	reptile
dragon								
bat	warm-blooded	hair	yes	no	yes	yes	yes	mammal
pigeon	warm-blooded	feathers	no	no	yes	yes	no	bird
cat	warm-blooded	fur	yes	no	no	yes	no	mammal
leopard	cold-blooded	scales	yes	yes	no	no	no	fish
shark								
turtle	cold-blooded	scales	no	semi	no	yes	no	reptile
penguin	warm-blooded	feathers	no	semi	no	yes	no	bird
porcupine	warm-blooded	quills	yes	no	no	yes	yes	mammal
eel	cold-blooded	scales	no	yes	no	no	no	fish
salamander	cold-blooded	none	no	semi	no	yes	yes	amphibian

source: http://www-users.cs.umn.edu/~kumar/dmbook/ch4.pdf

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source: http://www-users.cs.umn.edu/~kumar/dmbook/ch4.pdf

#### **EXAMPLE - DECISION TREE**

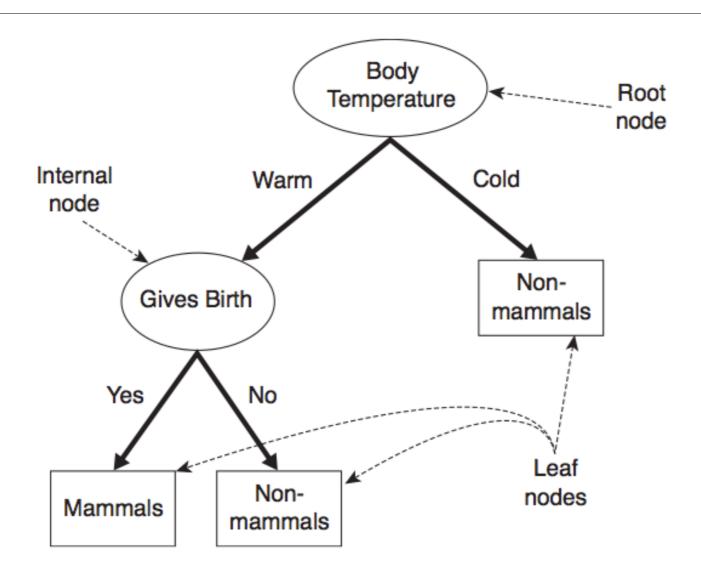
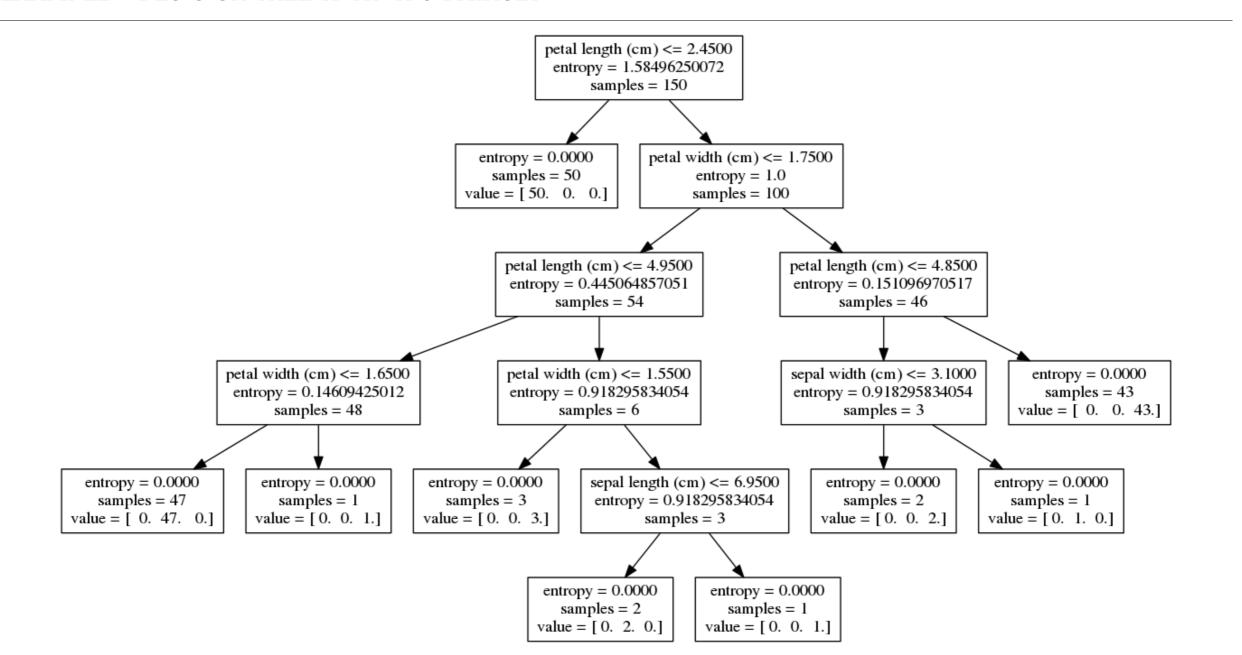


