

Student's Name:

Teacher's Initials:



Barker
College

Thursday 8th March 2018

Period 4 or 6

Time Allowed: 50 minutes

GPF AYG
TE RMH
DZP* ARP

YEAR 9 MATHEMATICS

5.3

ASSESSMENT 1

160 copies

**Algebra
Products and Factors**

INSTRUCTIONS TO STUDENTS

- * **Write ALL answers in the space provided.**
- * **ALL NECESSARY working for each question must be shown to gain full marks.**
- * **Marks may not be awarded for careless or badly arranged working.**
- * **DIAGRAMS ARE NOT TO SCALE**
- * **Write in blue or black pen**
- * **Board-approved, non-programmable calculators may be used.**

TOTAL: [68 marks]

* * * *

Question 1 (11 marks)

Simplify fully

(a) $\frac{m}{5} + \frac{2m}{5}$ **1**

(b) $\frac{3y}{4} - \frac{2y}{3}$ **2**

(c) $\frac{2a}{3} \times \frac{a}{4}$ **2**

(d) $\frac{3h}{14} \div \frac{2h}{21}$ **2**

(e) $\frac{2c}{3} + \frac{5c-4}{7}$ **2**

(f) $\frac{2x}{5} - \frac{3x+4}{10}$ **2**

Question 2 (7 marks)

Simplify fully

(a) $\frac{15xy^3}{3xy}$ 1

(b) $\frac{4ab}{6} \times \frac{9}{2a^2b}$ 2

(c) $\frac{15m^2}{8n} \div \frac{5m^4}{12n^3}$ 2

(d) $\frac{2}{d} - \frac{1}{2d}$ 2

Question 3 (6 marks)

Expand and simplify where possible

(a) $x(4 + y)$ 1

(b) $-5k^2(2 - 3k)$ 1

(c) $7(2g + 3) + 3g(4 + g)$ 2

(d) $3w(2 + w) - (w - 3)$ 2

Question 4 (7 marks)

Expand and simplify

(a) $(y-5)(y+2)$ **2**

(b) $(r+4)^2$ **1**

(c) $(2f+3)(2f-3)$ **2**

(d) $-2(x-7)(x-1)$ **2**

Question 5 (5 marks)

Factorise fully

(a) $24x+6$ **1**

(b) $15x^2y-3xy^2$ **2**

(c) $x(a+3)-(a+3)$ **2**

Question 6 (7 marks)

Factorise fully

(a) $x^2 - 64$

1

(c) $ab + ac^2 + 7b + 7c^2$

2

(b) $x^2 - 5x - 6$

2

(d) $2x^2 + 15x + 28$

2

Question 7 (14 marks)

Simplify each expression

(a) $\frac{5a + 25b}{5}$ **2**

(b) $\frac{9y^2 - 16}{6y + 8}$ **3**

(c) $\frac{3m - 6}{4} \times \frac{8m}{m^2 - 2m}$ **3**

(d) $\frac{14}{x^2 - 1} \div \frac{7x + 49}{x^2 + 8x + 7}$ **3**

(e) $\frac{4}{x^2 + x} - \frac{2}{x^2 - 1}$ **3**

Question 8 (11 marks)

(a) Complete this perfect square expansion $(x-4)^2 = x^2 - \dots\dots\dots + 16$

1

(b) Factorise fully

(α) $\frac{mn - n^2}{mn - m^2}$

2

(β) $3a + a^2 + 3b - b^2$

3

(γ) $x^4 - \frac{1}{16}$

3

(c) *By first factorising*, calculate the value of $158^2 - 142^2$

1

(d) *By factorising* (therefore without using a calculator and showing working) evaluate;

1

$$10^2 - 9^2 + 8^2 - 7^2 + 6^2 - 5^2 + 4^2 - 3^2 + 2^2 - 1^2$$

END OF PAPER

Year 9 5.3 Assessment 1 Student Solutions

1. a) $\frac{3m}{5}$

b) $\frac{9y-8y}{12} = \frac{y}{12}$

c) $\frac{2a^2}{12} = \frac{a^2}{6}$

d) $\frac{63h}{28h} = \frac{9}{4}$

e) $\frac{14c+15c-12}{21} = \frac{29c-12}{21}$

f) $\frac{4x-3x-4}{10} = \frac{x-4}{10}$

2. a) $5y^2$

b) $\frac{36ab}{12a^2b} = \frac{3}{a}$

c) $\frac{15m^2}{8n} \times \frac{12n^3}{5m^4} = \frac{9n^2}{2m^2}$

d) $\frac{4-1}{2d} = \frac{3}{2d}$

3. a) $4x+xy$

b) $-10k^2+15k^3$

c) $=14g+21+12g+3g^2$
 $=26g+21+3g^2$

d) $=6w+3w^2-w+3$
 $=3w^2+5w+3$

4. a) $y^2-3y-10$

b) $r^2+8r+16$

c) $4f^2-9$

d) $=(-2x+14)(x-1)$
 $=-2x^2+16x-14$

5. a) $6(4x+1)$

b) $3xy(5x-y)$

c) $(a+3)(x-1)$

6. a) $(x+8)(x-8)$

b) $(x-6)(x+1)$

c) $=a(b+c^2)+7(b+c^2)$
 $= (b+c^2)(a+7)$

d) $=2x^2+8xc+7xc+28$
 $=2x(x+4)+7(x+4)$
 $= (x+4)(2x+7)$

$$7. a) \frac{5(a+5b)}{5} = a+5b$$

$$b) \frac{(3y+4)(3y-4)}{2(3y+4)} = \frac{3y-4}{2}$$

$$c) \frac{3(m-2)}{4} \times \frac{8m}{m(m-2)} = 6$$

$$d) \frac{14}{(x+1)(x-1)} \times \frac{(x+7)(x+1)}{7(x+7)} = \frac{2}{x-1}$$

$$e) \frac{4}{x(x+1)} - \frac{2}{(x+1)(x-1)} = \frac{2x-4}{x(x+1)(x-1)}$$

$$8. a) 8x$$

$$b) a) = \frac{n(m-n)}{-m(m-n)} = -\frac{n}{m}$$

$$(b) = 3(a+b) + (a+b)(a-b) = (a+b)(3+a-b)$$

$$(x) = (x^2 + \frac{1}{4})(x^2 - \frac{1}{4}) = (x^2 + \frac{1}{4})(x + \frac{1}{2})(x - \frac{1}{2})$$

$$c) = (158+142)(158-142) = 300 \times 16 = 4800$$

$$d) = (10+9)(10-9) + (8+7)(8-7) + \dots + (2+1)(2-1) = 19+15+11+7+3 = 55$$