Graph embedding and transfer learning can help predict species interaction networks despite data limitations

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Last revision: June 19, 2022

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- 1. Metawebs, i.e. networks of potential interactions within a species pool, are a powerful abstraction to understand how large-scales species interaction networks are structured.
- 2. Because metawebs are typically expressed at large spatial and taxonomic scales, assembling them is a tedious and costly process; predictive methods can help circumvent the limitations in data deficiencies, by providing 'draft' metawebs.
- 3. One way to improve the predictive ability is to maximize the information used for prediction, by using graph embeddings rather than the list of species interactions. Graph embedding is an emerging field in machine learning that holds great potential for ecological problems.
- 4. In this perspective, we outline how the challenges associated with inferring metawebs line-up with the advantages of graph embeddings; furthermore, because metawebs are inherently spatial objects, we discuss how the choice of the species pool has consequences on the reconstructed network, but also embeds hypotheses about which human-made boundaries are ecologically meaningful.

- Being able to infer *potential* interactions could be the catalyst for significant breakthroughs in our ability
- to start thinking about species interaction networks over large spatial scales (Hortal et al., 2015).
- 3 Understanding species interactions holds enormous potential to not only understand and more rapidly
- 4 learn about species interactions and metawebs, but also how changes in management of a single species
- 5 may impact non-target species. In a recent overview of the field of ecological network prediction, Strydom,
- 6 Catchen, et al. (2021) identified two challenges of interest to the prediction of interactions at large scales.
- First, there is a relative scarcity of relevant data in most places globally paradoxically, this restricts our
- 8 ability to infer interactions for locations where inference is perhaps the least required (and leaves us
- 9 unable to make inference in regions without interaction data); second, accurate predictions often demand
- accurate predictors, and the lack of methods that can leverage small amount of accurate data is a serious
- impediment to our global predictive ability. In most places, our most reliable biodiversity knowledge is
- that of a species pool (i.e. a set of potentially interacting species in a given area): through the analysis of
- databases like GBIF or IUCN, it is possible to construct a list of species in a region of interest; but inferring
- the potential interactions between these species is difficult.
- Following the definition of Dunne (2006), a metaweb is the ecological network analogue to the species
- pool; specifically, it inventories all potential interactions between species for a spatially delimited area (and
- so captures the  $\gamma$  diversity of interactions). The metaweb is not a prediction of the network at a specific
- point within the spatial area it covers: it will have a different structure, notably by having a larger
- connectance (see e.g. Wood et al., 2015) and complexity (see e.g. Galiana et al., 2022), from any of these
- local networks. These local networks (which capture the  $\alpha$  diversity of interactions) are a subset of the
- metaweb's species and their interactions, and have been called "metaweb realizations" (Poisot et al., 2015).
- 22 Differences between local networks and their metawebs are due to chance, species abundance and
- 23 co-occurrence, local environmental conditions, and local distribution of functional traits, among others.
- 24 Yet, recent results by Saravia et al. (2021) strongly suggest that the local realizations only respond weakly
- 25 to local conditions: instead, they reflect constraints inherited by the structure of their metaweb. This
- establishes the metaweb structure as the core goal of predictive network ecology, as it is a required
- 27 information to accurately produce downscaled, local predictions.
- 28 Because the metaweb represents the joint effect of functional, phylogenetic, and macroecological
- 29 processes (Morales-Castilla et al., 2015), it holds valuable ecological information. Specifically, it is the
- 30 "upper bounds" on what the composition of the local networks, given the local species pool, can be (see

- e.g. McLeod et al., 2021); this information can help evaluate the ability of ecological assemblages to
  withstand the effects of, for example, climate change (Fricke et al., 2022). These local networks may be
- reconstructed given an appropriate knowledge of local species composition and provide information on
- the structure of food webs at finer spatial scales. This has been done for example for tree-galler-parasitoid
- systems (Gravel et al., 2018), fish trophic interactions (Albouy et al., 2019), tetrapod trophic interactions
- 36 (Braga et al., 2019; O'Connor et al., 2020), and crop-pest networks (Grünig et al., 2020). In this
- contribution, we highlight the power in viewing (and constructing) metawebs as *probabilistic* objects in
- the context of rare interactions, discuss how a family of machine learning tools (graph embeddings and
- transfer learning) can be used to overcome data limitations to metaweb inference, and highlight how the
- use of metawebs introduces important questions for the field of network ecology.