Figure 4.4. A decision tree for the mammal classification problem.

source: http://www-users.cs.umn.edu/~kumar/dmbook/ch4.pdf

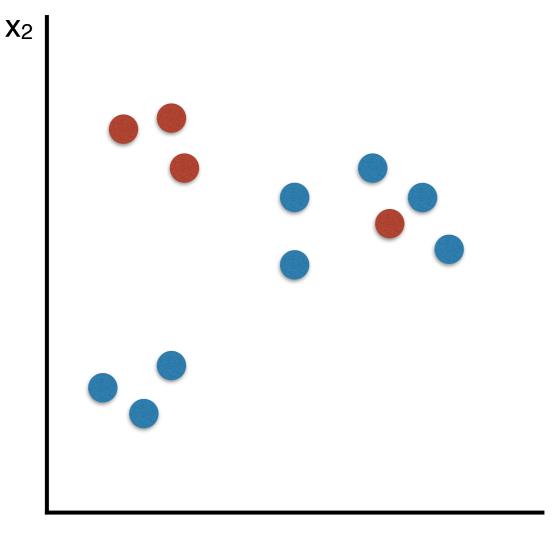
#### **EXAMPLE - DECISION TREE WITH IRIS DATASET**



# ILBUILDING DECISION TREES

Let's go over an example of how one might be built with binary classes in R<sup>2</sup> space (i.e. two features).

- Our goal will be to split the space into regions.
- Inside each region, we'll classify any point in that space as the **max voted class** within that region
- We will only consider constant splits (no linear splits based on more than one feature)
- We can finish when either every leaf is pure, we have reached a max depth, or when there are less than x amount of data points at a node



# Within a region:

Prediction: Most common class label

Error: Fraction of misclassified labels

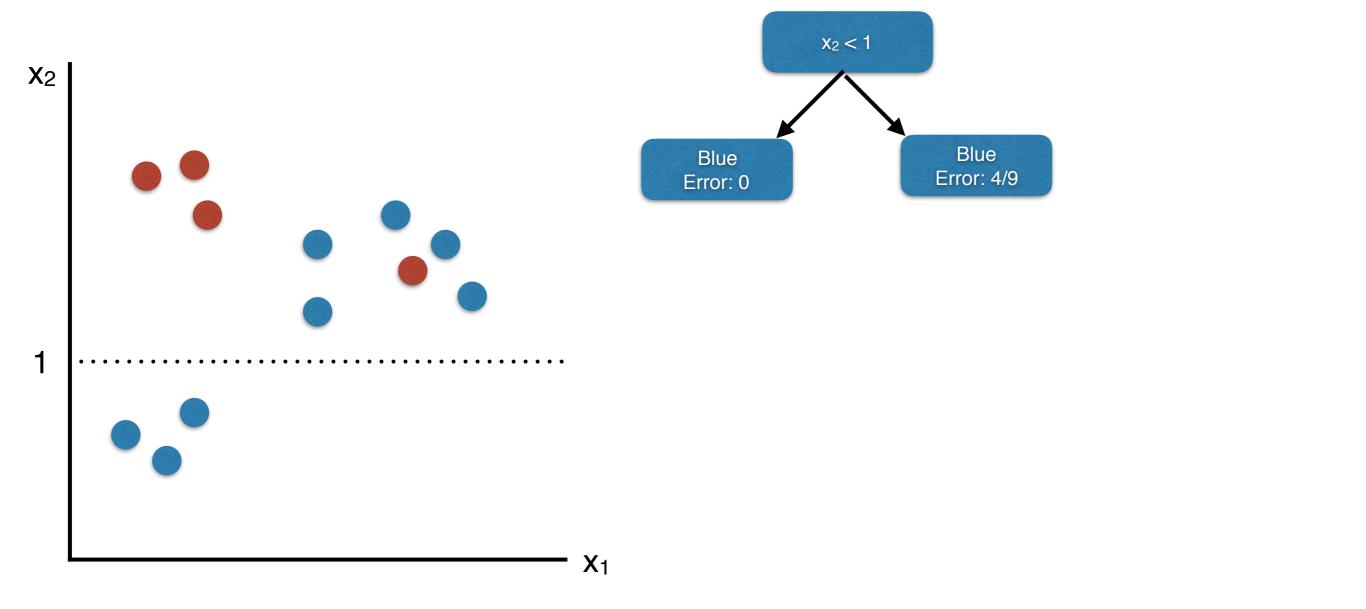
# In the entire space:

