



# Types for fun and profit\*

Part 1: Types and the Arcs Type Lattice

[go/arcs-types-for-fun-and-profit](https://go/arcs-types-for-fun-and-profit)

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Please call me 'J', they, them

\*Neither fun nor profit are guaranteed, conditions may apply :P



**(Just to make sure we're on the same page)**

Note: some of this is open to interpretation and I do make mistakes, please feel free to stop me if something seems off or there are questions.



# What do I mean when I say 'Type'

Broadly: “a category of people or things having common characteristics.”

- [Oxford Languages and Google - English](#)



# What do I mean when I say 'Type'

In Programming: “a category of ‘values’ having common characteristics.”

Aside: the definition of value is almost as vague as thing, but it makes me feel better [Wikipedia: Value](#)



# What do I mean when I say 'Type'

In Programming: “a category of ‘values’ having common characteristics.”

Examples from Kotlin:

```
val x: Int = 3
```

```
val value: (it: String) -> Int = {it.length}
```



# What do I mean when I say 'Type'

In Programming: “a category of ‘values’ having common characteristics.”

Examples from Arcs:

x: `Text`

oncall: reads `Employee {name: Text, employee_id: Long, uname: Text}`



# What do I mean when I say 'Type'

A syntactic phrase/expression that describes what 'actions' can be performed on/with a value.

Examples from Arcs in Kotlin:

with `oncall: reads Employee {name: Text, employee_id: Long, uname: Text}`

```
println("${oncall.name}")
```

```
println("${oncall.employee_id}")
```

```
oncall.name = "Some other name" // May be allowed but doesn't write to the DB
```



# What do I mean when I say 'Type'

A syntactic phrase/expression that describes what **functions can be called with a value as an argument** (+/receiver).

Examples from Arcs in Kotlin:

```
// with oncall: reads Employee {name: Text, employee_id: Long, uname: Text}
```

```
println("${oncall.name}")
```

```
println("${oncall.employee_id}")
```

```
oncall.name = "Some other name" // May be allowed but doesn't write to the DB
```





# What do I mean when I say 'Type system'

A model that relates Types to the set of allowed/expected behaviours in a context (normally a programming language).

This links syntax with semantics



# What do I mean when I say 'Type theory'

The study of Types & Type systems



# What do I mean when I say 'a Type theory'

A model that relates Types to the set of allowed/expected behaviours.

This links syntax with semantics.



# What do I mean when I say 'a Type theory'

Normally you can just think about a Type theory as a family of Type systems that share a bunch of properties, rules and conventions



**But what are Types for?**

**SAFETY**

But what are Types for?





## But what is Type Safety?

[Type] Safety: Progress + Preservation

Progress: A well typed program will not get into an invalid state

This means will work until it termination or error (infinite loops & errors typically don't count)

Preservation: Evaluation won't break any 'rules' of the type system

In other words: Safety means that the language won't violate it's own abstractions



## But what is Type Safety?

[Type] Safety: Progress + Preservation

Mostly we care about preservation.

We're interested in catching human error, before runtime to minimize the exhaustiveness of testing needed to gain confidence that a program is correct.



But what is Type Safety?





## But what is Type Safety for?

Bugs often caught using Types:

- Illegal operations (i.e. division by string, negation of unsigned integers, array access into an Int etc.)
- Buffer overflow
- Logic errors:
  - e.g. [Mar climate orbiter vs units](#), [units: A domain-specific type system for dimensional analysis](#)
- Memory safety (Rust can catch use after free at compile time [at a 'small' cost])

There's also some nice side benefits:

- Intellisense + type directed look up + feedback
- Rust & Haskell's derivation systems for generating code where needed based on types

Note: **Some languages let you break the rules**



Note: **Some languages have very flexible rules**



Note: **Some languages don't have (type based) rules**





# A refresher on Arcs' Type system

- Primitive Types:
  - Text, URL, Number, BigInt, Boolean, Bytes, Instant, Duration
  - Kotlin Types: Byte, Short, Int, Long, Char, Float, Double
- Types:
  - Unions: (t or s or u)
  - Tuples [Products]: (t, s)
  - Collections: [t]
  - Ordered Lists: List<t>
  - Singletons: ![e]
  - Nullables: t?
  - References: &e
  - Refinements: e [p]
- Schemas + Entity Types:
  - Name { field: t }

## Lesser known Types:

- Interfaces
- Mux type: #t
- Slot type: Slot {}
- Big Collection type: BigCollection<t>
- Type variables: ~t
- Constrained Type variables: ~t with u
- NullType (Paxel)
- Object
- More?



