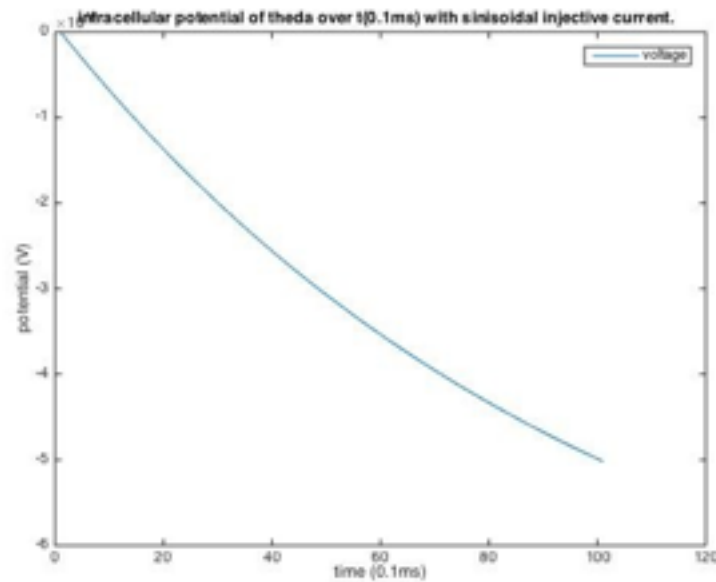


Neural Dynamics

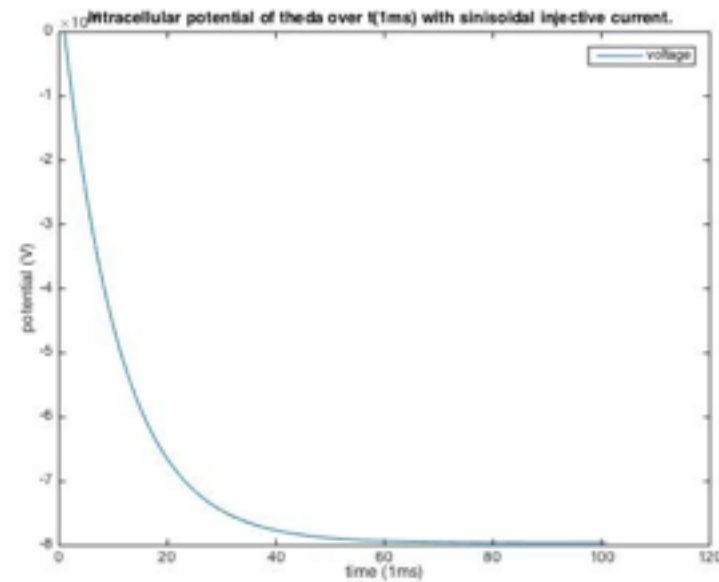
Exercise II

Question 3
Po-Hsuan Huang

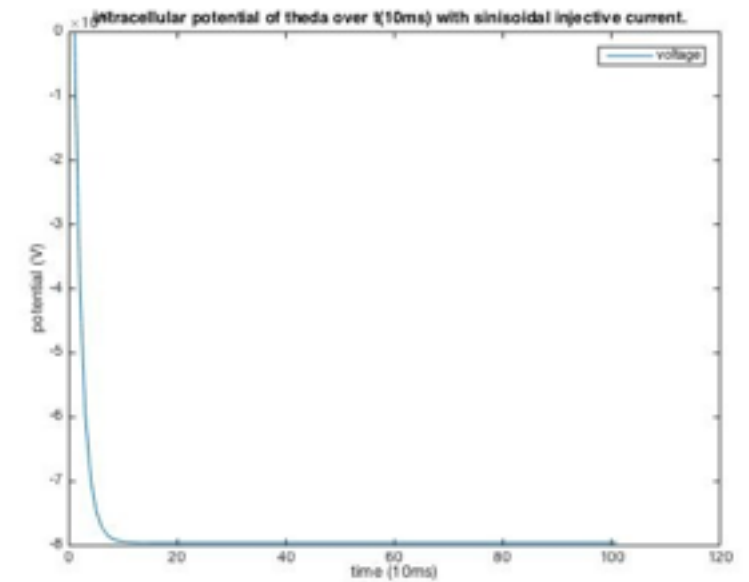
Q3.2 Set Δt to the values 1ms, 10ms. What changes in the simulation?