# The metaweb is an inherently probabilistic object

- Treating interactions as probabilistic (as opposed to binary) events is a more nuanced and realistic way to
- represent them. Dallas et al. (2017) suggested that most links in ecological networks are cryptic, i.e.
- 44 uncommon or hard to observe. This argument echoes Jordano (2016): sampling ecological interactions is
- difficult because it requires first the joint observation of two species, and then the observation of their
- interaction. In addition, it is generally expected that weak or rare links to be more prevalent in networks
- than common or rare links (Csermely, 2004), compared to strong, persistent links; this is notably the case
- in food chains, wherein many weaker links are key to the stability of a system (Neutel et al., 2002). In the
- light of these observations, we expect to see an over-representation of low-probability interactions under a
- 50 model that accurately predicts interaction probabilities. Yet the original metaweb definition, and indeed
- most past uses of metawebs, was based on the presence/absence of interactions. Moving towards
- probabilistic metawebs, by representing interactions as Bernoulli events (see e.g. Poisot et al., 2016), offers
- 53 the opportunity to weigh these rare interactions appropriately. The inherent plasticity of interactions is
- 54 important to capture: there have been documented instances of food webs undergoing rapid
- collapse/recovery cycles over short periods of time (e.g. Pedersen et al., 2017). These considerations
- emphasize why metaweb predictions should focus on quantitative (preferentially probabilistic)
- predictions; this should constrain the suite of appropriate models.
- Yet it is important to recall that a metaweb is intended as a catalogue of all potential interactions, which is

then filtered (Morales-Castilla et al., 2015). In a sense, that most ecological interactions are elusive can call
for a slightly different approach to sampling: once the common interactions are documented, the effort
required in documenting each rare interaction will increase exponentially. Recent proposals suggest that
machine learning algorithms, in these situations, can act as data generators (Hoffmann et al., 2019): high
quality observational data can generate the core rules underpinning the network structure, and be
supplemented with synthetic data coming from predictive models, increasing the volume of information
available for inference. Indeed, Strydom, Catchen, et al. (2021) suggested that knowing the metaweb may
render the prediction of local networks easier, because it fixes an "upper bound" on which interactions
can exist. In this context a probabilistic metaweb represents an aggregation of informative priors on the
interactions, elusive information with the potential to boost our predictive ability (Bartomeus et al., 2016).

[Figure 1 about here.]

# 70 Graph embedding offers promises for the inference of potential

## interactions

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- Graph embedding (fig. 1) is a varied family of machine learning techniques aiming to transform nodes and edges into a vector space (Arsov & Mirceva, 2019), usually of a lower dimension, whilst maximally 73 retaining key properties of the graph (Yan et al., 2005). Ecological networks are an interesting candidate for the widespread application of embeddings, as they tend to possess a shared structural backbone (Bramon Mora et al., 2018), which hints at structural invariants that can be revealed at lower dimensions. 76 Indeed, food webs are inherently low-dimensional objects, and can be adequately represented with less 77 than ten dimensions (Braga et al., 2019; Eklöf et al., 2013). Simulation results by Botella et al. (2022) 78 suggest that there is no best method to identify architectural similarities between networks, and that multiple approaches need to be tested and compared to the network descriptor of interest. This matches 80 previous, more general results on graph embedding, which suggest that the choice of embedding algorithm matters for the results (Goyal & Ferrara, 2018). In tbl. 1, we present a selection of common graph embedding methods, alongside examples of their use to predict species interactions; most of these methods rely either on linear algebra, or on pseudo-random walks on graphs.
- One prominent family of approaches we do not discuss in the present manuscript is Graph Neural

Networks (GNN; Zhou et al., 2020); GNN are, in a sense, a method to embed a graph into a dense subspace, but belong to the family of deep learning methods, which has its own set of practices (see e.g. 87 Goodfellow et al., 2016). An important issue with methods based on deep learning is that because their 88 parameter space is immense, the sample size of the data fed into them must be similarly large (typically thousands of instances). This is a requirement for the model to converge correctly during training, but this 90 assumption is unlikely to be met given the size of datasets about currently available metawebs (or single 91 time/location species interaction networks). This data volume requirement is mostly absent from the 92 techniques we list below. Furthermore, GNN still have some challenges related to their shallow structure, and concerns related to scalability (see Gupta et al., 2021 for a review), which are mostly absent from the methods listed in tbl. 1. Assuming that the uptake of next-generation biomonitoring techniques does indeed deliver larger datasets on species interactions (Bohan et al., 2017), there is a potential for GNN to become an applicable embedding/predictive technique in the coming years.

