

# Cyberfood

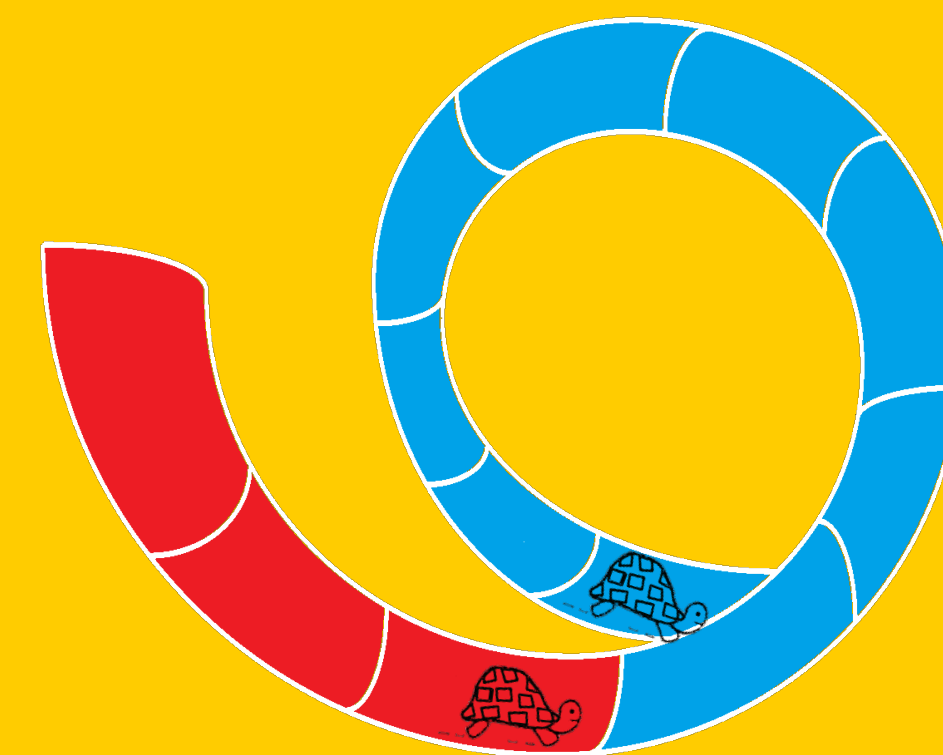
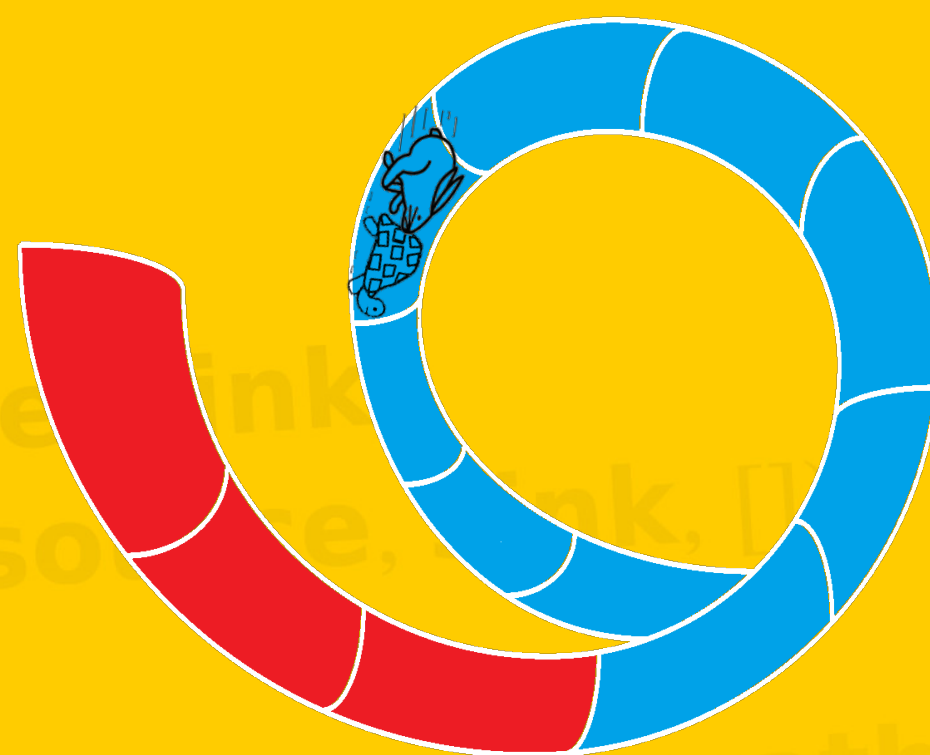
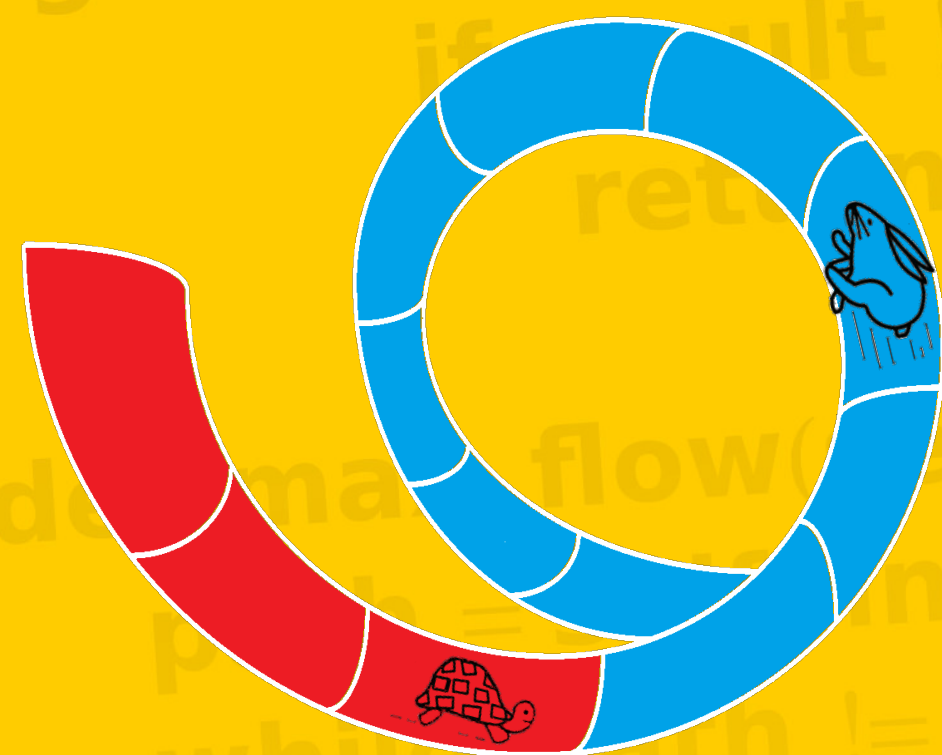
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## Easy: How many flavors are in the list?



