

## Problem A. Exponentiation

Time limit: please refer to DOM Judge  
Memory limit: please refer to DOM Judge

Your task is to efficiently calculate values  $a^b$  modulo  $10^9 + 7$ .

### Input

The first input line contains an integer  $n$ : the number of calculations.

After this, there are  $n$  lines, each containing two integers  $a$  and  $b$ .

- $1 \leq n \leq 2 \cdot 10^5$
- $1 \leq a, b \leq 10^9$

### Output

Print each value  $a^b \bmod 10^9 + 7$ .

### Examples

Standard Input	Standard Output
3	81
3 4	256
2 8	921450052
123 123	

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## Problem B. Longest Common Substring

Time limit: please refer to DOM Judge  
Memory limit: please refer to DOM Judge

You are given two string  $S$  and  $T$ , find the length of the longest common substring.

A substring is a contiguous sequence of characters within a string. For example, both "BAA" and "ABABA" are substring of "ABABABAA".

Longest common substring of two or more strings is a longest string that is a substring of all of them.

### Input

The first input line contains a string  $S$ .

The second input line contains a string  $T$ .

- $1 \leq |S|, |T| \leq 5 \cdot 10^5$ , where  $|S|$  denote the length of string  $S$ .
- Both  $S$  and  $T$  consist of two different lowercase English letters.

### Output

Print an integer, the length of the longest common substring of  $S$  and  $T$ .

### Examples

Standard Input	Standard Output
abccba bccd	3

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## Problem C. Convex Hull Area

Time limit: please refer to DOM Judge  
Memory limit: please refer to DOM Judge

Given  $n$  points on 2D plane. The coordinate of the  $i$ -th point is  $(x_i, y_i)$ .

Please find the area of their convex hull.

### Input

The first input line contains an integer  $n$  — the number of points.

The  $i$ -th of the next  $n$  lines contains two integers  $x_i, y_i$  — the coordinate of the  $i$ -th point.

- $3 \leq n \leq 2 \times 10^5$
- $-10^9 \leq x_i, y_i \leq 10^9$  for  $i = 1, 2, \dots, n$

### Output

You should print two integers  $2a$ , where  $a$  is the area of the convex hull.

### Examples

Standard Input	Standard Output
5 0 0 0 2 2 0 2 2 1 1	8
6 2 1 2 5 3 3 4 3 4 4 6 3	16

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## Problem D. Road Maintenance

Time limit: please refer to DOM Judge  
Memory limit: please refer to DOM Judge

There are  $n$  cities and  $m$  roads connect some of the cities. Sometimes, certain roads are under maintenance and we cannot go through the roads. After assessment, there are at most  $k$  roads under maintenance at the same time.

Your task is to determine the minimum number of road need to be added so that there is always a path from city 1 to city  $n$  at any moment.

Note that after adding these roads, there may be some cities  $u, v$  such that there is more than one road from  $u$  to  $v$ . The added road may also under maintenance.

### Input

The first input line contains three integers  $n, m, k$ .

The  $i$ -th of the next  $m$  lines contains two integers  $u_i, v_i$ , which means there is a road from city  $u_i$  to city  $v_i$ . For every pair of cities  $u, v$ , there is at most one road from  $u$  to  $v$ .

- $2 \leq n \leq 500$
- $1 \leq m, k \leq 1000$
- $1 \leq u_i, v_i \leq n$

### Output

Print an integer  $h$ : The minimum number of road need to be added so that there is always a path from city 1 to city  $n$  at any moment.

### Examples

Standard Input	Standard Output
6 7 2 1 2 1 3 2 6 3 4 3 5 4 6 5 6	1

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## Problem E. Link Cut Treap

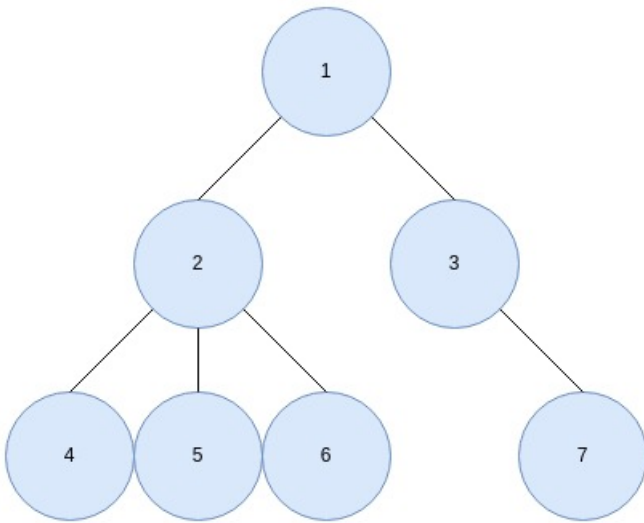
Time limit: please refer to DOM Judge  
Memory limit: please refer to DOM Judge

You are given a rooted tree with  $n$  vertices and  $n - 1$  edges. The tree is rooted at vertex 1.

