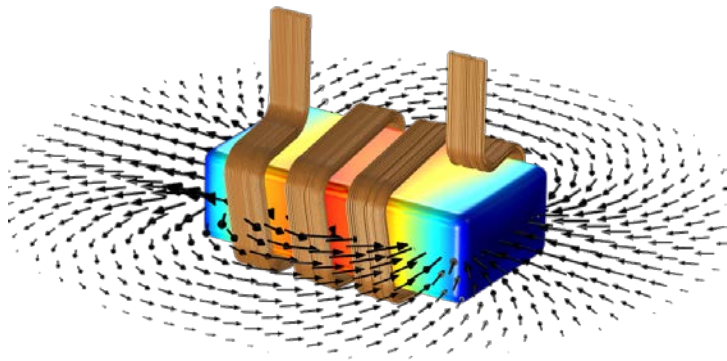




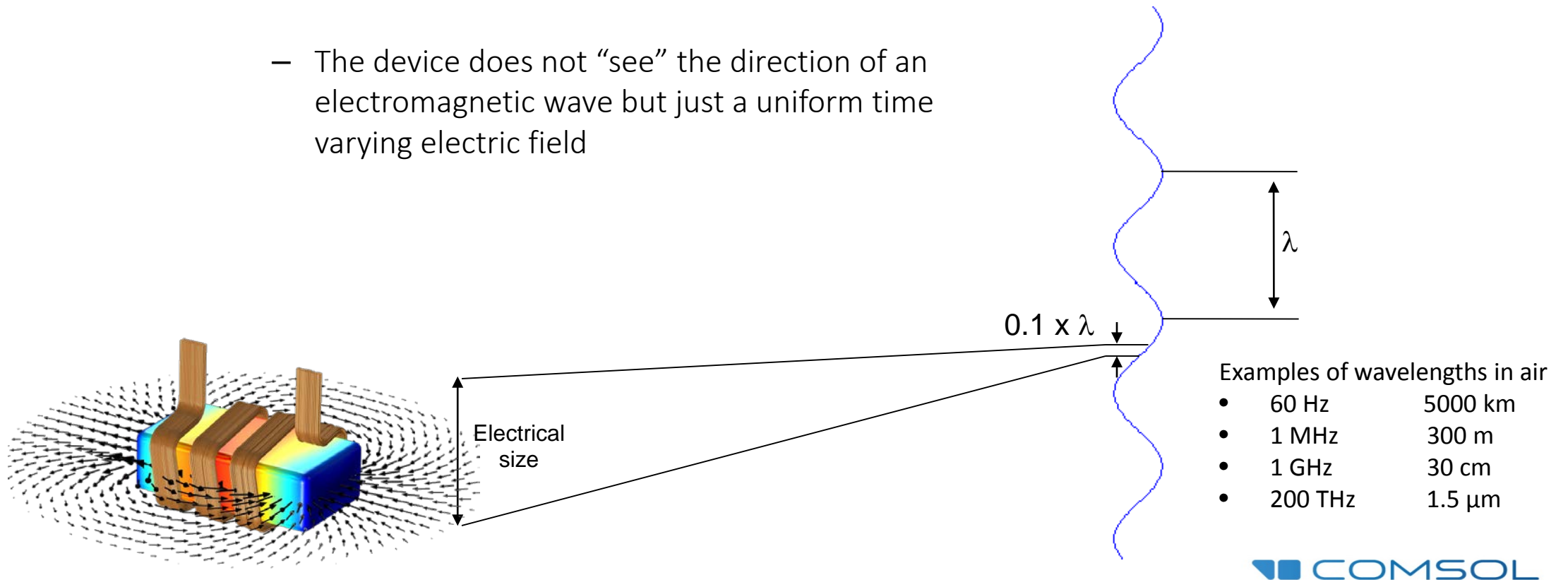
Low-Frequency Electromagnetics with COMSOL Multiphysics®



