

# The Entity/Relationship (ER) Model & DB Design

EECS3421 - Introduction to Database Management Systems

# Overview

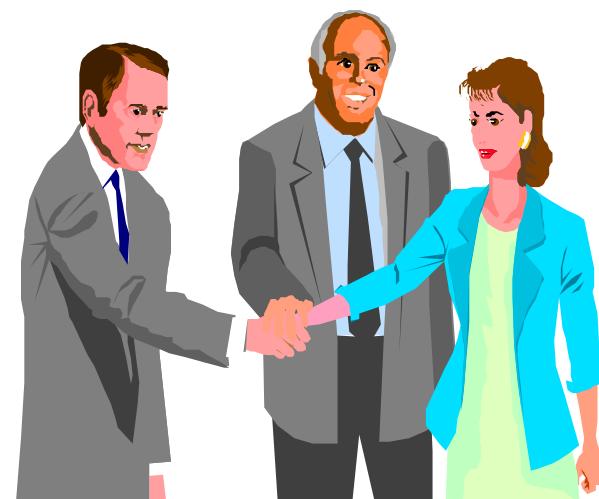
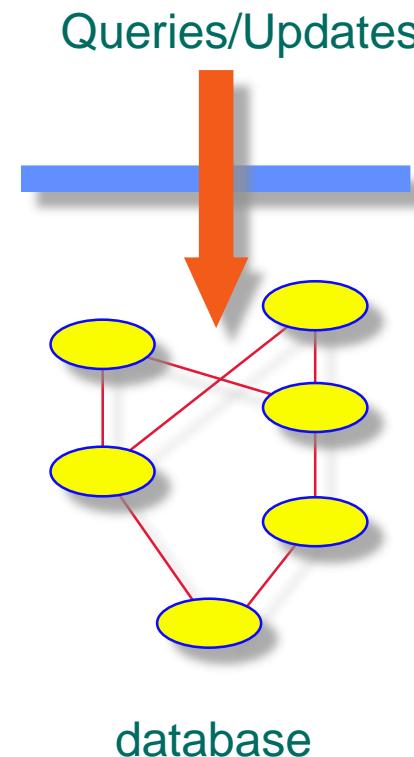
- The Entity/Relationship (ER) Model
- Designing a database schema
  - Restructuring of an E/R model
  - Translation of an E/R model into the logical model (DB Schema)

# THE ENTITY/RELATIONSHIP (ER) MODEL

Modeling → drafting / conceptualizing real world Scenario  
into database.

# Conceptualizing the real-world

**Modeling** is about **mapping** entities and relationships of the world into the concepts of a database

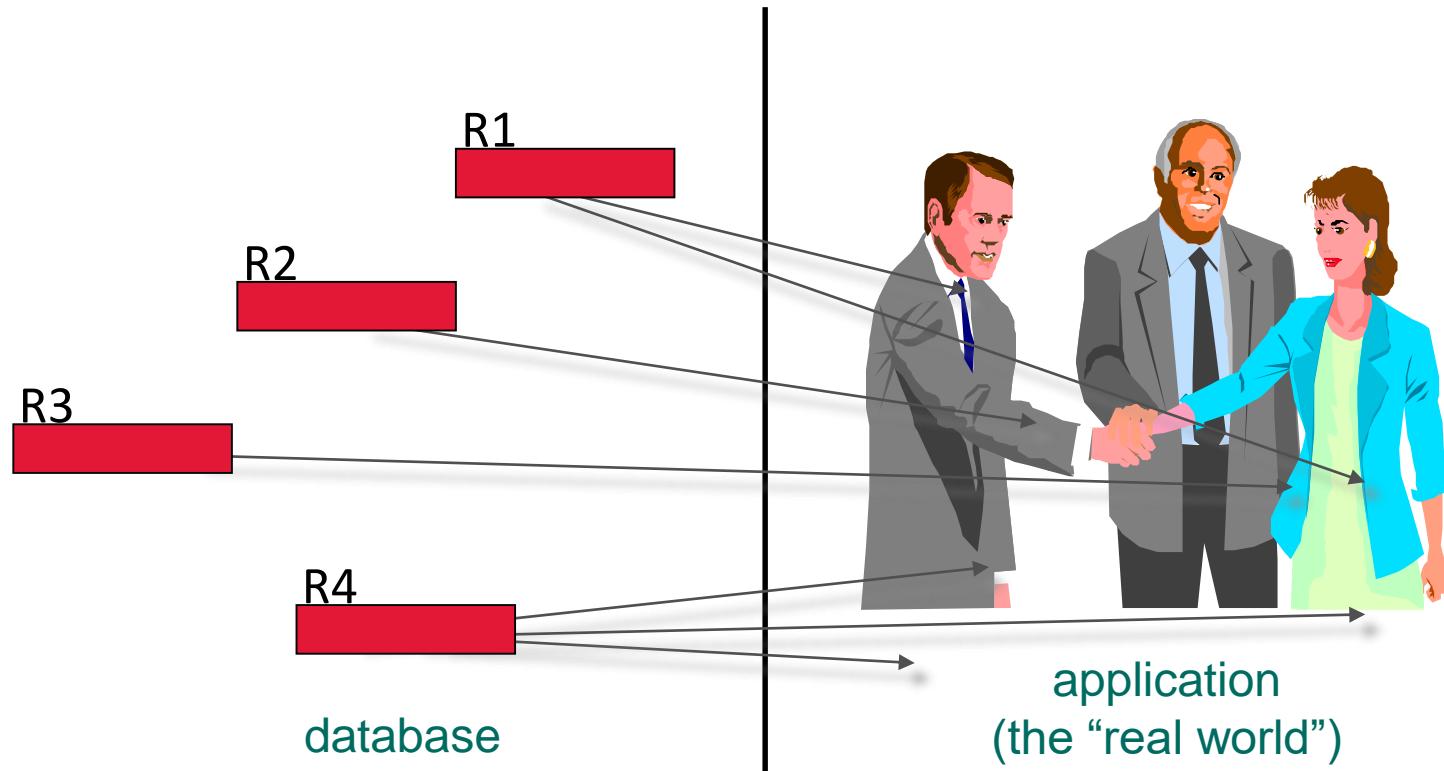


application  
(the “real world”)

→ not always clear or affirmative

# Mapping is Not Deterministic

The Relational Model uses relations to represent entities, relationships, or combinations thereof



The mapping process is not always clear

# Framework for E/R

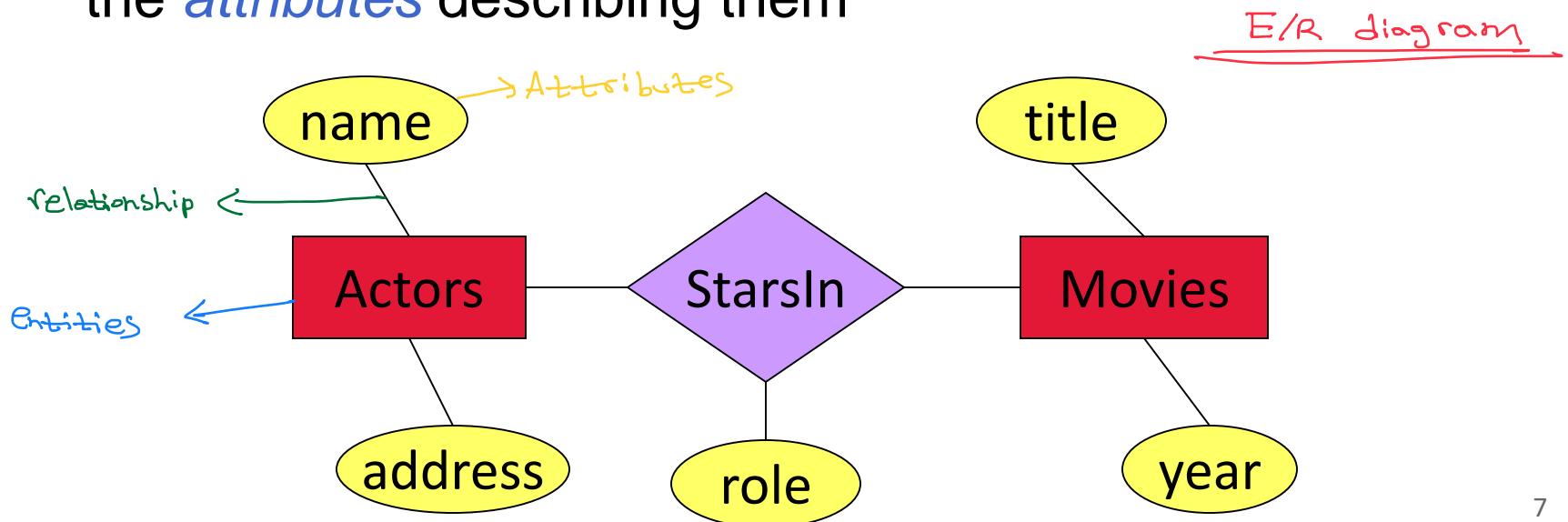
try understand what  
client wants.

- ① Design is serious business
  - The client wants a database
  - > but has no clue what to put in it
- ② Sketching the key components is an efficient way to develop a working database
  - Sketch out (and debug) schema designs
  - Express as many constraints as possible
  - Convert to relational DB once the client is happy

make a  
rough of  
the DB.  
before  
implementation

# Entity/Relationship Model

- Visual data model (diagram-based) → visual representation of the database model
  - Quickly “chart out” a database design
  - Easier to “see” big picture
  - Comparable to class diagrams in UML
- Basic concept: *entities* and their *relationships*, along with the *attributes* describing them



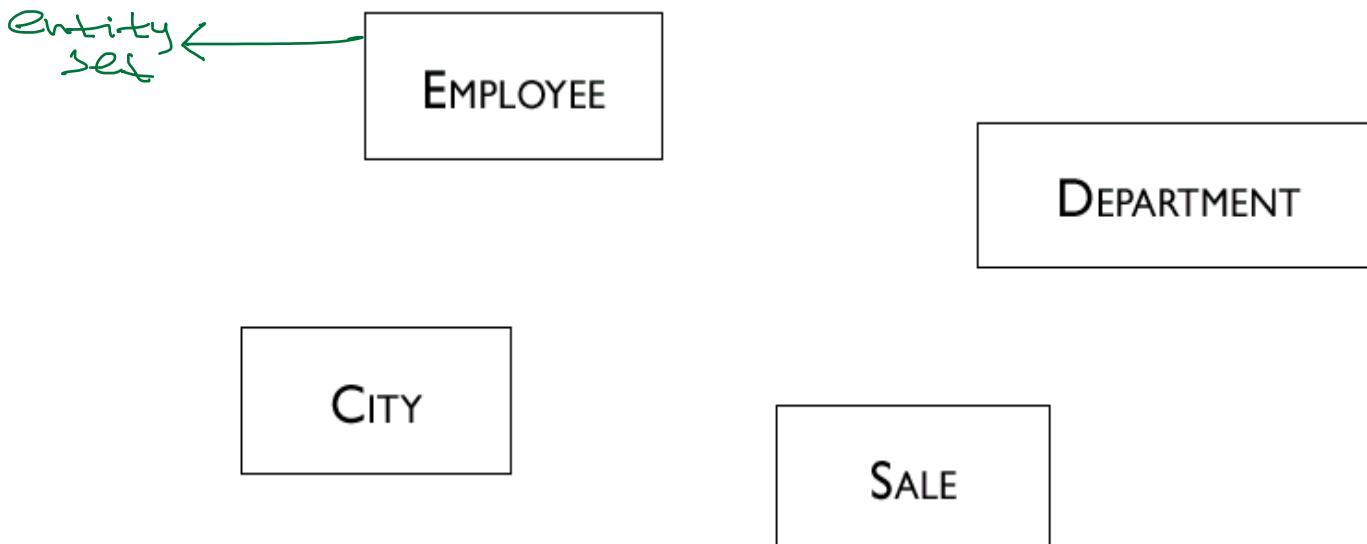
# Entity/Relationship vs other models

|   | E/R              | OO      | RA        |
|---|------------------|---------|-----------|
| <b>“thing” to be modeled</b>                      | Entity           | Object  | Tuple     |
| <b>set of similar “things”</b>                    | Entity set       | Class   | Relation  |
| <b>relationship</b>                               | Relationship     | Object? | Tuple?    |
| <b>set of similar relationships</b>               | Relationship Set | Class?  | Relation? |
| <b>property of a “thing” or of a relationship</b> | Attribute        | Field   | Attribute |

# Entity Sets

→ Represents the entity

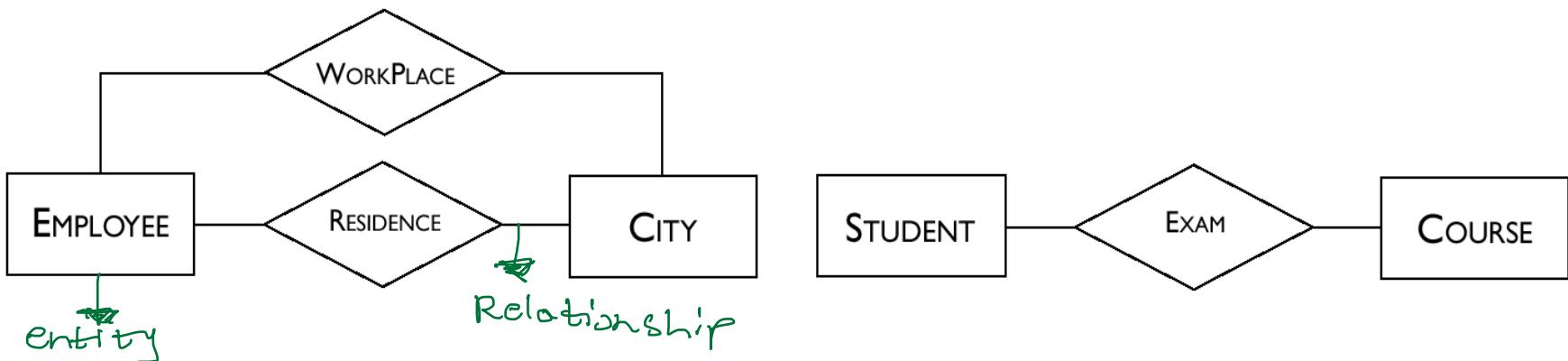
- An **entity set** represents a class of objects that have properties in common and an autonomous existence (e.g., City, Department, Employee, Sale)
- An **entity** is an instance of an entity set (e.g., Stockholm is a City; Peterson is an Employee)



# Relationship Sets

→ represents the relationship between the entity.

- A **relationship set** is an association between 2+ entity sets (e.g., Residence is a relationship set between entity sets City and Employee)
- A **relationship** is an instance of a n-ary relationship set (e.g., the pair <Johanssen, Stockholm> is a relationship instance of Residence)



