

The Relational Model

EECS3421 - Introduction to Database Management Systems

Data Models

→ notion for describing data

- Data model: a notation for describing data, including

- the **structure** of the data
- **constraints** on the content of the data
- **operations** on the data

} Features of data model

- Many possible data models:

- **network** data model
- **hierarchical** data model
- **relational** data model -- the most widely used
- **semi-structured** model (later in the term)

} Types of data model

Types of data model

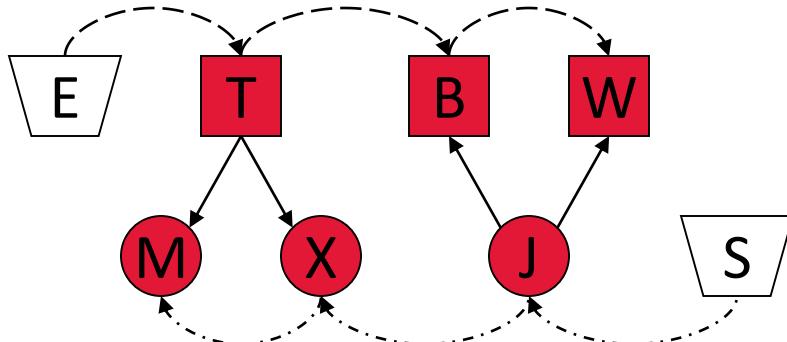
Comparing data models

Student job example

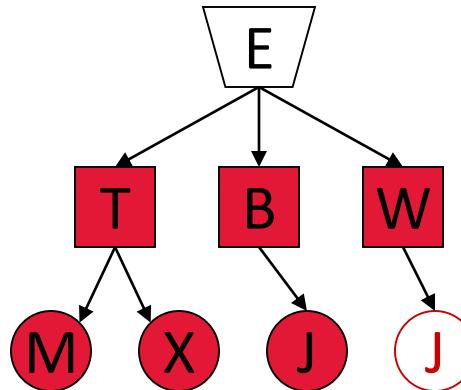
Mary (**M**) and Xiao (**X**) both work at Tim Hortons (**T**)

Jaspreet (**J**) works at both Bookstore (**B**) and Wind (**W**)

③ Network (graph)



① Hierarchical (tree)



② Relational (table)

E	S	R
B T W	J M X	M T X J B J W
...
...
...

(!) Network and hierarchical: no separation from underlying implementation

Why the relational model?

- Matches how we think about data
- Real reason: *data independence!* → separation of ① data
② programs
- Earlier models tied to physical data layout
 - Procedural access to data (low-level, explicit access)
 - Relationships stored in data (linked lists, trees, etc.)
 - Change in data layout => application rewrite
- Relational model
 - Declarative access to data (system optimizes for you)
 - Relationships specified by queries (schemas help, too)
 - Develop, maintain apps and data layout separately

Similar battle today with languages

What is the relational model?

- ① • Logical representation of data
 - Two-dimensional tables (relations)
- ② • Formal system for manipulating relations
 - Relational algebra (coming next)
- ③ • Result
 - High-level (logical, declarative) description of data
 - Mechanical rules for rewriting/optimizing low-level access
 - Formal methods to reason about soundness

Relational algebra is the key

The Relational Model

- Proposed by Edgar F. Codd in 1970 (**Turing Award**, 1981) as **a data model that strongly supports data independence**
 - Made available in commercial DBMSs in 1981 -- it is not easy to implement data independence efficiently and reliably!
 - It is based on (a variant of) the mathematical notion of **relation**
 - Relations are represented as tables
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Mathematical Relations

