Guidelines for the validation of machine learning predictions of species interactions

Timothée Poisot 1,2

¹ Université de Montréal ² Québec Centre for Biodiversity Sciences

Correspondance to:

 $Timoth\'{e}e \ Poisot - \ timothee.poisot@umontreal.ca$

This work is released by its authors under a CC-BY 4.0 license

Last revision: February 25, 2022

- 1. The prediction of species interactions is gaining momentum as a way to circumvent limitations in data volume. Yet, ecological networks are challenging to predict because they are typically small and sparse. Dealing with extreme class imbalance is a challenge for most binary classifiers, and there are currently no guidelines as to how predictive models can be trained for this specific problem.
- 2. Using simple mathematical arguments and numerical experiments in which a variety of classifiers (for supervised learning) are trained on simulated networks, we develop a series of guidelines related to the choice of measures to use for model selection, and the degree of unbiasing to apply to the training dataset.
- 3. Neither classifier accuracy nor the ROC-AUC are informative measures for the performance of interaction prediction. PR-AUC is a fairer assessment of performance. In some cases, even standard measures can lead to selecting a more biased classifier because the effect of connectance is strong. The amount of correction to apply to the training dataset depends on network connectance, on the measure to be optimized, and only weakly on the classifier.
- 4. These results reveal that training machines to predict networks is a challenging task, and that in virtually all cases, the composition of the training set needs to be experimented on before performing the actual training. We discuss these consequences in the context of the low volume of data.

- The accuracy paradox is the basis of a number of problems in statistical education, and lies in the fact that,
- when the desired class is rare, a model that gets less and less performant will become more and more
- accurate and useful, simply by (i) underpredicting true positive cases and (ii) over-predicting false
- 4 negatives. In other words, accuracy, defined as the proportion of predictions that are correct, is often
- 5 useless as a measure of how predictive a model is. This is particularly true in ecological networks; the
- 6 desired class (presence of an interaction between two species) is the one we care most about, and by far the
- ⁷ least commmon. Herein lies the core challenge of predicting species interactions: the extreme imbalance
- 8 between classes makes the training of predictive models difficult, and their validation even more so as we
- 9 do not reliably know which negatives are true. The connectance of empirical networks is usually well
- under 20%, with larger networks having a lower connectance (MacDonald et al., 2020). Recent
- contributions (Becker et al., 2021; Strydom et al., 2021) highlight that predictive models of interactions can
- likely be improved by adding information (in the form of, e.g. traits), but that we do not have robust
- guidelines as to how the predictive ability of these models should be evaluated, nor about how the models
- should be trained. Here, by relying on simple derivations and a series of simulations, we formulate a
- number of such guidelines, specifically for the case of binary classifiers derived from thresholded values.
- ¹⁶ Binary classifiers are usually assessed by measuring properties of their confusion matrix, *i.e.* the
- 17 contingency table reporting true/false positive/negative hits. A confusion matrix is laid out as

$$\begin{pmatrix} tp & fp \\ fn & tn \end{pmatrix}$$

- wherein tp is the number of interactions predicted as positive, tn is the number of non-interactions
- predicted as negative, fp is the number of non-interactions predicted as positive, and fn is the number of
- 20 interactions predicted as negative. Almost all measures based on the confusion matrix express rates of
- error or success as proportions, and therefore the values of these components matter in a *relative* way. At a
- 22 coarse scale, a classifier is accurate when the trace of the matrix divided by the sum of the matrix is close
- to 1, with other measures focusing on different ways in which the classifer is wrong.
- There is an immense diversity of measures to evaluate the performance of classification tasks (Ferri et al.,
- 25 2009). Here we will focus on five of them with high relevance for imbalanced learning (He & Ma, 2013);
- three threshold metrics (κ , informedness, and MMC, the Matthews Correlation Coefficient), and two

- 27 ranking metrics (the areas under the Receiving Operator Characteristic and the Precision-Recall curves;
- resp. ROC-ACU and PR-AUC). The κ measure of agreement (Landis & Koch, 1977) establishes the extent
- to which two observers (here the data and the prediction) agree, and is measured as

$$2\frac{tp\times tn-fn\times fp}{(tp+fp)\times (fp+tn)+(tn+fp)\times (tn+fn)}\,.$$

- Informedness (Youden, 1950) (also known as bookmaker informedness or the True Skill Statistic) is
- TPR + TNR 1, where TPR = tp/(tp + fn) and TNR = tn/(tn + fp); informedness can be used to find
- the optimal cutpoint in thresholding analyses (Schisterman et al., 2005). The MCC is defined as

$$\frac{tp\times tn-fn\times fp}{\sqrt{(tp+fp)\times (tp+fn)\times (tn+fp)\times (tn+fn)}}\,.$$

- Finally, F_1 is the harmonic mean of precision (the chance that a positive even was correctly classified) and
- sensitivity (the ability to correctly classify positive events), and is defined as

$$2\frac{tp}{2\times tp + fp + fn}.$$

- A lot of binary classifiers are built by using a regressor (whose task is to guess the value of the interaction,
- and can therefore return a value considered to be a pseudo-probability); in this case, the optimal value
- below which predictions are assumed to be negative (i.e. the interaction does not exist) can be determined
- by picking a threshold maximizing some value on the ROC curve or the PR curve. The area under these
- 39 curves (ROC-AUC and PR-AUC henceforth) give ideas on the overall goodness of the classifier. Saito &
- 40 Rehmsmeier (2015) established that the ROC-AUC is biased towards over-estimating performance for
- 41 imbalanced data; on the contrary, the PR-AUC is able to identify classifiers that are less able to detect
- 42 positive interactions correctly, with the additional advantage of having a baseline value equal to
- 43 prevalence. Therefore, it is important to assess whether these two measures return different results when
- 44 applied to ecological network prediction. The ROC curve is defined by the false positive rate on the x axis,
- and the true positive rate on the y axis, and the PR curve is defined by the true positive rate on the x axis,
- and the positive predictive value on the y axis. By comparison with the previous paragraph, it is obvious
- that F_1 has ties to the PR curve (being close to the expected PR-AUC), and that informedness has ties to
- the ROC curve (whereby the threshold maximizing informedness is also the point of maximal inflection