Types of relationships

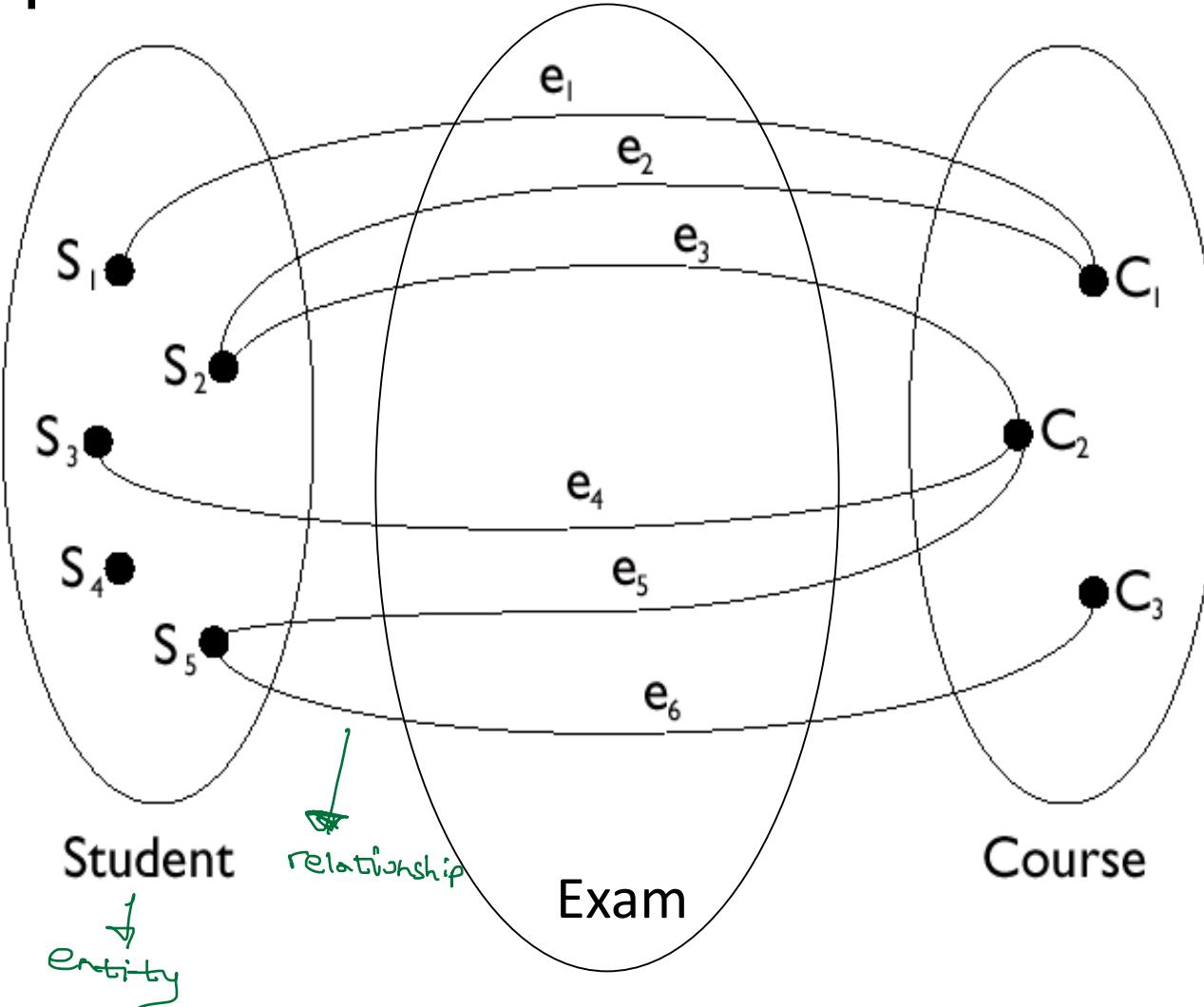
Unary

Binary

Ternary

N-ary

# Example of Instances for Exam

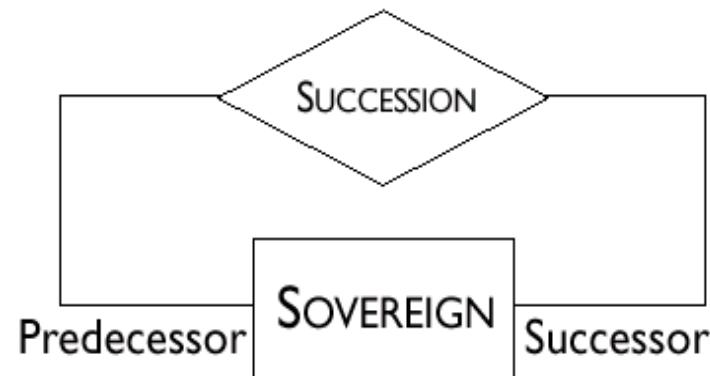
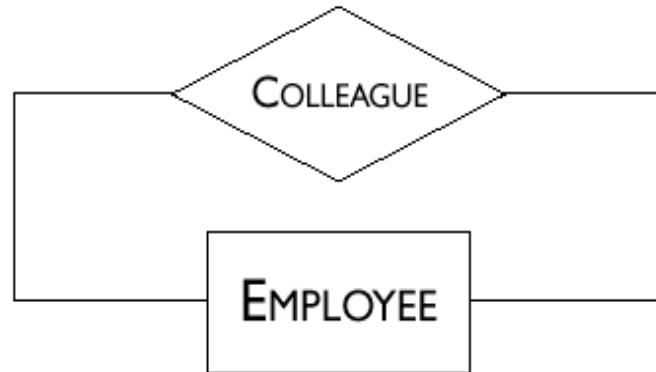


A student can't take more than one exam for a particular course

11

# Recursive Relationships

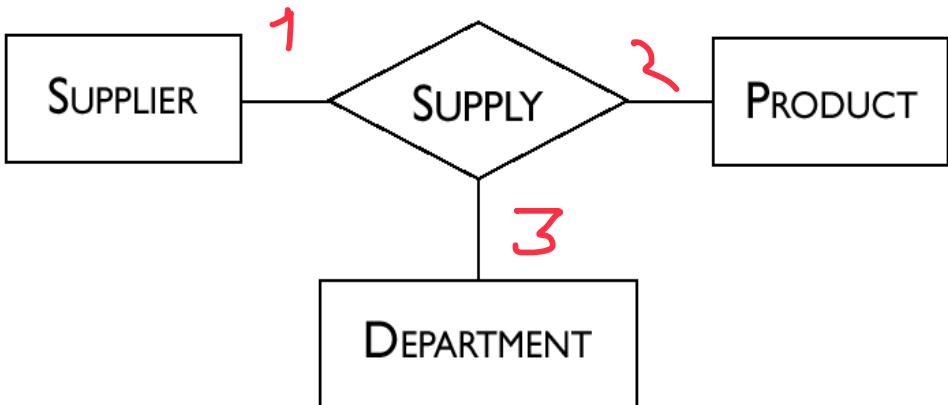
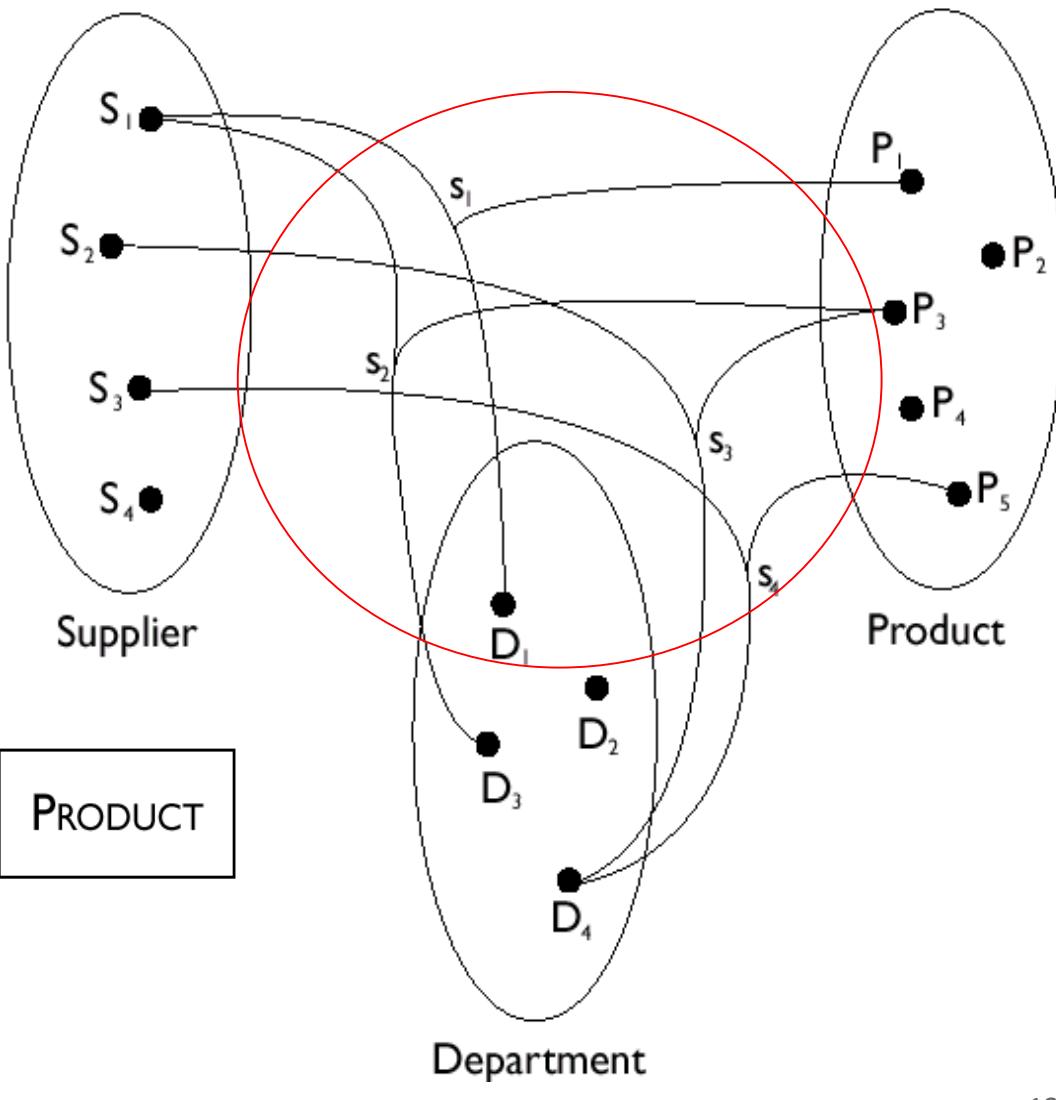
- Recursive relationships relate an entity to itself
- Note in the second example that the relationship is not symmetric
  - In this case, it is necessary to indicate the two **roles** that the entity plays in the relationship



M

3 way relationship (3-ary)  
number of places in a relationship  
is 3 way.

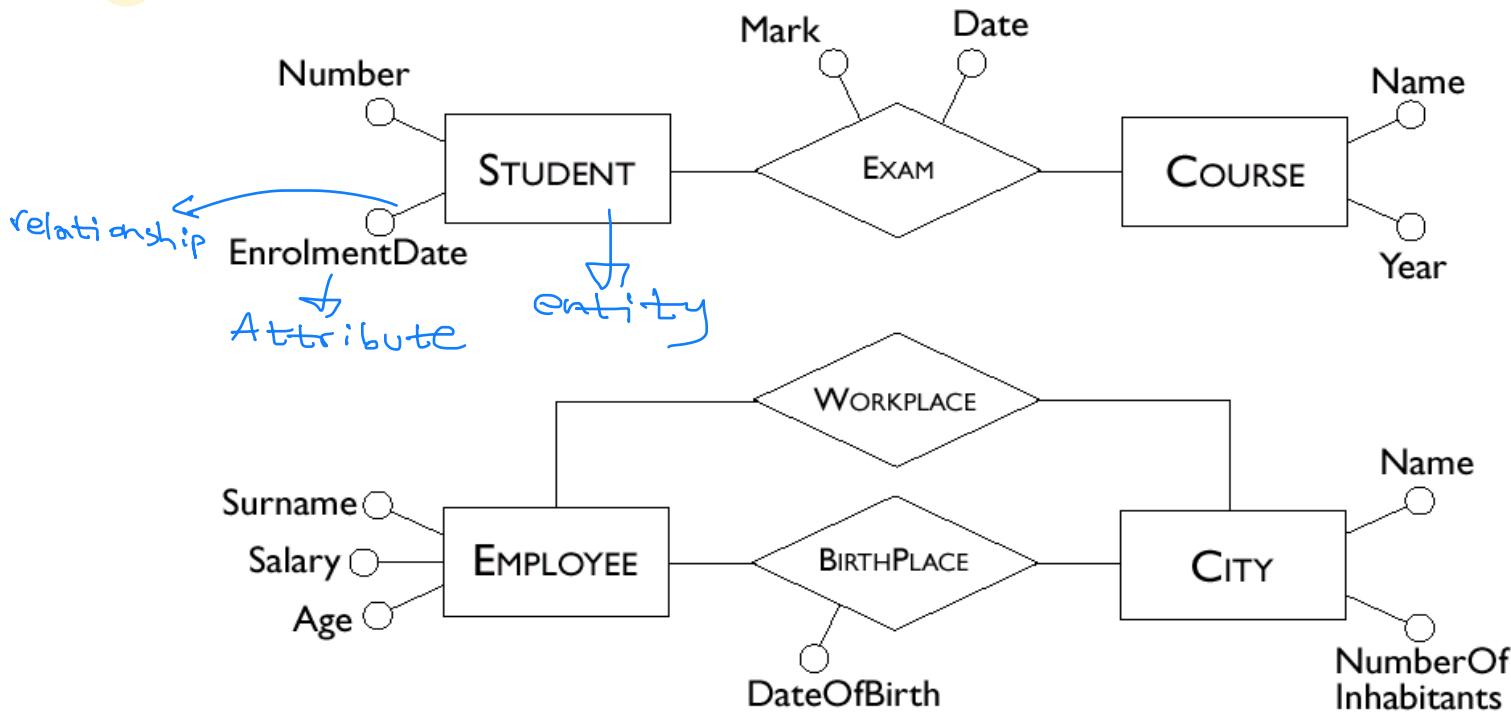
# Ternary Relationships



# Attributes

→ describe properties of entities or relationships

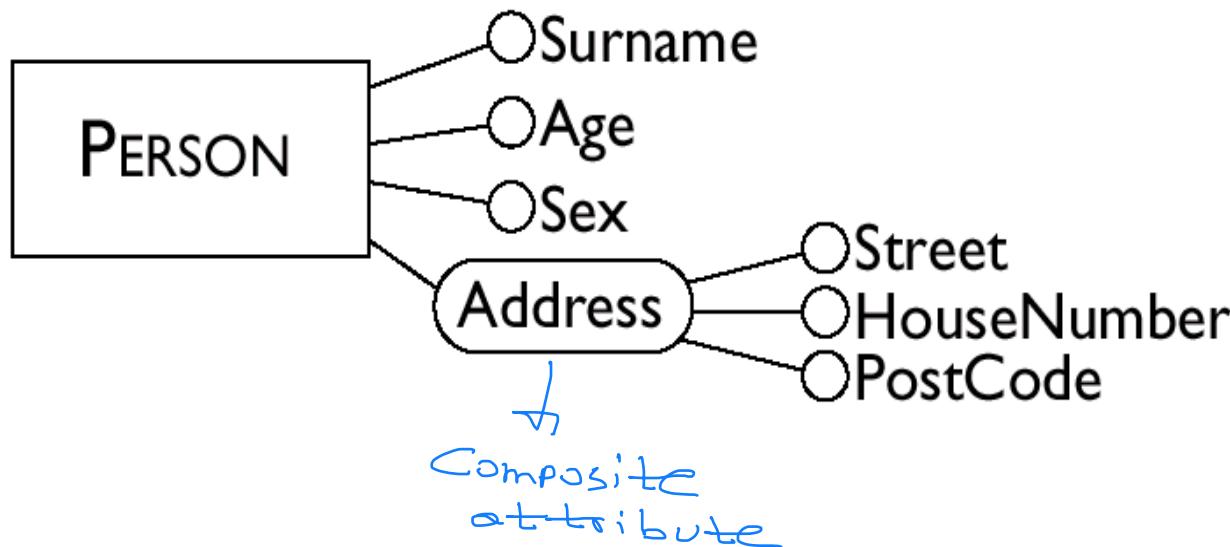
- Describe elementary properties of entities or relationships (e.g., Surname, Salary and Age are attributes of Employee)
- May be single-valued, or multi-valued



# Composite Attributes

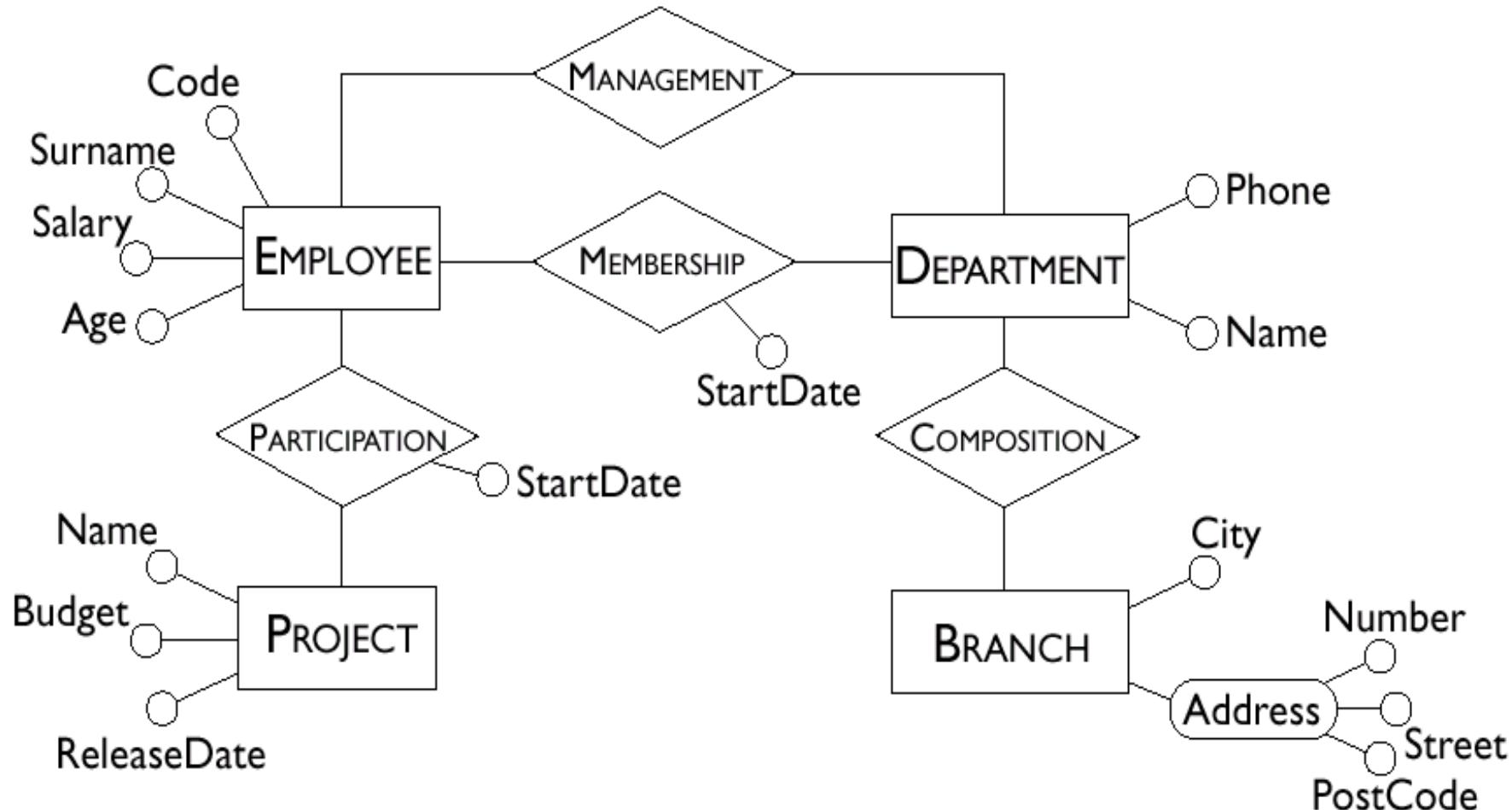
→ attributes that is shown as comprising two or more simpler attributes,