#### [Table 1 about here.]

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The popularity of graph embedding techniques in machine learning is more than the search for structural invariants: graphs are discrete objects, and machine learning techniques tend to handle continuous data 100 better. Bringing a sparse graph into a continuous, dense vector space (Xu, 2020) opens up a broader variety 101 of predictive algorithms, notably of the sort that are able to predict events as probabilities (Murphy, 2022). 102 Furthermore, the projection of the graph itself is a representation that can be learned; Runghen et al. 103 (2021), for example, used a neural network to learn the embedding of a network in which not all 104 interactions were known, based on nodes metadata. This example has many parallels in ecology (see fig. 1 105 C), in which node metadata can be given by phylogeny or functional traits. Rather than directly predicting 106 biological rules (see e.g. Pichler et al., 2020 for an overview), which may be confounded by the sparse nature of graph data, learning embeddings works in the low-dimensional space that maximizes 108 information about the network structure. This approach is further justified by the observation, for 109 example, that the macro-evolutionary history of a network is adequately represented by some graph embeddings (RDPG; see Dalla Riva & Stouffer, 2016). In a recent publication, Strydom et al. (2022) have 111 used an embedding (based on RDPG) to project a metaweb of trophic interactions between European 112 mammals, and transfered this information to mammals of Canada by using the phylogenetic distance 113 between related clades to infer the values in the latent sub-space into which the metaweb was projected.

By performing the RDPG step on re-constructed value, this approach yields a probabilistic trophic metaweb for mammals of Canada based on knowledge of European species, despite a limited ( $\approx 5\%$ ) 116 taxonomic overlap. 117 Graph embeddings can serve as a dimensionality reduction method. For example, RDPG (Strydom et al., 2022) and t-SVD (Poisot et al., 2021) typically embed networks using fewer dimensions than the original 119 network (the original network has as many dimensions as species, and as many informative dimensions as 120 trophically unique species; Strydom, Dalla Riva, et al., 2021). But this is not necessarilly the case - indeed, one may perform a PCA (a special case of SVD) to project the raw data into a subspace that improves the 122 efficacy of t-SNE (Maaten, 2009). There are many dimensionality reductions (Anowar et al., 2021) that can 123 be applied to an embedded network should the need for dimensionality reduction (for example for data visualisation) arise. In brief, many graph embeddings can serve as dimensionality reduction steps, but not 125 all do, neither do all dimensionality reduction methods provide adequate graph embedding capacities. In 126 the next section (and fig. 2), we show how the amount of dimensionality reduction can affect the quality of 127 the embedding. 128

## 29 An illustration of metaweb embedding

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In this section, we illustrate the embedding of a collection of bipartite networks collected by Hadfield et al. (2014), using truncated Singular Value Decomposition (t-SVD) and RDPG (see Strydom et al., 2022 for the 131 full details). Briefly, an RDPG decomposes a network into two subspaces (left and right), which are 132 matrices that when multiplied give an approximation of the original network. The code to reproduce this example is available as supplementary material (note, for the sake of comparison, that Strydom, Catchen, 134 et al., 2021 have an example using embedding through PCA followed by prediction using a deep neural 135 network on the same dataset). The resulting (binary) metaweb  $\mathcal{M}$  has 2131 interactions between 206 136 parasites and 121 hosts, and its adjacency matrix has full rank (i.e. it represents a space with 121 137 dimensions). All analyses were done using Julia (Bezanson et al., 2017) version 1.7.2, Makie.jl (Danisch & 138 Krumbiegel, 2021), and EcologicalNetworks.jl (Poisot et al., 2019). 139

[Figure 2 about here.]