- on the ROC curve). One important difference between ROC and PR is that the later does not prominently
- account for the size of the true negative compartments: in short, it is more sensitive to the correct positive
- predictions. In a context of strong imbalance, PR-AUC is therefore a more stringent test of model
- 52 performance.
- The same approach is used to evaluate e.g. species distribution models (SDMs). Indeed, the training and
- evaluation of SDMs as binary classifiers suffers from the same issue of low prevalence; this is not
- 55 surprising that the two fields (SDMs and network predictions) would share methods and their attached
- conceptual issues, as they suffer from data limitations, class imbalance, and the conversion of quantitative
- prediction into a binary classification. In previous work, Allouche et al. (2006) suggested that κ was a
- better test of model performance than the True Skill Statistic (TSS; which we refer to as Youden's
- informedness); these conclusions were later criticized by Somodi et al. (2017), who emphasized that
- 60 informedness' relationship to prevalence depends on assumptions about bias in the model, and therefore
- recommend the use of κ as a validation of classification performance. Although this work offers
- recommendations about the comparison of models, it doesn't establishes baselines or good practices for
- training on imbalanced ecological data. Within the context of networks, there are three specific issues that
- need to be adressed. First, what values of performance measures are we expecting for a classifier that has
- 65 poor performance? This is particularly important as it can evaluate whether low prevalence can lull us
- into a false sense of predictive accuracy. Second, independently of the question of model evaluation, is low
- 67 prevalence an issue for training, and can we remedy it? Finally, because the low amount of data on
- interaction makes a lot of imbalance correction methods (see e.g. Branco et al., 2015) hard to apply, which
- 69 indicators can be optimized with the least amount of positive interaction data?
- 70 In addition to the literature on SDMs, most of the research on machine learning application to life
- 71 sciences is focused on genomics (which has very specific challenges, see a recent discussion by Whalen et
- ⁷² al., 2021); this sub-field has generated largely different recommendations. Chicco & Jurman (2020)
- suggest using Matthews correlation coefficient (MCC) over F_1 , as a protection against over-inflation of
- predicted results; Delgado & Tibau (2019) advocate against the use of Cohen's κ , again in favor of MCC, as
- the relative nature of κ means that a worse classifier can be picked over a better one; similarly, Boughorbel
- et al. (2017) recommend MCC over other measures of performance for imbalanced data, as it has more
- desirable statistical properties. More recently, Chicco et al. (2021) temper the apparent supremacy of the
- MCC, by suggesting it should be replaced by Youden's informedness (also known as J, bookmaker's

- 79 accuracy, and the True-Skill Statistic) when the imbalance in the dataset may not be representative
- 80 (Jordano, 2016a, which is the case as networks are under-sampled; 2016b), when classifiers need to be
- compared across different datasets (for example when predicting a system in space, where undersampling
- varies locally; McLeod et al., 2021), and when comparing the results to a no-skill (baseline) classifier is
- important. As these conditions are likely to be met with network data, there is a need to evaluate which
- measures of classification accuracy respond in a desirable way.
- We establish that due to the low prevalence of interactions, even poor classifiers applied to food web data
- will reach a high accuracy; this is because the measure is dominated by the accidentally correct
- predictions of negatives. On simulated confusion matrices with ranges of imbalance that are credible for
- ecological networks, MCC had the most desirable behavior, and informedness is a linear measure of
- classifier skill. By performing simulations with four models and an ensemble, we show that informedness
- and ROC-AUC are consistently high on network data, and that MCC and PR-AUC are more accurate
- measures of the effective performance of the classifier. Finally, by measuring the structure of predicted
- networks, we highlight an interesting paradox: the models with the best performance measures are not
- ₉₃ the models with the closest reconstructed network structure. We discuss these results in the context of
- establishing guidelines for the prediction of ecological interactions.

95 Baseline values

- In this section, we will assume a network of connectance ρ , i.e. having ρS^2 interactions (where S is the
- species richness), and $(1 \rho)S^2$ non-interactions. Therefore, the vector describing the *true* state of the
- network (assumed to be an unweighted, directed network) is a column vector $\mathbf{o}^T = [\rho, (1-\rho)]$ (we can
- safely drop the S^2 terms, as we will work on the confusion matrix, which ends up expressing *relative*
- values). We will apply skill and bias to this matrix, and measure how a selection of performance metrics
- respond to changes in these values, in order to assess their suitability for model evaluation.

102 Confusion matrix with skill and bias

- In order to write the values of the confusion matrix for a hypothetical classifier, we need to define two
- characteristics: its skill, and its bias. Skill, here, refers to the propensity of the classifier to get the correct

answer (*i.e.* to assign interactions where they are, and to not assign them where they are not). A no-skill classifier guesses at random, *i.e.* it will guess interactions with a probability ρ . The predictions of a no-skill classifier can be expressed as a row vector $\mathbf{p} = [\rho(1-\rho)]$. The confusion matrix \mathbf{M} for a no-skill classifier is given by the element-wise (Hadamard, outer) product of these vectors $\mathbf{o} \odot \mathbf{p}$, *i.e.*

$$\mathbf{M} = \begin{pmatrix} \rho^2 & \rho(1-\rho) \\ (1-\rho)\rho & (1-\rho)^2 \end{pmatrix}.$$

In order to regulate the skill of this classifier, we can define a skill matrix **S** with diagonal elements equal to s, and off-diagonal elements equal to s, and re-express the skill-adjusted confusion matrix as **M** \odot **S**, *i.e*.

$$\begin{pmatrix} \rho^2 & \rho(1-\rho) \\ (1-\rho)\rho & (1-\rho)^2 \end{pmatrix} \odot \begin{pmatrix} s & (1-s) \\ (1-s) & s \end{pmatrix}.$$

Note that when s = 0, $Tr(\mathbf{M}) = 0$ (the classifier is *always* wrong), when s = 0.5, the classifier is no-skill and guesses at random, and when s = 1, the classifier is perfect.