- composite attributes are grouped attributes of the same entity or relationship that have closely connected meaning or uses



CL

# Example Schema with Attributes



# Cardinalities

↗ uniqueness of data values in the column

- Each entity set participates in a relationship set with a minimum (min) and a maximum (max) cardinality
- Cardinalities **constrain** how entity instances participate in relationship instances
- Graphical representation in E/R Diagrams: pairs of (min, max) values for each entity set



An entity might not participate in any relationship

# Cardinalities (cont.)



- In principle, cardinalities are pairs of non-negative integers ( $n$ ,  $N$ ) such that  $n \leq N$ , where  $n$  represents minimum and  $N$  represents maximum cardinality
- minimum cardinality  $n$ :
  - If 0, entity participation in a relationship is optional
  - If 1, entity participation in a relationship is mandatory
- maximum cardinality  $N$ :
  - If 1, each instance of the entity is associated at most with a single instance of the relationship
  - If  $N$ , then each instance of the entity is associated with many instances of the relationship

~~Ack~~

Learn this

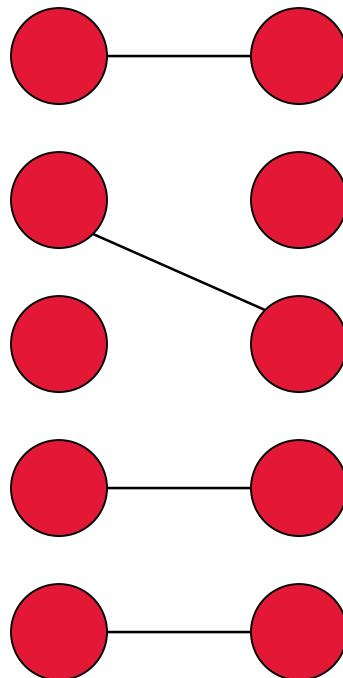
# Cardinality Examples



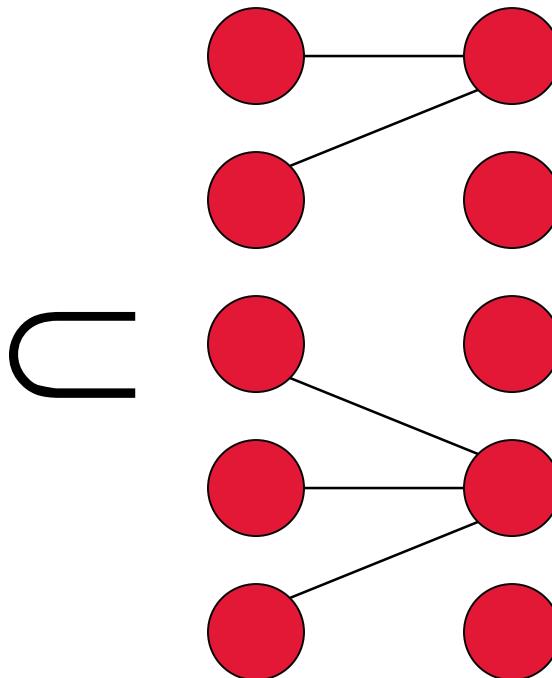
U

# Multiplicity of relationships

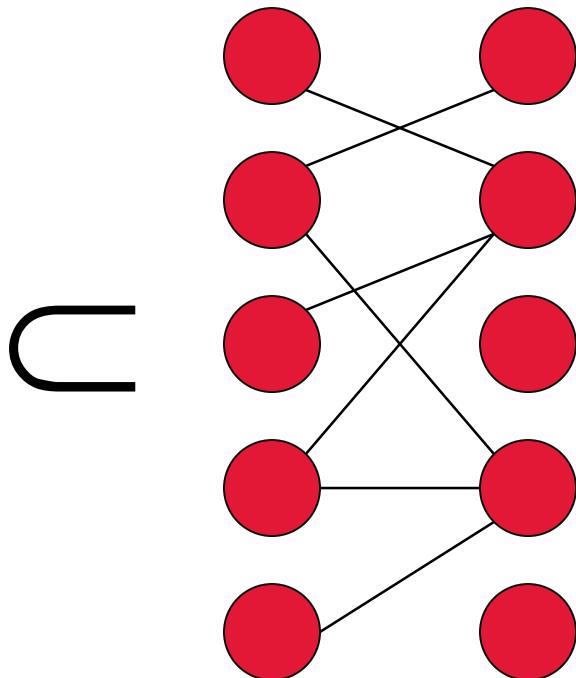
If entities  $E_1$  and  $E_2$  participate in relationship  $R$  with cardinalities  $(n_1, N_1)$  and  $(n_2, N_2)$  then the multiplicity of  $R$  is  $N_1-N_2 (= N_2-N_1)$



1-1



N-1 OR 1-N

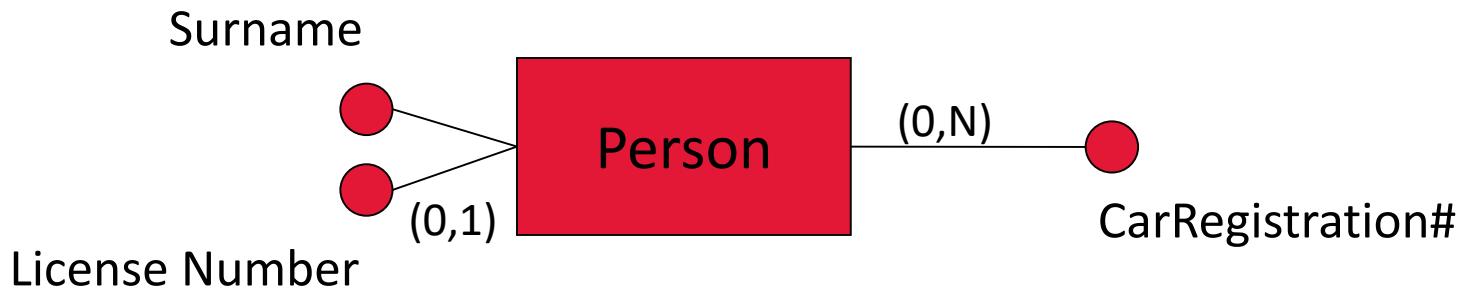


N-N

11

# Cardinalities of Attributes

- Describe min/max number of values an attribute can have
- When the cardinality of an attribute is (1, 1) it can be omitted (**single-valued attributes**)
- The value of an attribute, may also be null, or have several values (**multi-valued attributes**)



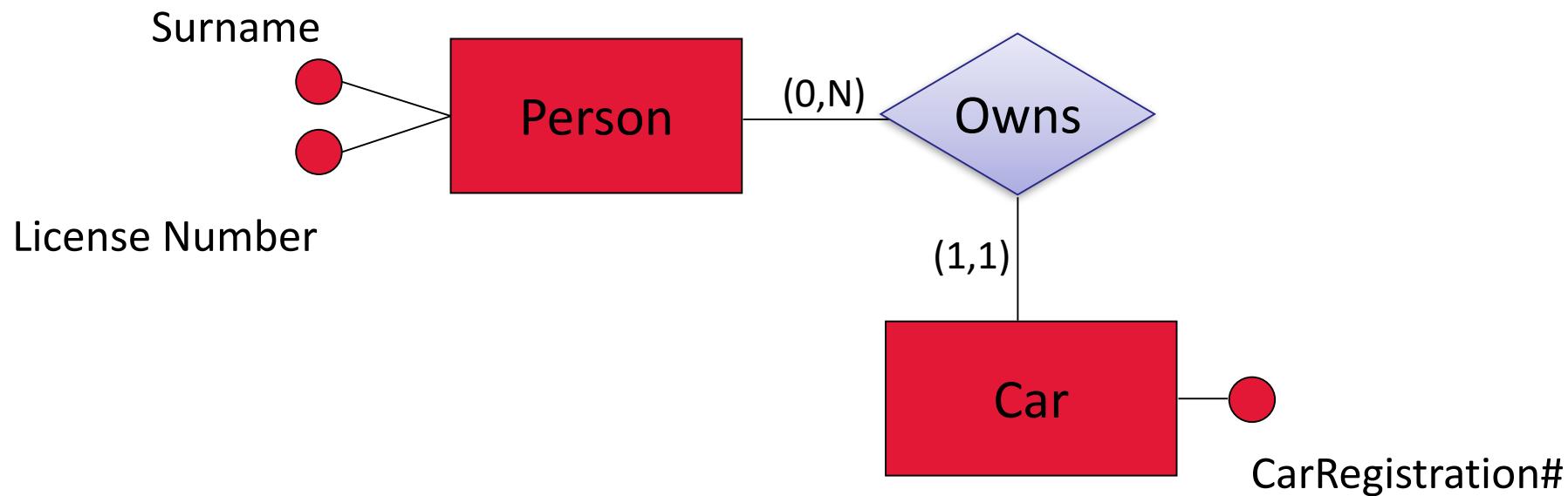
Note:

$(1,1)$   $\rightarrow$  Single-valued attributes

Cardinality can be null.

# Cardinalities of Attributes (cont.)

- Multi-valued attributes often represent situations that can be modeled with additional entities. E.g., the ER schema of the previous slide can be revised into:



Primary key → attribute that is unique  
Foreign key → column or group of columns  
that enforces links between  
two tables

# Keys in E/R

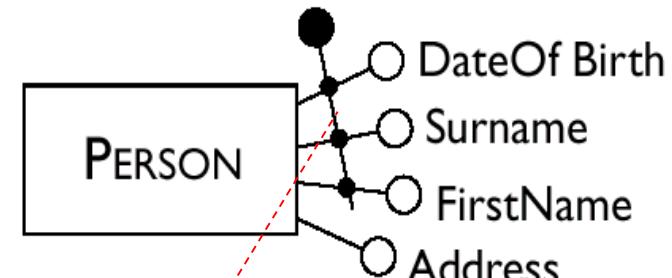
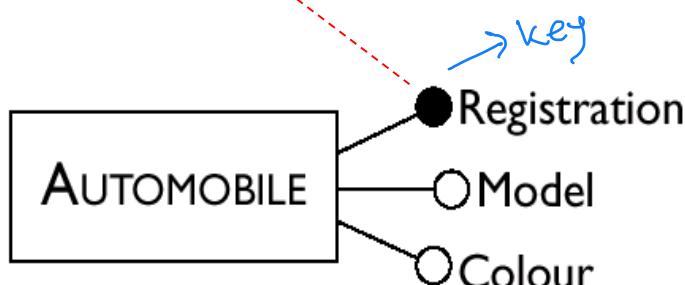
↳ Field in database or combination of fields

- **Keys** consist of minimal sets of attributes which identify uniquely instances of an entity set
  - socialInsurance# may be a key for Person
  - firstName, middleName, lastName, address may be a key for Person
- In most cases, a key is formed by one or more attributes of the entity itself (*internal keys*)
- Sometimes, other entities are involved in the identification (*foreign keys, weak entities*)
- A key for a relationship consists of keys of entities it relates