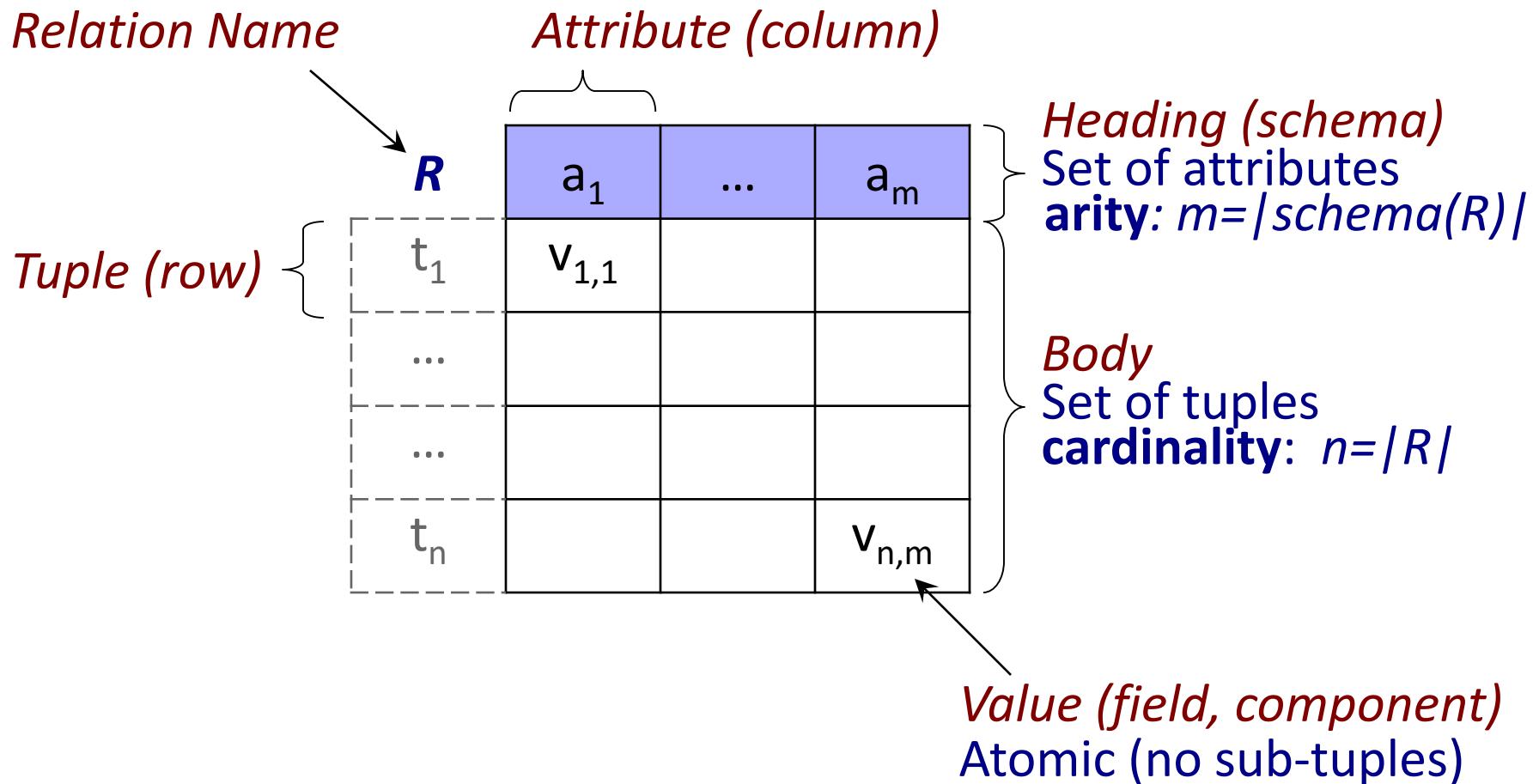
→ cartesian Products
→ Mathematical relation
→ Cardinality.

sets

- Given sets D_1, D_2, \dots, D_n , not necessarily distinct, the *Cartesian product* $D_1 \times D_2 \times \dots \times D_n$ is the set of all (ordered) n-tuples $\langle d_1, d_2, \dots, d_n \rangle$ such that $d_1 \in D_1, d_2 \in D_2, \dots, d_n \in D_n$
- A *mathematical relation* on D_1, D_2, \dots, D_n is a subset of the Cartesian product $D_1 \times D_2 \times \dots \times D_n$
- D_1, D_2, \dots, D_n are *domains* of the relation, while *n* is the *degree* of the relation
- The number of *n-tuples* in a given relation is the *cardinality* of that relation

~~DATA~~
Schema \rightarrow Skeleton structure that represents logical view of entire database.