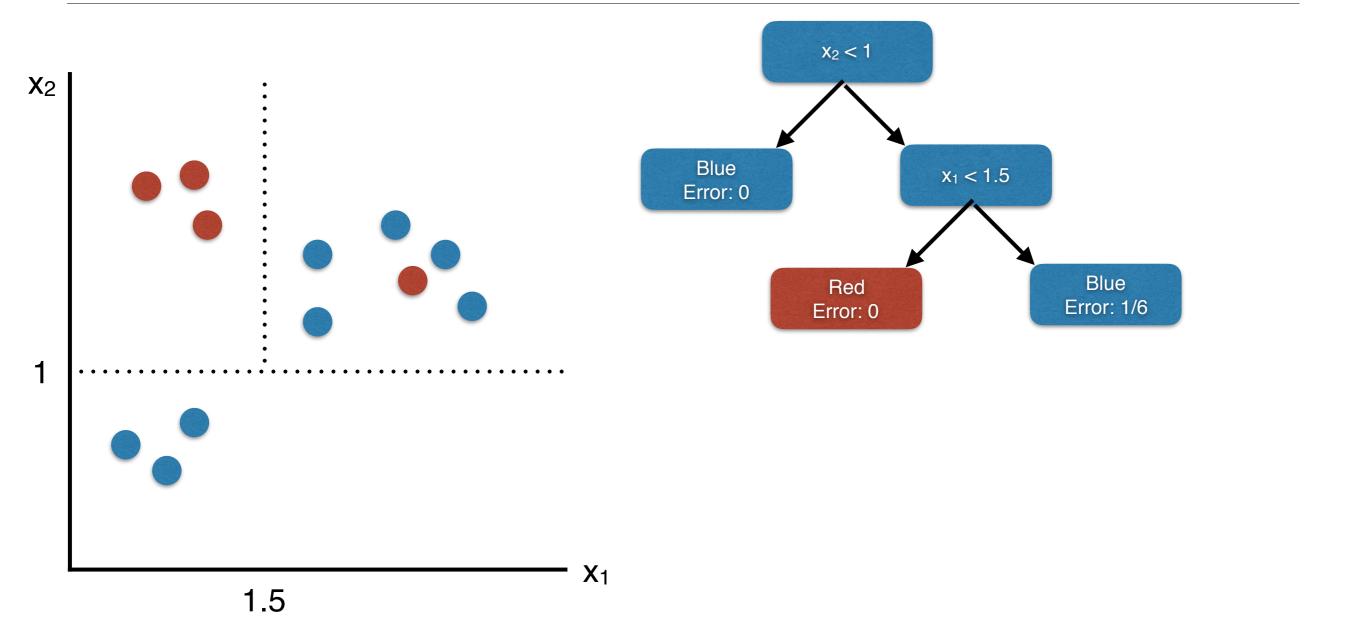
N = 12 points

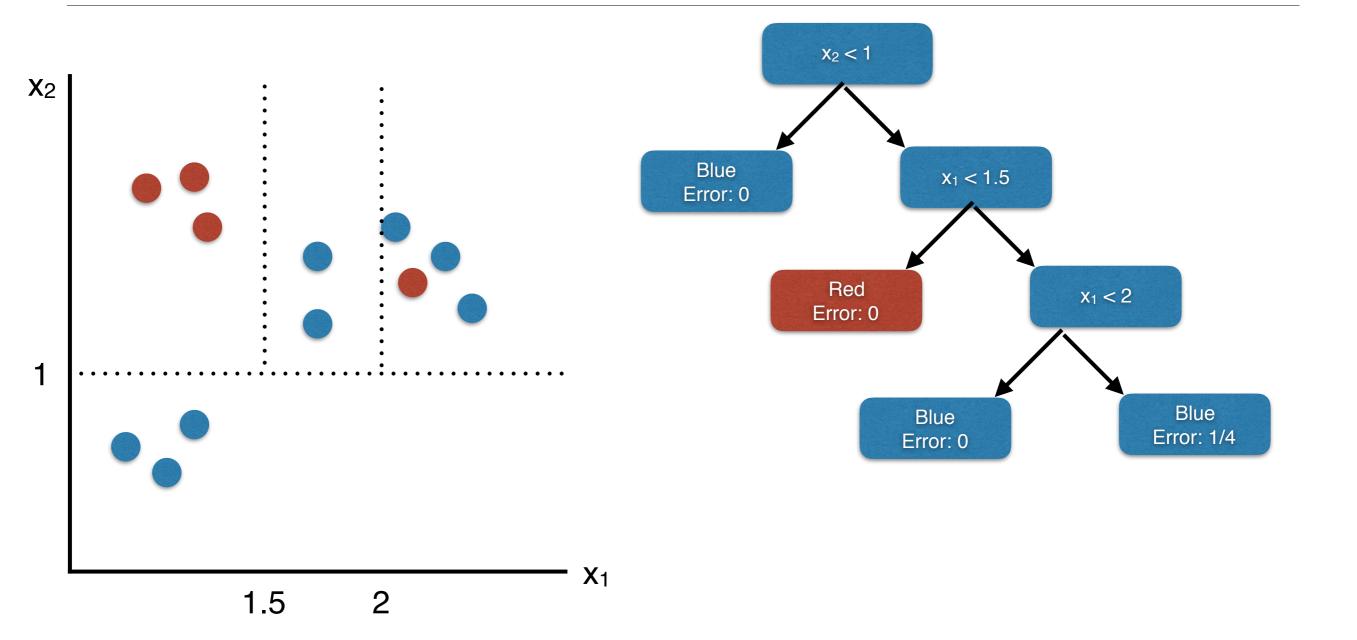
Prediction = Blue

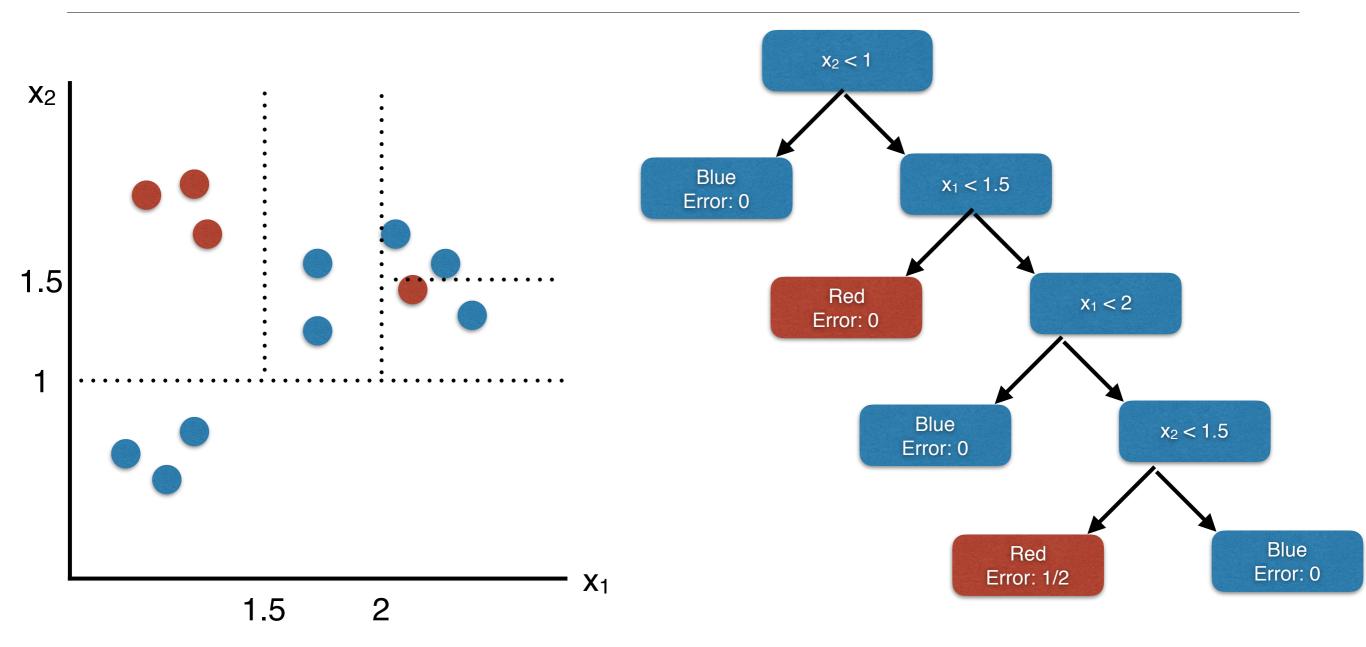
Error = 4 / 12 = 33% misclassification

error









Okay, so we went over an example process of what the subdivision of the regions looked like. Let's formalize this more.

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But this is generally too complex to be practical  $\rightarrow 0(2^n)$ .

- Q: How do we find a practical solution that works?
- A: Use a heuristic algorithm.

The basic method used to build (or "grow") a decision tree is Hunt's algorithm.

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This is a greedy recursive algorithm that leads to a local optimum.

greedy — algorithm makes locally optimal decision at each step recursive — splits task into subtasks, solves each the same way local optimum — solution for a given neighborhood of points

Hunt's algorithm builds a decision tree by recursively partitioning records into smaller & smaller subsets.

