

Performance of Magnetic Refrigerators Operating with Different Magnetic Profiles

Fábio P. Fortkamp · Gusttav B. Lang · Jaime A. Lozano · Jader R. Barbosa Jr.

Abstract Magnetic refrigeration is a technology based on the concept of the active magnetic regenerator (AMR), which is a solid porous matrix of magnetocaloric material that undergoes temperature variations according to changes in the magnetization synchronized with oscillatory fluid flows. The magnetic field can be applied to the AMR in different profiles (waveforms). In this work, the performance of a magnetic refrigerator is evaluated in terms of two of the most common magnetic profiles: an instantaneous profile and a rectified cosine profile. The results show that the performance of an AMR operating with the instantaneous profile is consistently better than an AMR using the cosine profile with the same average high magnetic field and same minimum value, and that this improvement is higher for larger utilizations (ratio of solid to fluid thermal capacities). For an AMR frequency of 1 Hz and an utilization of 1.0, the cooling capacity of an AMR device operating with the instantaneous profile was 196.3 % higher than the equivalent rectified cosine profile. The instantaneous profile was then analyzed in more detail, and it was concluded that using high values of magnetic field allows for smaller regenerators and lower mass flow rates to keep a desired level of cooling power.

Keywords magnetic refrigeration · active magnetic regenerator · numerical modeling · magnetocaloric effect

1 INTRODUCTION

An active magnetic regenerator (AMR) is a thermal regenerator composed of a solid porous matrix of magnetocaloric material, which changes its temperature according to the application of a varying magnetic field in synchronization with oscillatory fluid flows, due to the so-called magnetocaloric effect (MCE). Active magnetic regenerators are employed in magnetic refrigeration, a promising alternative to vapor compression systems due to its use of

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non-gaseous refrigerants and potentially higher thermodynamic efficiency [?]. A magnetic refrigerator may contain multiple regenerator beds, in combination with rotary permanent magnets, to achieve higher levels of performance [1].

The time variation of the magnetic field experienced by an AMR is known as the magnetic profile. The magnetic profile is directly related to the thermodynamic cycle that drives the magnetic refrigerator, and therefore has an important influence on its performance. AMRs can operate according to different thermodynamic cycles, but the most common is the Brayton AMR cycle, which has two isentropic processes of instantaneous magnetization and demagnetization of the magnetocaloric material and two isofield processes [2], as shown in Fig. 1. In practice, it is difficult to generate stepwise variations of the magnetic field (as required by the Brayton cycle) using permanent magnets arrays (the apparently only viable solution for domestic magnetic refrigerators due to low cooling requirements and energy consumption). Most magnetic refrigerators developed so far operate with a more continuous magnetic profile, such as the rectified cosine profile [3–5], which is easily generated with compact devices and capable of achieving high levels of magnetic field [1], but at the cost of too brief demagnetization periods.

Fig. 1: Temperature-entropy diagram for the Brayton AMR cycle, as experienced by the magnetocaloric (MC) material [2]. The applied magnetic field is denoted by H .

In Fig. 2, the instantaneous and rectified cosine waveforms evaluated in this work are shown in terms of the average applied magnetic field (\bar{B}) that acts on the regenerator (vertical axis) for one AMR cycle parameterized in a time variable (t) ranging from 0 to the cycle period τ (horizontal axis).

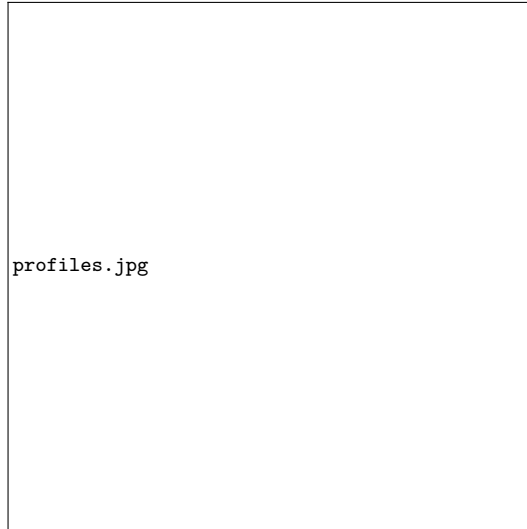


Fig. 2: Instantaneous and rectified cosine magnetic profiles in terms of the average magnetic field over the regenerator for one AMR cycle as a function of time (t).