The second element we can adjust in this hypothetical classifier is its bias, specifically its tendency to over-predict interactions. Like above, we can do so by defining a bias matrix \mathbf{B} , where interactions are over-predicted with probability b, and express the final classifier confusion matrix as $\mathbf{M} \odot \mathbf{S} \odot \mathbf{B}$, *i.e.*

$$\begin{pmatrix} \rho^2 & \rho(1-\rho) \\ (1-\rho)\rho & (1-\rho)^2 \end{pmatrix} \odot \begin{pmatrix} s & (1-s) \\ (1-s) & s \end{pmatrix} \odot \begin{pmatrix} b & b \\ (1-b) & (1-b) \end{pmatrix}.$$

The final expression for the confusion matrix in which we can regulate the skill and the bias is

$$\mathbf{C} = \begin{pmatrix} s \times b \times \rho^2 & (1-s) \times b \times \rho(1-\rho) \\ (1-s) \times (1-b) \times (1-\rho)\rho & s \times (1-b) \times (1-\rho)^2 \end{pmatrix}.$$

In all further simulations, the confusion matrix **C** is transformed so that it sums to 1.

What are the baseline values of performance measures?

In this section, we will change the values of b, s, and ρ , and report how the main measures discussed in 120 the introduction (MCC, F_1 , κ , and informedness) are responding to issues with the classifier. Before we do 121 so, it is important to explain why we will not focus on accuracy too much. Accuracy is the number of 122 correct predictions $(Tr(\mathbf{C}))$ divided by the sum of the confusion matrix. For a no-skill, no-bias classifier, 123 accuracy is equal to $\rho^2 + (1 - \rho)^2$; for $\rho = 0.05$, this is ≈ 0.90 , and for $\rho = 0.01$, this is equal to ≈ 0.98 . In 124 other words, the values of accuracy are expected to be so high that they are not really informatived (this is simply explained by the fact that for ρ small, $\rho^2 \ll (1-\rho)^2$). More concerning is the fact that introducing 126 bias changes the response of accuracy in unexpected ways. Assuming a no-skill classifier, the numerator 127 of accuracy becomes $b\rho^2 + (1-b)(1-\rho)^2$, which increases when b is low, which specifically means that at equal skill, a classifier that under-predicts interactions will have higher accuracy than an un-biased 129 classifier. These issues are absent from balanced accuracy, but should nevertheless lead us to not report 130 accuracy as the primary measure of network prediction success; moving forward, we will focus on other measures. 132 In order to examine how MCC, F_1 , κ , and informedness change w.r.t. the imbalance, skill, and bias, we 133 performed a grid exploration of the values of logit(s) and logit(b) linearly from -10 to 10, of ρ linearly in 134 [0, 0.5], which is within the range of usually observed connectance values for empirical food webs. Note 135 that at this point, there is no food web model to speak of; rather, the confusion matrix we discuss can be 136 obtained for any classification task. Based on the previous discussion, the desirable properties for a measure of classifier success should be: an increase with classifier skill, especially at low bias; a 138 hump-shaped response to bias, especially at high skill, and ideally center around logit(b) = 0; an increase 139 with prevalence up until equiprevalence is reached.

[Figure 1 about here.]

In fig. 1, we show that none of the four measures satisfy all the considerations at once: F_1 increases with skill, and increases monotonously with bias; this is because F_1 does not account for true negatives, and the increase in positive detection masks the over-prediction of interactions. Informedness varies with skill, reaching 0 for a no-skill classifier, but is entirely unsensitive to bias. Both MCC and κ have the same behavior, whereby they increase with skill. κ peaks at increasing values of biass for increasing skill, *i.e.* is

likely to lead to the selection of a classifier that over-predicts interactions. By contract, MCC peaks at the same value, regardless of skill, but this value is not logit(b) = 0: unless at very high classifier skill, MCC risks leading to a model that over-predicts interactions. In fig. 2, we show that all measures except F_1 give a value of 0 for a no-skill classifier, and are forced towars their correct maximal value when skill changes (*i.e.* a more connected networks will have higher values for a skilled classifierd, and lower values for a classifier making mostly mistakes).

[Figure 2 about here.]

These two analyses point to the following recommendations: MCC is indeed more appropriate than κ , as 154 although sensitive to bias, it is sensitive in a consistent way. Informedness is appropriate at discriminating 155 between different skills, but confounded by bias. As both of these measures bring valuable information on 156 the model behavior, we will retain them for future analyses. F_1 is increasing with bias, and should not be 157 prioritized to evalue the performance of the model. The discussion of sensitivity to bias should come with a domain-specific caveat: although it is likely that interactions documented in ecological networks are 159 correct, a lot of non-interactions are simply unobserved; as predictive models are used for data-inflation 160 (i.e. the prediction of new interactions), it is not necessarily a bad thing in practice to select models that 161 predict more interactions than the original dataset, because the original dataset misses some interactions. 162 Furthermore, the weight of positive interactions could be adjusted if some information about the extent of 163 undersampling exists (e.g. Branco et al., 2015). In a recent large-scale imputation of interactions in the 164 mammal-virus networks, Poisot et al. (2021) for example estimated that 93% of interactions are yet to be 165 documented. 166