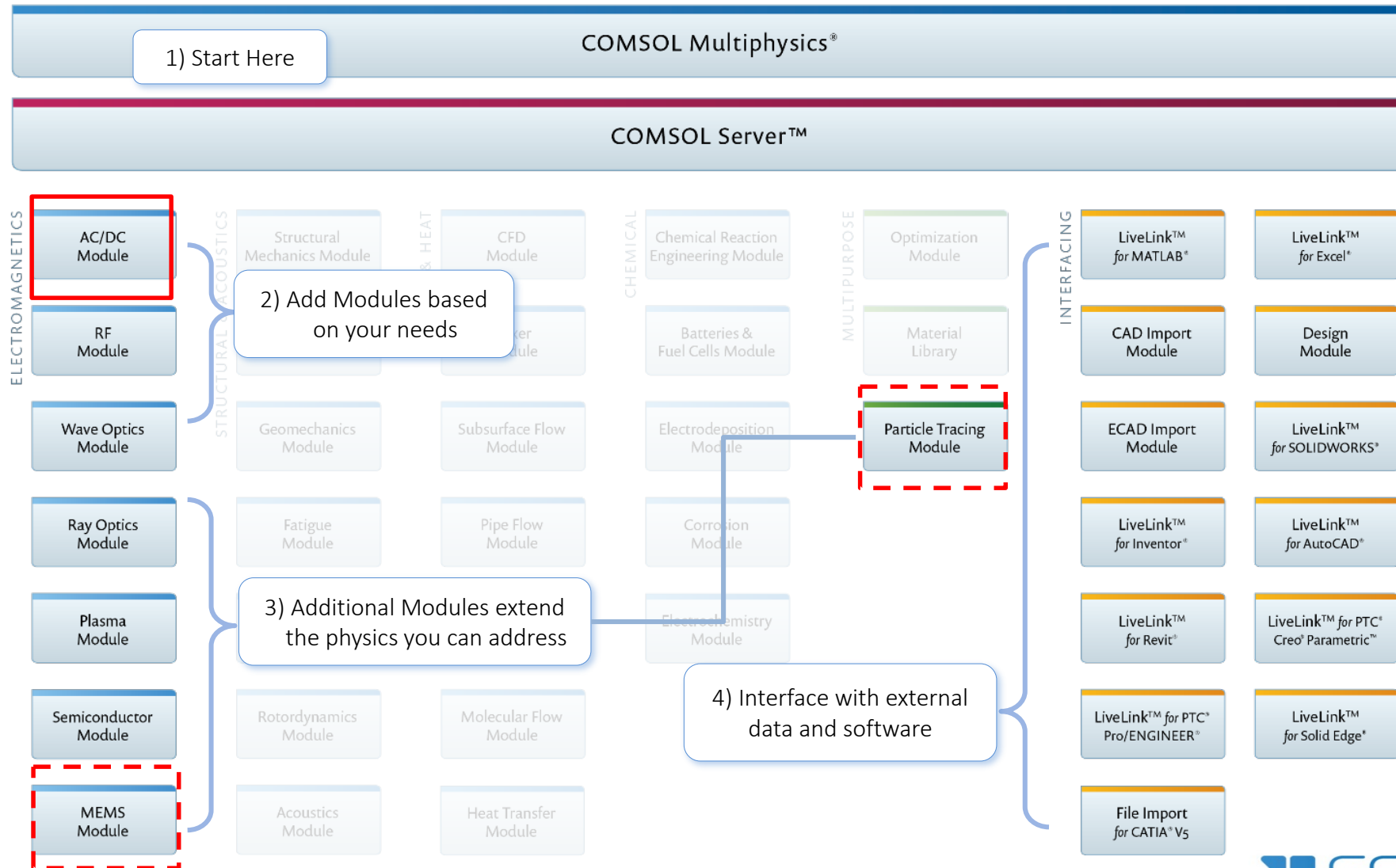
Ping Chu
Los Angeles, COMSOL, Inc.

Low Frequency or High Frequency?