100x0.1ms/step



100x1ms/step



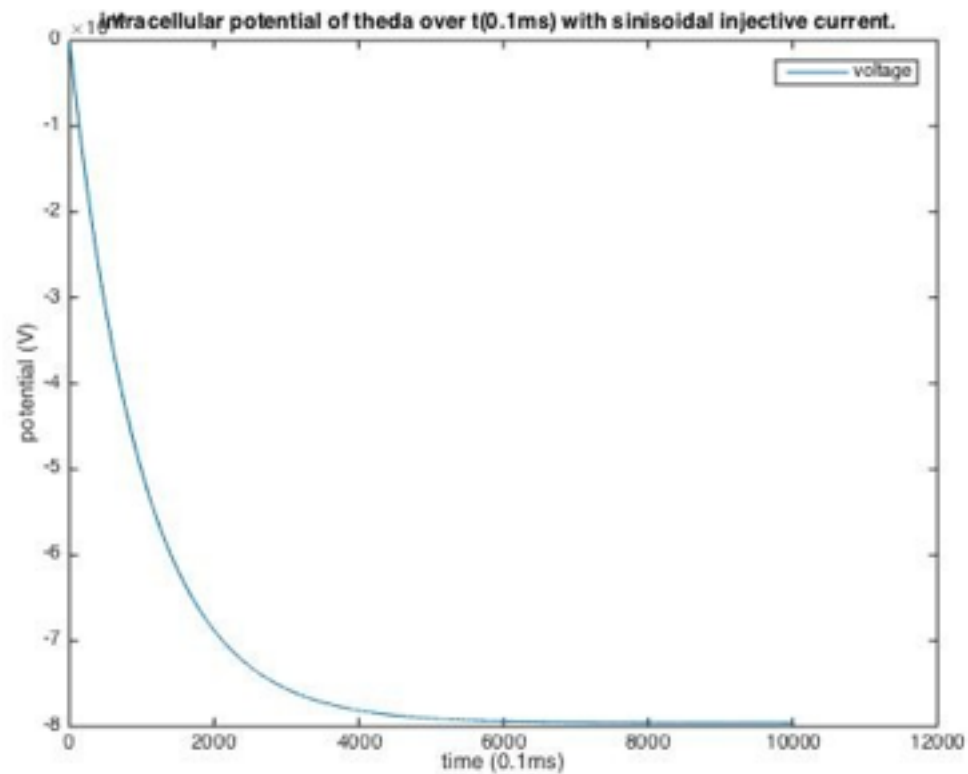
100x10ms/step

Because the step is amplified by 10 times, the error of the simulation is enlarged by 10 times, which can be deduced from the analytical solution.

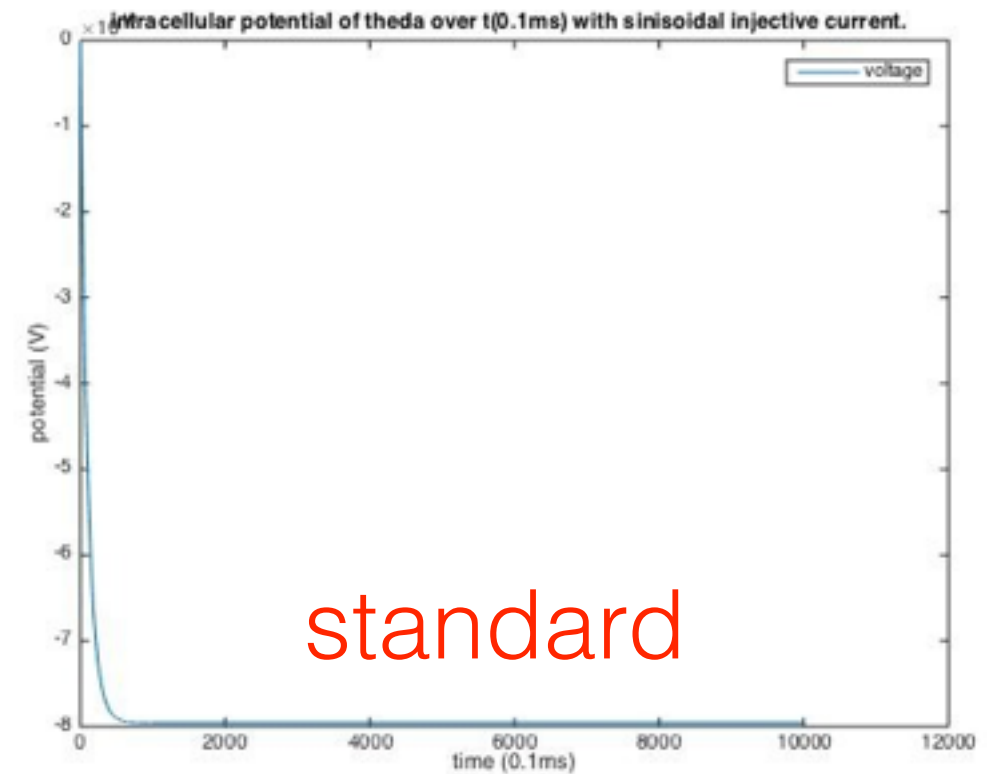
Also, the scale is enlarged the same amount of steps.