Numerical experiments on training strategy

153

In the following section, we will generate random bipartite networks (this works without loss of generality on unipartite networks), and train four binary classifiers (as well as an ensemble model using the sum of ranged outputs from the component models) on 30% of the interaction data. Networks are generated by picking a random infectiousness trait v_i for 100 species (from a B(6,8) distribution), and a resistance trait h_j for 100 species (from a B(2,8) distribution). There is an interaction between i and j when $v_i - \xi/2 \le h_j \le v_i + \xi/2$, where ξ is a constant regulating the connectance of the network (there is an

almost 1:1 relationship between ξ and connectance), and varies uniformly in [0.05, 0.35]. This model gives fully interval networks that are close analogues to the bacteria-phage model of Weitz et al. (2005), with 175 both a modular structure and a non-uniform degree distribution. This model is easy to learn: when 176 trained with features $[v_i, h_j, abs(v_i, h_i)]^T$ to predict the interactions between i and j, all four models presented below were able to reach almost perfect predictions all the time (data not presented here) – this 178 is in part because the rule is fixed for all interactions. In order to make the problem more difficult to solve, 179 we use $[v_i, h_i]$ as a feature vector (i.e. the traits on which the models are trained), and therefore the models 180 will have to uncover that the rule for interaction is $abs(v_i, h_i) \le \xi$. 181 The training sample is composed of 30% of the 10^4 possible entries in the network, i.e. n = 3000. Out of 182 these interactions, we pick a proportion ν (the training set bias) to be positive, so that the training set has 183 νn interactions, and $(1-\nu)n$ non-interactions. We vary ν uniformly in]0,1[. This allows to evaluate how 184 the measures of binary classification performance respond to artificially rebalanced dataset for a given 185 network connectance. The rest of the dataset (n = 7000 pairs of species) is used as a testing set, on which all furher measures are calculated. Note that although the training set is balanced, the testing set is not, 187 and retains (part of) the imbalance of the original data. 188 The dataset used for numerical experiments is composed of 64000 such (ξ, ν) pairs, on which four 189 machines are trained: a decision tree regressor, a boosted regression tree, a ridge regressor, and a random 190 forest regressor. All models were taken from the MLJ. jl package (Blaom et al., 2020; Blaom & Vollmer, 191 2020) in Julia 1.7 (Bezanson et al., 2017). All machines use the default parameterization; this is an obvious deviation from best practices, as the hyperparameters of any machine require training before its 193 application on a real dataset. As we use 64000 such datasets, this would require 256000 unique instances 194 of tweaking the hyperparameters, which is not realistic. Therefore, we assume that the default parameterizations are comparable across networks. All machines return a quantitative prediction, usually 196 (but not necessarily) in [0, 1], which is proportional (but not necessarily linearly) to the probability of an 197 interaction between *i* and *j*. 198 In order to pick the best adjacency matrix for a given trained machine, we performed a thresholding 199 approach using 500 steps on predictions from the testing set, and picking the threshold that maximized 200 Youden's informedness, which is usually the optimized target for imbalanced classification. During the thresholding step, we measured the area under the receiving-operator characteristic (ROC-AUC) and 202 precision-recall (PR-AUC) curves, as measures of overall performance over the range of returned values.

We report the ROC-AUC and PR-AUC, as well as a suite of other measures as introduced in the next section, for the best threshold. The ensemble model was generated by summing the predictions of all 205 component models on the testing set (ranged in [0,1]), then put through the same thresholding process. 206 The complete code to run the simulations is given as an appendix; running the final simulation required 4.8 core days (approx. 117 hours). 208 After the simulations were completed, we removed all runs (i.e. pairs of ξ and ν) for which at least one of 209 the following conditions was met: the accuracy was 0, the true positive or true negative rates were 0, the 210 connectance was larger than 0.25. This removes both the obviously failed model runs, and the networks 211 that are more densely connected compared to the connectance of empirical food webs (and are therefore 212 less difficult to predict, being less imbalanced; preliminary analyses of data with a connectance larger than 3 revealed that all machines reached consistently high performance). 214

Effect of training set bias on performance

225

In fig. 3, we present the response of MCC and informedness to (i) five levels of network connectance and (ii) a gradient of training set bias, for the four component models as well as the ensemble. All models 217 reached a higher performance on more connected networks, and using more biased training sets (with the 218 exception of ridge regression, whose informedness decreased in performance with training set bias). In all cases, informedness was extremely high, which is an expected consequence of the fact that this is the 220 value we optimized to determine the cutoff. MCC increased with training set bias, although this increase 221 became less steep with increasing connectance. Interestingly, the ensemble almost always outclassed its 222 component models. In a few cases, both MCC and informedness stared decreasing when the training set 223 bias got too close to one, which suggests that it is possible to over-correct the imbalance. 224

[Figure 3 about here.]

In fig. 4, we present the same information as fig. 3, this time using ROC-AUC and PR-AUC. ROC-AUC is
always high, and does not vary with training set bias. On the other hand, PR-AUC shows very strong
responses, increasing with training set bias. It is notable here that two classifiers that seemed to be
performing well (Decision Tree and Random Forest) based on their MCC are not able to reach a high
PR-AUC even at higher connectances. As in fig. 3, the ensemble outperforms its component models.

245

255

Based on the results presented in fig. 3 and fig. 4, it seems that informedness and ROC-AUC are not
necessarily able to discriminate between good and bad classifiers (although this result may be an artifact
for informedness, as it has been optimized when thresholding). On the other hand, MCC and PR-AUC
show a strong response to training set bias, and may therefore be more useful at model comparison.

236 Required amount of positives to get the best performance

The previous results revealed that the measure of classification performance responds both to the bias in
the training set *and* to the connectance of the network; from a practical point of view, assembling a
training set requires to withold positive information, which in ecological networks are very scarce (and
typically more valuable than negatives, on which there is a doubt). For this reason, across all values of
connectance, we measured the training set bias that maximized a series of performance measures. When
this value is high, the training set needs to skew more positive in order to get a performant model; when
this value is about 0.5, the training set needs to be artificially balanced to optimize the model performance.
These results are presented in fig. 5.

[Figure 5 about here.]

The more "optimistic" measures (ROC-AUC and informedness) required a biasing of the dataset from about 0.4 to 0.75 to be maximized, with the amount of bias required decreasing only slightly with the 247 connectance of the original network. MCC and PR-AUC required values of training set bias from 0.75 to 248 almost 1 to be optimized, which is in line with the results of the previous section, i.e. they are more 249 stringent tests of model performance. These results suggest that learning from a dataset with very low 250 connectance can be a different task than for more connected networks: it becomes increasingly important 251 to caputre the mechanisms that make an interaction exist, and therefore having a slightly more biased 252 training dataset might be beneficial. As connectance increases, the need for biased training sets is less 253 prominent, as learning the rules for which interactions do not exist starts gaining importance. 254

[Figure 6 about here.]