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The partitioning decision is made at each node according to a metric called purity.

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The partitioning decision is made at each node according to a metric called purity.

A partition is 100% pure when all of its records belong to a single class.

Consider a binary classification problem with classes  $Y_1$ ,  $Y_2$ . Given a set of records  $D_t$  at node t, Hunt's algorithm proceeds as follows:

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1) If all records in  $D_t$  belong to class  $Y_1$ , then t is a leaf node corresponding to class  $Y_1$ .

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1) If all records in D<sub>t</sub> belong to class Y<sub>1</sub>, then t is a leaf node corresponding to class Y<sub>1</sub>.

### NOTE

This is the *base case* for the recursive algorithm.

Consider a binary classification problem with classes  $Y_1$ ,  $Y_2$ . Given a set of records  $D_t$  at node t, Hunt's algorithm proceeds as follows:

2) If  $D_t$  contains records from both classes, then a test condition is created to partition the records further. In this case, t is an internal node whose outgoing edges correspond to the possible outcomes of this test condition.

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2) If  $D_t$  contains records from both classes, then a test condition is created to partition the records further. In this case, t is an internal node whose outgoing edges correspond to the possible outcomes of this test condition.

These outgoing edges terminate in **child nodes**. A record d in  $D_t$  is assigned to one of these child nodes based on the outcome of the test condition applied to d.

Consider a binary classification problem with classes  $Y_1$ ,  $Y_2$ . Given a set of records  $D_t$  at node t, Hunt's algorithm proceeds as follows:

3) These steps are then recursively applied to each child node.

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### NOTE

Decision trees are easy to interpret, but the algorithms to create them are a bit complicated.

Q: How do we partition the training records?

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A: There are a few ways to do this.

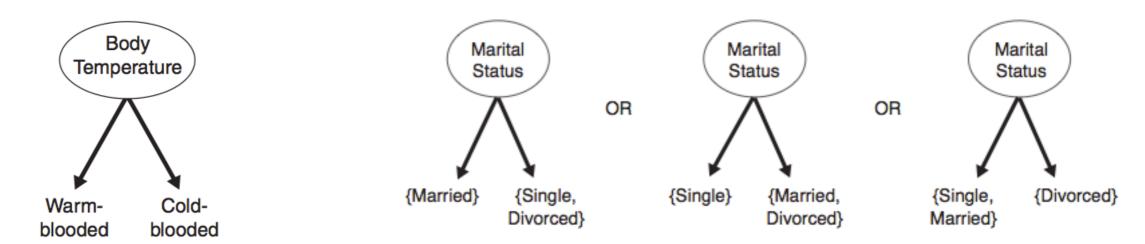
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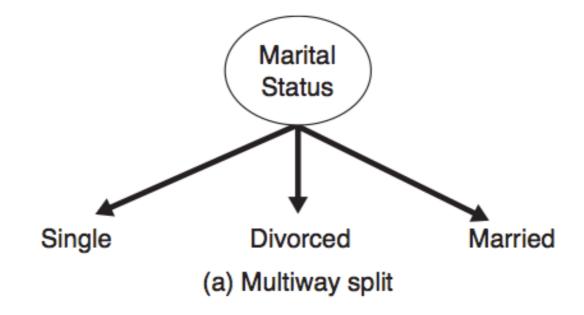
**Figure 4.8.** Test condition for binary attributes.

(b) Binary split {by grouping attribute values}

Q: How do we partition the training records?

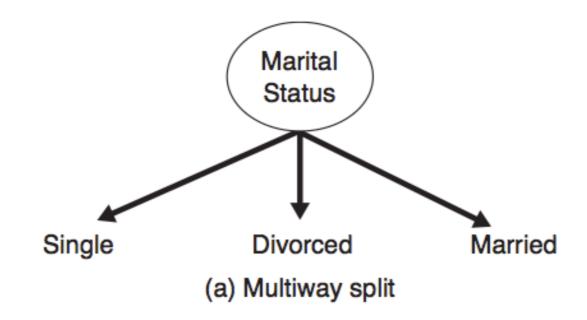
A: There are a few ways to do this.

Alternatively, we can create multiway splits:



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#### NOTE

Multiway splits can produce purer subsets, but may lead to overfitting!

- Q: How do we partition the training records?
- A: There are a few ways to do this.