Besides the applied magnetic field variations shown in Fig. 2, an AMR cycle is also composed of two hydraulic processes: (i) cold blow, occurring after the magnetization, where cold fluid flows through the porous matrix to absorb energy from it and rejects heat to an external hot source, and (ii) hot blow, occurring after the demagnetization, where the magnetocaloric material is cooled down and removes heat from the fluid flowing, which then can absorb the thermal load from the cold source.

Many works on the analysis of magnetic profiles used a ramp profile as an approximation of the instantaneous profile with finite transition times between the magnetization levels, making it easier to generate the profiles with permanent magnets. The performance of an AMR subjected to a ramp profile with different parameters was performed by [6], but the emphasis was on the synchronization with the fluid flow profile and the authors did not compare different magnetic profiles. The previously cited investigation by [2] implemented different cycles through a ramp profile and a modification of the rectified cosine (consisting only of linear variations), and concluded that, with the same operating parameters parameters (temperature span between heat source and heat sink, frequency, mass flow rate, regenerator geometry, maximum applied magnetic field), the Brayton cycle (realized by a ramp profile) results in the highest cooling capacities; the same profile could be used in Ericsson cycles, with the magnetization processes done isothermally instead of adiabatically, and the result is higher values of the coefficient of performance. A comparison of different magnetic profiles for an AMR device was also performed by [7], and the authors concluded that, for same levels of maximum and minimum magnetic field, the instantaneous profile results in higher cooling capacities for a given temperature span.

The present work extends these analyses and attempts to systematically compare the performance of a magnetic refrigerator operating with instantaneous and rectified cosine profiles under different parameters, with the goal of selecting the best magnetic profile for certain requirements of cooling capacity of a target application. In comparison with the previously cited works, we analyze the effect of different regenerator geometries and different levels of the magnetic field and mass flow rate. In particular, in comparison with the work of [2], where the authors studied different combinations of flow and magnetic profiles to yield various thermodynamic cycles, we fix the fluid flow profile to better investigate the effect of the magnetic profile, which is used in the design of magnetic circuits.

2 NUMERICAL SIMULATIONS

Simulations were performed using a one-dimensional AMR mathematical model [7,8]. The simulated magnetic refrigerators are composed of multiple prismatic regenerators filled with gadolinium (Gd) spheres as the magnetocaloric solid matrix, with the parameters shown in Table 1. The fluid is a mixture of water and ethylene glycol, in the proportion of 80 %-20 % in volume.

The AMR model solves mass and energy conservation equations for the solid and the fluid domains in an active magnetic regenerator. In this work, regenerators were assumed to be adiabatic to the environment. All beds experience the same flow and magnetic profiles, as detailed in the following sections.

Table 1: Geometric and operation parameters for the simulated AMR devices

Parameter	Value
Regenerator height	20 mm
Regenerator width	25 mm
Regenerator length	100 mm
Number of regenerators	11
Particle diameter	0.5 mm
Hot source temperature	298 K
Cold source temperature	278 K

2.1 Flow profile

The flow profile through a given bed, i.e. the mass flow rate as a function of time $\dot{m}_f(t)$, is assumed to be a square wave as that shown in Fig. 3. The cold blow has a duration of τ_{CB} and the hot blow a duration of τ_{HB} , while the period of one AMR cycle is τ . Limiting the blow times during each half-cycle to periods where the magnetic field is at its maximum and minimum can result in increased performance [9]. In this work, the blows are supposed to be in balance, thus, $\tau_{CB} = \tau_{HB}$. An important parameter regarding the flow profiles can be defined, which is the blow fraction, F_B :

$$F_B = \frac{\tau_{CB} + \tau_{HB}}{\tau} \quad (1)$$

Fig. 3: Instantaneous flow profile used in the numerical simulations. "Positive" mass flow rate indicates flow in the direction from the cold to the hot source, and negative values represent the opposite direction.

2.2 Magnetic profile

The AMR mathematical model takes the magnetic profile as an input, and the profiles represented in Fig. 2 were tested with different parameters. The mathematical definitions for the magnetic profiles over a cycle of period τ are as follows; the instantaneous profile (represented by the index "I") and the rectified cosine profile (represented by "RC") are defined solely in terms of the extrema values B_{\max} and B_{\min} :

$$\bar{B}_I(t) = \begin{cases} \bar{B}_{\max}, & 0 \leq t < \tau/2 \\ \bar{B}_{\min}, & \tau/2 \leq t < \tau \end{cases} \quad (2)$$

$$\bar{B}_{RC}(t) = B_{\min} + (B_{\max} - B_{\min}) \left| \cos \left(\frac{\pi}{\tau} \left(t - \frac{\tau}{4} \right) \right) \right| \quad (3)$$

In this work, the average values of the magnetic field during each half-AMR cycle are considered for comparison between profiles. The average magnetic profile during the hot cycle ($0 \leq t < \tau/2$) is denoted B_h and the average during the cold cycle ($\tau/2 \leq t < \tau$) is denoted B_l .