When trained at their optimal training set bias, connectance still had a significant impact on the
performance of some machines fig. 6. Notably, Decision Tree, Random Forest, and Ridge Regression had
low values of PR-AUC. In all cases, the Boosted Regression Tree was reaching very good predictions
(esepcially for connectances larger than 0.1), and the ensemble was almost always scoring perfectly. This
suggests that all the models are biased in different ways, and that the averaging in the ensemble is able to
correct these biases. We do not expect this last result to have any generality, and provide a discussion of a
recent exemple in which the ensemble was performing worse than its components models.

Do better classification accuracy result in more realistic networks?

In this last section, we generate a network using the same model as before, with $S_1, S_2 = 50$, 80 species, a connectance of ≈ 0.16 ($\xi = 0.19$), and a training set bias of 0.7. The prediction made on the complete dataset is presented in fig. 7. Visualizing the results this way highlights the importance of exploratory data analysis: whereas all models return a network with interactions laying mostly on the diagonal (as expected), the Ridge Regression is quite obviously biased. Despite this, we can see that the ensemble is close to the initial dataset.

[Figure 7 about here.]

270

The trained models were then thresholded (again by optimising informedness), and their predictions 271 transformed back into networks for analysis; specifically, we measured the connectance, nestedness 272 (REF), and modularity (REF). This process was repeated 250 times, and the results are presented in tbl. 1. 273 The random forest model is an interesting instance here: it produces the network that looks the most like 274 the original dataset, despite having a very low PR-AUC, suggesting it hits high recall at the cost of low 275 precision. Although the ensemble was able to reach a very high PR-AUC (and a very high ROC-AUC), this 276 did not necessarily translate into more accurate reconstructions of the structure of the network. This 277 result bears elaborating. Measures of model performance capture how much of the interactions and 278 non-interactions are correctly identified. As long as these predictions are not perfect, some interactions will be predicted at the "wrong" position in the network; these measures cannot describe the structural 280 effect of these mistakes. On the other hand, measures of network structure can have the same value with 281 interactions that fall at drastically different positions; this is in part because a lot of these measures covary

with connectance, and in part because as long as these values are not 0 or their respective maximum, there
is a large number of network configurations that can have the same value. That ROC-AUC is consistently
larger than PR-AUC may be a case of this measure masking models that are not, individually, strong
predictors (Jeni et al., 2013).

Table 1: Values of four performance metrics, and three network structure metrics, for 250 independent predictions similar to the ones presented in fig. 7. The values in **bold** indicate the best value for each column (including ties). Because the values have been rounded, values of 1.0 for the ROC-AUC column indicate an average ≥ 0.99 .

Model	MCC	Inf.	ROC-AUC	PR-AUC	Conn.	η	Q
Decision tree	0.85	0.92	0.97	0.12	0.21	0.76	0.31
BRT	0.90	0.90	0.98	0.86	0.23	0.82	0.27
Random Forest	0.90	0.96	1.00	0.27	0.20	0.72	0.32
Ridge Regression	0.80	0.91	0.95	0.58	0.24	1.0	0.18
Ensemble	0.88	0.94	1.00	0.96	0.20	0.75	0.31
Data					0.18	0.66	0.34

Guidelines for the assesment of network predictive models

The results presented here highlight an interesting paradox: although the Random Forest was ultimately 288 able to get a correct estimate of network structure tbl. 1, it ultimately remains a poor classifier, as 289 evidenced by its low PR-AUC. This suggests that the goal of predicting interactions and predicting 290 networks may not be solvable in the same way – of course a perfect classifier of interactions would make a 291 perfect network prediction; but even the best scoring predictor of interactions (the ensemble model) had 292 not necessarily the best prediction of network structure. The tasks of predicting networks structure and of 293 predicting interactions within networks are essentially two different ones. For some applications (.e.g. 294 comparison of network structure across gradients), one may care more about a robust estimate of the structure, at the cost at putting some interactions at the wrong place. For other applications (e.g. 296 identifying pairs of interacting species), one may conversely care more about getting as many pairs right, 297 even though the mistakes accumulate in the form of a slightly worse estimate of network structure. How 298 these two approaches can be reconciled is undoubtedly a task for further research. Despite this apparent

tension at the heart of the predictive exercise, we can use the results presented here to suggest a number of guidelines. 301 First, because we should have more trust in reported interactions than in reported absences of interactions, 302 we can draw on previous literature to recommend informedness as a measure to decide on a threshold (Chicco et al., 2021); this being said, because informedness is insensitive to bias, the model performance is 304 better evaluated through the use of MCC fig. 3. Because F_1 is monotonously sensitive to classifier bias 305 fig. 1 and network connectance fig. 2, MCC should be prefered as a measure of model evaluation. 306 Second, because the PR-AUC responds more to network connectance fig. 6 and training set imbalance 307 fig. 4, it should be used as a measure of model performance over the ROC-AUC. This is not to say that 308 ROC-AUC should be discarded (in fact, a low ROC-AUC is a sign of an issue with the model), but that its 309 interpretation should be guided by the PR-AUC value. Specifically, a high ROC-AUC is not informative, as it can be associated to a low PR-AUC (see e.g. Random Forest in tbl. 1) This again echoes 311 recommendations from other fields (Jeni et al., 2013; Saito & Rehmsmeier, 2015). 312 Thirdly, regardless of network connectance, maximizing informedness required a training set bias of about 313 0.5, and maximizing the MCC required a training set bias of 0.7 and more. This has an important 314 consequence in ecological networks, for which the pool of positive cases (interactions) to draw from is 315 typically small: the most parsimonious measure (i.e. the one requiring to discard the least amount of 316 information to train the model) will give the best validation potential, and is probably the informedness 317 (maximizing informedness is the generally accepted default for imbalanced classification; Schisterman et 318 al., 2005). 319 Finally, it is noteworthy that the ensemble model was systematically better than the component models; 320 even when the models were individually far form perfect, the ensemble was able to leverage the different 321 biases expressed by the models to make an overall more accurate prediction. We do not expect that 322 ensembles will always be better than single models. In a recent multi-model comparison, Becker et al. 323 (2021) found that the ensemble was not the best model. There is no general conclusion to draw from this 324 besides reinforcing the need to be pragmatic about which models should be included in the ensemble, or 325 whether to use an ensemble at all. In a sense, the surprising performance of the ensemble model should 326 form the basis of the last recommendation: optimal training set bias and its interaction with connectance 327 and binary classifier is, in a sense, an hyperparameter that should be assessed. The distribution of results 328 in fig. 5 and fig. 6 show that there are variations around the trend; furthermore, networks with different