# Subtyping / Assignability

Assuming there are two types  $t$  and  $u$ .  $t$  is a subtype of  $u$  where any value of  $u$  is also a value of  $t$ .

Example:

$t = \text{Int}$ ,  $u = \text{Long}$ .

$\text{Int}$  is a subtype of  $\text{Long}$

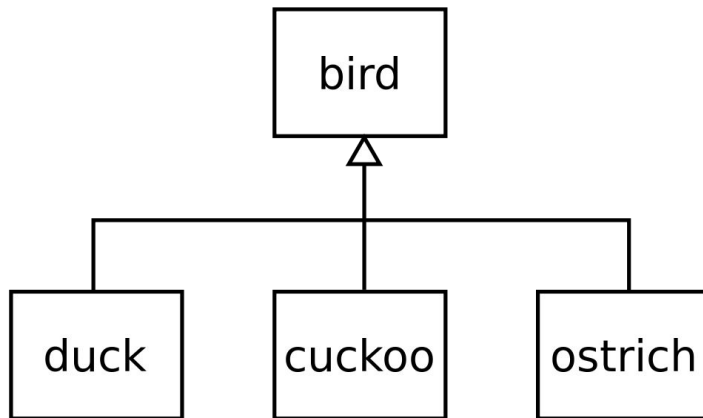
$x: \text{Int} = 3$

$y: \text{Long} = 3$

## Subtyping / Assignability

Another example:

All ducks are birds, so you can accept a duck wherever you need a bird.

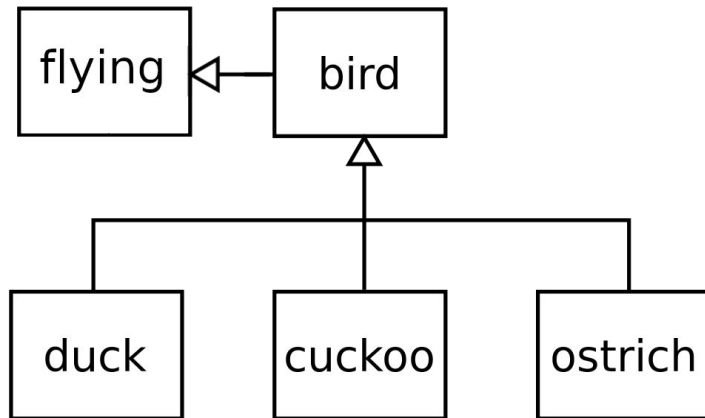




## Subtyping / Assignability

Counter example:

All birds can fly, so you can accept a bird wherever you need something that can fly.



## Subtyping / Assignability: type safe 'duck' types





# Subtypes + Supertypes

We can write 'X is a subtype of Y' as

$X <: Y$

Or

$X < Y$



## Subtypes + Supertypes

It's a **preorder** just like ' $<$ ', so there's a corresponding ' $>$ '

We can write ' $X$  is a supertype of  $Y$ ' as

$X \geq Y$

Or

$X > Y$



## Meet = (greatest) shared subtype

If two types share a subtype\*, that's called the **meet** (or *infimum*)

i.e.

If  $s \geq j, t \geq j$

then

*$j$  is the meet of  $s$  and  $t$*

*The meet type meets the requirements of both  $s$  and  $t$*



## Meet = (greatest) shared subtype

e.g.

The meet of  $s$  and  $t$

Where  $s = \text{Person Named \{name: Text, fav: Colour\}}$  and  $t = \text{Employee Named \{name: Text, id: BigInt\}}$  is  
 $\text{Named \{name: Text\}}$

*The meet type meets the requirements of both  $s$  and  $t$*



## Join = (least) shared supertype

e.g.