Q3.3

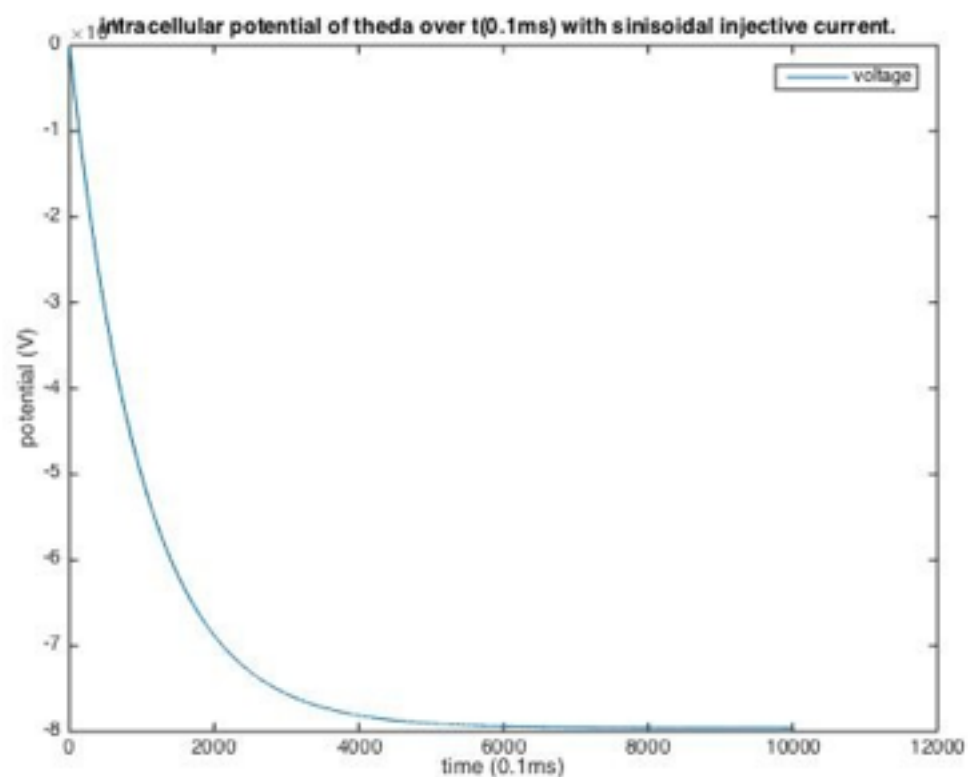
$$\tilde{R}_m = 1 \Omega m^2 \quad \tilde{c}_m = 10^{-1} F m^{-2}$$