- 330 structures than the one we simulated here may respond in different ways.
- Acknowledgements: We acknowledge that this study was conducted on land within the traditional
- unceded territory of the Saint Lawrence Iroquoian, Anishinabewaki, Mohawk, Huron-Wendat, and
- Omàmiwininiwak nations. We thank Colin J. Carlson, Michael D. Catchen, Giulio Valentino Dalla Riva,
- and Tanya Strydom for inputs on earlier versions of this manuscript. This research was enabled in part by
- support provided by Calcul Québec (www.calculquebec.ca) and Compute Canada
- 336 (www.computecanada.ca) through the Narval general purpose cluster. TP is supported by a NSERC
- Discovery Grant and Discovery Acceleration Supplement, by funding to the Viral Emergence Research
- Initiative (VERENA) consortium including NSF BII 2021909, and by a grant from the Institut de
- ³³⁹ Valorisation des Données (IVADO).

References

- Allouche, O., Tsoar, A., & Kadmon, R. (2006). Assessing the accuracy of species distribution models:
- Prevalence, kappa and the true skill statistic (TSS). *Journal of Applied Ecology*, 43(6), 1223–1232.
- https://doi.org/10.1111/j.1365-2664.2006.01214.x
- Becker, D., Albery, G. F., Sjodin, A. R., Poisot, T., Bergner, L., Dallas, T., Eskew, E. A., Farrell, M. J., Guth,
- S., Han, B. A., Simmons, N. B., Stock, M., Teeling, E. C., & Carlson, C. J. (2021). Optimizing predictive
- models to prioritize viral discovery in zoonotic reservoirs. *bioRxiv*, 2020.05.22.111344.
- https://doi.org/10.1101/2020.05.22.111344
- Bezanson, J., Edelman, A., Karpinski, S., & Shah, V. (2017). Julia: A Fresh Approach to Numerical
- 349 Computing. SIAM Review, 59(1), 65–98. https://doi.org/10.1137/141000671
- Blaom, A. D., Kiraly, F., Lienart, T., Simillides, Y., Arenas, D., & Vollmer, S. J. (2020). MLJ: A Julia package
- for composable machine learning. *Journal of Open Source Software*, 5(55), 2704.
- https://doi.org/10.21105/joss.02704
- Blaom, A. D., & Vollmer, S. J. (2020, December 31). Flexible model composition in machine learning and its
- implementation in MLJ. http://arxiv.org/abs/2012.15505
- Boughorbel, S., Jarray, F., & El-Anbari, M. (2017). Optimal classifier for imbalanced data using Matthews
- Correlation Coefficient metric. *PloS One*, *12*(6), e0177678.

```
https://doi.org/10.1371/journal.pone.0177678
    Branco, P., Torgo, L., & Ribeiro, R. (2015, May 13). A Survey of Predictive Modelling under Imbalanced
358
       Distributions. http://arxiv.org/abs/1505.01658
359
    Chicco, D., & Jurman, G. (2020). The advantages of the Matthews correlation coefficient (MCC) over F1
360
       score and accuracy in binary classification evaluation. BMC Genomics, 21(1), 6.
361
       https://doi.org/10.1186/s12864-019-6413-7
362
    Chicco, D., Tötsch, N., & Jurman, G. (2021). The Matthews correlation coefficient (MCC) is more reliable
363
       than balanced accuracy, bookmaker informedness, and markedness in two-class confusion matrix
364
       evaluation. BioData Mining, 14, 13. https://doi.org/10.1186/s13040-021-00244-z
365
    Delgado, R., & Tibau, X.-A. (2019). Why Cohen's Kappa should be avoided as performance measure in
366
       classification. PloS One, 14(9), e0222916. https://doi.org/10.1371/journal.pone.0222916
367
    Ferri, C., Hernández-Orallo, J., & Modroiu, R. (2009). An experimental comparison of performance
368
       measures for classification. Pattern Recognition Letters, 30(1), 27–38.
369
       https://doi.org/10.1016/j.patrec.2008.08.010
370
    He, H., & Ma, Y. (Eds.). (2013). Imbalanced Learning: Foundations, Algorithms, and Applications (1st
371
       edition). Wiley-IEEE Press.
372
    Jeni, L. A., Cohn, J. F., & De La Torre, F. (2013). Facing Imbalanced Data-Recommendations for the Use
373
       of Performance Metrics. 2013 Humaine Association Conference on Affective Computing and Intelligent
374
       Interaction, 245-251. https://doi.org/10.1109/ACII.2013.47
375
    Jordano, P. (2016a). Chasing Ecological Interactions. PLOS Biol, 14(9), e1002559.
       https://doi.org/10.1371/journal.pbio.1002559
377
    Jordano, P. (2016b). Sampling networks of ecological interactions. Functional Ecology.
378
       https://doi.org/10.1111/1365-2435.12763
379
    Landis, J. R., & Koch, G. G. (1977). The Measurement of Observer Agreement for Categorical Data.
380
       Biometrics, 33(1), 159–174. https://doi.org/10.2307/2529310
381
    MacDonald, A. A. M., Banville, F., & Poisot, T. (2020). Revisiting the Links-Species Scaling Relationship in
382
       Food Webs. Patterns, 1(0). https://doi.org/10.1016/j.patter.2020.100079
383
```