The embedding of the metaweb holds several pieces of information (fig. 2). In panel A, we show that the

 $L_2$  loss (i.e. the sum of squared errors) between the empirical and reconstructed metaweb decreases when number of dimensions (rank) of the subspace increases, with a point of inflection around 25 dimensions. As discussed by Runghen et al. (2021), there is often a trade-off between the number of dimensions to use (more dimensions are more computationally demanding) and the quality of the representation. In this instance, accepting  $L_2 = 500$  as an approximation of the network means that the error for every position in 146 the metaweb is  $\approx (500/(206 \times 121))^{1/2}$ . In **B**, we show the positions of hosts and parasites on the first two 147 dimensions of the left and right subspaces. Note that these values largely skew negative, because the first 148 dimensions capture the coarse structure of the network: most pairs of species do not interact, and therefore have negative values. In C, we show the predicted weight (i.e. the result of the multiplication of 150 the RDGP subspaces at a rank of 25) as a function of whether the interactions are observed, not-observed, 151 or unknown due to lack of co-occurence. This reveals that the obserbed interactions have higher predicted weights, although there is some overlap; the usual approach to identify possible interactions based on this 153 information would be a thresholding analysis, which is outside the scope of this manuscript (and is done 154 in the papers cited in this illustration). Note that the values are not bound to the unit interval, which emphasizes the need for either scaling or clamping (although thresholding analyses are insensitive to this 156 choice). Finally, in **D**, we show that the embedding, as it captures structural information about the 157 network, holds ecological information; indeed, the position of the parasite on the first dimension of the left sub-space is a linear predictor of its number of hosts.

# The metaweb embeds both ecological hypotheses and practices

The goal of metaweb inference is to provide information about the interactions between species at a large spatial scale. But as Herbert (1965) rightfully pointed out, "[y]ou can't draw neat lines around planet-wide problems"; any inference of a metaweb at large scales must contend with several novel, and interwoven, families of problems. In this section, we list some of the most pressing research priorities (*i.e.* problems that can be adressed with subsequent data analysis or simulations), as well as issues related to the application of these methods at the science-policy interface.

The first open research problem is the taxonomic and spatial limit of the metaweb to embed and transfer.

168 If the initial metaweb is too narrow in scope, notably from a taxonomic point of view, the chances of

finding another area with enough related species (through phylogenetic relatedness or similarity of

functional traits) to make a reliable inference decreases; this would likely be indicated by large confidence intervals during estimation of the values in the low-rank space, meaning that the representation of the 171 original graph is difficult to transfer to the new problem. In addition, other problems can arise due to 172 non-overlapping trait distributions in the known and unknown species. Alternatively a metaweb is too large (taxonomically), then the resulting embeddings would need to represent interactions between 174 taxonomic groups that are not present in the new location. This would lead to a much higher variance in 175 the starting dataset, and to under-dispersal in the target dataset, resulting in the potential under or over 176 estimation of the strength of new predicted interactions. The lack of well documented metawebs is 177 currently preventing the development of more concrete guidelines. The question of phylogenetic 178 relatedness and dispersal is notably true if the metaweb is assembled in an area with mostly endemic 179 species (e.g. a system that has undergone recent radiation and might not have an analogous system with 180 which to draw knowledge from), and as with every predictive algorithm, there is room for the application 181 of our best ecological judgement. Because this problem relates to dispersal of species in the geographic or 182 phylogenetic space, it can certainly be approached through assessing the performance of embedding transfer in simulated starting/target species pools. 184 The second series of problems relate to determining which area should be used to infer the new metaweb 185 in, as this determines the species pool that must be used. Metawebs can be constructed by assigning 186 interactions in a list of species within geographic boundaries. The upside of this approach is that 187 information at the country level is likely to be required for biodiversity assessments, as countries set goals 188 at the national level (Buxton et al., 2021), and as quantitative instruments are designed to work at these scales (Turak et al., 2017); specific strategies are often enacted at smaller scales, nested within a specific 190 country (Ray et al., 2021). But there is no guarantee that these boundaries are meaningful. In fact, we do 191 not have a satisfying answer to the question of "where does a food web stop?"; the most promising solutions involve examining the spatial consistency of network area relationships (Fortin et al., 2021; see 193 e.g. Galiana et al., 2018, 2019, 2021), which is impossible in the absence of enough information about the 194 network itself. This suggests that inferred metawebs should be further downscaled to allow for a posteriori 195 analyses. The methodology for metaweb downscaling is currently limited, and it is likely that the 196 sustained effort to characterize the spatial dependency of food web structure will lead to more prescriptive 197 guidelines about the need for prediction downscaling. 198

The final family of problems relates less to ecological methods than to the praxis of ecological research.