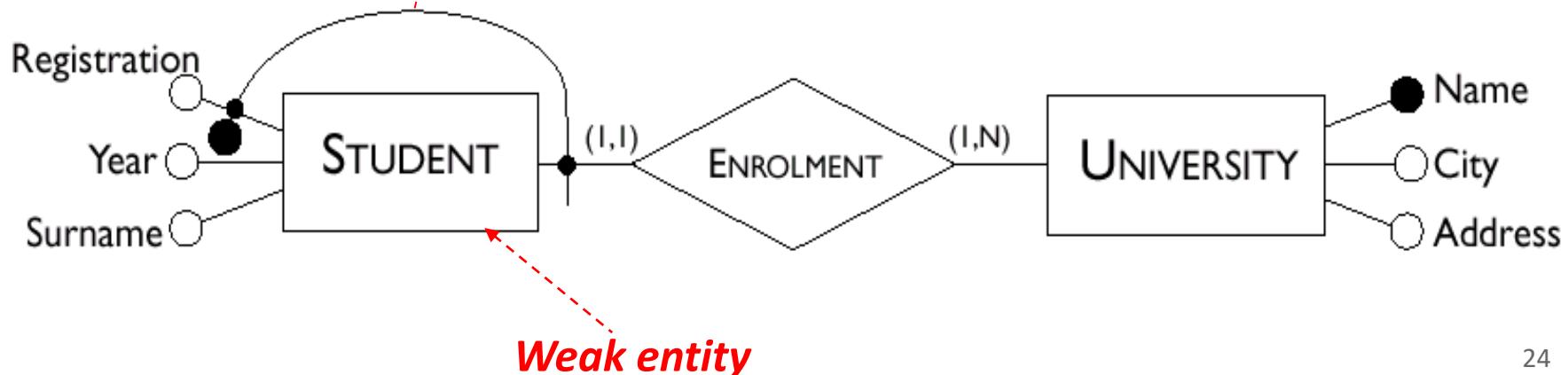
# Examples of Keys in E/R

AA

*internal, single-attribute*

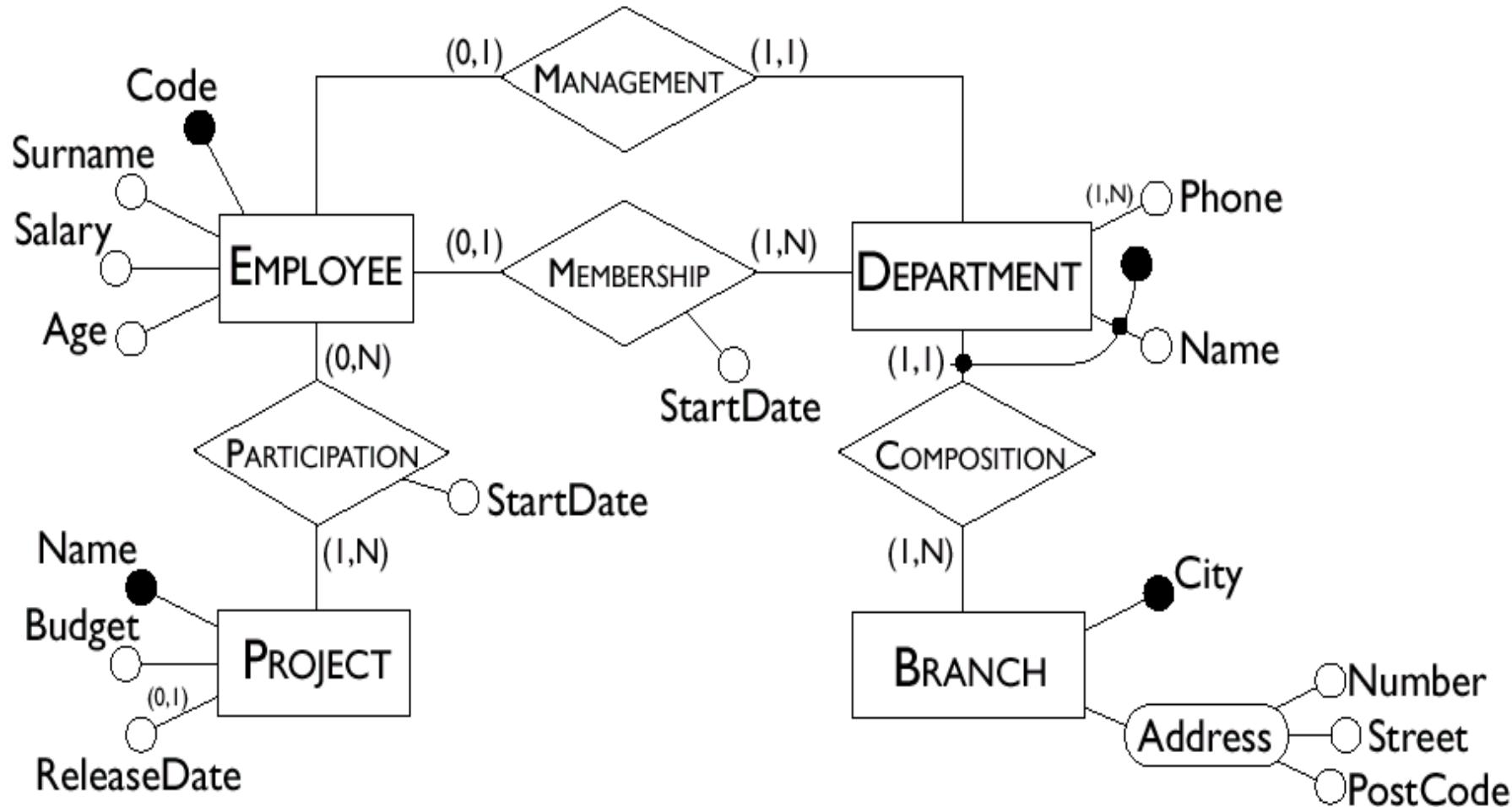


*foreign, multi-attribute*



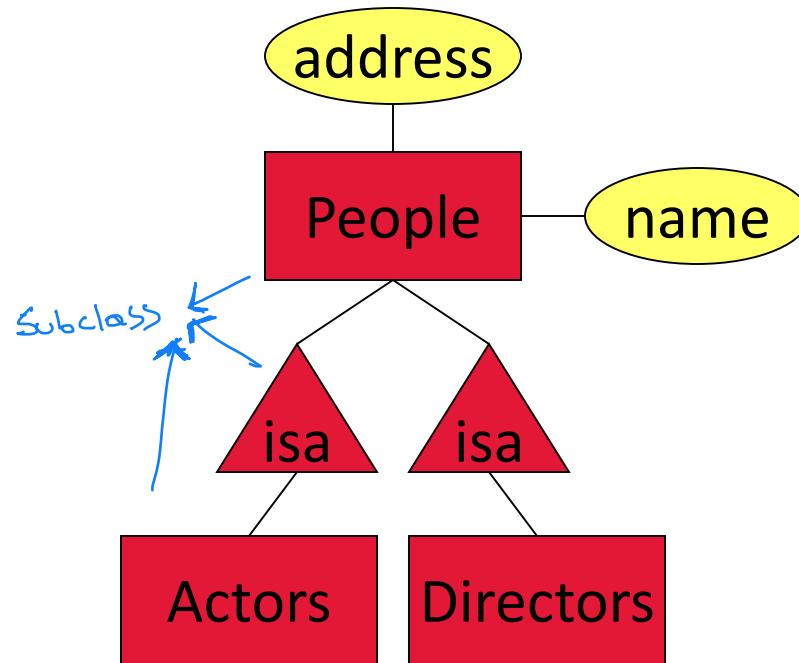
~~AB~~

# Schema with Keys



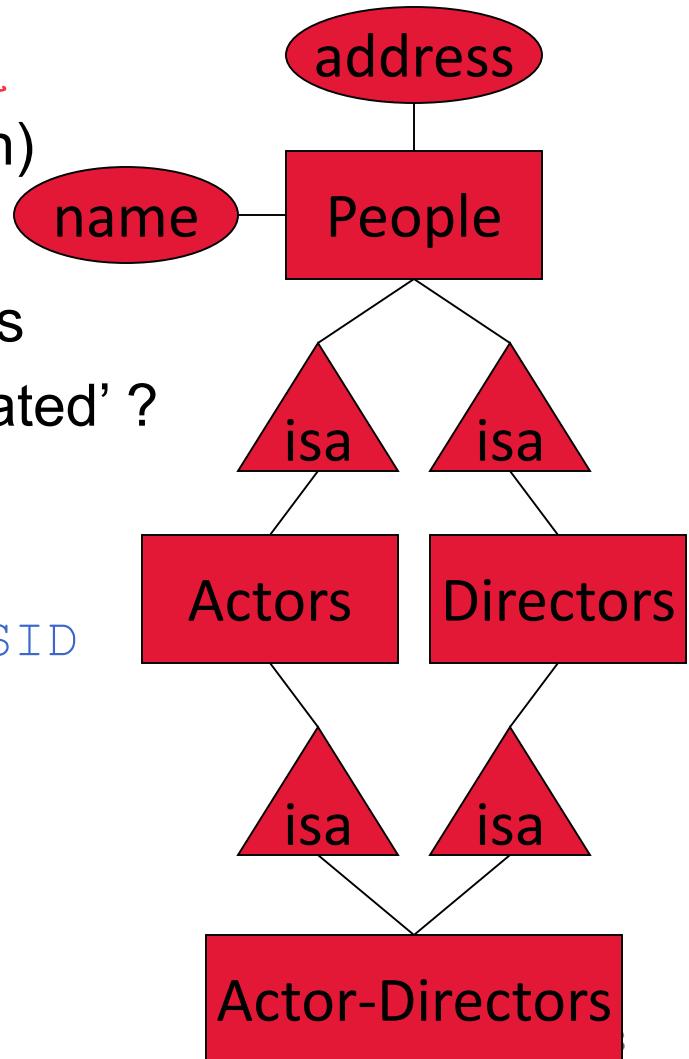
# Subclasses in E/R

- Subclass = special case → Inheritance
  - Fewer instances, more attributes (usually)
  - One-one relationship between classes
  - Attributes: union of classes involved



# Multiple inheritance in E/R

- Allowed, but not usually necessary
  - Entity can “be” many classes (union)
- Usually not a good idea
  - Naming collisions, semantic clashes
    - => What if both have attribute ‘nominated’ ?
  - Queries often work just as well
    - => `SELECT A.* FROM Actors A,  
Directors D WHERE A.SID = D.SID`
- Usable classes usually form a tree



# Weak entity sets

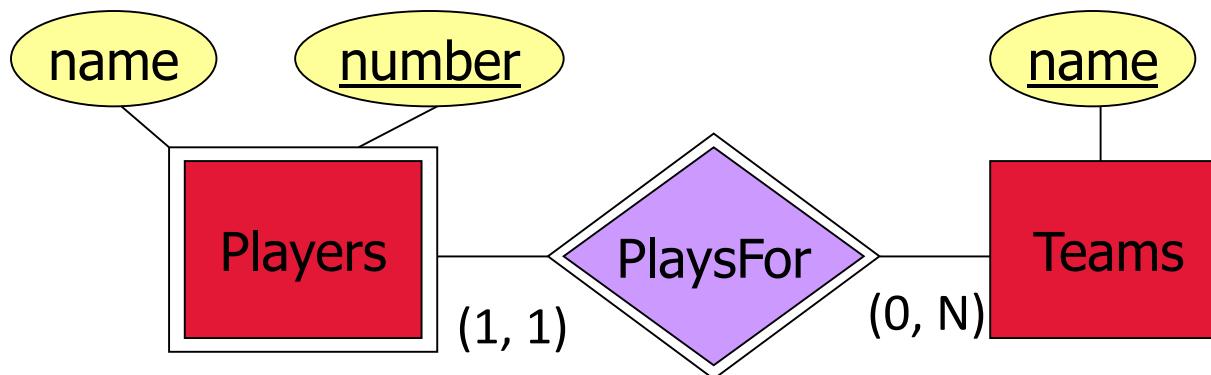


- Occasionally, entities of an entity set need “help” to identify them uniquely
- Entity set  $E$  is said to be *weak* if in order to identify entities of  $E$  uniquely, we need to follow one or more many-one relationships from  $E$  and include the key of the related entities from the connected entity sets
- Weak entities never exist alone
  - Always at least one *supporting* relationship to identify them
  - Other relationships allowed as well



# Weak entity sets – example

- **name** is almost a key for football players, but there might be two with the same name
- **number** is certainly not a key, since players on two teams could have the same number
- But **number**, together with the team **name** related to the player by **PlaysFor** should be unique

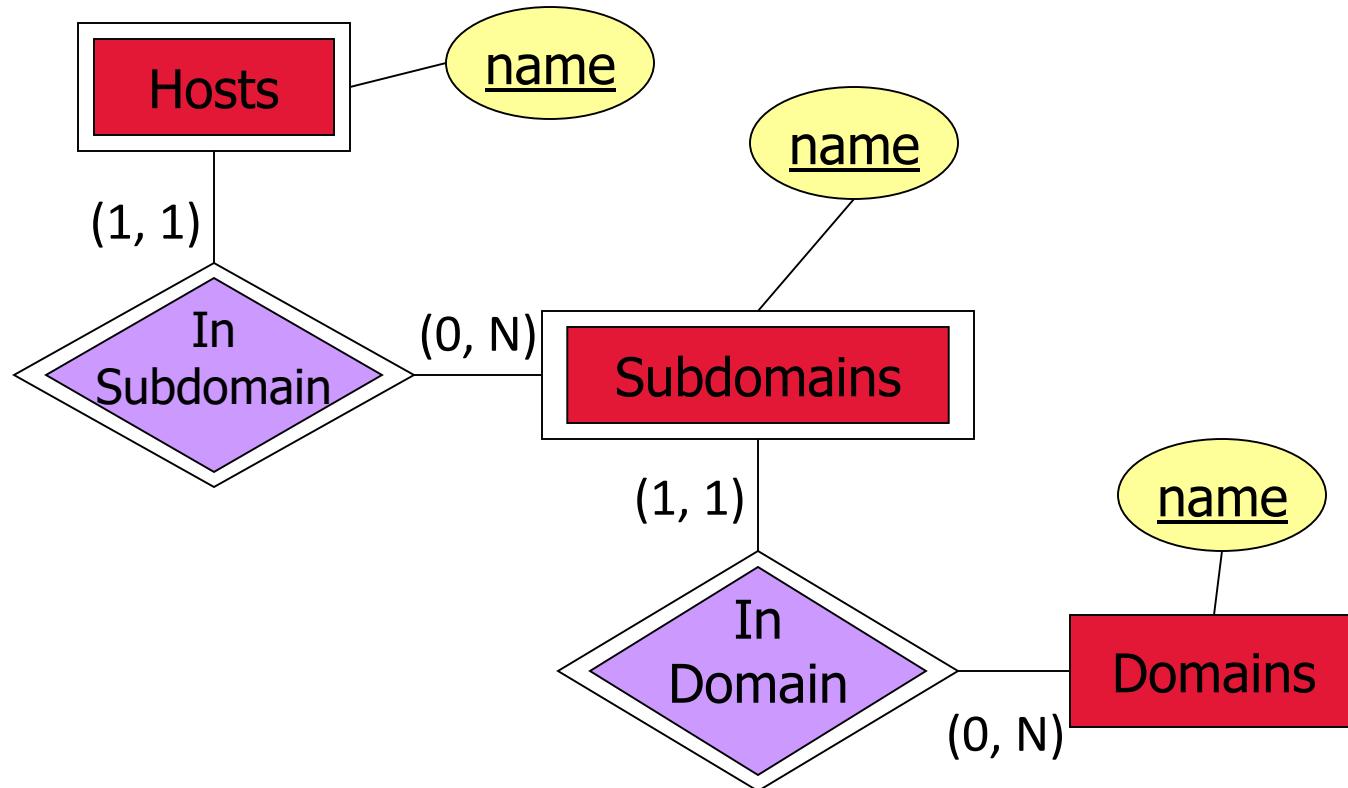


Double rectangle for the weak entity set

Double diamond for *supporting* many-one relationship



# “Chained” weak entity sets



*Key: host + subdomain + domain*

# Weak entity sets in practice

- Question: how does a supporting relationship identify an entity having an incomplete key?
  - Example: print servers  
=> CS: inkblot, treekiller  
=> Math: papershredder, treekiller
- Answer: it doesn't.
  - Option 1: replicate Printers (CSPrinters and MathPrinters)
  - Option 2: create/use some artificial key (serial number, etc.)
  - Option 3: store full key in weak entity (most common)
- Weak entities: a (sometimes useful) myth

*Recommendation: need a good reason to use*

# Challenge: modeling the “real world”

- Life is arbitrarily complex
  - Directors who are also actors? Actors who play multiple roles in one movie? Animal actors?
- Design choices: Should a concept be modeled as an entity, an attribute, or a relationship?
- Constraints on the ER Model: A lot of data semantics can be captured but some cannot
- Key to successful model: parsimony
  - As complex as necessary, but no more
  - Choose to represent only “relevant” things

check these

# EXAMPLE

# From real world to E/R Model

We wish to create a database for a company that runs training courses. For this, we must store data about trainees and instructors. For each course participant (about 5,000 in all), identified by a code, we want to store her social security number, surname, age, sex, place of birth, employer's name, address and telephone number, previous employers (and periods employed), the courses attended (there are about 200 courses) and the final assessment for each course. We need also to represent the seminars that each participant is attending at present and, for each day, the places and times the classes are held.

Each course has a code and a title and any course can be given any number of times. Each time a particular course is given, we will call it an 'edition' of the course. For each edition, we represent the start date, the end date, and the number of participants. If a trainee is self-employed, we need to know her area of expertise, and, if appropriate, her title. For somebody who works for a company, we store the level and position held. For each instructor (about 300), we will show the surname, age, place of birth, the edition of the course taught, those taught in the past and the courses that the tutor is qualified to teach. All the instructors' telephone numbers are also stored. An instructor can be permanently employed by the training company or freelance.

# From real world to E/R Model

We wish to create a database for a company that runs training courses. For this, we must store data about the *trainees* and the *instructors*. For each *course participant* (about 5,000), identified by a code, we want to store her social security number, surname, age, sex, place of birth, employer's name, address and telephone number, previous employers (and periods employed), the courses attended (there are about 200 courses) and the final assessment for each course. We need also to represent the *seminars* that each participant is attending at present and, for each day, the places and times the classes are held.

Each *course* has a code and a title and any course can be given any number of times. Each time a particular course is given, we will call it an 'edition' of the course. For each edition, we represent the start date, the end date, and the number of participants. If a trainee is self-employed, we need to know her area of expertise, and, if appropriate, her title. For somebody who works for a company, we store the level and position held. For each *instructor* (about 300), we will show the surname, age, place of birth, the edition of the course taught, those taught in the past and the courses that the *tutor* is qualified to teach. All the instructors' telephone numbers are also stored. An instructor can be permanently employed by the training company or freelance.

# Glossary

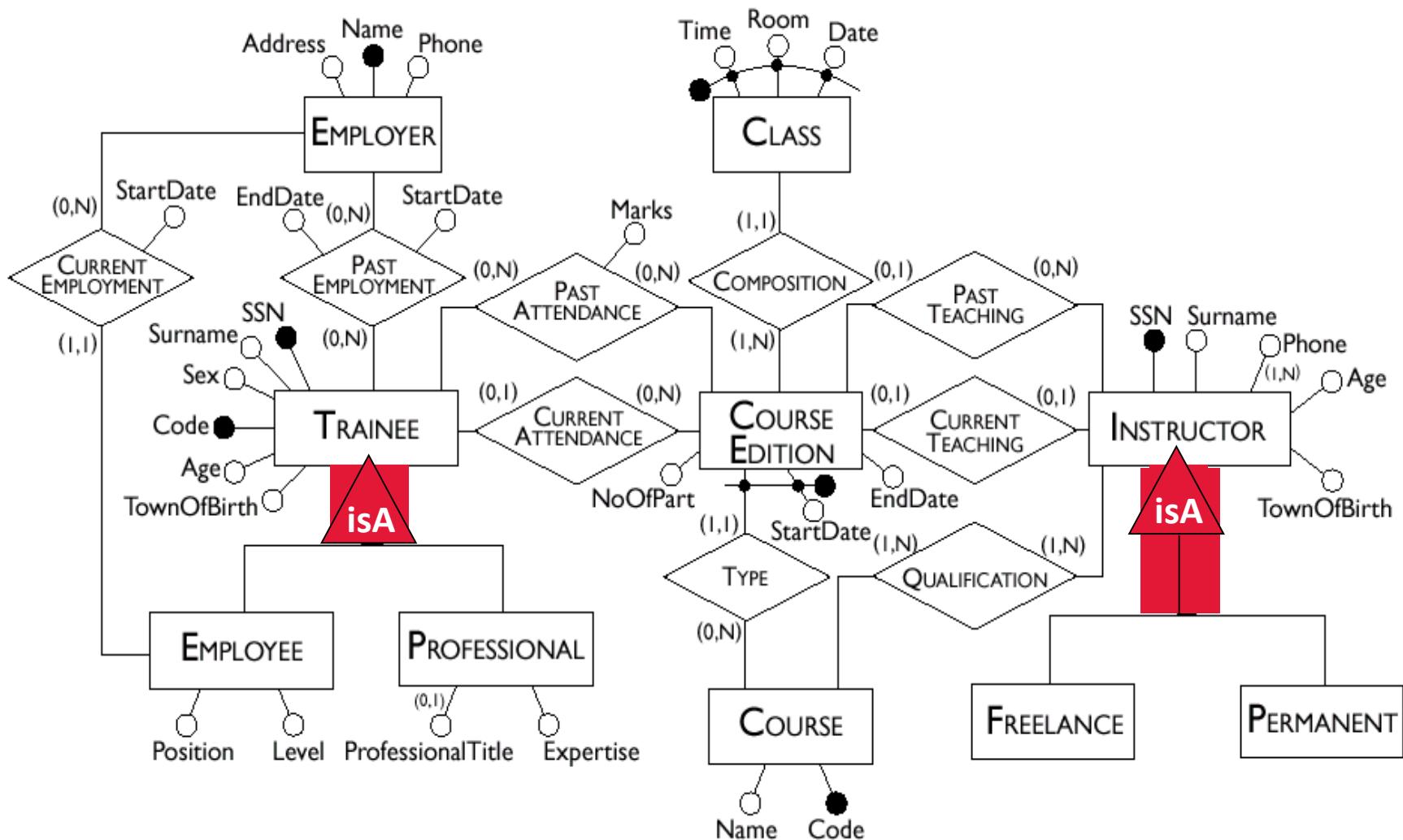
| Term       | Description   | Synonym     | Links               |
|------------|---|-------------|---------------------|
| Trainee    | Participant in a course. Can be an employee or self-employed. | Participant | Course, Company     |
| Instructor | Course tutor. Can be freelance.                               | Tutor       | Course              |
| Course     | Course offered. Can have various editions.                    | Seminar     | Instructor, Trainee |
| Company    | Company by which a trainee is employed or has been employed.  |             | Trainee             |

# More Annotations

We wish to create a database for a company that runs training courses. For this, we must store data about *trainees* and *instructors*. For each *course participant* (about 5,000), identified by a code, we want to store her *social security number, surname, age, sex, place of birth, employer's name, address and telephone number, previous employers (and periods employed)*, courses attended (there are about 200 courses) and the final assessment for each course. We need also to represent *seminars* that each participant is attending at present and, *for each day, the places and times the classes are held*.