$$\tilde{R}_m = 1 \Omega m^2 \quad \tilde{c}_m = 10^{-2} F m^{-2}$$



$$\tilde{R}_m = 10 \Omega m^2 \quad \tilde{c}_m = 10^{-2} F m^{-2}$$



characteristic time constant = $R_m C_m$

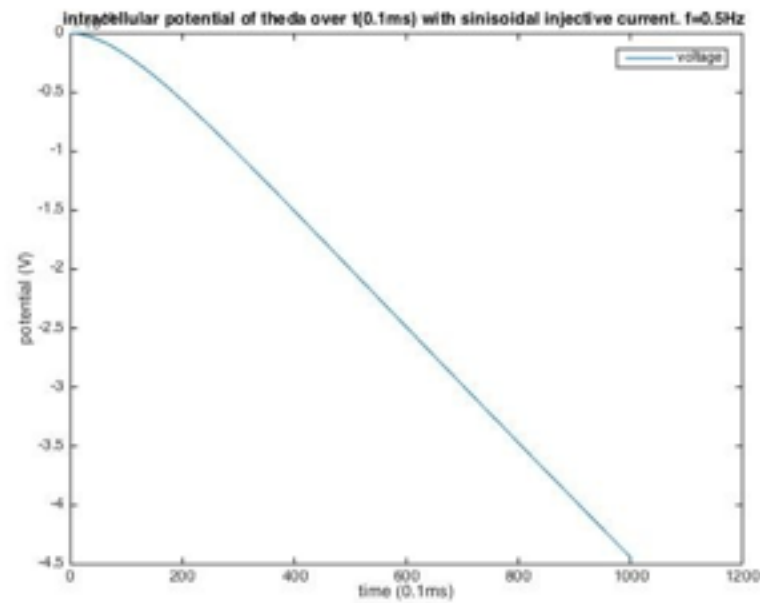
Characteristic time constant describes how fast the function decayed to $1/e$ times of its initial value. Analytically, both case should decay 10 times slower, but due to the simulation error, they look different.

Q3.4

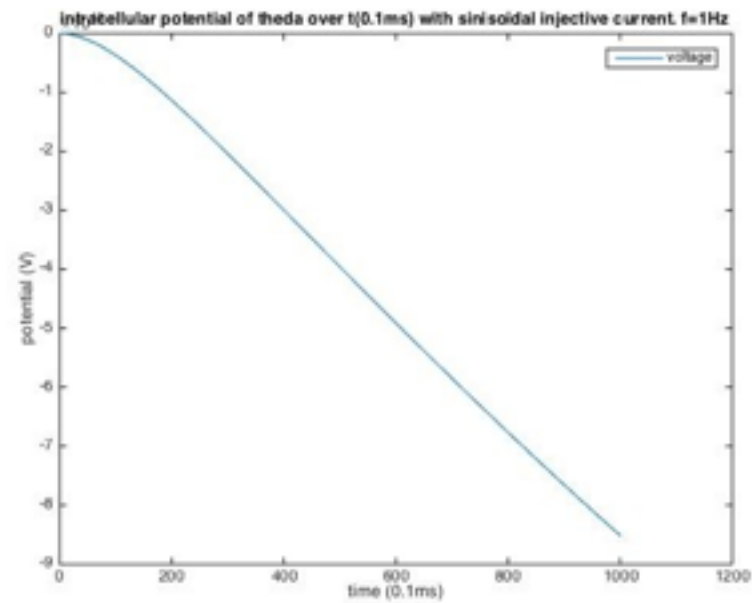
$$I_e(t) = 100\text{pA} \sin(2\pi f t)$$