The meet of  $s$  and  $t$

Where  $s = \text{Person}\{\text{name: Text}\}$  and  $t = \text{Employee}\{\text{id: BigInt}\}$  is

$\text{Employee Person}\{\text{id: BigInt, name: Text}\}$

*The join type **joins**  $s$  and  $t$  and guarantees only things that are true of both*



## Join = (least) shared supertype

If two types share a supertype\*, that's called the **join** (or *supremum*)

i.e.

If  $s <: j$ ,  $t <: j$

then

*$j$  is the join of  $s$  and  $t$*

The join type **joins**  $s$  and  $t$  and guarantees only things that are true of both



## Subtypes + Supertypes

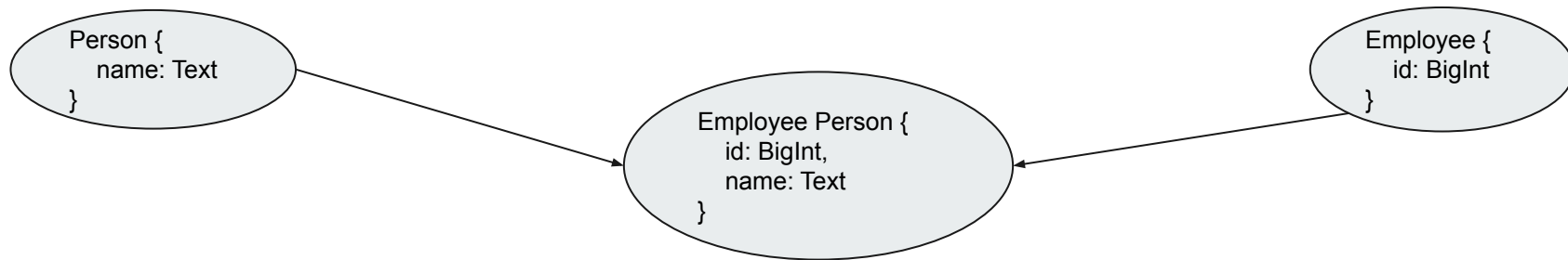


These relationships give us a 'lattice'



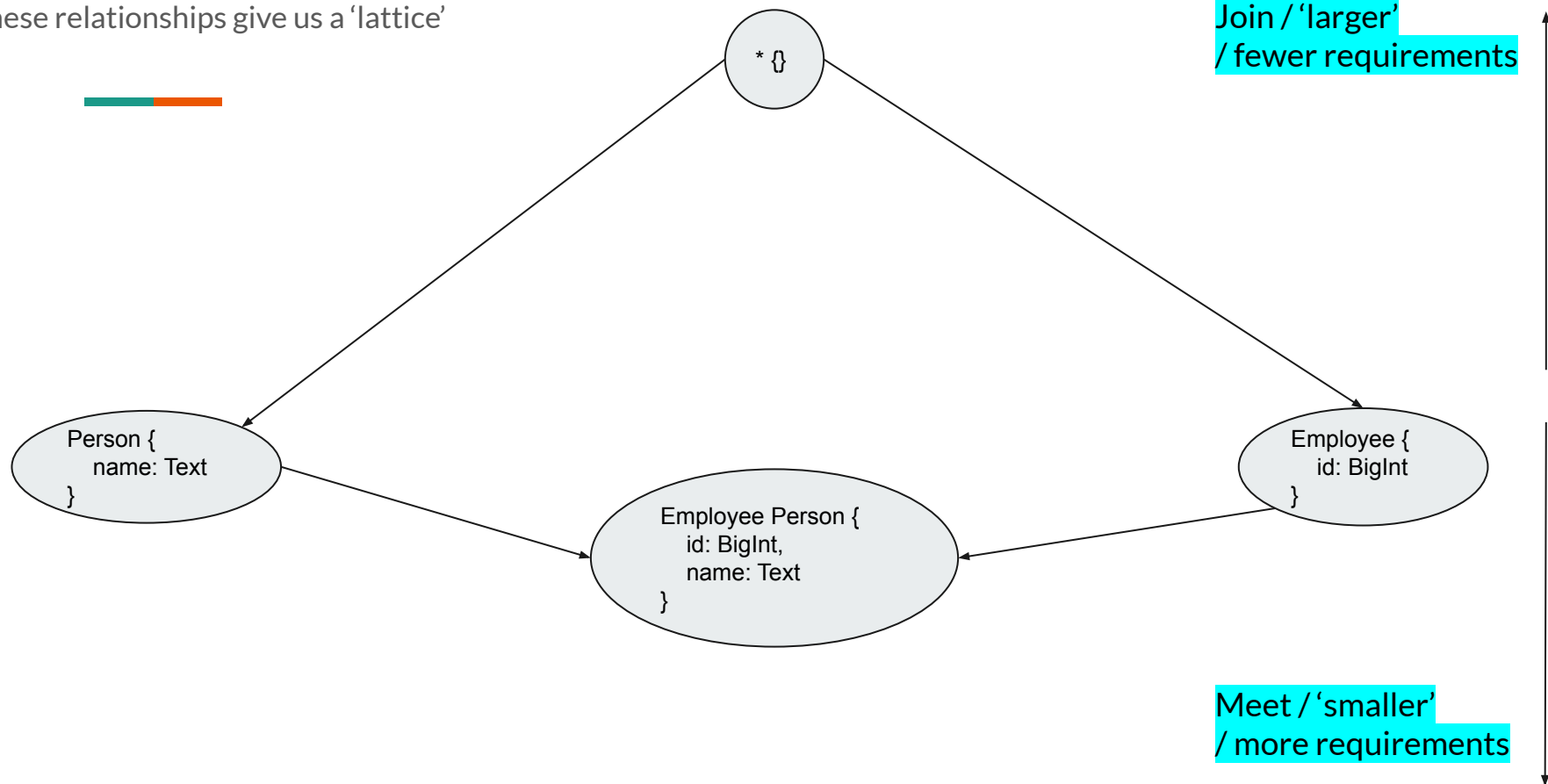
$X \longrightarrow Y$   
means  
 $X \supseteq Y$