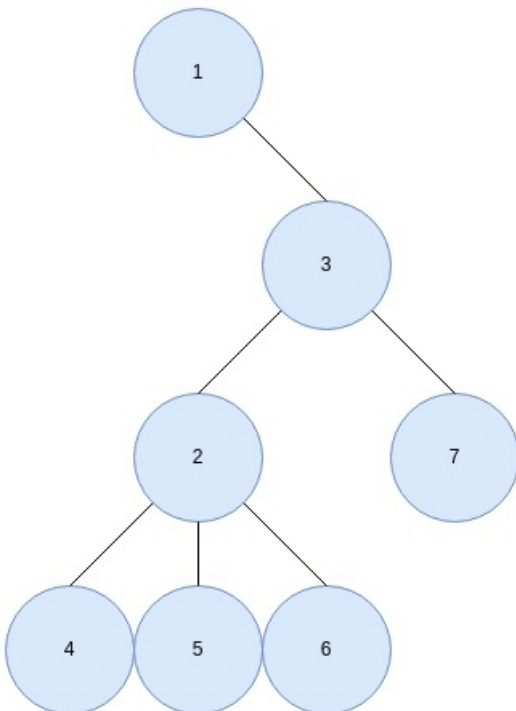
You are asked to perform  $q$  operations. There are 2 types of operations:

- For  $type = 1$ , cut the subtree rooted at  $u$  and link its parent to  $v$ .
- For  $type = 2$ , output the maximum vertex id in the subtree of  $p$ .

Here's an example of a tree rooted at vertex 1.



After an operation of  $type = 1, u = 2, v = 3$ , the tree becomes



Please output an integer for each operation of  $type = 2$ .

## Input

The first input line contains an integer  $n$ : the number of vertices of the tree.

After that, there are  $n - 1$  lines. Each line consists of 2 integers  $x$  and  $y$ , representing that there is an edge between  $x$  and  $y$  in the tree.

The next line contains an integer  $q$ : the number of operations.

After that, there are  $q$  lines describing the operations. The format of each operation is one of the following: " $1\ u\ v$ " or " $2\ p$ ".

- $3 \leq n, q \leq 2 \cdot 10^5$
- $type \in \{1, 2\}$
- $1 \leq u, v \leq n$
- For  $type = 1$  operations,  $v$  is guaranteed not in subtree of  $u$ .

## Output

Please output an integer for each operation of  $type = 2$ .

## Examples

Standard Input	Standard Output
7 1 2 3 1 5 2 2 4 6 2 3 7 7 2 2 2 3 2 6 1 2 3 2 2 2 3 2 6	6 7 6 6 7 6
3 1 2 1 3 7 2 1 2 2 2 3 1 3 2 2 1 2 2 2 3	3 2 3 3 3 3

## Problem F. Rectangles Perimeter

Time limit: please refer to DOM Judge  
Memory limit: please refer to DOM Judge

Given  $n$  rectangles, your task is to calculate the total perimeter length of their boundary.  
Here is an example with 7 rectangles is shown in Figure 1.

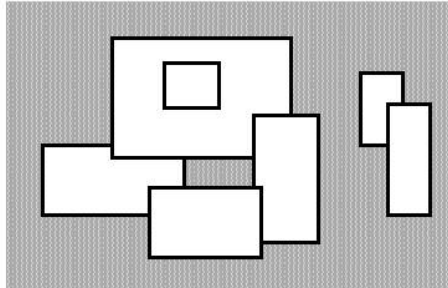


Figure 1. A set of 7 rectangles

The corresponding boundary is the whole set of line segments drawn in Figure 2.

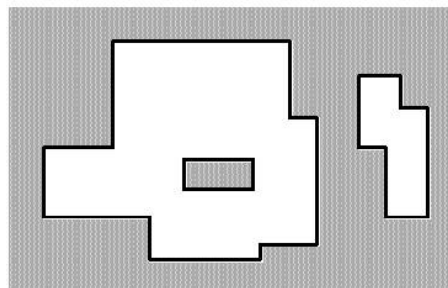


Figure 2. The boundary of the set of rectangles

### Input

The first input line contains an integer  $n$ : the number of rectangles.

After that, there are  $n$  lines describing the rectangles. Each line has four integers  $x_1, y_1, x_2$  and  $y_2$ : a rectangle begins at point  $(x_1, y_1)$  and ends at point  $(x_2, y_2)$

- $1 \leq n \leq 10^5$
- $-10^6 \leq x_1, x_2 \leq 10^6$
- $-10^6 \leq y_1, y_2 \leq 10^6$

### Output

The output must contain a single line with a non-negative integer which corresponds to the perimeter for the input rectangles.

## Examples

Standard Input	Standard Output
7 -15 0 5 10 -5 8 20 25 15 -4 24 14 0 -6 16 4 2 15 10 22 30 10 36 20 34 0 40 16	228
3 0 0 1 1 1 0 2 1 2 0 3 1	8
2 0 0 1 1 1 1 2 2	8