2.3 AMR operating parameters

Different numerical simulations were carried with different operating parameters such as: AMR cycle frequency (f), blow fraction (F_B) and utilization (Φ) which is defined as:

$$\Phi = \frac{\dot{m}_{f,\max} F_B \frac{\tau}{2} c_{p,f}}{m_s c_s} \quad (4)$$

where $c_{p,f}$ is the constant-pressure specific heat for the fluid, and m_s and c_s are the mass and specific heat of the solid phase in one bed.

3 RESULTS AND DISCUSSIONS

3.1 Comparison of the instantaneous and rectified cosine profiles

When comparing the magnetic profiles, the average magnetic field during the hot cycle is the same; this implies in a higher peak for the rectified cosine. For the cold cycle, there are two possible comparison methods:

1. The minimum values for both profiles is the same;
2. The average value for both profiles during the cold cycle is the same.

As a reference, in all simulations the minimum value for the rectified cosine was fixed at $\bar{B}_{\min,RC} = 0.1$ T. For the first comparison, the minimum value for the instantaneous value was kept at the same level ($\bar{B}_{\min,I} = \bar{B}_{\min,RC}$), hence, the average low value for the RC profile was higher ($B_{l,RC} > B_{l,I}$). Although this does not seem a fair comparison, in practice it is feasible to generate a profile with a constant low-valued plateau for the magnetic field [?,10]. For the other comparison method, the low level of the instantaneous profile was increased ($\bar{B}_{\min,I} > \bar{B}_{\min,RC}$) to keep the average the same ($B_{l,RC} = B_{l,I}$). In addition, simulations were ran for various values of blow fraction and the optimal cases were selected; the rectified cosine profile can benefit from a smaller blow fraction because this can concentrate the flow during the periods of very high or low fields. In this section, all results show the resulting optimal case of the blow fraction for each profile (for the values tested): fluid flowing during the entire period for the instantaneous profile, and only during 60 % of the period for the cosine profile.

Figure 4 shows the cooling capacity attained by the device at a frequency of 1 Hz and different utilizations, for both comparison methods. The horizontal axis shows the average value during the high field region. Notice how the results are conflicting; for Fig. ??, the instantaneous profile almost always yields a higher performance, while for Fig. ?? the rectified cosine profile generates higher cooling capacities. Since the average during the hot cycle (high field stage) is the same, the main difference is due to the low magnetic field levels. For the “same minimum” comparison, the instantaneous profile is capable of keeping the magnetic field at low levels for the whole half-cycle, which is beneficial for performance; for $\Phi = 1.0$ and $B_h = 1.40$ T, the cooling capacity for the instantaneous profile is 196.3 % higher than for the cosine profile. As demonstrated by [7], a higher average magnetic field during the low-field stage increases the solid temperature and consequently results in warmer fluid entering the cold heat exchanger, representing a thermal loss. In the “same-average” comparison, the cosine profile is capable of achieving much lower levels (since its minimum value is fixed), therefore providing more cooling power. However, as explained before, it is possible to design near-instantaneous profiles with very low levels of the magnetic field.

Fig. 4: Cooling capacity as a function of the average high magnetic field, for different utilizations. “I”: instantaneous (blow fraction of 100 %); “RC”: rectified cosine (blow fraction of 60 %), for both comparison methods.

The only exception in the “same minimum” comparison is seen for the lowest utilization of $\Phi = 0.2$, where the performance is slightly better for the RC profile. Since the blow fraction for the cosine is lower, the mass flow rate must be higher to yield the same utilization (cf. Eq. (4)), and this increases heat transfer rate, as previously explained — outweighing the effects of the magnetic field.

In general, the performance of the AMRs operating with the instantaneous magnetic profile yields better results. As can be seen on Fig. 4, an instantaneous profile with the lowest possible value of B_{\min} and the highest possible value of B_{\max} , with a flow profile occupying the whole cycle with average values of utilization, results in the highest values of cooling capacity among all simulations, therefore, representing the ideal magnetic profile for an AMR.