Operating under the context of national divisions, in large parts of the world, reflects nothing more than the legacy of settler colonialism, which drives a disparity in available ecological data. Applying any 201 embedding to biased data does not debias them, but instead embeds these very same biases, propagating 202 them to the machine learning models using embeddings tomake predictions. Indeed, the use of ecological data is not an apolitical act (Nost & Goldstein, 2021), as data infrastructures tend to be designed to answer 204 questions within national boundaries (therefore placing contingencies on what is available to be 205 embedded), and their use often draws upon and reinforces territorial statecraft. As per Machen & Nost 206 (2021), this is particularly true when the output of "algorithmic thinking" (e.g. relying on machine 207 learning to generate knowledge) can be re-used for governance (e.g. enacting conservation decisions at the 208 national scale). As information on species interaction networks structure is increasingly leveraged as a 209 tool to guide conservation actions (see e.g. recent discussions for food-web based conservation; Eero et al., 2021; Naman et al., 2022; Stier et al., 2017), the need to appraise and correct biases that are unwittingly 211 propagated to algorithms when embedded from the original data is paramount. Predictive approaches 212 deployed at the continental scale, no matter their intent, originate in the framework that contributed to the ongoing biodiversity crisis (Adam, 2014) and reinforced environmental injustice (Choudry, 2013; 214 Domínguez & Luoma, 2020). Particularly on Turtle Island and other territories that were traditionally 215 stewarded by Indigenous people, these approaches should be replaced (or at least guided and framed) by Indigenous principles of land management (Eichhorn et al., 2019; No'kmaq et al., 2021), as part of an 217 "algorithm-in-the-loop" approach. Human-algorithm interactions are notoriously difficult and can yield 218 adverse effect (Green & Chen, 2019; Stevenson & Doleac, 2021), suggesting the need to systematically 219 study them for the specific purpose of biodiversity governance, as well as to improve the algorithmic 220 literacy of decision makers. As we see artificial intelligence/machine learning being increasingly 221 mobilized to generate knowledge that is lacking for conservation decisions (e.g. Lamba et al., 2019; 222 Mosebo Fernandes et al., 2020) and drive policy decisions (Weiskopf et al., 2022), our discussion of these tools need to go beyond the technical and statistical, and into the governance consequences they can have. 224 Acknowledgements: We acknowledge that this study was conducted on land within the traditional 225 unceded territory of the Saint Lawrence Iroquoian, Anishinabewaki, Mohawk, Huron-Wendat, and 226 Omàmiwininiwak nations. TP, TS, DC, and LP received funding from the Canadian Institute for Ecology 227 & Evolution. FB is funded by the Institute for Data Valorization (IVADO). TS, SB, and TP are funded by a 228 donation from the Courtois Foundation. CB was awarded a Mitacs Elevate Fellowship no. IT12391, in

- partnership with fRI Research, and also acknowledges funding from Alberta Innovates and the Forest
- 231 Resources Improvement Association of Alberta. M-JF acknowledges funding from NSERC Discovery
- 232 Grant and NSERC CRC. RR is funded by New Zealand's Biological Heritage Ngā Koiora Tuku Iho
- National Science Challenge, administered by New Zealand Ministry of Business, Innovation, and
- Employment. BM is funded by the NSERC Alexander Graham Bell Canada Graduate Scholarship and the
- FRQNT master's scholarship. LP acknowledges funding from NSERC Discovery Grant (NSERC
- 236 RGPIN-2019-05771). TP acknowledges financial support from the Fondation Courtois, and NSERC
- through the Discovery Grants and Discovery Accelerator Supplement programs. MJF is supported by an
- 238 NSERC PDF and an RBC Post-Doctoral Fellowship.
- 239 **Conflict of interest:** The authors have no conflict interests to disclose
- 240 **Authors' contributions:** TS, and TP conceived the ideas discussed in the manuscript. All authors
- contributed to writing and editing the manuscript.
- Data availability: There is no data associated with this manuscript.

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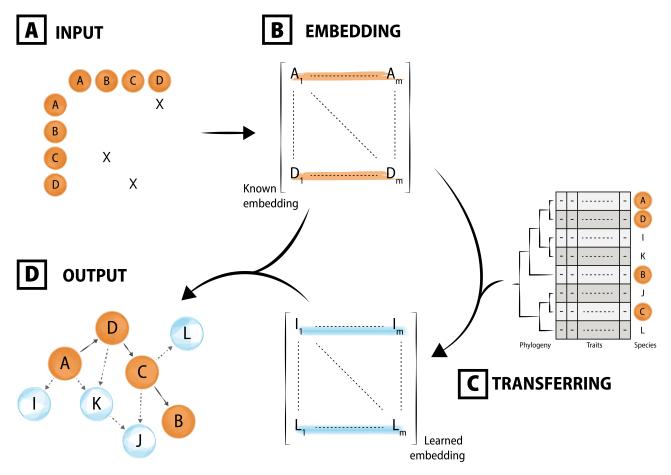