For continuous features, we can use either method:

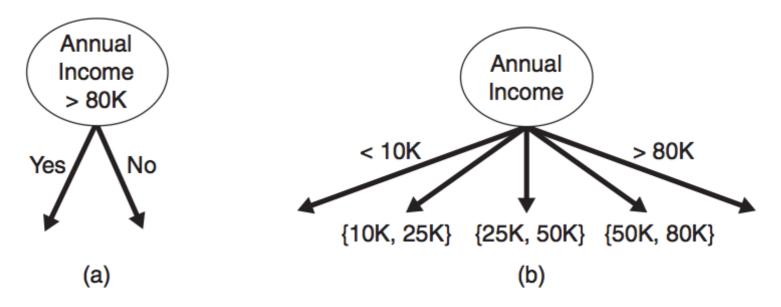


Figure 4.11. Test condition for continuous attributes.

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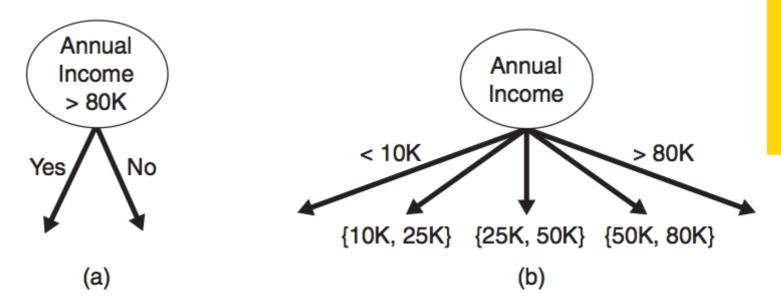


Figure 4.11. Test condition for continuous attributes.

#### NOTE

There are optimizations that can improve the naïve quadratic complexity of determining the optimum split point for continuous attributes.

Q: How do we determine the best split?

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Therefore we want each step to create the partition with the highest possible purity.

We need an objective function to optimize!

We want our objective function to measure the gain in purity from a particular split.

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Therefore we want it to depend on the class distribution over the nodes (before and after the split).

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For example, let  $p(i \mid t)$  be the probability of class i at node t (eg, the fraction of records labeled i at node t).

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Therefore we want it to depend on the class distribution over the nodes (before and after the split).

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#### NOTE

We are using the frequentist definition of probability here!

Then for a binary (0/1) classification problem,

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The minimum purity partition is given by the distribution:

$$p(0|t) = p(1|t) = 0.5$$

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The maximum purity partition is given (eg) by the distribution:

$$p(0|t) = 1 - p(1|t) = 1$$

# Some measures of impurity include:

Entropy(r) = 
$$-\sum_{c \in C} p(c \mid r) \log(c \mid r)$$

$$Gini(\mathbf{r}) = \sum_{c \in C} p(c \mid r) (1 - p(c \mid r))$$

ClassificationError(r) = 
$$1 - \max_{c} [p(c \mid r)]$$

Note that each measure achieves its max at 0.5, min at 0 & 1.

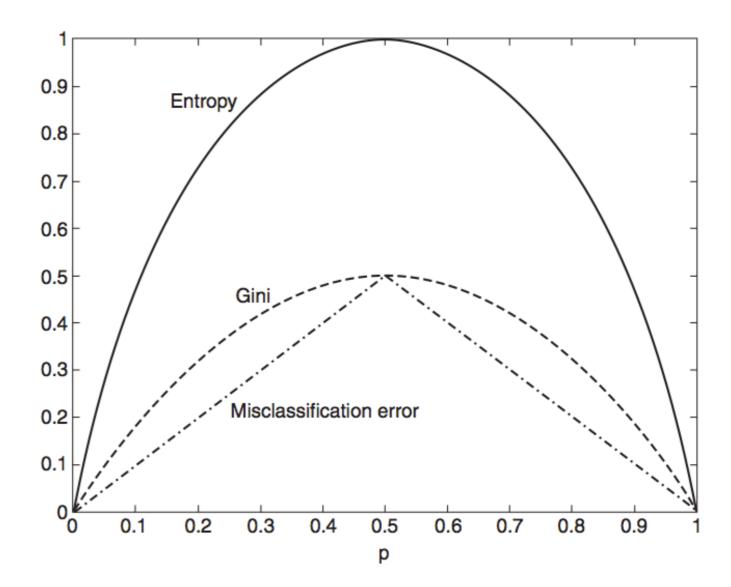


Figure 4.13. Comparison among the impurity measures for binary classification problems.

Note that each measure achieves its max at 0.5, min at 0 & 1.

#### NOTE

Despite consistency, different measures may create different splits.