Each *course* has a code and a title and any course can be given any number of times. Each time a particular course is given, we will call it an 'edition' of the course. For *each edition, we represent the start date, the end date, and the number of participants*. If a trainee is self-employed, we need to know her area of expertise, and, if appropriate, her title. For somebody who works for a company, we store the level and position held. For each *instructor* (about 300), we will show the surname, age, place of birth, the edition of the course taught, those taught in the past and the courses that the *tutor* is qualified to teach. All the instructors' telephone numbers are also stored. An instructor can be permanently employed by the training company or freelance.

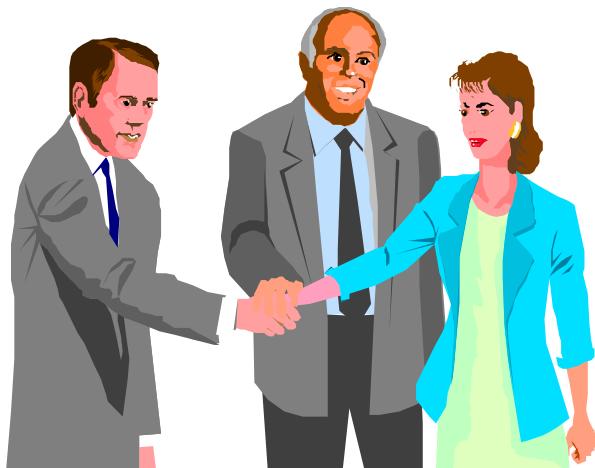
# ... the E/R model result



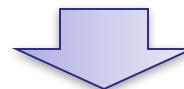
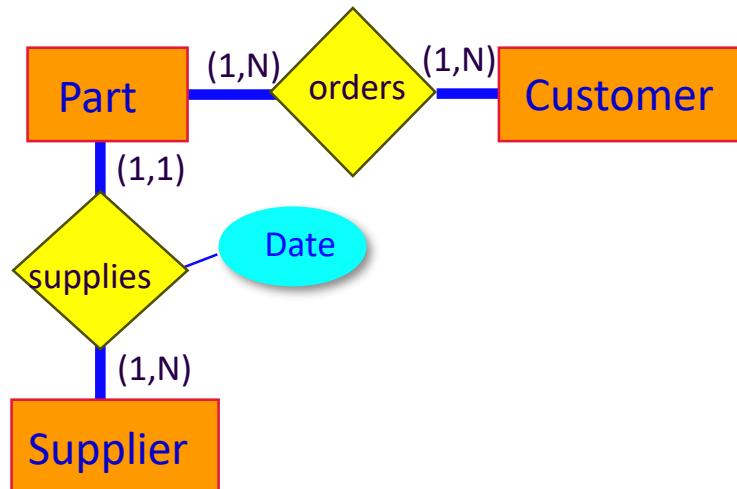
# DESIGNING A DATABASE SCHEMA

# Designing a Database Schema

The “real world”



The E/R Model (Conceptual Model)



The Relational Schema

**Part** (Name, Description, Part#)  
**Supplier** (Name, Addr)  
**Customer** (Name, Addr)  
**Supplies** (Name, Part#, Date)  
**Orders** (Name, Part#)



# (Relational) Database Design

- Given a conceptual schema (ER, but could also be UML), generate a logical (relational) schema
- This is *not* just a simple translation from one model to another for two main reasons:
  - not all the constructs of the ER model can be translated naturally into the relational model
  - the schema must be restructured in such a way as to make the execution of the projected operations as efficient as possible



# Logical Design Steps

It is helpful to divide the design into two steps:

- ① • *Restructuring of the Entity-Relationship schema*, based on criteria for the optimization of the schema
- ② • *Translation into the logical model*, based on the features of the logical model (in our case, the relational model)

# RESTRUCTURING OF AN E/R MODEL

# Restructuring Overview

**Input:** E/R Schema

**Output:** Restructured E/R Schema

Restructuring parts:

- Analysis of Redundancies
- Removing Generalizations (Subclasses)
- Partitioning/Merging of Entities and Relations
- Limit the Use of Weak Entity Sets
- Selection of Primary Identifiers (Keys)

# Analysis of Redundancies

↳ saying the same thing over again in a different way

**Redundancy** = saying the same thing in two (or more) different ways

- Wastes space and (more importantly) encourages inconsistency
  - Two representations of the same fact become inconsistent if we change one and forget to change the other
- Usually indicates a design flaw as well
  - Example: storing actor's address with movies  
=> Address at time of filming? Now? Hotel near studio?

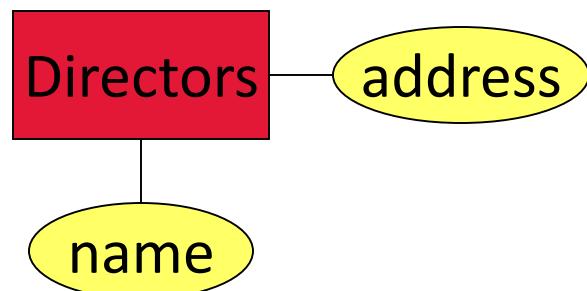
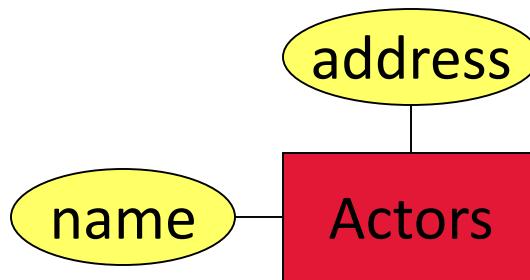
# Two types of redundancy

- ① • Repeated information

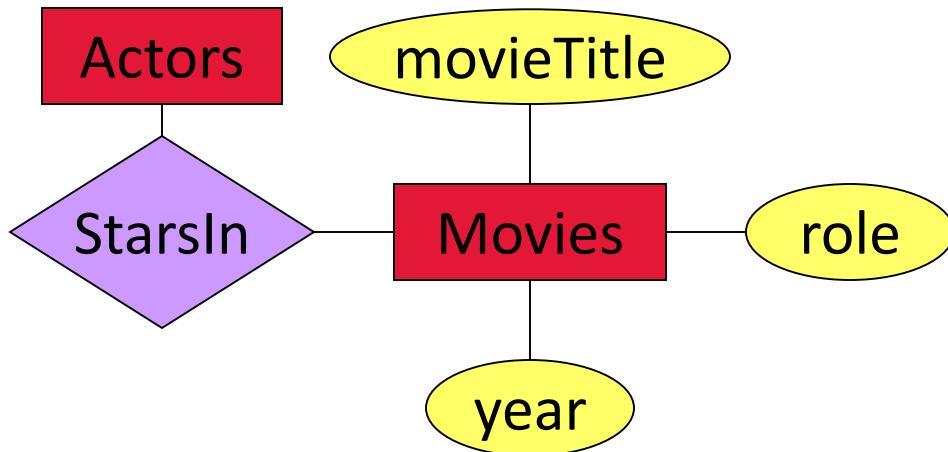
| name        | address   | role    |
|-------------|-----------|---------|
| James Jones | Villa, CA | Vader   |
| James Jones | Villa, CA | Vader   |
| James Jones | Villa, CA | Vader   |
| James Jones | Villa, CA | Greer   |
| James Jones | Villa, CA | Mustafa |

*Causes Redundancy*

- ② • Repeated designs (same or similar attributes)

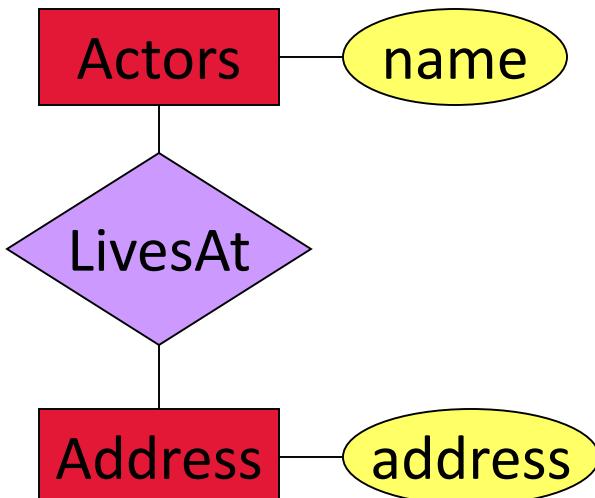


# E.S. vs. attributes: bad examples



*Many movies, one role?*

*Many roles, one movie?*



*Redundant Entity Set  
and Relationship Set*

# Entity Sets Versus Attributes

- An entity set should satisfy at least one of the following conditions:
  - ⌚ – It is more than the name of something; it has at least one nonkey attribute.  
or
  - ⌚ – It is the “many” in a many-one or many-many relationship.
- Rules of thumb
  - A “thing” in its own right => Entity Set
  - A “detail” about some other “thing” => Attribute
  - A “detail” correlated among many “things” => Entity Set

*Really this is just about avoiding redundancy*

# Deciding about Redundancy



The presence of a redundancy in a database may be

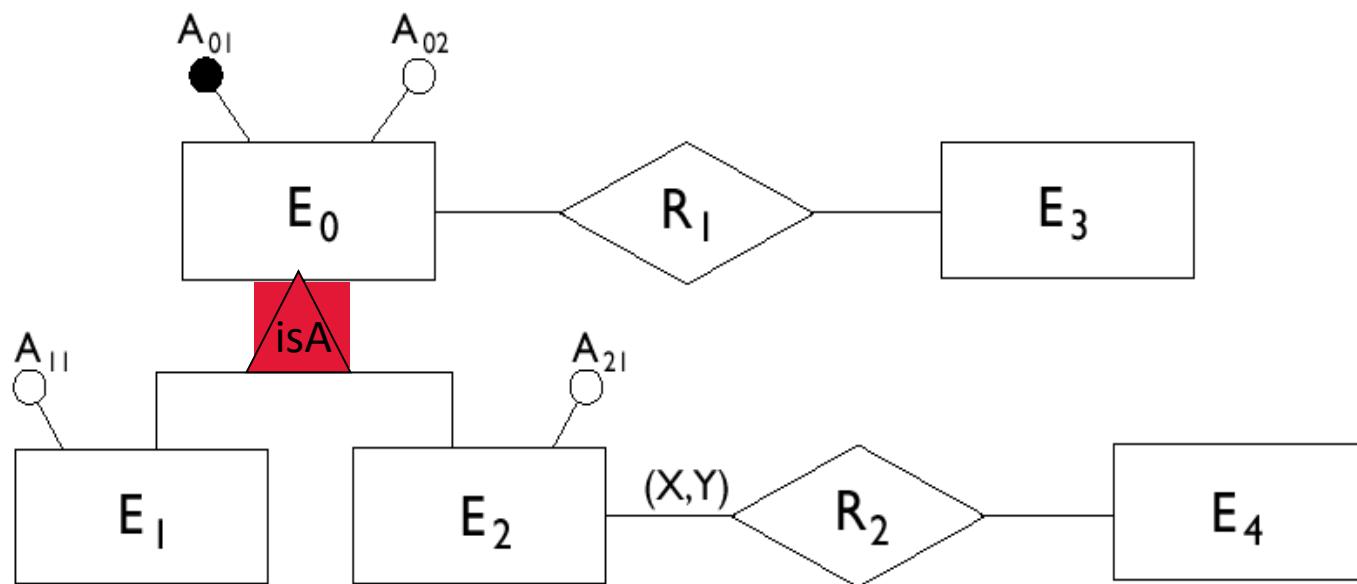
- **an advantage**: a reduction in the number of accesses necessary to obtain derived information
- **a disadvantage**: because of larger storage requirements, (but, usually at negligible cost) and the necessity to carry out additional operations in order to keep the derived data consistent

**Interesting Tradeoff**: The decision to maintain or eliminate a redundancy is made by comparing the cost of operations that involve the redundant information and **the storage needed**, in the case of presence or absence of redundancy.

*Performance analysis is required to decide about redundancy*

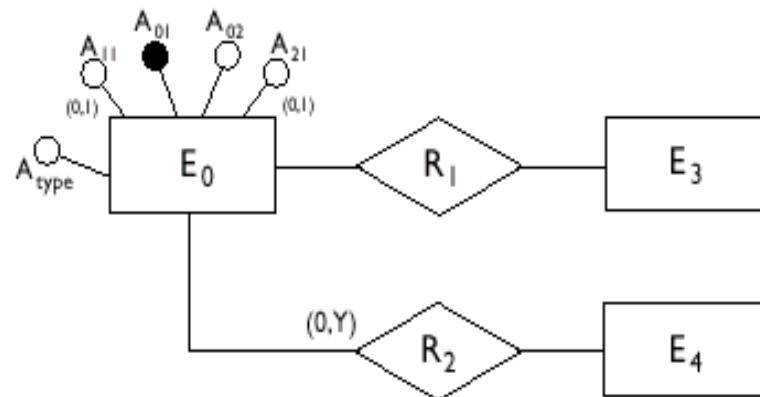
# Removing Generalizations

- The relational model does not allow direct representation of generalizations that may be present in an ER diagram. For example, here is an ER schema with generalizations:

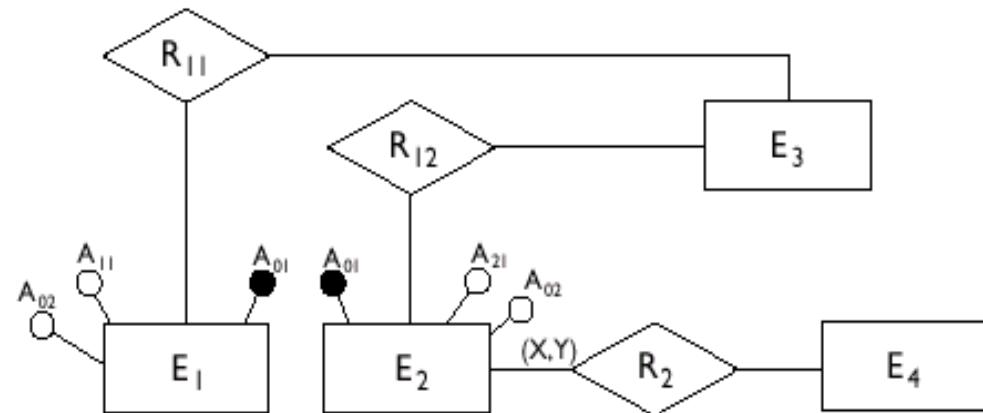


# Possible Restructurings

Option 1

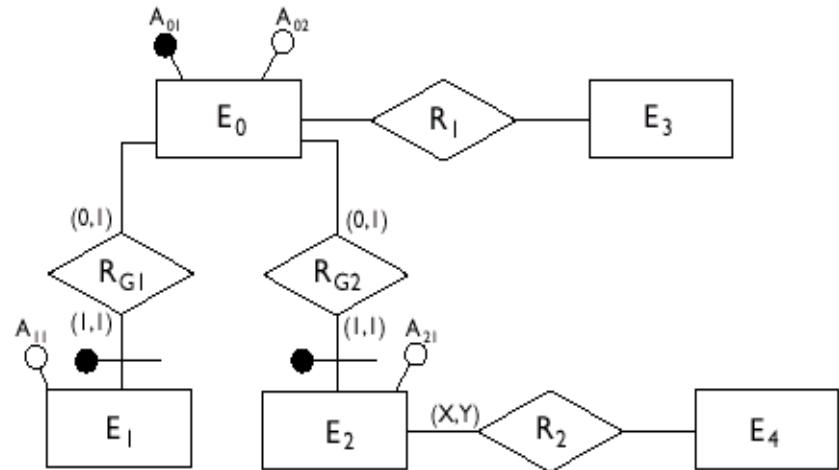


Option 2

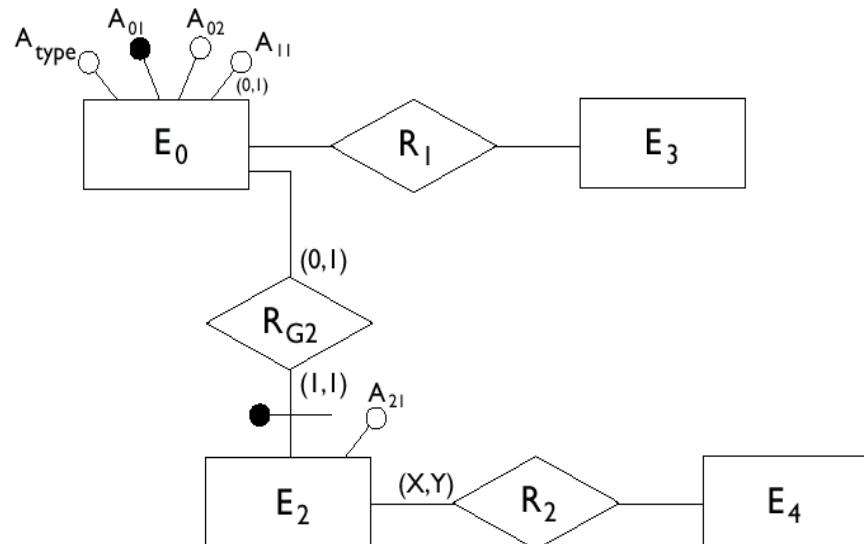


# Possible Restructurings

Option 3



Option 4

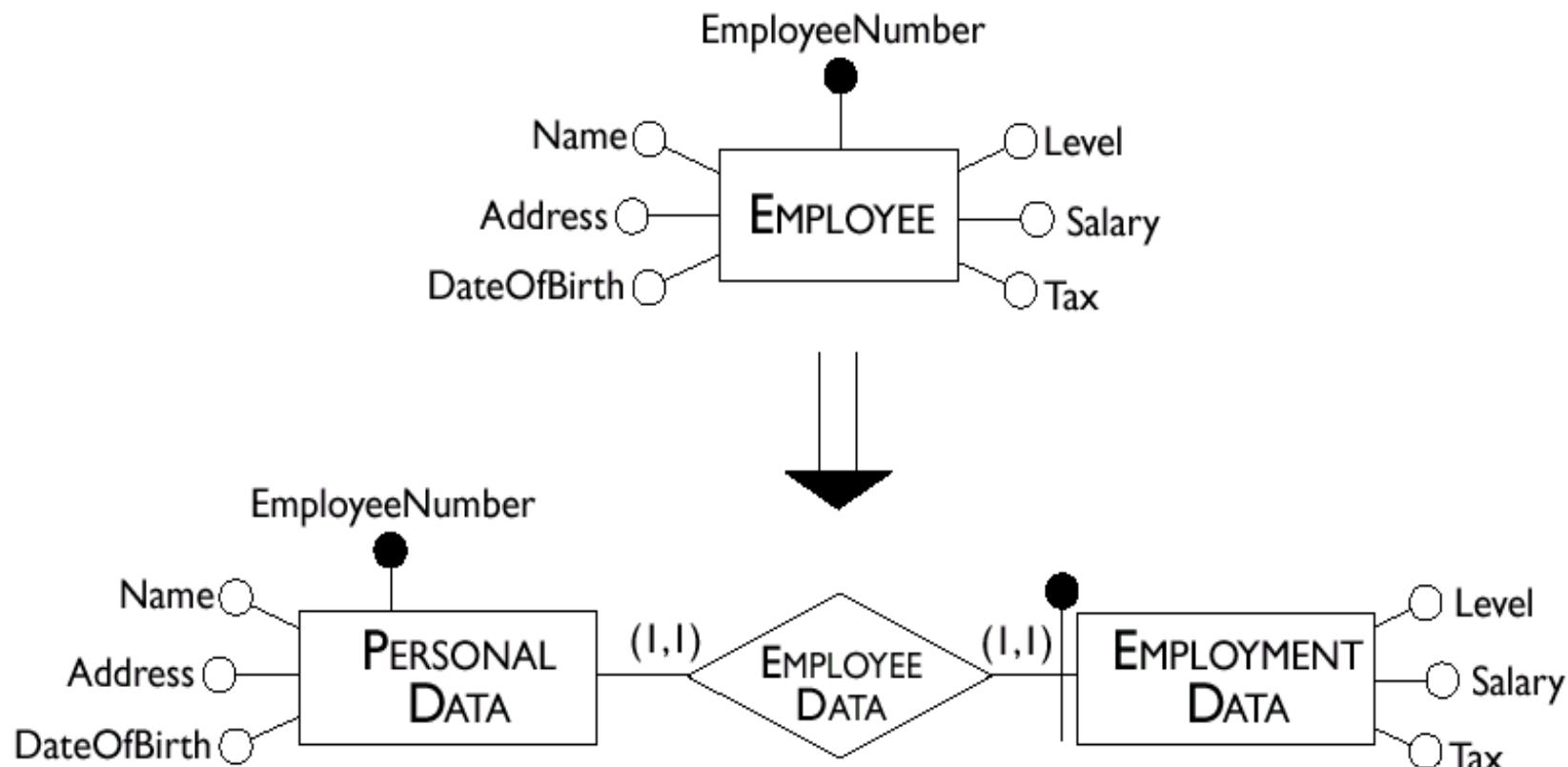


# Partitioning and Merging of E/R

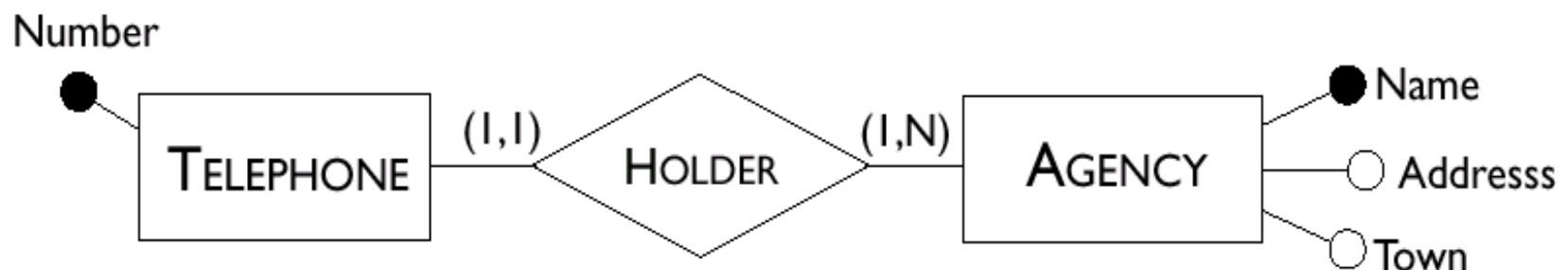
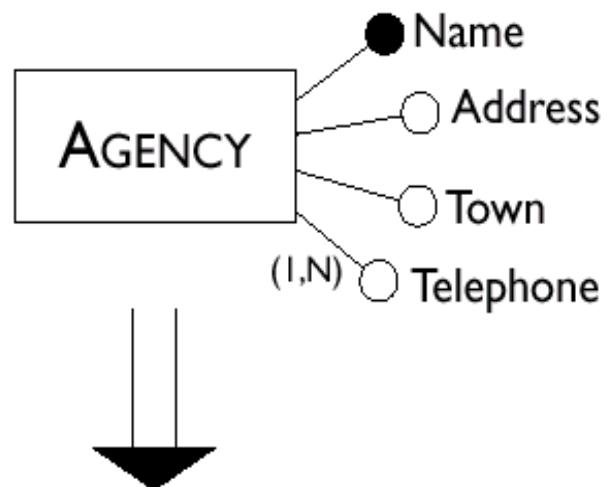
4

- Entities and relationships of an E-R schema can be partitioned or merged to improve the efficiency of operations
- Accesses are reduced by:
  - Ⓐ - separating attributes of the same concept that are accessed by different operations and
  - Ⓑ - merging attributes of different concepts that are accessed by the same operations

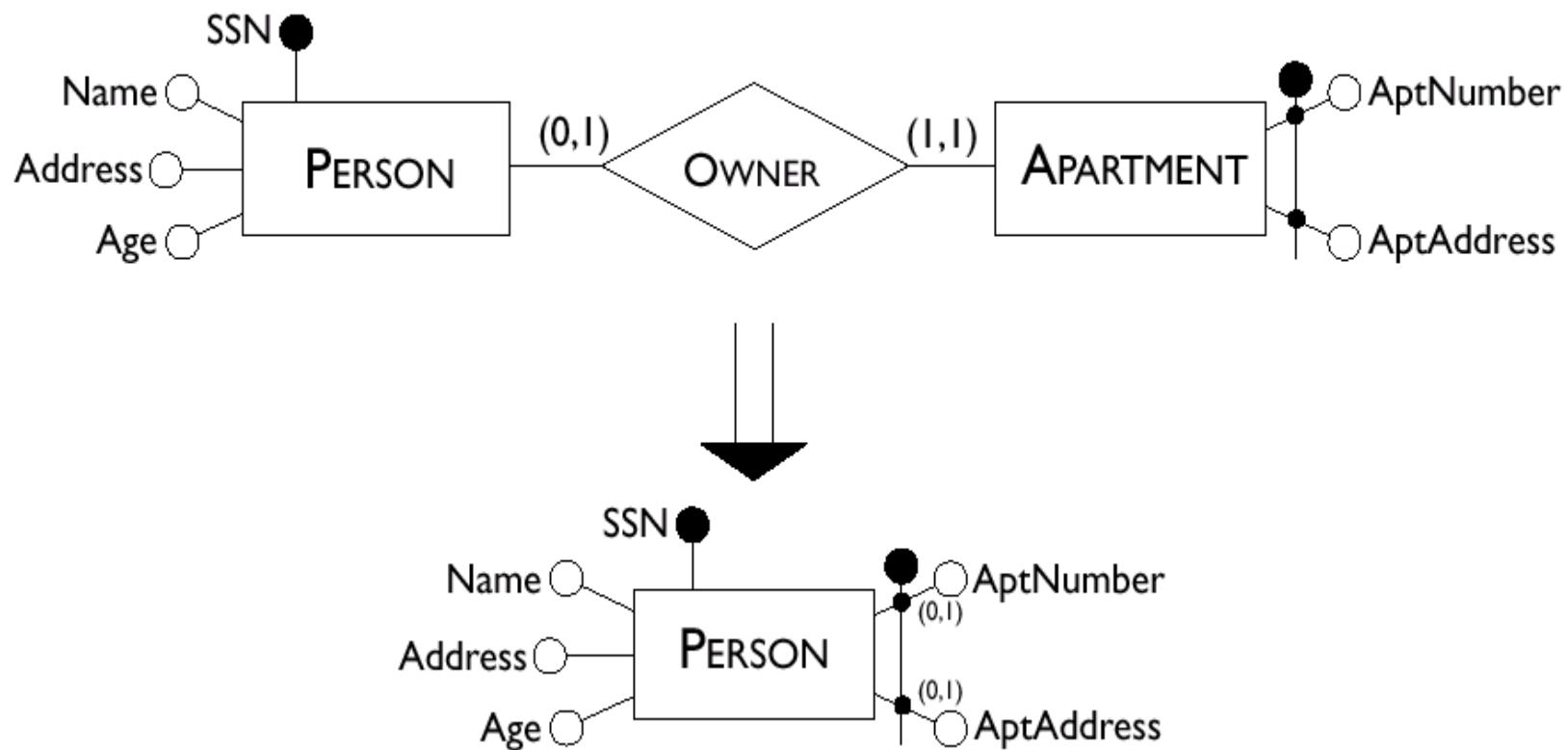
# Example of Partitioning



# Elimination of Multi-valued Attrib.

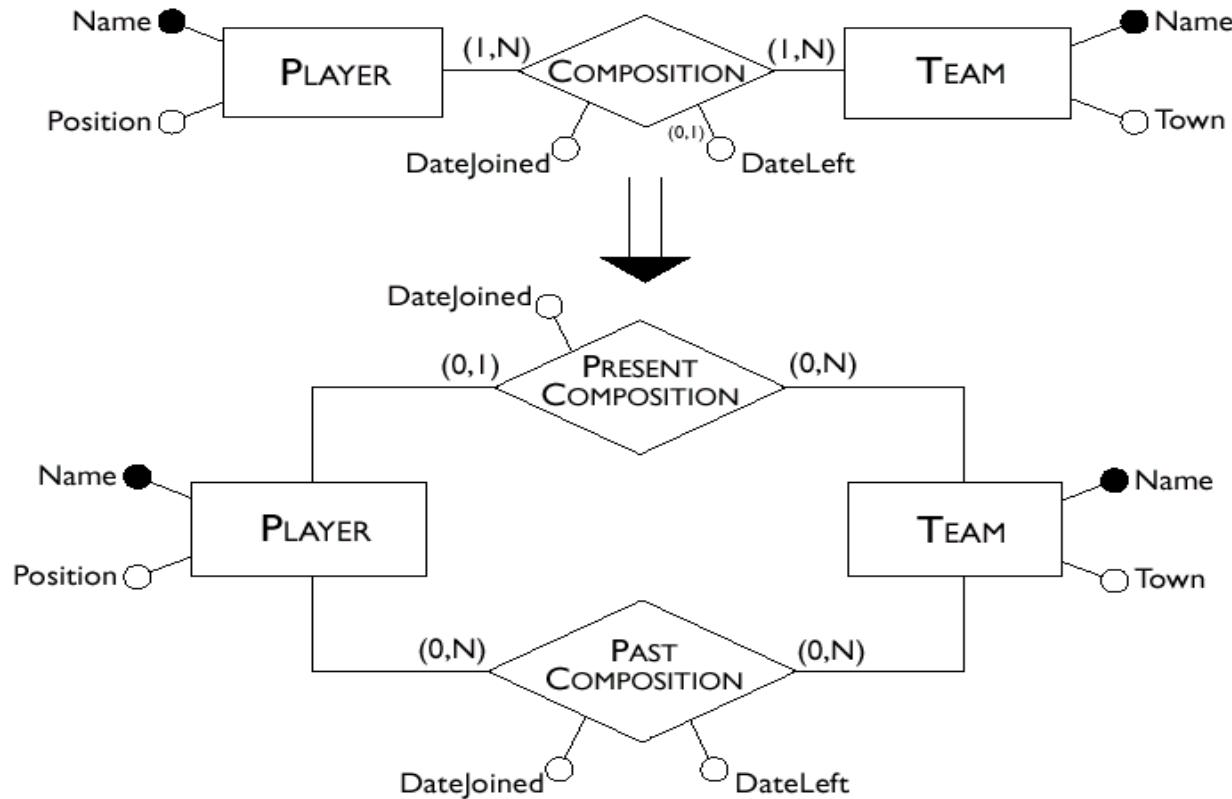


# Merging Entities



# Partitioning of a Relationship

Suppose that composition represents current and past compositions of a team



# When to use weak entity sets?

- The usual reason is that there is no global authority capable of creating unique ID's
- **Example:** it is unlikely that there could be an agreement to assign unique player numbers across all football teams in the world

# Don't Overuse Weak Entity Sets

- Beginning database designers often doubt that anything could be a key by itself
  - They make all entity sets weak, supported by all other entity sets to which they are linked
- In reality, each entity gets a unique ID anyway
  - Social insurance number, automobile VIN, etc.
  - Useful for many reasons (next slide)

# Selecting a Primary Key

- Every relation must have a unique primary key
- The criteria for this decision are as follows:
  - Attributes with null values cannot form primary keys
  - One/few attributes is preferable to many attributes
  - Internal keys preferable to external ones (weak entities depend for their existence on other entities)
  - A key that is used by many operations to access instances of an entity is preferable to others



# Keeping keys simple

Multi-attribute and/or string keys...