Figure 1: Overview of the embedding process. A network (A), represented here as its adjacency matrix, is converted into a lower-dimensional object (B) where nodes, subgraphs, or edges have specific values (see tbl. 1 for an overview of methods and their use for species interactions). For the purposes of prediction, this low-dimensional object encodes feature vectors for e.g. the nodes. Embedding also allows to visualize the structure in the data differently (see fig. 2), much like with a principal component analysis. From a low-dimensional feature vector, it is possible to develop predictive approaches. Nodes in an ecological network are usually species ( $\mathbf{C}$ ), for which we can leverage phylogenetic relatedness (e.g. Strydom et al., 2022) or functional traits to fill the values of additional species we would like to project in this space (here for nodes I, J, K, and L) from the embedding of known species (here, nodes A, B, C, and D). Because embeddings can be projected back to a graph, this allows us to reconstruct a network with these new species ( $\mathbf{D}$ ). This entire cycle constitutes an instance of transfer learning, where the transfered information is the representation of graph  $\mathbf{A}$  through its embedding.

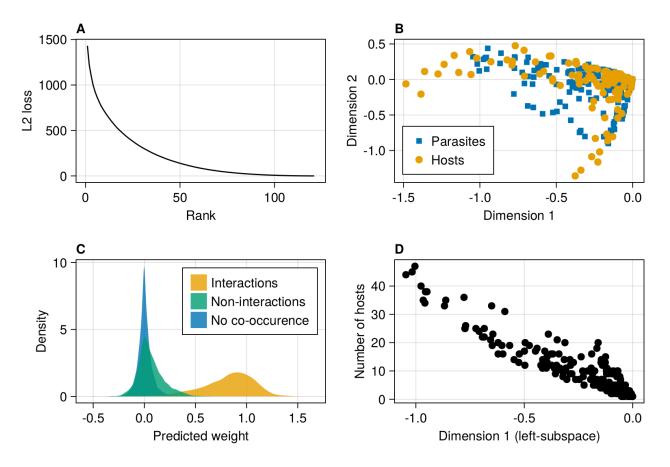


Figure 2: Illustration of an embedding for an host-parasite metaweb, using Random Dot Product Graphs. **A**, decrease in approximation error as the number of dimensions in the subspaces increases. **B**, position of hosts and parasites in the first two dimensions of their respective subspaces. **C**, predicted interaction weight from the RDPG based on the status of the species pair in the metaweb. **D**, relationship between the position on the first dimension and parasite generalism.

Table 1: Overview of some common graph embedding approaches, by time of publication, alongside examples of their use in the prediction of species interactions. These methods have not yet been routinely used to predict species interactions; most examples that we identified were either statistical associations, or analogues to joint species distribution models. <sup>a</sup>: statistical interactions; <sup>b</sup>: joint-SDM-like approach.

			Application in species
Method	Embedding approach	Reference	interactions
tSNE	nodes through statistical	Hinton &	Cieslak et al. (2020) <sup>a</sup>
	divergence	Roweis (2002)	
RDPG	graph through SVD	Young &	Poisot et al. (2021); Dalla Riva &
		Scheinerman	Stouffer (2016)
		(2007)	
DeepWalk	graph walk	Perozzi et al.	Wardeh et al. (2021)
		(2014)	
FastEmbed	graph through PCA/SVD	Ramasamy &	
	analogue	Madhow (2015)	
LINE	nodes through statistical	Tang et al.	
	divergence	(2015)	
SDNE	nodes through auto-encoding	D. Wang et al.	
		(2016)	
node2vec	nodes embedding	Grover &	
		Leskovec (2016)	
graph2vec	sub-graph embedding	Narayanan et al.	
		(2017)	
DMSE	joint nodes embedding	D. Chen et al.	D. Chen et al. (2017) <i>b</i>
		(2017)	
HARP	nodes through a meta-strategy	H. Chen et al.	
		(2017)	
GraphKKE	graph embedding	Melnyk et al.	Melnyk et al. $(2020)^a$
		(2020)	
Joint	multiple graphs	S. Wang et al.	
methods		(2021)	