357

```
McLeod, A., Leroux, S. J., Gravel, D., Chu, C., Cirtwill, A. R., Fortin, M.-J., Galiana, N., Poisot, T., & Wood,
       S. A. (2021). Sampling and asymptotic network properties of spatial multi-trophic networks. Oikos,
385
       n/a(n/a). https://doi.org/10.1111/oik.08650
386
    Poisot, T., Ouellet, M.-A., Mollentze, N., Farrell, M. J., Becker, D. J., Albery, G. F., Gibb, R. J., Seifert, S. N.,
387
       & Carlson, C. J. (2021, May 31). Imputing the mammalian virome with linear filtering and singular
388
       value decomposition. http://arxiv.org/abs/2105.14973
389
    Saito, T., & Rehmsmeier, M. (2015). The Precision-Recall Plot Is More Informative than the ROC Plot
390
       When Evaluating Binary Classifiers on Imbalanced Datasets. PLOS ONE, 10(3), e0118432.
391
       https://doi.org/10.1371/journal.pone.0118432
392
    Schisterman, E. F., Perkins, N. J., Liu, A., & Bondell, H. (2005). Optimal Cut-point and Its Corresponding
393
       Youden Index to Discriminate Individuals Using Pooled Blood Samples. Epidemiology, 16(1), 73–81.
394
       https://doi.org/10.1097/01.ede.0000147512.81966.ba
395
    Somodi, I., Lepesi, N., & Botta-Dukát, Z. (2017). Prevalence dependence in model goodness measures with
396
       special emphasis on true skill statistics. Ecology and Evolution, 7(3), 863–872.
397
       https://doi.org/10.1002/ece3.2654
398
    Strydom, T., Catchen, M. D., Banville, F., Caron, D., Dansereau, G., Desjardins-Proulx, P., Forero-Muñoz,
399
       N. R., Higino, G., Mercier, B., Gonzalez, A., Gravel, D., Pollock, L., & Poisot, T. (2021). A roadmap
400
       towards predicting species interaction networks (across space and time). Philosophical Transactions of
401
       the Royal Society B: Biological Sciences, 376(1837), 20210063.
402
       https://doi.org/10.1098/rstb.2021.0063
403
    Weitz, J. S., Hartman, H., & Levin, S. A. (2005). Coevolutionary arms races between bacteria and
404
       bacteriophage. Proceedings of the National Academy of Sciences of the United States of America, 102(27),
405
       9535-9540. https://doi.org/10.1073/pnas.0504062102
406
    Whalen, S., Schreiber, J., Noble, W. S., & Pollard, K. S. (2021). Navigating the pitfalls of applying machine
407
       learning in genomics. Nature Reviews Genetics, 1–13.
408
       https://doi.org/10.1038/s41576-021-00434-9
409
    Youden, W. J. (1950). Index for rating diagnostic tests. Cancer, 3(1), 32–35.
```

https://doi.org/10.1002/1097-0142(1950)3:1%3C32::AID-CNCR2820030106%3E3.0.CO;2-3

411

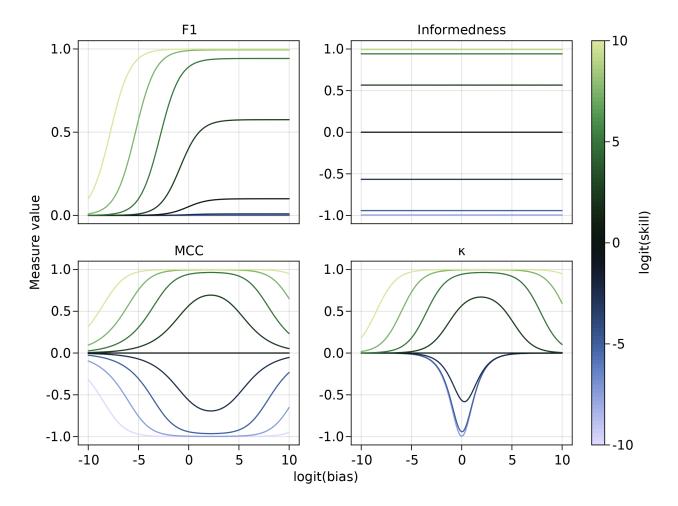


Figure 1: Consequences of changing the classifier skills (s) and bias (s) for a connectance $\rho=0.15$, on accuracy, F_1 , postive predictive value, and κ . Accuracy increases with skill, but also increases when the bias tends towards estimating *fewer* interactions. The F_1 score increases with skill but also increases when the bias tends towards estimating *more* interactions; PPV behaves in the same way. Interestingly, κ responds as expected to skill (being negative whenever s<0.5), and peaks for values of $b\approx0.5$; nevertheless, the value of bias for which κ is maximized in *not* b=0.5, but instead increases with classifier skill. In other words, at equal skill, maximizing κ would lead to select a *more* biased classifier.



Figure 2: As in fig. 1, consequences of changing connectance for different levels of classifier skill, assuming no classifier bias. Informedness, κ , and MCC do increase with connectance, but only when the classifier is not no-skill; by way of contrast, a more connected network will give a higher F_1 value even with a no-skill classifier.

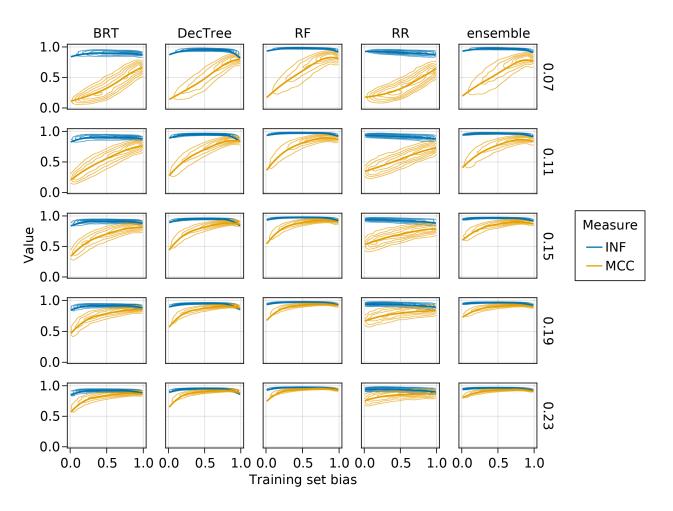


Figure 3: Response of MCC and Informedness to changes in the training set bias for a fixed connectance (rows). Both of these values approach 1 for a good model. Informedness is consistently high, and by contrast, MCC increases with additional training set bias. Across all models, training on a more connected network is easier.