- What is low frequency?
 - The device does not “see” the direction of an electromagnetic wave but just a uniform time varying electric field



Electromagnetics is Extended by Add-on Modules



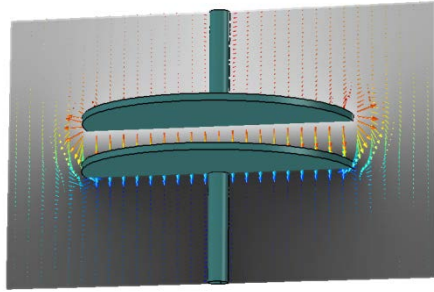
Built-in Physics Interfaces

- AC/DC Module
 - *Electrostatics¹, Electrostatics BEM*
 - *Electric Currents¹*
 - *Electric Currents – Shell*
 - *Electrical Circuit*
 - *Magnetic Fields, No Currents (FEM/BEM)*
 - *Magnetic Fields¹*
 - *Magnetic and Electric Fields*
 - *Rotating Machinery, Magnetic*
 - *Magnetic Field Formulation*
 - *Joule Heating^{1,2}*
 - *Induction Heating²*
 - *Magnetostriction²*

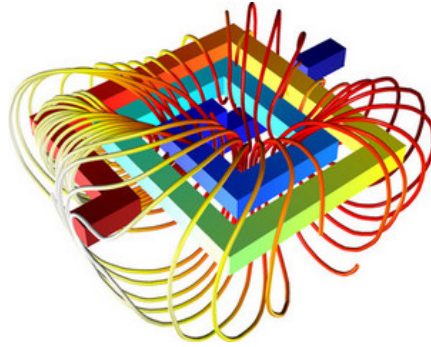
1 This physics interface is included with the core COMSOL Multiphysics® package but has added functionality for this module.

2 This physics interface is a predefined multiphysics coupling that automatically adds all of the physics interfaces and coupling features required.

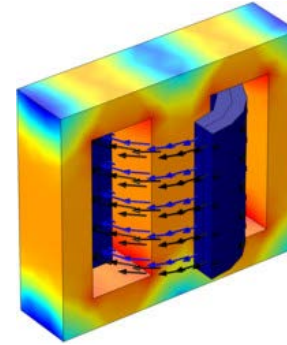
AC/DC Module Applications: (Static, Low Frequency, Some Transient)



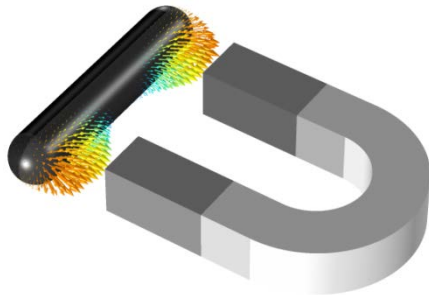
Resistive and Capacitive Devices
(Including Touchscreens)