Relations (tables) and tuples (rows)



Set-based: arbitrary row/col ordering

*Logical: physical layout might be *very* different!*

An Example

- $\text{Games} \subseteq \text{String} \times \text{String} \times \text{Integer} \times \text{Integer}$

Juve	Lazio	3	1
Lazio	Milan	2	0
Juve	Roma	1	2
Roma	Milan	0	1

- Note that **String** and **Integer** each play two roles, distinguished by means of position
- The structure of a mathematical relation is positional

Attributes → unique name

- We can make the structure of a relation **non-positional** by associating a unique name (**attribute**) with each domain that describes its role in the relation
- In the tabular representation, attributes are used as column headings

Attributes

HomeTeam	VisitingTeam	HomeGoals	VisitorGoals
Juve	Lazio	3	1
Lazio	Milan	2	0
Juve	Roma	1	2
Roma	Milan	0	1

Notation

*tuple
Attributes*

- $t[A]$ (or $t.A$) denotes the value on attribute A for a tuple t
- In our example, if t is the first tuple in the table

$t[VisitingTeam] = Lazio$

- The same notation is extended to sets of attributes, thus denoting tuples:

$t[VisitingTeam, VisitorGoals]$ is a tuple on two attributes,
 $\langle Lazio, 1 \rangle$

- More generally, if X is a sequence of attributes A_1, \dots, A_n ,
 $t[X]$ is $\langle t[A_1], t[A_2], \dots, t[A_n] \rangle$

Value-based References

unique num

↑

Students	RegNum	Surname	FirstName	BirthDate
	6554	Rossi	Mario	5/12/1978
	8765	Neri	Paolo	3/11/1976
	9283	Verdi	Luisa	12/11/1979
	3456	Rossi	Maria	1/2/1978