- ... are redundant
  - e.g. Movies(title, year, ...): 2 attributes, ~16 bytes
  - Number of movies ever made <<  $2^{32}$  (4 bytes)  
=> Integer movieID key saves 75% space and a lot of typing
- ... break encapsulation
  - e.g. Patient(firstName, lastName, phone, ...)
  - Security/privacy hole  
=> Integer patientID prevents information leaks
- ... are brittle (nasty interaction of above two points)
  - Name or phone number change? Parent and child with same name?
  - Patient with no phone? Two movies with same title and year?  
=> Internal ID always exists, immutable, unique

*Also: computers are really good at integers...*

# TRANSLATION OF AN E/R MODEL INTO THE LOGICAL MODEL (DB SCHEMA)

# Translation into a Logical Schema

**Input:** E/R Schema

**Output:** Relational Schema

- Starting from an E-R schema, an equivalent relational schema is constructed
  - “**equivalent**”: a schema capable of representing the same information
- We will deal with the translation problem systematically

# Many-to-Many Relationships



Employee(Number, Surname, Salary)

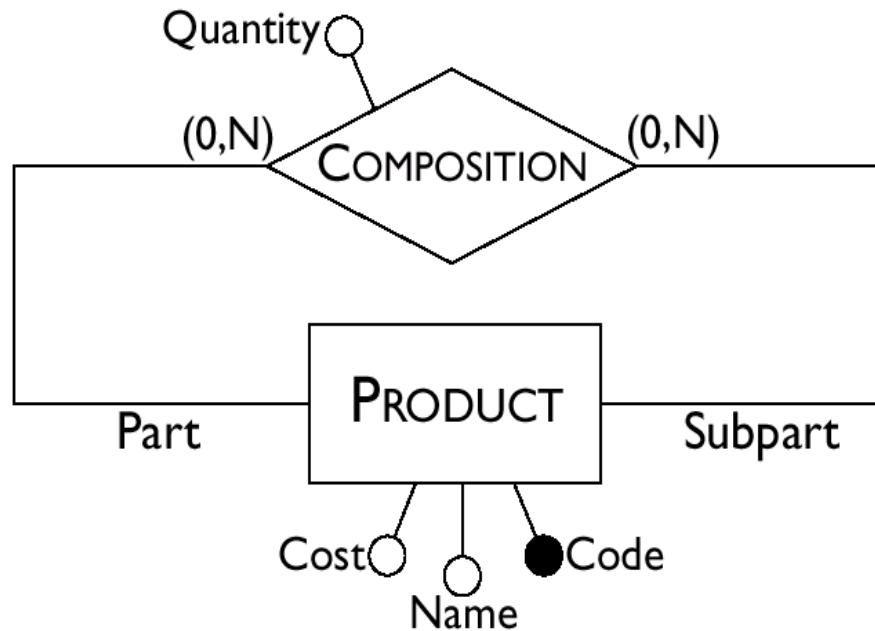
Project(Code, Name, Budget)

Participation(Number, Code, StartDate)

**Red Bold:** Foreign Key

W

# Many-to-Many Recursive Relationsh.

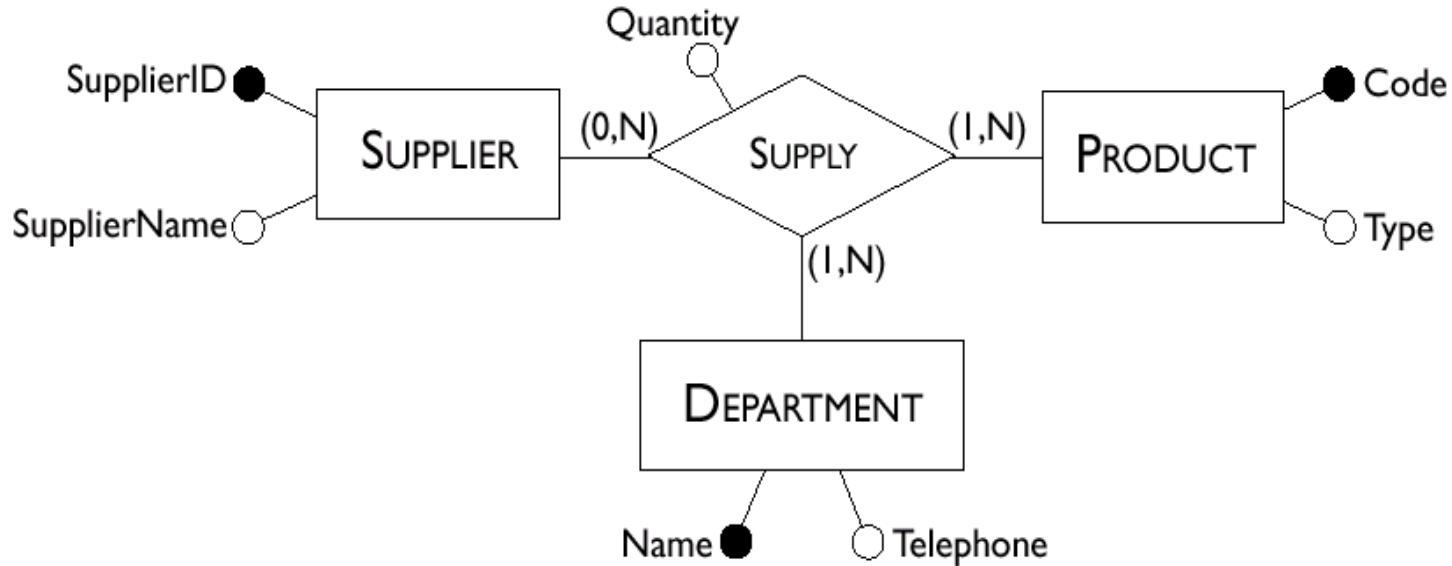


Product(Code, Name, Cost)

Composition(Part, SubPart, Quantity)

✓✓

# Ternary Relationships

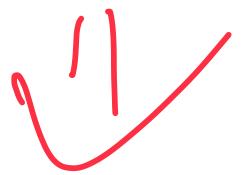


Supplier(SupplierID, SupplierName)

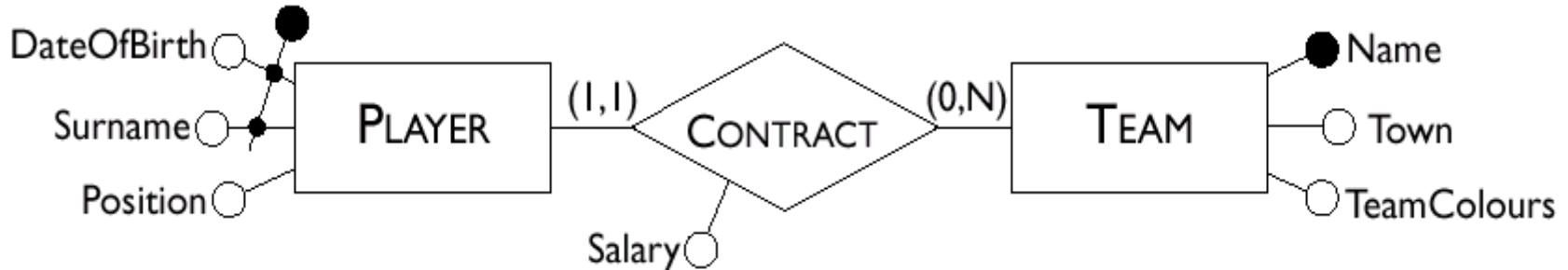
Product(Code, Type)

Department(Name, Telephone)

Supply(**SupplierID**, **Code**, **Name**, **Quantity**)



# One-to-Many Relationships



Player(Surname, DateOfBirth, Position)

Team(Name, Town, TeamColours)

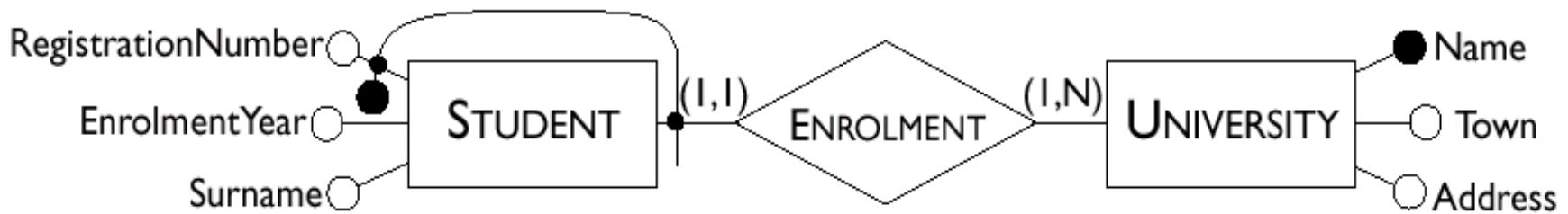
Contract(PlayerSurname, PlayerDateOfBirth, Salary, **Name**)

*OR (preferred)*

Player(Surname, DateOfBirth, Position, Salary, **Name**)

Team(Name, Town, TeamColours)

# Weak Entities



University(Name, Town, Address)

Student(RegistrationNumber, **Name**, Surname, EnrolmentYear)

# One-to-One Relationships



Head(Number, Name, Salary, StartDate, **DepartmentName**)

Department(Name, Telephone, Branch)

*Or*

Head(Number, Name, Salary)

Department(Name, Telephone, Branch, StartDate, **HeadNumber**)

✓

# Optional One-to-One Relationships



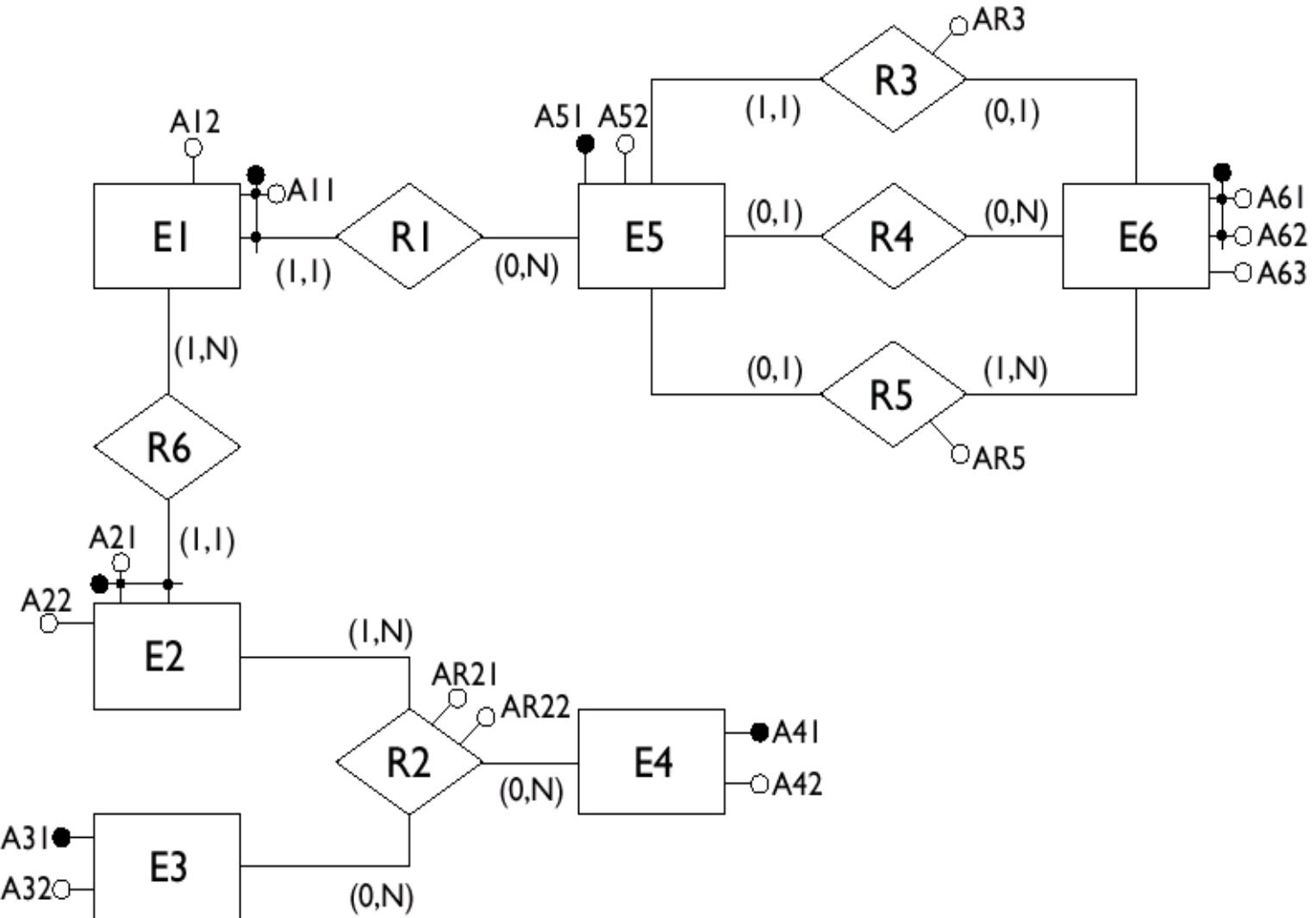
Employee(Number, Name, Salary)  
Department(Name, Telephone, Branch, StartDate, **Head**)

*Or, if both entities are optional*

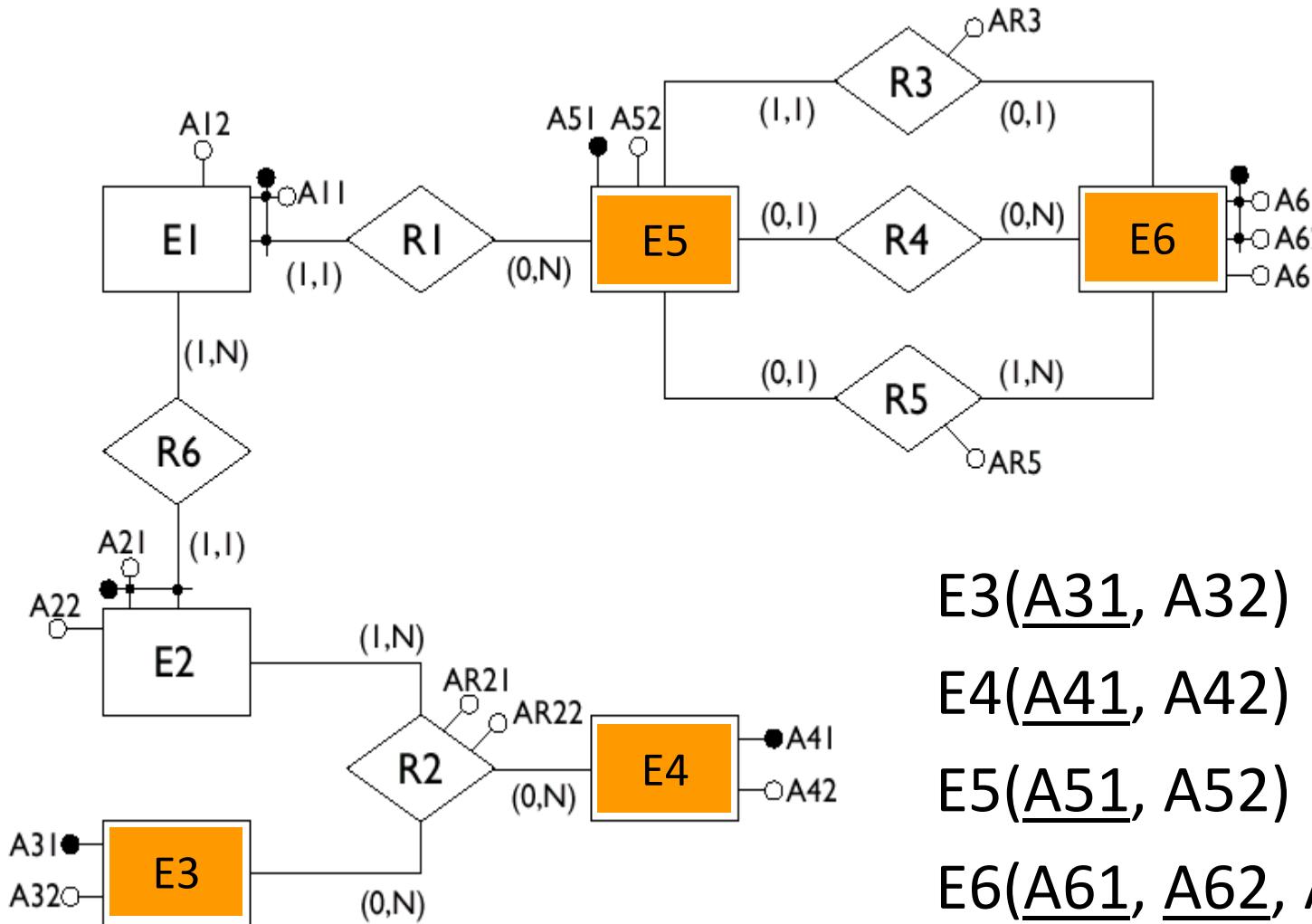
Employee(Number, Name, Salary)  
Department(Name, Telephone, Branch)  
Management(**Head**, **Department**, StartDate)