Join / 'larger'  
/ fewer requirements

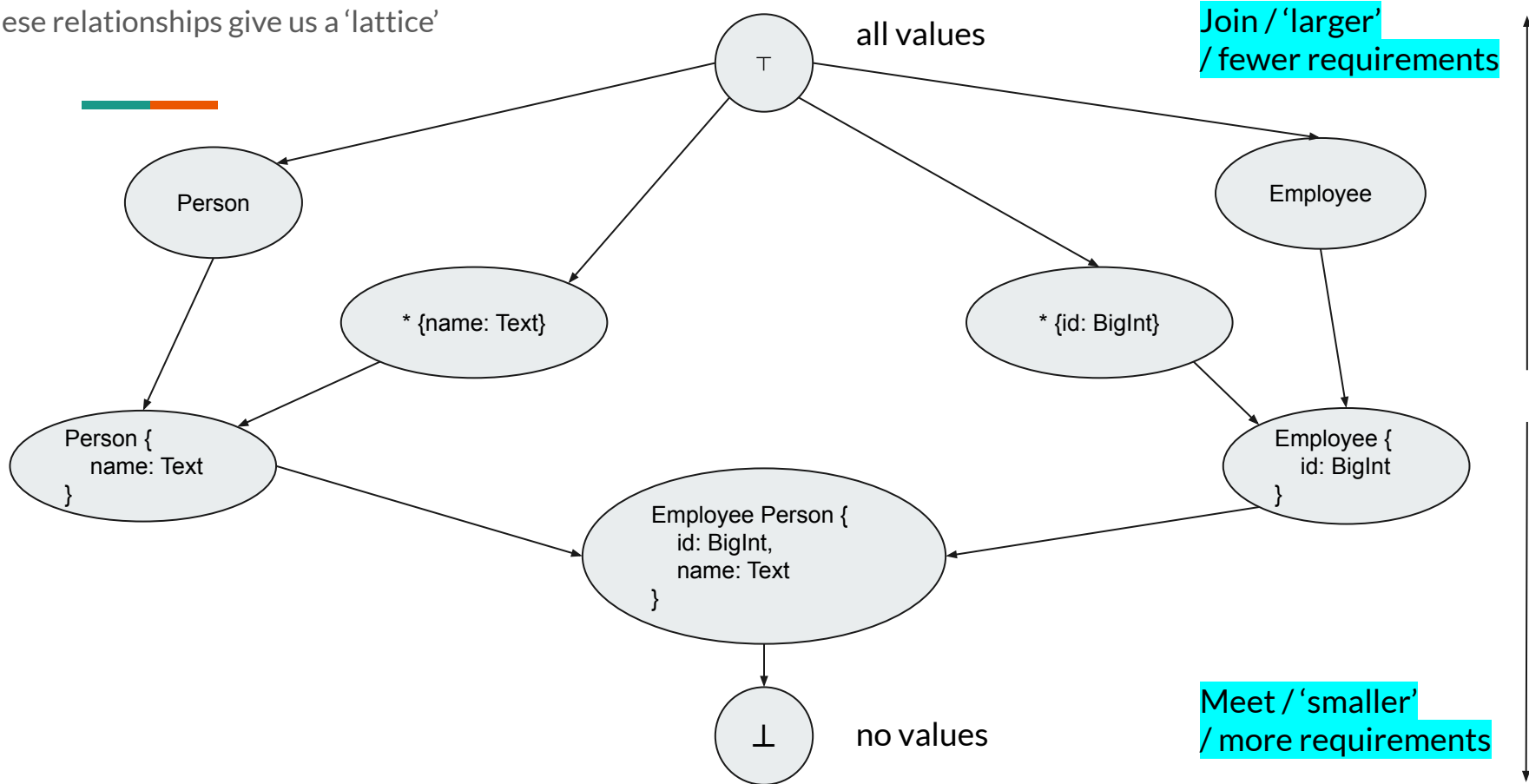


Meet / 'smaller'  