3.2 Analysis of the instantaneous profile

As shown in the previous section, the instantaneous profile yields the highest values for cooling capacity. Therefore, in this section, a more detailed analysis of such profile has been carried out. Figure 5 shows the cooling capacity as function of utilization, for several levels of the maximum magnetic field for the instantaneous profile, for two different operating frequencies. Because of the conflicts between a low heat transfer rate for flow rates too low and a loss in regenerator effectiveness in flow rates too high, there are critical values of utilization that maximize cooling capacity, and this critical value grows with the level of magnetic field. With higher magnetic field, the increase in the MCE surpasses the loss of effectiveness, and one can go to higher flow rates without losing performance. It can also be seen in Fig. 5 that at higher frequencies, the values of cooling power are higher, and also the critical values of utilization are lower; however, this usually is achieved at the cost of higher power consumption in AMR devices at higher frequencies [11, 12].

The parameters in Table 1 were chosen from preliminary simulations, but they are not guaranteed to be the optimal choices. To understand the impact of regenerator geometry on the performance with the instantaneous profile, the regenerator height was varied in Fig. 6, and all other parameters from Table. 1 were kept fixed. As expected, higher magnetic fields allow for smaller regenerators (and hence more compact systems). For instance, to achieve a capacity of 100 W, increasing the field from 1.0 to 1.2 T result in using regenerators 36 % smaller.

4 CONCLUSIONS

A one-dimensional AMR numerical model was used to compare the performance of a magnetic refrigerator under different operating and geometric parameters and with the instantaneous and rectified cosine magnetic profiles. Most of the AMRs operating with an instantaneous magnetic profile have resulted in better performances than those with a cosine profile, except in cases of low utilization. Although the cosine profile reaches higher levels of the

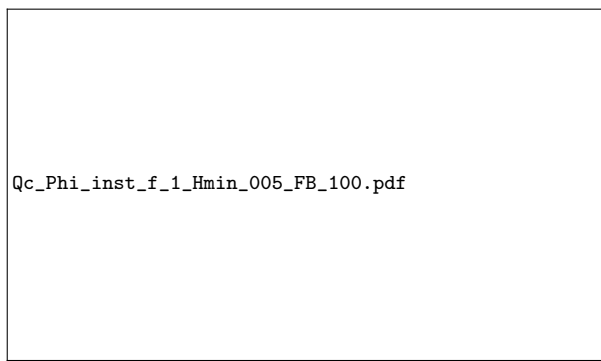
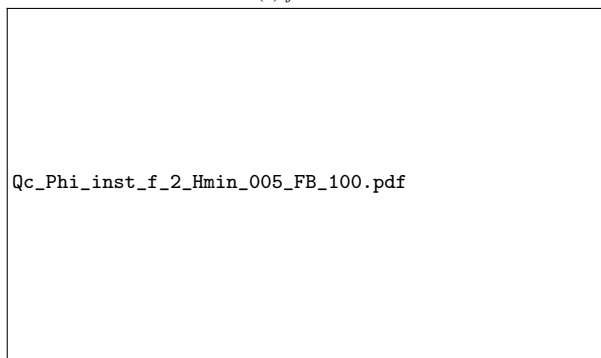
(a) $f = 1 \text{ Hz}$ (b) $f = 2 \text{ Hz}$

Fig. 5: Cooling capacity as a function of utilization, for various values of the high magnetic field of the instantaneous profile

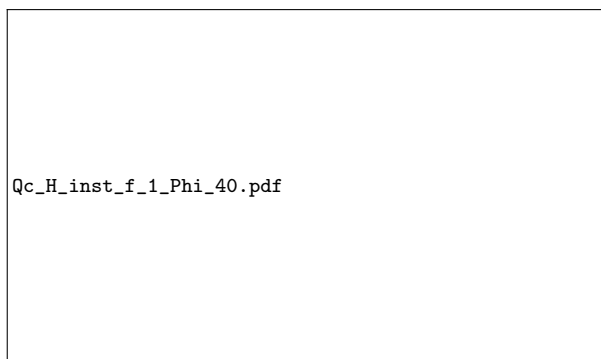


Fig. 6: Cooling capacity as a function of regenerator height (all other parameters from Table 1 constant) for various values of the high magnetic field of the instantaneous profile

magnetic field, the instantaneous profile can keep the magnetization (and demagnetization) for a longer period, which is shown to be beneficial to performance. Further analysis of the instantaneous profile has shown that the use of the highest possible value of the maximum

magnetic field allows for using smaller regenerators and lower utilization, without losing performance.

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