time step = 0.1 ms 1000 steps

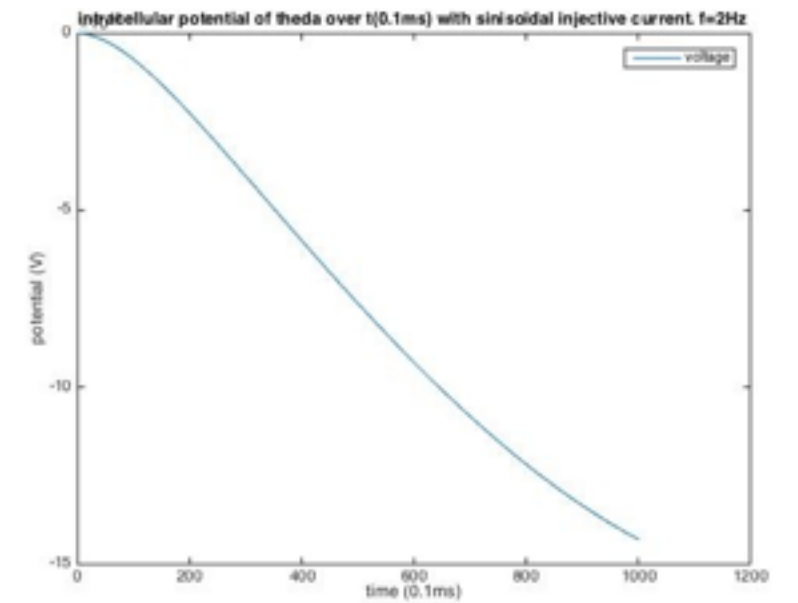
$f_1 = 0.5\text{Hz}$



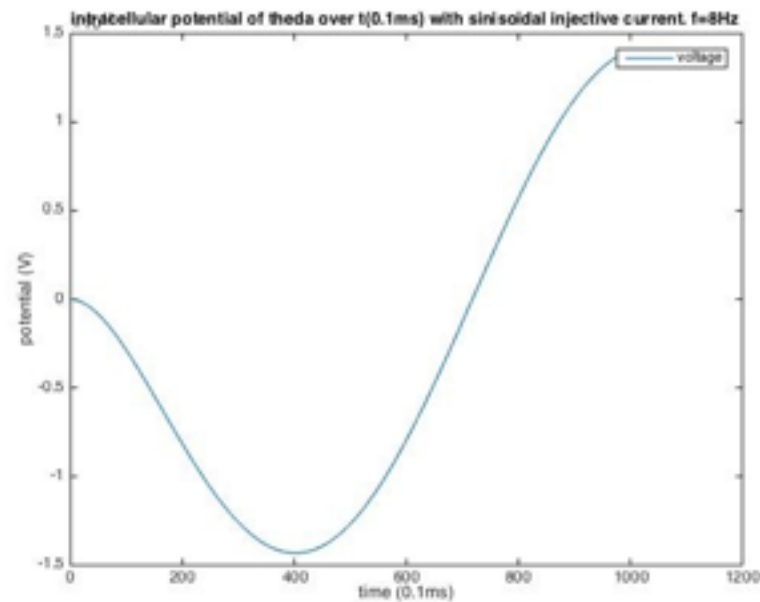
$f_2 = 1\text{Hz}$



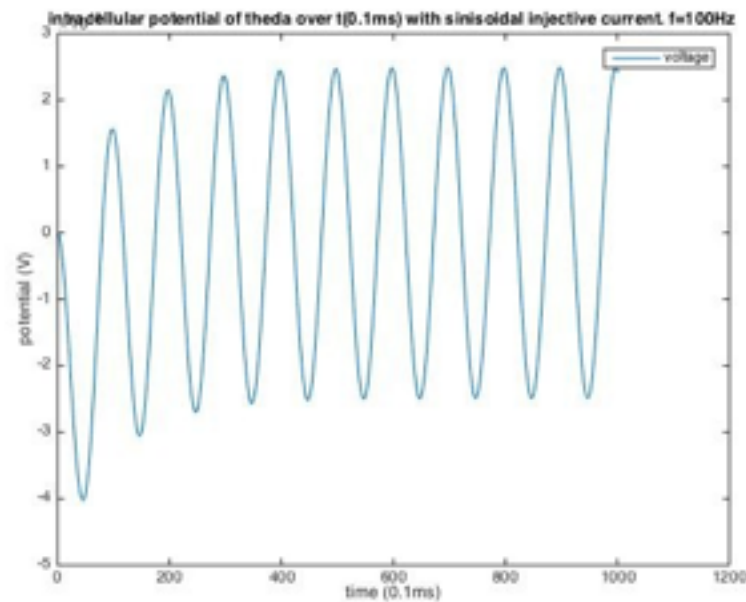
$f_3 = 2\text{Hz}$



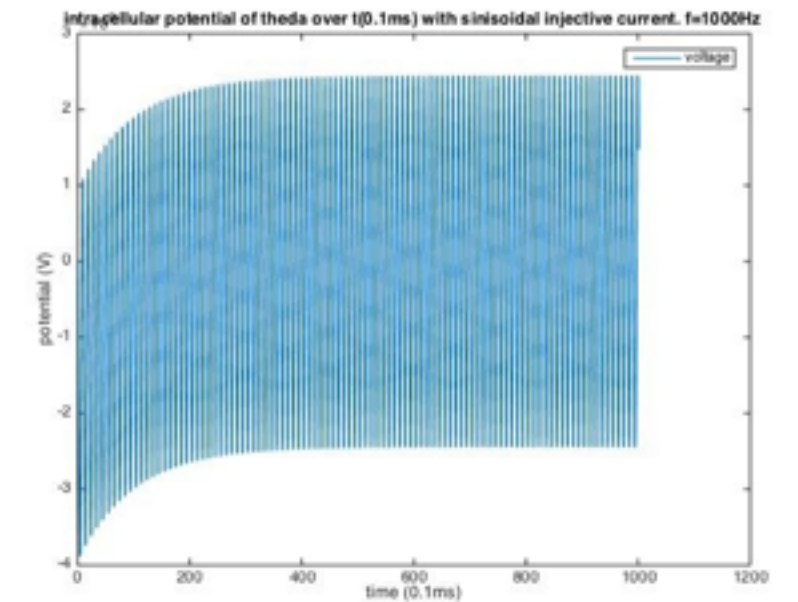
$f_4 = 8\text{Hz}$



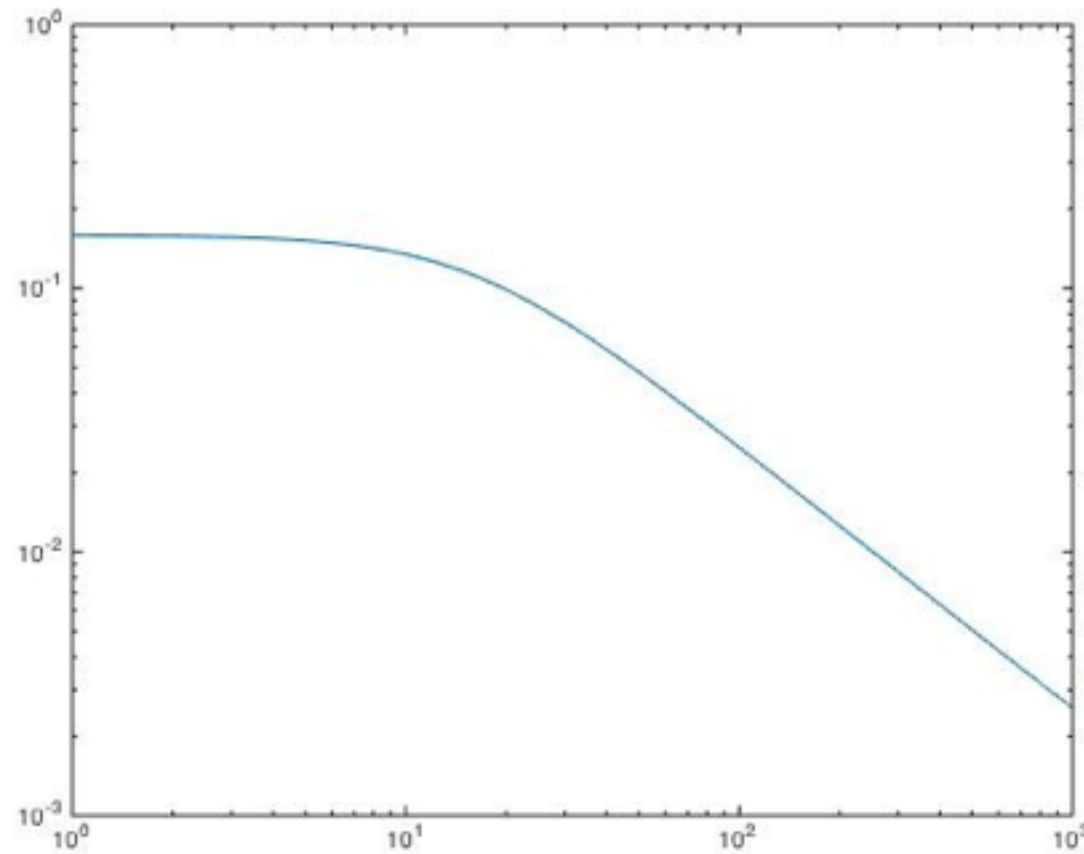
$f_5 = 100\text{Hz}$



$f_6 = 1000\text{Hz}$



Q3.4 For the converged state, plot the log of the amplitude of the voltage $V(t)$ against the log of the frequency (Bode diagram). Explain the result.



Take logarithm to analytical solution of $V(t)$, and let $t = N \cdot \text{period}$, where N is a positive integer. We can show function $\log V(\log \omega)$ is a straight line with slope $= -1$ when angular frequency $\gg (1/C_m R_m)$. Detailed derivation please check the paper version.