/ more requirements

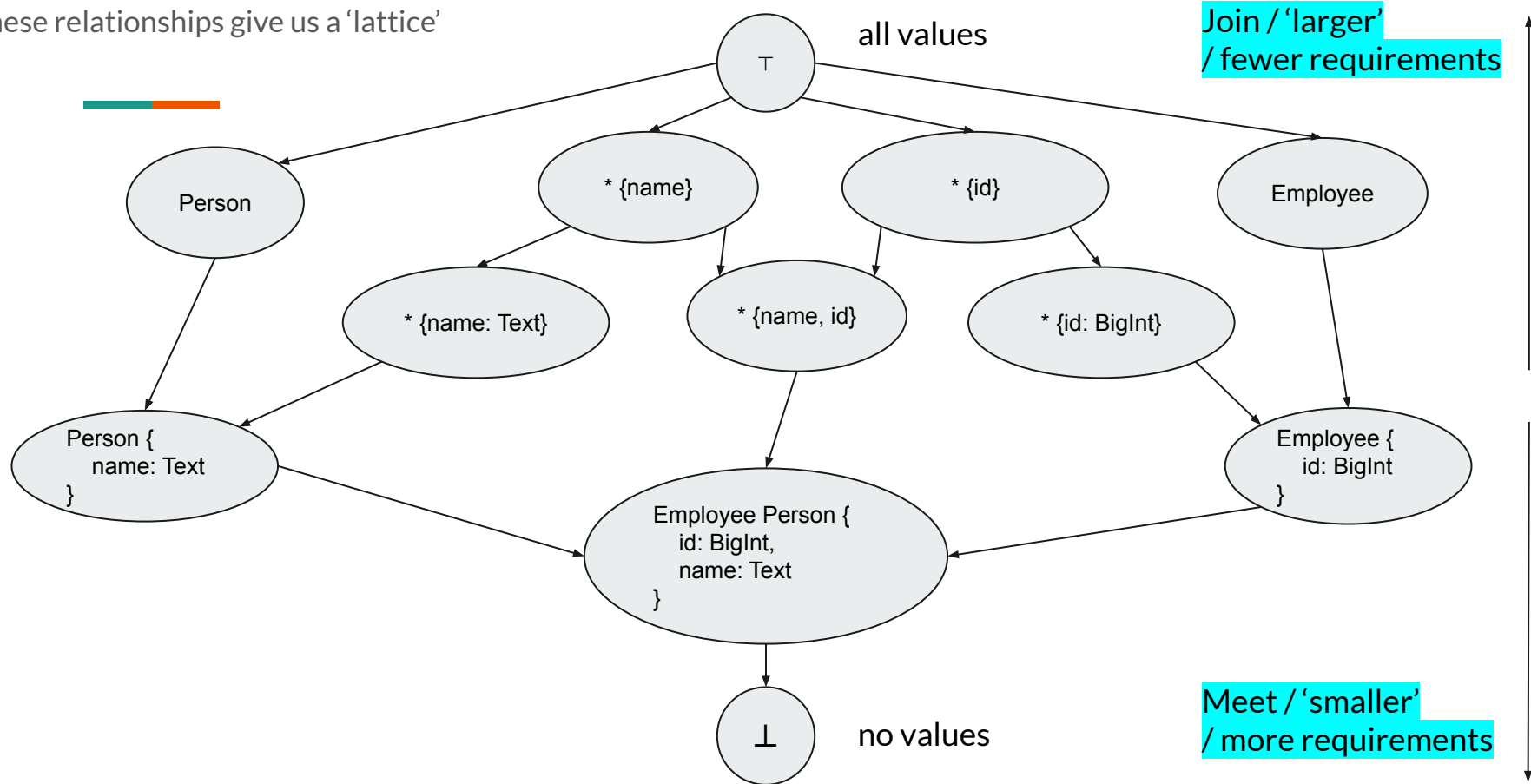
These relationships give us a 'lattice'



