

Quarantine

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Easy: How many white pixels in row r / column c ?

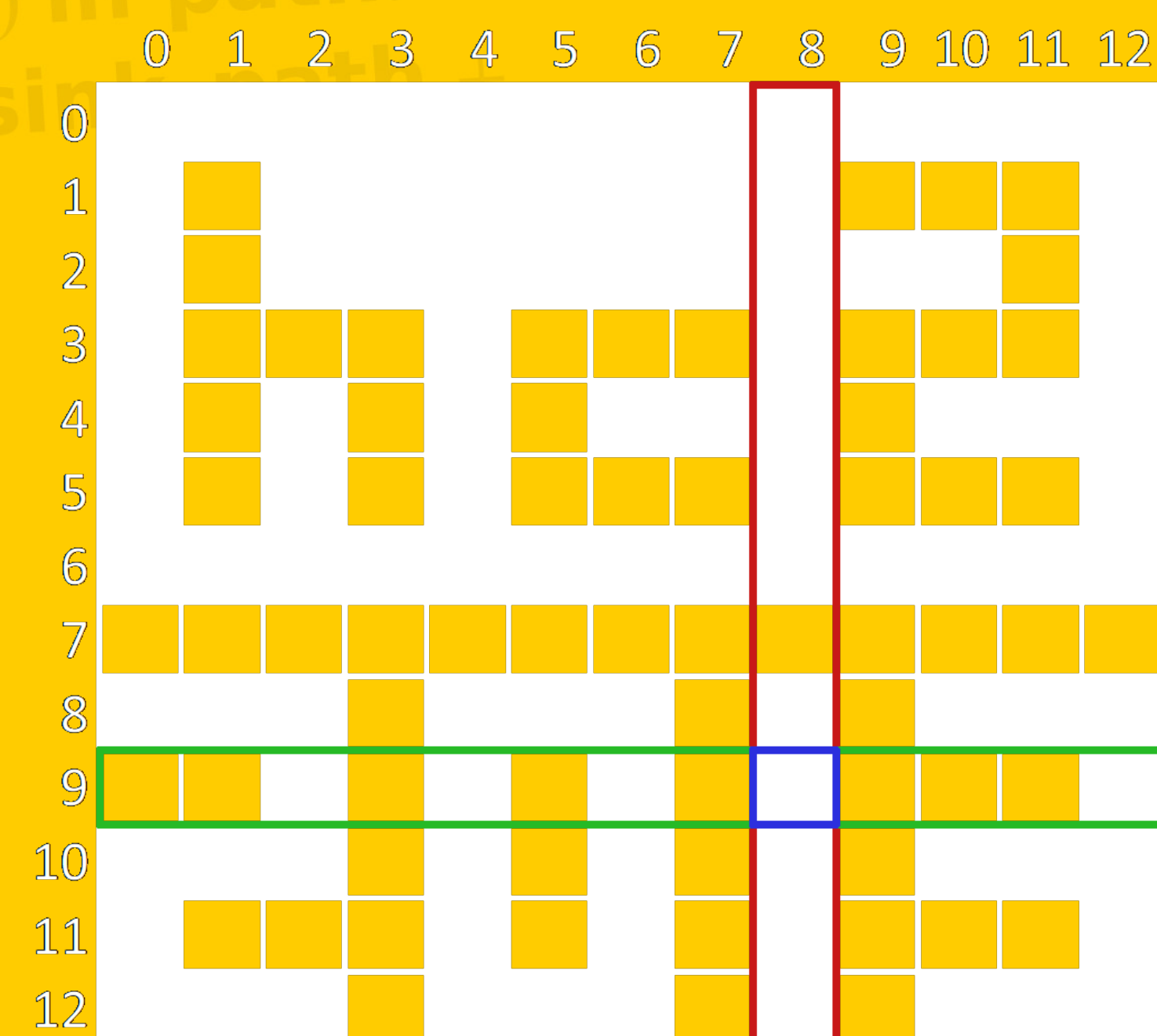


Count pixels for each query
 $\Rightarrow O(N \cdot Q)$

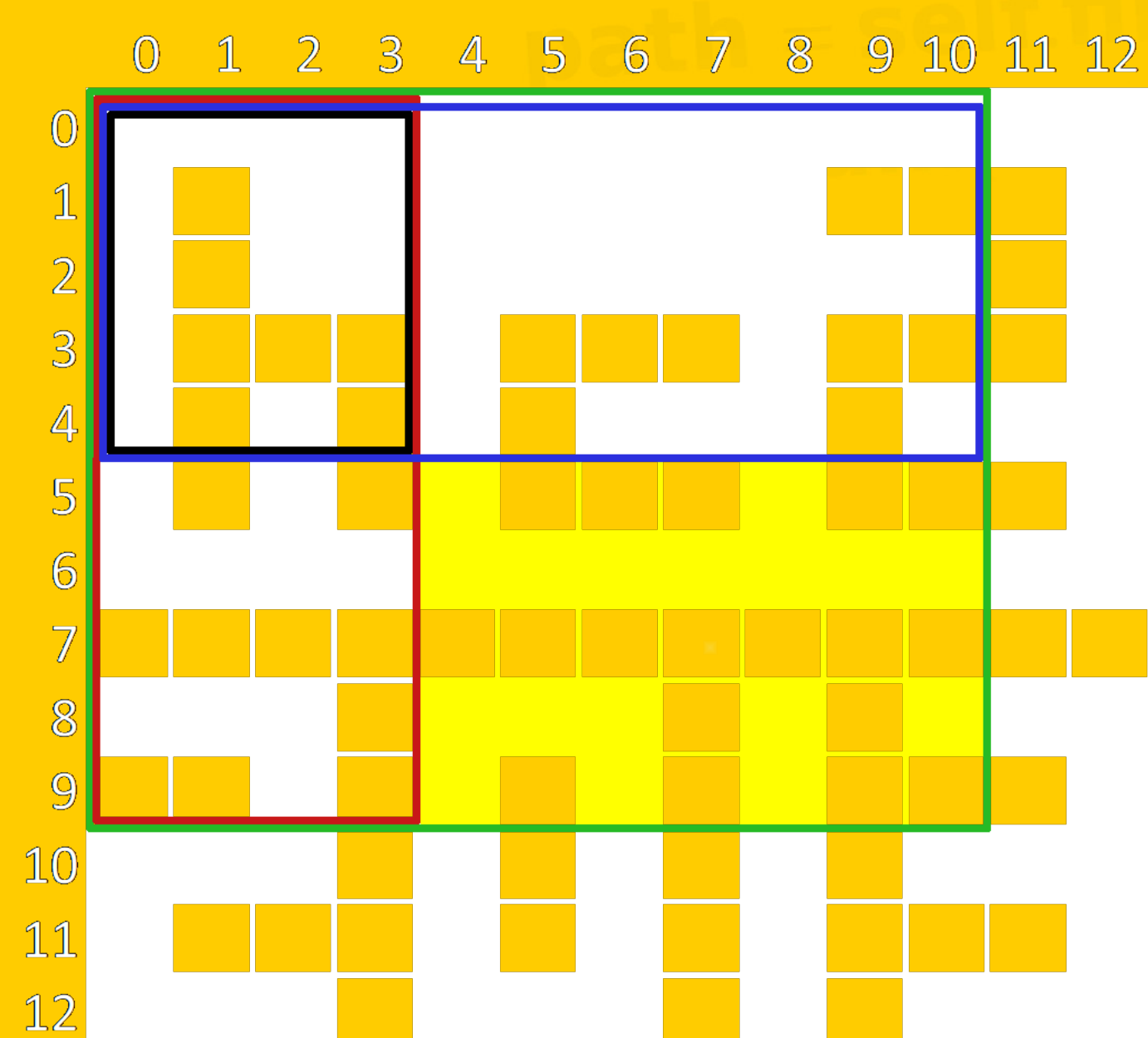
Count pixels once for each row and column!

Answer: $\text{row}[r] + \text{column}[c] - \text{pixel}[r][c]$

$\Rightarrow O(N^2 + Q)$



Medium: How many white pixels in a rectangle?



Count pixels for each query
 $\Rightarrow O(N^2 \cdot Q)$

Count once the pixels for each rectangle $[0..r] \times [0..c]$

Answer: $\text{rect}[r2][c2] - \text{rect}[r2][c1-1]$

$- \text{rect}[r1-1][c2] + \text{rect}[r1-1][c1-1]$

$\Rightarrow O(N^2 + Q)$



Hard: Is pixel (r, c) white after a series of toggles?



Simply simulate all toggles... $\Rightarrow O(N^2 \cdot Q)$

Replace each toggle with four toggles of rectangles rooted at the origin.
Use a fancy data structure to keep track of toggles :-)

- 2D Binary Indexed Tree
- Quad Tree
- 2D Interval Tree



Answer: $\text{count}(r2, c2) - \text{count}(r2, c1-1) - \text{count}(r1-1, c2) + \text{count}(r1-1, c1-1)$

$\Rightarrow O(Q \cdot \log^2 N)$