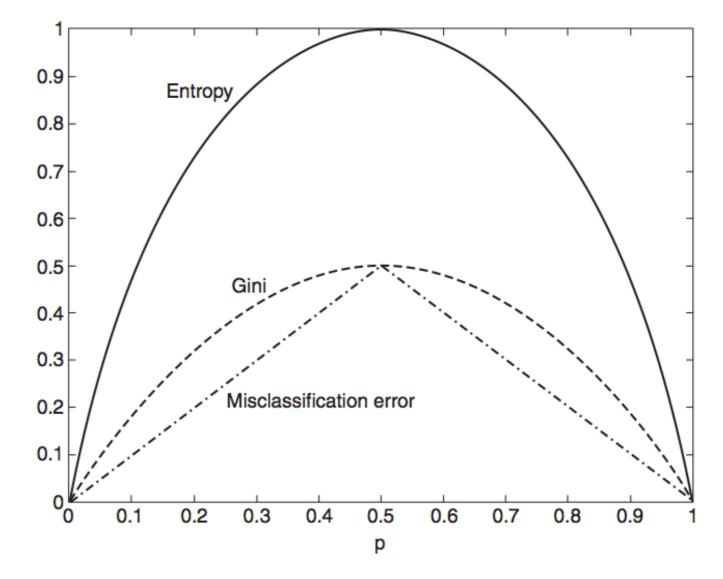


Figure 4.13. Comparison among the impurity measures for binary classification problems.

Impurity measures put us on the right track, but on their own they are not enough to tell us how our split will do.

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Q: Why is this true?

Impurity measures put us on the right track, but on their own they are not enough to tell us how our split will do.

Q: Why is this true?

A: We still need to look at impurity before & after the split.

### We can make this comparison using the gain:

$$\Delta = I(\text{parent}) - \sum_{\text{children } j} \frac{N_j}{N} I(\text{child } j)$$

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(Here I is the impurity measure,  $N_j$  denotes the number of records at child node j, and N denotes the number of records at the parent node.)

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$$\Delta = I(\text{parent}) - \sum_{\text{children } j} \frac{N_j}{N} I(\text{child } j)$$

(Here I is the impurity measure,  $N_j$  denotes the number of records at child node j, and N denotes the number of records at the parent node.)

When I is the entropy, this quantity is called the information gain.

Generally speaking, a test condition with a high number of outcomes can lead to overfitting (ex: a split with one outcome per record).

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One way of dealing with this is to restrict the algorithm to binary splits only (CART).

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One way of dealing with this is to restrict the algorithm to binary splits only (CART).

Another way is to use a splitting criterion which explicitly penalizes the number of outcomes (C4.5)

We can use a function of the information gain called the gain ratio to explicitly penalize high numbers of outcomes:

gain ratio = 
$$\frac{\Delta_{info}}{-\sum p(v_i)log_2p(v_i)}$$

(Where  $p(v_i)$  refers to the probability of label i at node v)

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gain ratio = 
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NOTE

This is a form of regularization!

(Where  $p(v_i)$  refers to the probability of label i at node v)

In addition to determining splits, we also need a stopping criterion to tell us when we're done.

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For example, we can stop when all records belong to the same class, or when all records have the same attributes.

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This is correct in principle, but would likely lead to overfitting.

One possibility is pre-pruning, which involves setting a minimum threshold on the gain, and stopping when no split achieves a gain above this threshold.

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This prevents overfitting, but is difficult to calibrate in practice (may preserve bias!)

Alternatively we could build the full tree, and then perform pruning as a post-processing step.

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To prune a tree, we examine the nodes from the bottom-up and simplify pieces of the tree (according to some criteria).

Complicated subtrees can be replaced either with a single node, or with a simpler (child) subtree.

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The first approach is called subtree replacement, and the second is subtree raising.

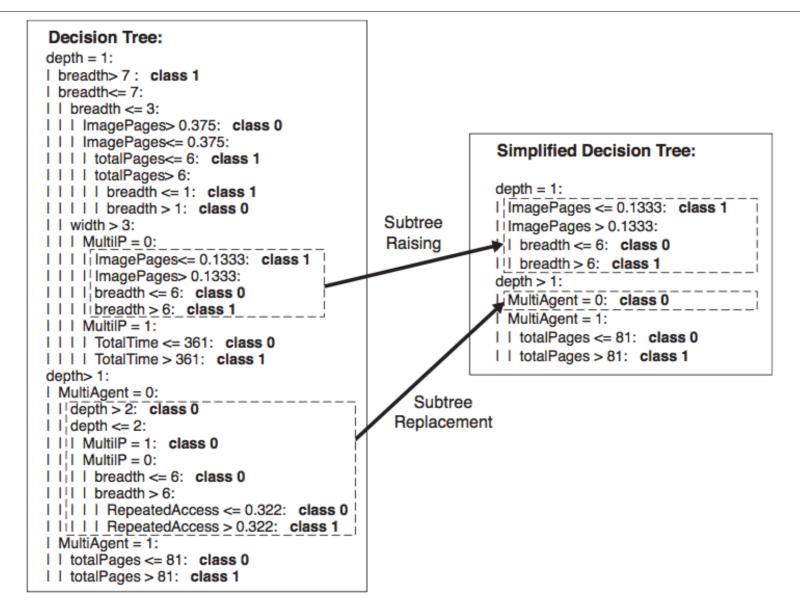


Figure 4.29. Post-pruning of the decision tree for Web robot detection.