✓

# A Sample ER Schema



# Entities with Internal Identifiers



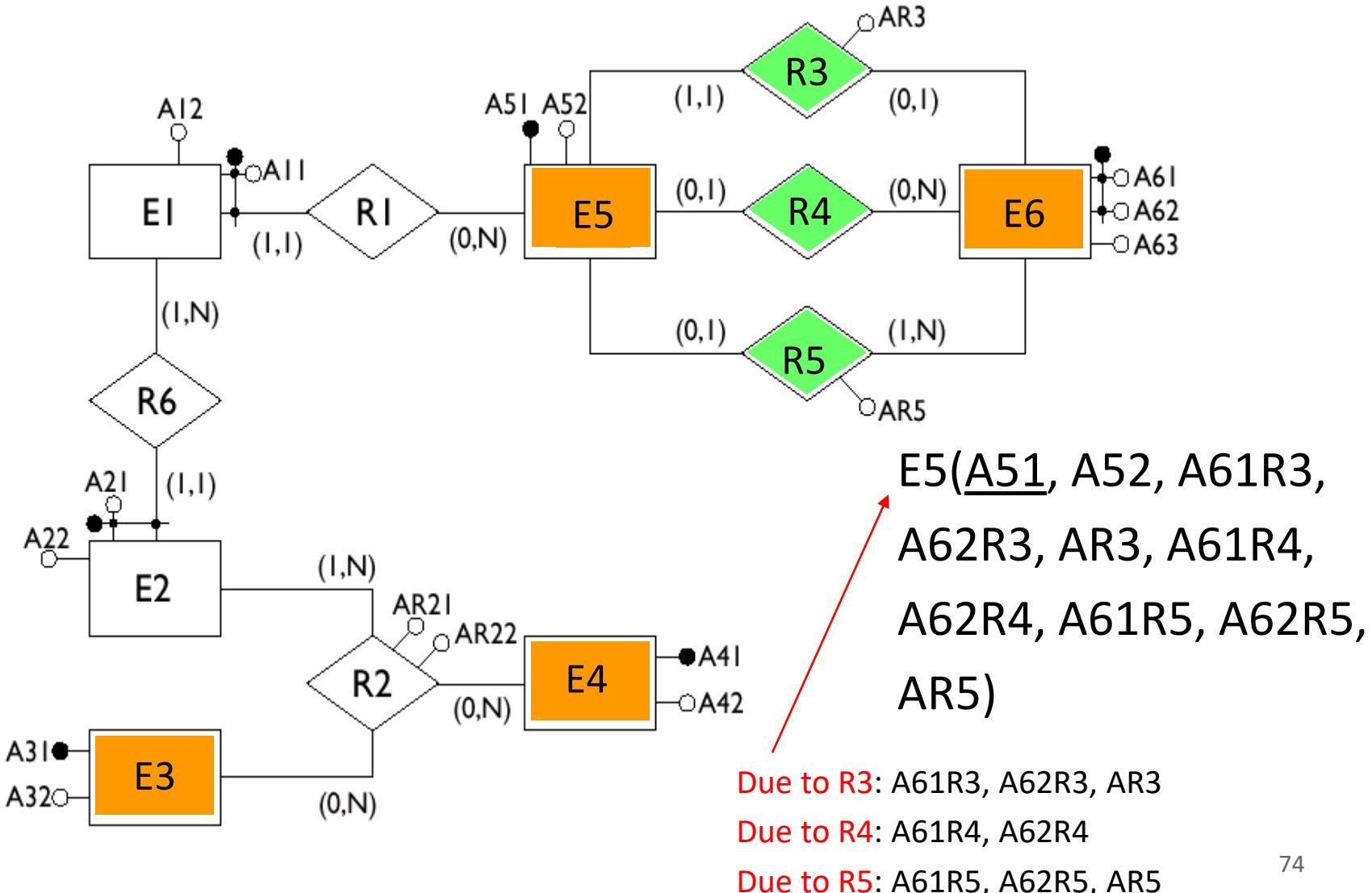
$E3(\underline{A31}, \underline{A32})$

$E4(\underline{A41}, \underline{A42})$

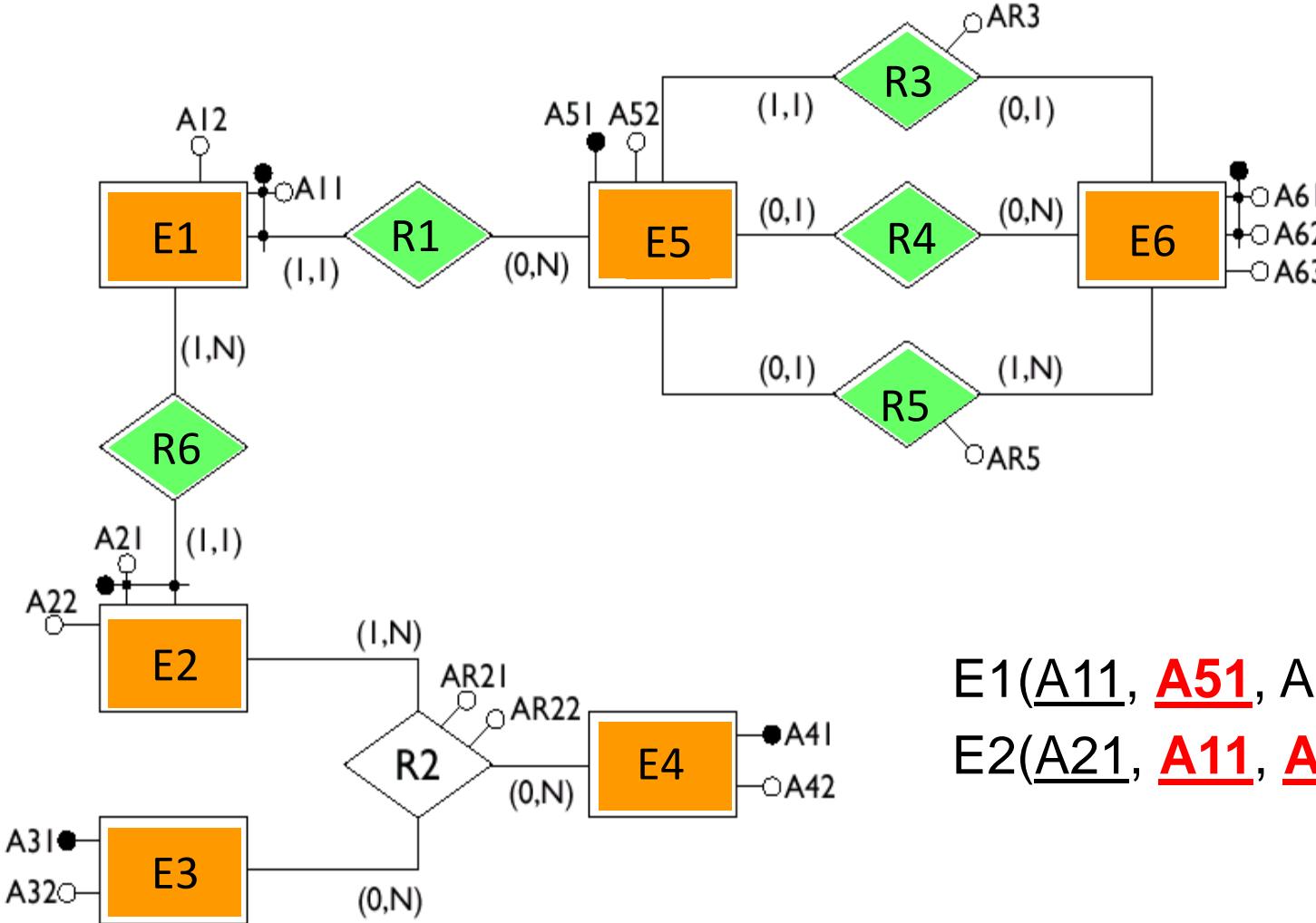
$E5(\underline{A51}, \underline{A52})$

$E6(\underline{A61}, \underline{A62}, \underline{A63})$

# 1-N, 1-1 and Opt. 1-1 Relationships

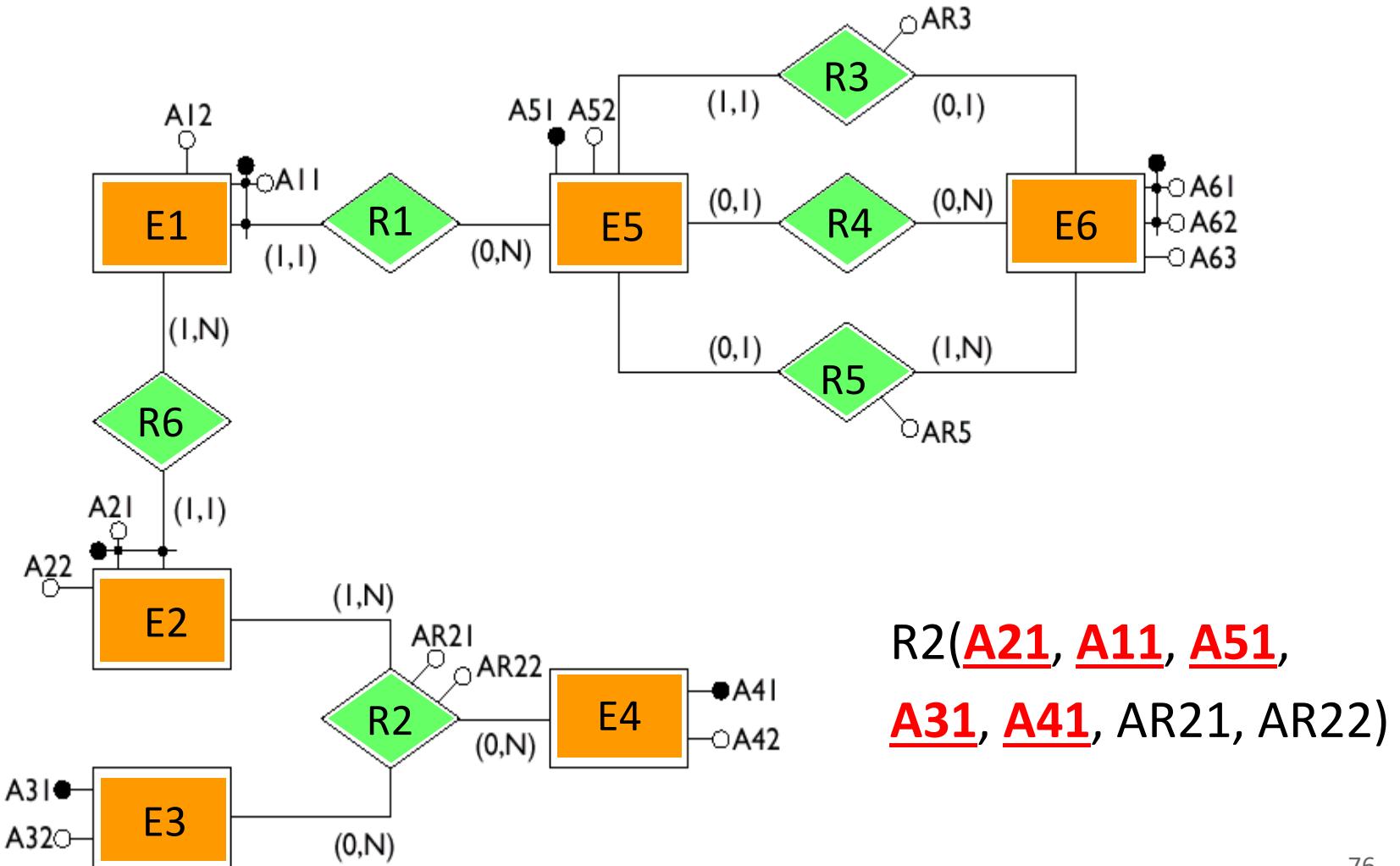


# Weak Entities



E1(A11, A51, A12)  
E2(A21, A11, A51, A22)

# Many-to-Many Relationships



# Result of the Translation

E1(A11, **A51**, A12)

E2(A21, **A11**, **A51**, A22)

E3(A31, A32)

E4(A41,A42)

E5(**A51**, A52, A61R3, A62R3, AR3, A61R4, A62R4, A61R5,  
A62R5, AR5)

E6(A61, A62, A63)

R2(**A21**, **A11**, **A51**, **A31**, **A41**, AR21, AR22)

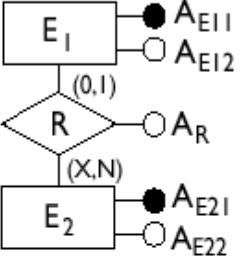
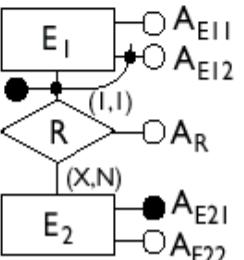
*We have a Database Schema!*

*Ready to create our tables in the DBMS!*

# Summary of Transformation Rules

| Type  | Initial schema | Possible translation   |
|---|----------------|--|
| Binary many-to-many relationship                      |                | $E_1(\underline{A_{E11}}, \underline{A_{E12}})$<br>$E_2(\underline{A_{E21}}, \underline{A_{E22}})$<br>$R(\underline{A_{E11}}, \underline{A_{E21}}, \underline{A_R})$   |
| Ternary many-to-many relationship                     |                | $E_1(\underline{A_{E11}}, \underline{A_{E12}})$<br>$E_2(\underline{A_{E21}}, \underline{A_{E22}})$<br>$E_3(\underline{A_{E31}}, \underline{A_{E32}})$<br>$R(\underline{A_{E11}}, \underline{A_{E21}}, \underline{A_{E31}}, \underline{A_R})$ |
| One-to-many relationship with mandatory participation |                | $E_1(\underline{A_{E11}}, \underline{A_{E12}}, \underline{A_{E21}}, \underline{A_R})$<br>$E_2(\underline{A_{E21}}, \underline{A_{E22}})$   |

# ...More Rules...

| Type   | Initial schema   | Possible translation   |
|--|--|--|
| One-to-many relationship with optional participation |  <p>ER diagram description: Entity E1 has attributes A_E11 (marked with a dot) and A_E12. Entity E2 has attributes A_E21 (marked with a dot) and A_E22. Relationship R connects E1 and E2. R has attributes A_R, A_E11 (marked with a dot), and A_E21 (marked with a dot). Participation constraints: E1 is optional (0..1), R is mandatory (X,N), and E2 is mandatory (X,N).</p>  | $E_1(A_{E11}, A_{E12})$<br>$E_2(\underline{A_{E21}}, A_{E22})$<br>$R(\underline{A_{E11}}, \underline{A_{E21}}, A_R)$<br>Alternatively:<br>$E_1(\underline{A_{E11}}, A_{E21}, A_{E21}^*, A_R^*)$<br>$E_2(\underline{A_{E21}}, A_{E22})$ |
| Relationship with external identifiers               |  <p>ER diagram description: Entity E1 has attributes A_E12 (marked with a dot) and A_E11. Entity E2 has attributes A_E21 (marked with a dot) and A_E22. Relationship R connects E1 and E2. R has attributes A_R, A_E12 (marked with a dot), and A_E21 (marked with a dot). Participation constraints: E1 is mandatory (1,1), R is mandatory (X,N), and E2 is mandatory (X,N).</p> | $E_1(\underline{A_{E12}}, \underline{A_{E21}}, A_{E11}, A_R)$<br>$E_2(\underline{A_{E21}}, A_{E22})$   |

\_ : Primary keys

...: Alternative primary keys

\*: NULL values are allowed

# ...Even More Rules...

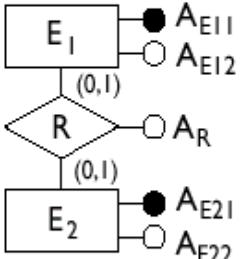
| Type   | Initial schema   | Possible translation   |
|--|--|--|
| One-to-one relationship with mandatory participation for both entities | <pre>     graph TD       E1[Entity E1] ---&gt; R((R))       E2[Entity E2] ---&gt; R       R ---&gt; A_E11[A_E11]       R ---&gt; A_E12[A_E12]       R ---&gt; A_E21[A_E21]       R ---&gt; A_E22[A_E22]       style R fill:none,stroke:none       style E1 fill:#fff,stroke:#000,stroke-width:1px       style E2 fill:#fff,stroke:#000,stroke-width:1px       style A_E11 fill:#fff,stroke:#000,stroke-width:1px       style A_E12 fill:#fff,stroke:#000,stroke-width:1px       style A_E21 fill:#fff,stroke:#000,stroke-width:1px       style A_E22 fill:#fff,stroke:#000,stroke-width:1px   </pre> | $E_1(A_{E11}, \underline{A_{E12}}, A_{E21}, A_R)$<br>$\underline{E_2(A_{E21}, A_{E22})}$<br>Alternatively:<br>$E_2(A_{E21}, \underline{A_{E22}}, A_{E11}, A_R)$<br>$\underline{E_1(A_{E11}, A_{E12})}$ |
| One-to-one relationship with optional participation for one entity     | <pre>     graph TD       E1[Entity E1] ---&gt; R((R))       E2[Entity E2] ---&gt; R       R ---&gt; A_E11[A_E11]       R ---&gt; A_E12[A_E12]       R ---&gt; A_E21[A_E21]       R ---&gt; A_E22[A_E22]       style R fill:none,stroke:none       style E1 fill:#fff,stroke:#000,stroke-width:1px       style E2 fill:#fff,stroke:#000,stroke-width:1px       style A_E11 fill:#fff,stroke:#000,stroke-width:1px       style A_E12 fill:#fff,stroke:#000,stroke-width:1px       style A_E21 fill:#fff,stroke:#000,stroke-width:1px       style A_E22 fill:#fff,stroke:#000,stroke-width:1px   </pre> | $E_1(A_{E11}, \underline{A_{E12}}, A_{E21}, A_R)$<br>$\underline{E_2(A_{E21}, A_{E22})}$   |

\_ : Primary keys

...: Alternative primary keys

\*: NULL values are allowed

# ...and the Last One...

| Type  | Initial schema   | Possible translation   |
|---|--|--|
| One-to-one relationship with optional participation for both entities |  <pre>     erDiagram         class E1 {             string A_E11;             string A_E12;         }         class E2 {             string A_E21;             string A_E22;         }         E1 }o--o{ R : o--o{ E2     </pre> | $E_1(A_{E11}, \underline{A_{E12}})$<br>$E_2(\underline{A_{E21}}, A_{E22}, A_{E11}^*, A_R^*)$<br>Alternatively:<br>$E_1(A_{E11}, A_{E12}, A_{E21}^*, A_R^*)$<br>$E_2(\underline{A_{E21}}, A_{E22})$<br>Alternatively:<br>$E_1(A_{E11}, \underline{A_{E12}})$<br>$E_2(\underline{A_{E21}}, A_{E22})$<br>$R(A_{E11}, A_{E21}, A_R)$ |

\_ : Primary keys

...: Alternative primary keys

\*: NULL values are allowed