These relationships give us a 'lattice'



These relationships give us a 'lattice'





**What can you do with types?**

**BUILD MORE TYPES**



# What can you do with types?

- Refinement types
- Union types (oneof / unions)
- Product types (tuples, records, etc.)
- Dependent types
- Function types
- Intersection types
- Session types



# What can you do with types?

- Refinement types
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- Session types

Legend

We have these

We could have these

But that's a topic for another talk!





# What are we doing with Types?

## Recent work:

- [BigInt](#) support
- [Instant](#) support

## In progress:

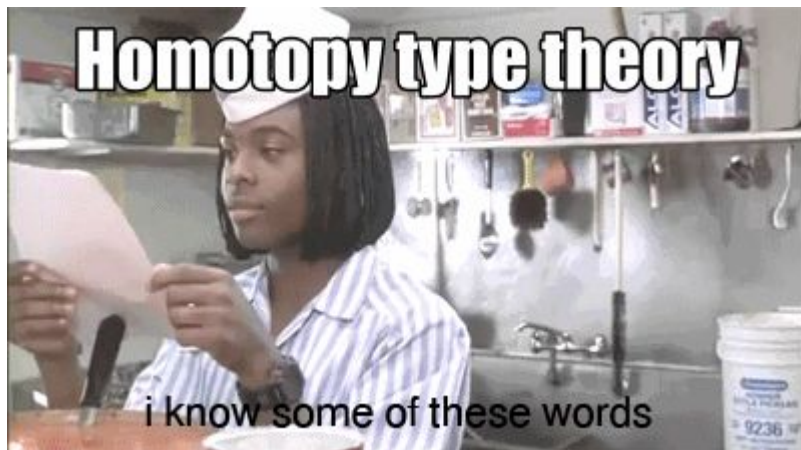
- [Arcs Nullables](#)
- [BigInt, Instant and Duration Refinement Support](#)

## For the future:

- [Arcs Requests for Type Features in October of 2020](#)
- [Relaxed Reads and Writes](#)

## Sources + Further reading

- The Arcs Type System - [go/arcs-type-system](https://go/arcs-type-system)
- [Types and Programming Languages](#) (Free PDF)
- [On the Expressive Power of Prog. Languages](#)
- [Join & Meet wiki](#)
- nLab: [type theory in nLab](#)
- Particularly exciting new research is in [Intuitionistic and homotopy type theory](#)





## Sources + Further reading from Gogul

- [Type Inference in Arcs](#)
- [Formal Methods in Arcs Dataflow Analysis](#)
- [Types & References](#)



# **That's all folks**

**Thanks for coming. Questions?**