Turtle moves at speed one

Bunny moves at speed two



- Suppose the list is composed of a tail of length  $T$  and a cycle of length  $C$
- Turtle and bunny start simultaneously from the beginning of the list at time 0
- They enter the cycle at time  $T$ , when the bunny has an advance of  $T$

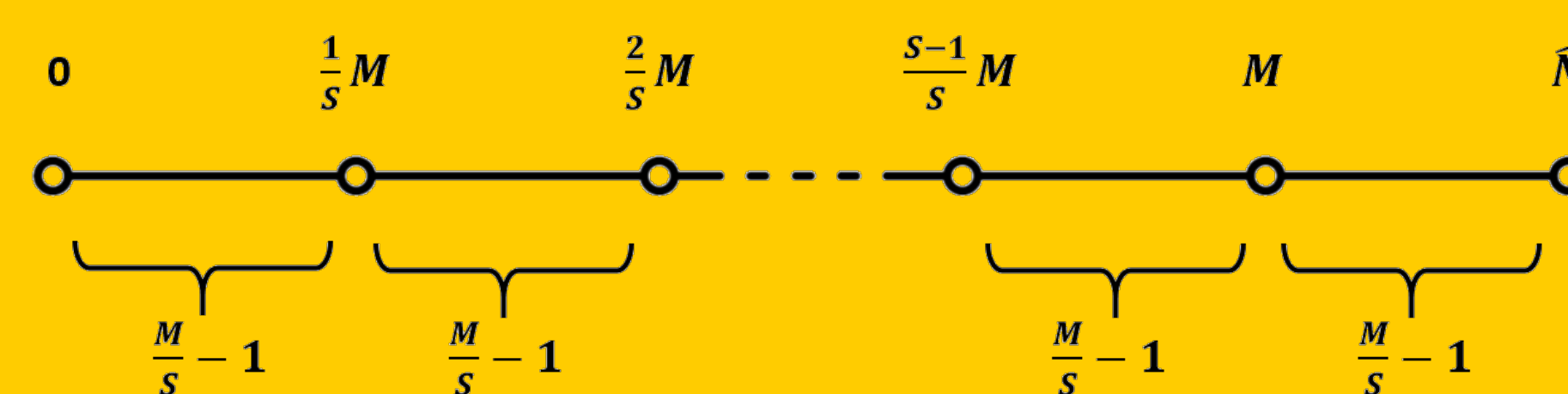
They meet back after some time  $T+X$  such that  $X = T+2X \pmod{C}$ , i.e. at time  $C$ .

- Right now start a second turtle at the beginning of the list.
- As a matter of fact both turtles will meet at time  $C+T$  at the cycle's entry!

## Medium: How many flavors do exist?

- Flavours are uniformly distributed between 1 and  $N$
- Let  $M$  be the maximum of the  $S$  samples
- The minimum-variance unbiased estimator of  $N$  is  $\hat{N} = M + \frac{M-S}{S}$

Imagine your  $S$  samples evenly space throughout the range.



The gap between two samples is  $\frac{M}{S} - 1$

## Hard: Exploration-Exploitation trade-off

- Exploration : Try leaves from different trees to enhance your estimate of their probability to please Heidi.
- Exploitation : Prefer leaves from trees that are most likely to please Heidi
- Trade-off : You need to balance these two components in your decisions

Be creative ;- ) and use any reinforcement learning approach (sampling, backtracking, heuristics, ...)

An astonishingly trivial and fast, but efficient solution is:

#tasty leaves  $\leftarrow$   $\rightarrow$  total #leaves

Optimistic initialization  $s[i]=t[i]=1$

Act greedily : pick leave from tree with highest probability  $s[i]/t[i]$

Update  $s[i]$  according to Heidi's feedback