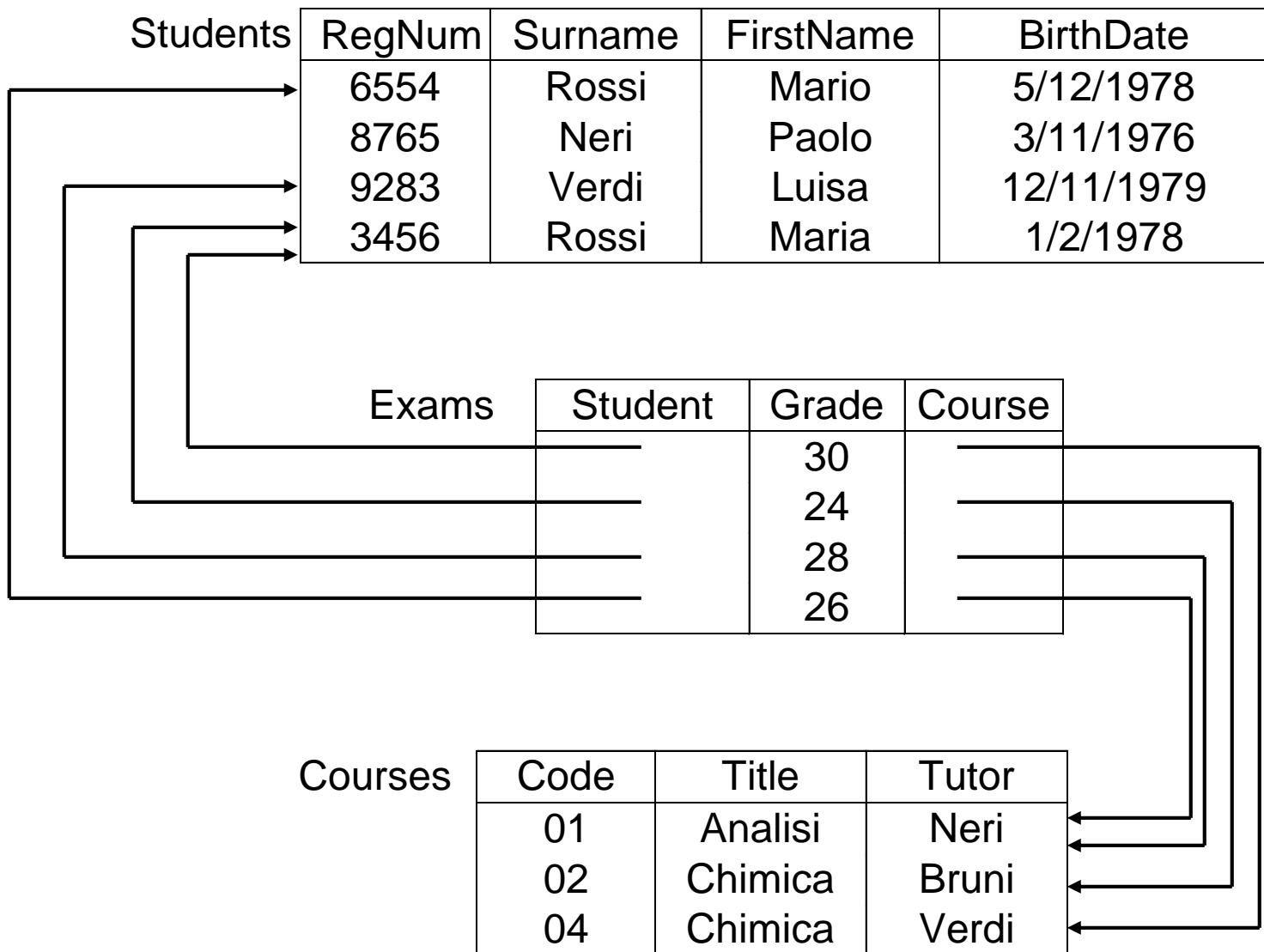
Exams

	Student	Grade	Course
	3456	30	04
	3456	24	02
	9283	28	01
	6554	26	01

Courses

	Code	Title	Tutor
	01	Analisi	Neri
	02	Chimica	Bruni
	04	Chimica	Verdi

Value-based References (cont.)



Advantages of Value-based References

- Value-based references lead to independence from physical data structures, such as pointers
 - Pointers are implemented differently on different hardware, inhibit portability of a database

Definitions

⊗⊗

- **Relation schema:** Relation name R with a set of attributes A_1, \dots, A_n :
 $\underline{R(A_1, \dots, A_n)}$ *set of attributes*
- **Database schema:** A set of relation schemata with different names
 $D = \underline{\{R_1(X_1), \dots, R_n(X_n)\}}$ *set of relation schemata*
- **Relation** (instance) on a relation schema
 $R(X)$: Set r of tuples on X
- **Database** (instance) on a schema
 $D = \{R_1(X_1), \dots, R_n(X_n)\}$: Set of relations $r = \{r_1, \dots, r_n\}$
(where r_i is a relation on R_i)

Example Data

Da Mario		
Receipt No: 1357		
Date: 5/5/92		
3	covers	3.00
2	hors d'oeuvre	5.00
3	first course	9.00
2	steak	12.00
Total:		29.00

Da Mario		
Receipt No: 2334		
Date: 4/7/92		
2	covers	2.00
2	hors d'oeuvre	2.50
2	first course	6.00
2	bream	15.00
2	coffee	2.00
Total:		27.50