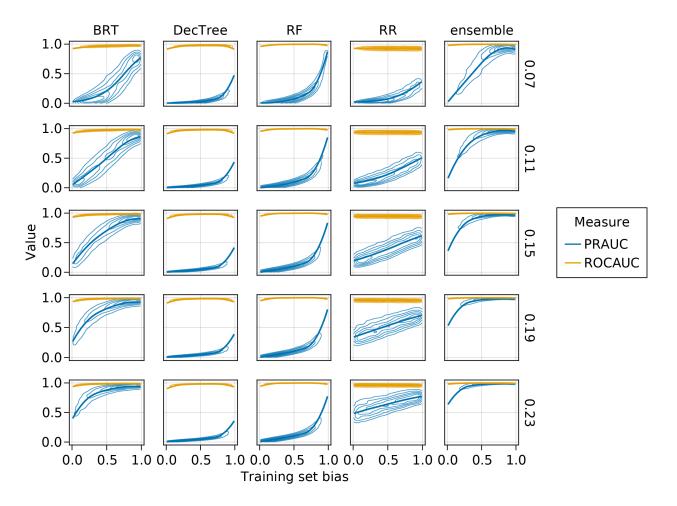


Figure 4: Response of ROC-AUC and PR-AUC to changes in the training set bias for a fixed connectance (rows). ROC-AUC is consistently high, and therefore not properly able to separate good from poor classifiers. On the other hand, PR-AUC responds to changes in the training set. As in fig. 3, training on more connected networks is easier.

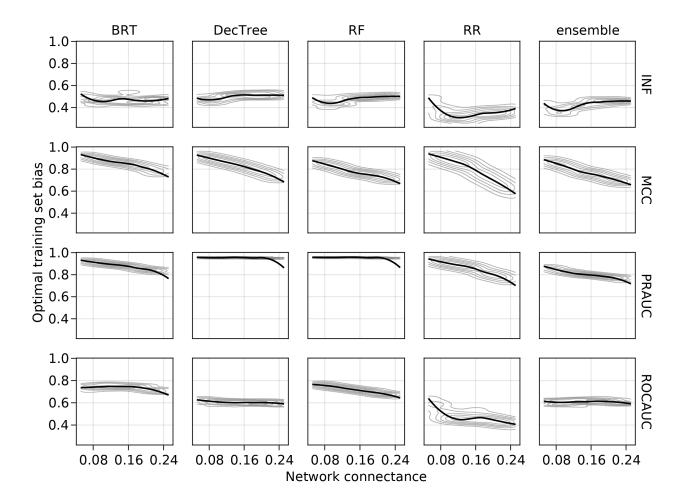


Figure 5: Value of the optimal training set bias for the different models and measures evaluated here, over a range of connectances. Informedness was reliably maximized for balanced training sets, and kept this behavior across models. For other measures, larger connectances in the true network allowed lower biases in the training set. In a large number of cases, "over-correcting" by having training sets with more than half instances representing interactions would maximize the values of the model performance measures.

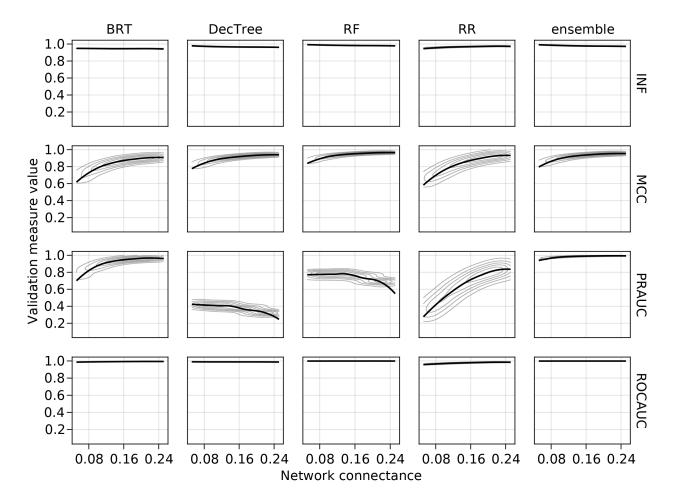


Figure 6: When trained on their optimally biased training set, most models were able to maximize their performance; this is not true for decision tree, which had a very low PR-AUC, and to some extent for ridge regression who had a slow increase with network connectance. The ensemble had a consistently high performance despite incorporating poor models.

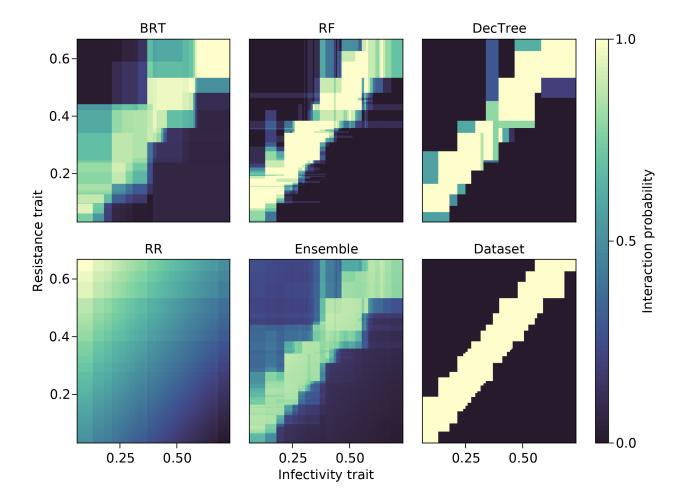


Figure 7: Visualisation of the models predictions for one instance of a network prediction problem (shown in the "Dataset" panel). This figure reveals how inspecting the details of the prediction is important: indeed, although the performance measures hint at the fact that ridge regression is mediocre, this figure reveals that it is making predictions that correspond to a network with an entirely different topology (namely, nested as opposed to diagonal).