

18K41A05F9

## Assignment - 03

### Stochastic Gradient Descent

Step-1:  $[x, y]$   
 $\text{epochs} = 2$   
 $\eta = 0.1$   
 $m = 1$   
 $c = -1$

Data	
X	Y
0.2	3.4
0.4	3.8

Step-2: iter = 1, Step-3: sample = 1

Step-4:

$$\begin{aligned}\text{Error}(E) &= \frac{1}{2} (y_i - mx_i - c)^2 \\ &= \frac{1}{2} (3.4 - (1)(0.2) - (-1))^2 \\ &= 8.82\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial m} &= -(y_i - mx_i - c)x_i \\ &= -(3.4 - (1)(0.2) - (-1))(0.2) \\ &= -0.84\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial m} &= -(y_i - mx_i - c) \\ &= -(3.4 - (1)(0.2) - (-1)) \\ &= -4.2\end{aligned}$$

Step-5:

$$\Delta m = -\eta \frac{\partial E}{\partial m}$$

$$= -(0.1)(-0.84)$$

$$= 0.084$$

$$\Delta c = -\eta \frac{\partial E}{\partial c}$$

$$= -(0.1)(-4.2)$$

$$= 0.42$$

Step-6:

$$m = m + \Delta m = 1 + 0.084 = 1.084$$

$$c = c + \Delta c = -1 + 0.42 = -0.58$$

Step-7:

$$\text{Sample} = \text{sample} + 1$$

$$= 1 + 1 = 2$$

$$\text{Sample} = 2 \leq n_s$$

Step-8:

Go to Step-4

$$\text{Here, } y = mx + c$$

Hence

$$y = (1.084)(0.4) + (-0.58)$$

$$E = \frac{1}{2} (y_i - mx_i - c)^2$$

$$= 0.1464$$

$$= (0.5) (\cancel{3.2 - (1)(0.4) - (-1)})^2$$

$$= \frac{1}{2} (3.2 - (1.084)(0.4) - (-0.58))^2$$

$$= 7.79$$

Step-9:

$$\begin{aligned}\frac{\partial E}{\partial m} &= -(y_i - mx_i - c) x_i \\ &= -\left(3.8 - (1.084)(0.4) - (-0.58)\right)(0.4) \\ &= -1.58\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial c} &= -(y_i - mx_i - c) \\ &= -3.9464 \approx -3.94\end{aligned}$$

Step-10:

$$\Delta m = -\eta \frac{\partial E}{\partial m} = -(0.1)(-1.58) = 0.158$$

$$\begin{aligned}\Delta c &= -\eta \frac{\partial E}{\partial c} = -(0.1)(-3.94) = 0.394 \\ &= 0.394\end{aligned}$$

Step-11:

$$m = m + \Delta m = 1.084 + 0.158 = 1.242$$

$$\begin{aligned}c &= c + \Delta c = -0.58 + 0.394 = \\ &= -0.186\end{aligned}$$

Step-12: Sample = 2+1 = 3 ≤ ns → False  
Go to next step.

Step-13: iter = iter + 1  
= 1+1 = 2 ≤ epochs

Go to step-3

Step-14: sample = 1

$$\begin{aligned}\text{Step-15: } Y &= ((1.242)(0.2) + (-0.186)) \\ &= 0.0624\end{aligned}$$

$$E = \frac{1}{2} (3.4 - 0.0624) = 1.6688$$

step-16:  $\frac{\partial E}{\partial m} = -(3.4 - (1.242)(0.2) - (-0.186))(0.2)$   
 $= -0.66752$

$$\frac{\partial E}{\partial c} = -(3.4 - (1.242)(0.2) - (-0.186))$$

$$= -3.3376$$

step-17:  $\Delta m = -\eta \frac{\partial E}{\partial m} = -(0.1)(-0.66752)$   
 $= 0.066752$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = -(0.1)(-3.3376)$$

$$= 0.33376$$

step-18:  $m = m + \Delta m$   
 $= 1.242 + 0.066752 = 1.90952$

$$c = c + \Delta c$$

$$= -0.186 + 0.33376$$

$$= 0.14776$$

step-19: sample =  $1+1=2 \leq ns$  — True  
 Go to step-4

step-20:  $\frac{\partial E}{\partial m} = -(y_i - mx_i - c)x_i$   
 $= -(3.8 - (1.90952)(0.4) - (0.14776))(0.4)$   
 $= -1.155372$

$$\frac{\partial E}{\partial m} = -(y_i - mx_i - c)$$

$$= -(3.8 - (1.90952)(0.4) - (0.14776))$$

$$= -2.888432$$

Step-21:  $\Delta m = -\eta \frac{\partial C}{\partial m} = -(0.1)(-1.155372)$   
 $= 0.1155372$

$\Delta C = -\eta \frac{\partial C}{\partial C} = -(0.1)(-2.888432)$   
 $= 0.2888432$

Step-22:  $m = m + \Delta m = 1.90952 + 0.1155372$   
 $= 2.025057$

$C = C + \Delta C = 0.14776 + 0.2888432$   
 $= 0.4366032$

Step-23:  $\text{sample} = 2+1 = 3 \leq n_s$  — false  
 Go to next step

Step-24:  $\text{iter} = 2+1 = 3 \leq \text{epochs}$  — False  
 Go to next step

Step-25: Print  $m, C$   
 $m = 2.025057$   
 $C = 0.4366032$

Step-26: Calculating Mean Square Error

$$= \frac{((3.4) - (2.025057)(0.2) - (0.4366032))^2}{2} + \frac{(3.8 - (2.025057)(0.4) - (0.4366032))^2}{2}$$

$$= \frac{(2.558386)^2 + (2.55374)^2}{2}$$

MSE = ~~2.556063~~ 13.06692