Da Mario		
Receipt No: 3007		
Date: 4/8/92		
2	covers	3.00
2	hors d'oeuvre	6.00
3	first course	8.00
1	bream	7.50
1	salad	3.00
2	coffee	2.00
Total:		29.50

Data Representation

Details

Receipts

Number	Date	Total
1357	5/5/92	29.00
2334	4/7/92	27.50
3007	4/8/92	29.50

Number	Quantity	Description	Cost
1357	3	Covers	3.00
1357	2	Hors d'oeuvre	5.00
1357	3	First course	9.00
1357	2	Steak	12.00
2334	2	Covers	2.00
2334	2	Hors d'oeuvre	2.50
2334	2	First course	6.00
2334	2	Bream	15.00
2334	2	Coffee	2.00
3007	2	Covers	3.00
3007	2	Hors d'oeuvre	6.00
3007	3	First course	8.00
3007	1	Bream	7.50
3007	1	Salad	3.00
3007	2	Coffee	2.00

Questions

- Have we represented all details of receipts?
- Well, it depends on what we are interested in:
 - does the order of lines matter?
 - could we have duplicate lines in a receipt?
 - If so, there is a problem ... Why?
- If needed, an alternative representation is possible ...

More Detailed Representation

Receipts

Details

Number	Date	Total
1357	5/5/92	29.00
2334	4/7/92	27.50
3007	4/8/92	29.50

Number	Line	Quantity	Description	Cost
1357	1	3	Covers	3.00
1357	2	2	Hors d'oeuvre	5.00
1357	3	3	First course	9.00
1357	4	2	Steak	12.00
2334	1	2	Covers	2.00
2334	2	2	Hors d'oeuvre	2.50
2334	3	2	First course	6.00
2334	4	2	Bream	15.00
2334	5	2	Coffee	2.00
3007	1	2	Covers	3.00
3007	2	2	Hors d'oeuvre	6.00
3007	3	3	First course	8.00
3007	4	1	Bream	7.50
3007	5	1	Salad	3.00
3007	6	2	Coffee	2.00

Incomplete Information: Motivation

(County towns have government offices, other towns do not.)

- Florence is a county town; so it has a government office, but we do not know its address
- Tivoli is not a county town; so it has no government office
- Prato has recently become a county town; has the government office been established? We don't know!

City	GovtAddress
Roma	Via IV novembre
Florence	?
Tivoli	??
Prato	???

Null Value

denotes absence of a value
null in java

- A **null value** is a special value (not a value of any domain) which denotes the absence of a value
- Types of Null Values:
 - ① – **unknown value**: there is a domain value, but it is not known (Florence)
 - ② – **non-existent value**: the attribute is not applicable for the tuple (Tivoli)
 - ③ – **no-information value**: we don't know if a value exists or not (Prato). (This is the disjunction - logical or - of the other two)
- DBMSs do not distinguish between these types: they implicitly adopt the no-information value

A Meaningless Database ...

Exams	RegNum	Name	Course	Grade	Honours
	6554	Rossi	B01	K	
	8765	Neri	B03	C	
	3456	Bruni	B04	B	honours
	3456	Verdi	B03	A	honours

Courses	Code	Title
	B01	Physics
	B02	Calculus
	B03	Chemistry

Honours are awarded only if grade is A. Can you spot some others?



Integrity Constraints

↳ Set of rules used to maintain quality of information.

- An **integrity constraint** is a property that must be satisfied by all meaningful database instances
- A database is legal if it satisfies all integrity constraints
- Types of constraints:

① Intra-relational constraints

- domain constraints
- tuple constraints
- keys

② Inter-relational constraints

- foreign keys

■ Integrity constraints: Provide a way of ensuring that changes made to the database by authorized users don't result in a loss of data consistency.