# V.PROS CONS USES

#### PROS AND CONS OF DECISION TREES

#### Pros:

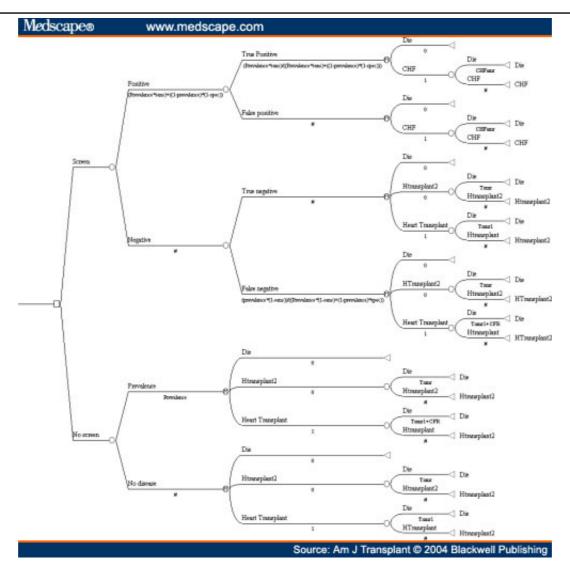
- Extremely intuitive and simple to use
- Very easy to explain and visualize
- Can use any categorical or continuous variable without preprocessing!
- Can handle both numerical and categorical data and multiple classes easily

#### Cons:

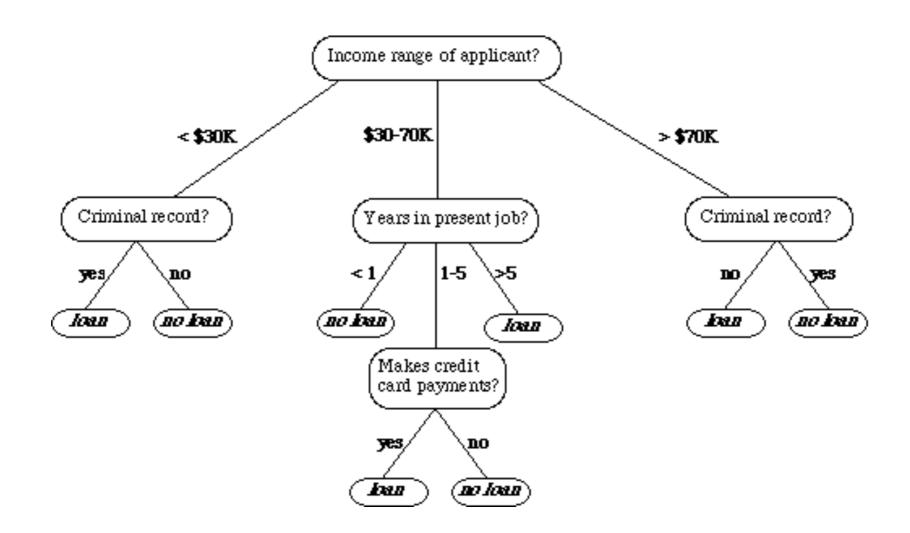
- Prone to overfitting
- Creation of trees are unstable
- Heuristics used to create trees i.e. suboptimal
- Decision trees can create biased trees if the data is unbalanced



Netflix challenge



Medical diagnostics



Financial applications (i.e. intuition and explainability)

### XGBoost eXtreme Gradient Boosting

Underlying mechanism for EXTREME models

## VI.DECISION TREE LAB

# VII.RANDOM FORESTS

A random forest is an **ensemble** of decision trees where each base classifier is grown using a random effect.

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For a small number of features, we can also create linear combinations of features and select splits from the enhanced feature set (Forest-RC)

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One way to do this is to choose the top feature amongst k randomly chosen features.

For a small number of features, we can also create linear combinations of features and select splits from the enhanced feature set (Forest-RC) Or we can select splitting features completely at random (Forest-RI)

#### THAT'S IT!

- Exit Tickets: DAT1 Lesson 12 Trees
- Pretty good video series https://www.youtube.com/watch?v=p17C9q2M00Q
- Milestone 3 is due Feb 17 https://github.com/brianchandbound/ga-ds/blob/master/ extra/project.md
- Peer Reviews
- Next week, we build upon trees into Ensemble methods