Stop here

Rationale for Integrity Constraints

- Describe the application in greater detail
- Contribute to **data quality**
- An important part of the database design process (we will discuss later **normal forms**)
- Used by the system in choosing a strategy for query processing

Tuple and Domain Constraints

- A *tuple constraint* expresses conditions on the values of each tuple, independently of other tuples
 - NOT((Honours = 'honours') OR (Grade = 'A'))
 - Net = Gross - Deductions
- A *domain constraint* is a tuple constraint that involves a single attribute
 - (Grade ≤ 'A') AND (Grade ≥ 'F')

Unique Identification for Tuples

RegNum	Surname	FirstName	BirthDate	DegreeProg
284328	Smith	Luigi	29/04/59	Computing
296328	Smith	John	29/04/59	Computing
587614	Smith	Lucy	01/05/61	Engineering
934856	Black	Lucy	01/05/61	Fine Art
965536	Black	Lucy	05/03/58	Fine Art

- Registration number identifies students
 - no pair of tuples with the same value for **RegNum**
- Personal data could identify students as well
 - E.g. no pair of tuples with the same values for all of **Surname**, **FirstName**, **BirthDate**

Keys

- ① set of attributes
- ② Uniquely identifies tuples in a relation.

- A **key** is a set of attributes that uniquely identifies tuples in a relation
- More formally:
 - A set of attributes K is a superkey for a relation r if r cannot contain two distinct tuples t_1 and t_2 such that $t_1[K] = t_2[K]$;
 - K is a **key** for r if K is a minimal superkey; that is, there exists no other superkey K' such that $K' \subset K$

An Example

RegNum	Surname	FirstName	BirthDate	DegreeProg
284328	Smith	Luigi	29/04/59	Computing
296328	Smith	John	29/04/59	Computing
587614	Smith	Lucy	01/05/61	Engineering
934856	Black	Lucy	01/05/61	Fine Art
965536	Black	Lucy	05/03/58	Fine Art

- **RegNum** is a key
 - **RegNum** is a superkey and it contains a sole attribute, so it is minimal
- **Surname, Firstname, BirthDate** is a key
 - the three attributes form a superkey and there is no proper subset that is also a superkey
- **Surname, Firstname, BirthDate, DegreeProg** is not a key
 - It is a superkey, but it is not minimal supekey

Beware!

RegNum	Surname	FirstName	BirthDate	DegreeProg
296328	Smith	John	29/04/59	Computing
587614	Smith	Lucy	01/05/61	Engineering
934856	Black	Lucy	01/05/61	Fine Art
965536	Black	Lucy	05/03/58	Engineering

- There is no pair of tuples with the same values on both **Surname** and **DegreeProg**; i.e., it assumes that in each programme students have different surnames
- Can we conclude that **Surname** and **DegreeProg** form a key for this relation?
 - It would be a bad choice! There **could be** students with the same surname in the same programme

Existence of Keys (Proof Sketch)

A.S.

- Relations are sets; therefore each relation is composed of distinct tuples
- It follows that the whole set of attributes for a relation defines a superkey
- Therefore each relation has a key, which is the set of all its attributes (or a subset thereof)
- The existence of keys guarantees that each piece of data in the database can be accessed

Keys are a major feature of the Relational Model and allow to say that it is “**value-based**”

Keys and Null Values

- If there are nulls, keys do not work well:
 - They do not guarantee unique identification
 - They do not help in establishing correspondences between data in different relations

RegNum	Surname	FirstName	BirthDate	DegreeProg
NULL	Smith	John	NULL	Computing
587614	Smith	Lucy	01/05/61	Engineering
934856	Black	Lucy	NULL	NULL
NULL	Black	Lucy	05/03/58	Engineering

How do we access the first tuple?
Are the third and fourth tuple the same?

Primary Keys

- The presence of nulls in keys has to be limited
- Each relation must have a **primary key** on which nulls are not allowed
- Notation: the attributes of the primary key are **underlined**
- References between relations are realized through primary keys

<u>RegNum</u>	Surname	FirstName	BirthDate	DegreeProg
643976	Smith	John	NULL	Computing
587614	Smith	Lucy	01/05/61	Engineering
934856	Black	Lucy	NULL	NULL
735591	Black	Lucy	05/03/58	Engineering

References Between Relations

Students

<u>RegNum</u>	<u>Surname</u>	<u>FirstName</u>	<u>BirthDate</u>
6554	Rossi	Mario	5/12/1978
8765	Neri	Paolo	3/11/1976
9283	Verdi	Luisa	12/11/1979
3456	Rossi	Maria	1/2/1978

Exams

<u>Student</u>	<u>Grade</u>	<u>Course</u>
3456	30	04
3456	24	02
9283	28	01
6554	26	01

Courses

<u>Code</u>	<u>Title</u>	<u>Tutor</u>
01	Analisi	Neri
02	Chimica	Bruni
04	Chimica	Verdi

Do we Always Have Primary Keys?

- In most cases YES
- In other cases NO
 - need to introduce new attributes by identifying codes
- Goal: Unambiguously identify things
 - social insurance number
 - student number
 - area code
 - ...

...Consider...

- Suppose we want a database that maintains information on course offerings at the York University and use the following relation schema

Course(name,title,dept,year,sem)

- What would it mean if we used each of the following attribute sets as a primary key:

name?

name,sem,dept?

sem,year?

name,dept?

dept,year?

~~A~~

Referential Constraints (Foreign Keys)

- Data in different relations are referenced through primary key values
- **Referential integrity constraints** are imposed in order to guarantee that the values refer to existing tuples in the referenced relation
- For example, if a student with id “3456” took an exam for course with id “04”, there better be a student with such an id and a course with such an id in the referenced relations
- Also called **inclusion dependencies**

Example of Referential Constraints

Offences	<u>Code</u>	Date	Officer	Dept	Registration
	143256	25/10/1992	567	75	5694 FR
	987554	26/10/1992	456	75	5694 FR
	987557	26/10/1992	456	75	6544 XY
	630876	15/10/1992	456	47	6544 XY
	539856	12/10/1992	567	47	6544 XY

Officers	<u>RegNum</u>	Surname	FirstName
	567	Brun	Jean
	456	Larue	Henri
	638	Larue	Jacques

Cars	<u>Registration</u>	<u>Dept</u>	Owner	...
	6544 XY	75	Cordon Edouard	...
	7122 HT	75	Cordon Edouard	...
	5694 FR	75	Latour Hortense	...
	6544 XY	47	Mimault Bernard	...

Referential Constraints

~~A A~~

- A **referential constraint** requires that the values on a set X of attributes of a relation R1 must appear as values for the primary key of another relation R2
- In such a situation, we say that X is a **foreign key** of relation R1
- In the previous example, we have referential constraints between the attribute **Officer** of the relation **Offences** and the relation **Officers**; also between the attributes **Registration** and **Department** of relations **Offences** and **Cars**.

Violation of Referential Constraints

Offences	<u>Code</u>	Date	Officer	Dept	Registration
	987554	26/10/1992	456	75	5694 FR
	630876	15/10/1992	456	47	6544 XY
Officers	<u>RegNum</u>	Surname	FirstName		
	567	Brun	Jean		
	638	Larue	Jacques		
Cars	<u>Registration</u>	<u>Dept</u>	Owner	...	
	7122 HT	75	Cordon Edouard	...	
	5694 FR	93	Latour Hortense	...	
	6544 XY	47	Mimault Bernard	...	

Referential Constraints: Comments

- Referential constraints play an important role in making the relational model value-based
- It is possible to have features that support the management of referential constraints (“actions” activated by violations)

Summary

- The relational model
 - Relations, tuples, attributes
 - Value-based References
 - Incomplete information: The NULL value
 - Integrity Constraints
 - domain constraint
 - tuple constraint
 - unique tuple identification constraint (primary key)
 - referential constraints (foreign Key)
- Next: Relational Algebra