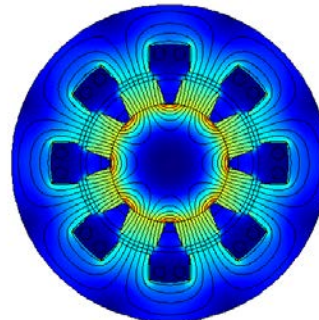
Inductors and Coils



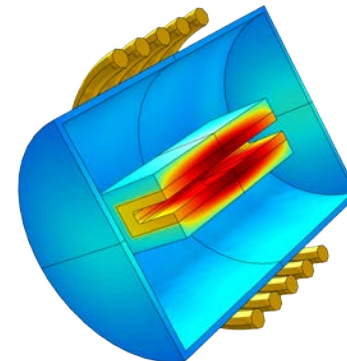
Nonlinear Magnetic Material



Magnets



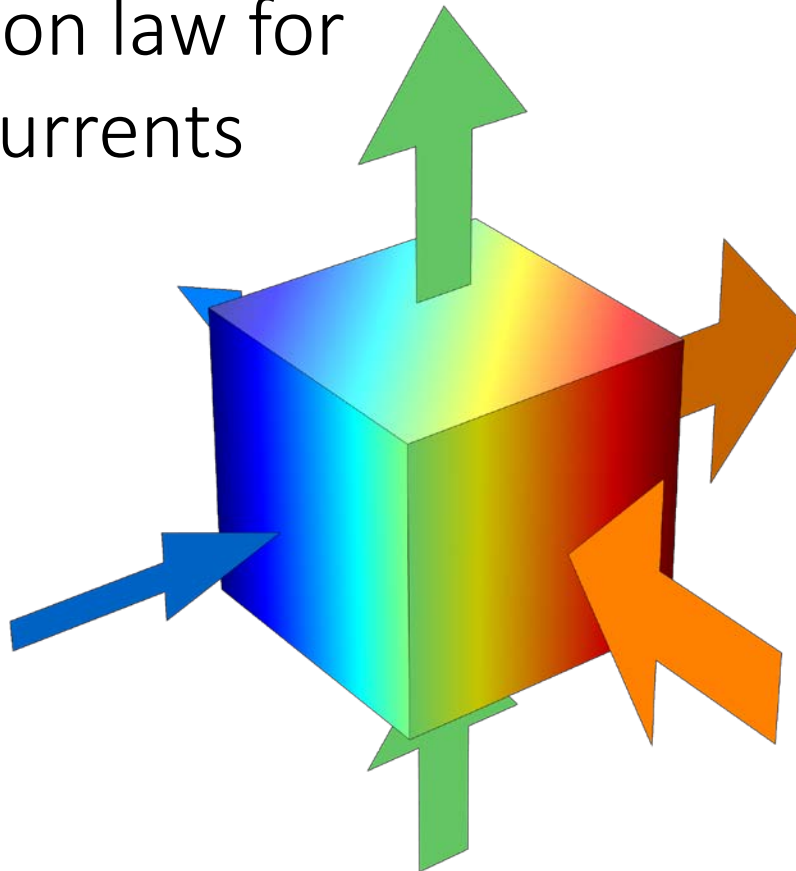
Motors and Actuators



Multiphysics: Heating and Magnetostriction

Poisson's Equation

- We get a conservation law for stationary electric currents
- Other examples:
 - Magnetostatics
 - Electrostatics
 - Heat transfer



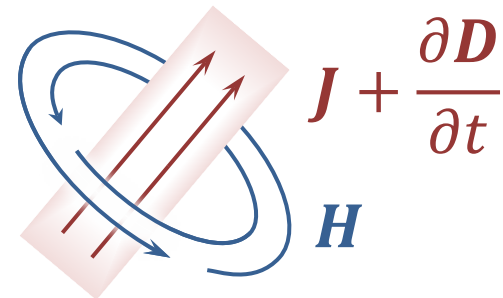
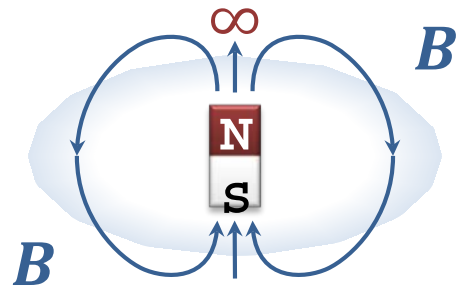
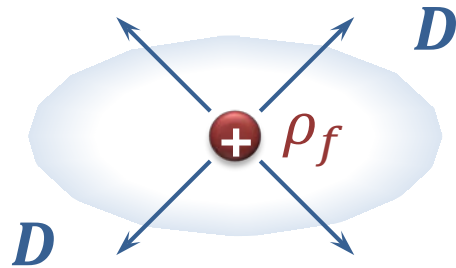
$$-\nabla \cdot (\boldsymbol{\sigma} \nabla V) = Q_j$$

$$\nabla \cdot (\boldsymbol{\sigma} \mathbf{E}) = Q_j$$

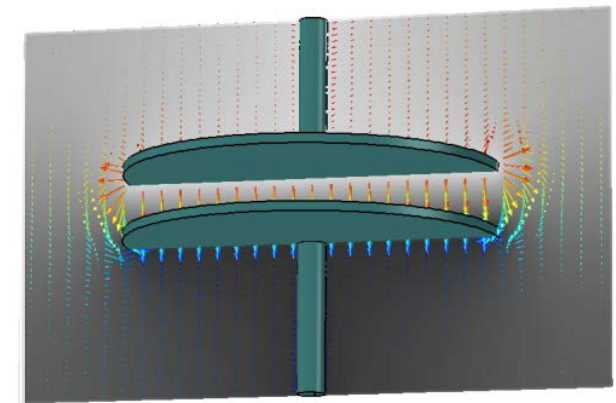
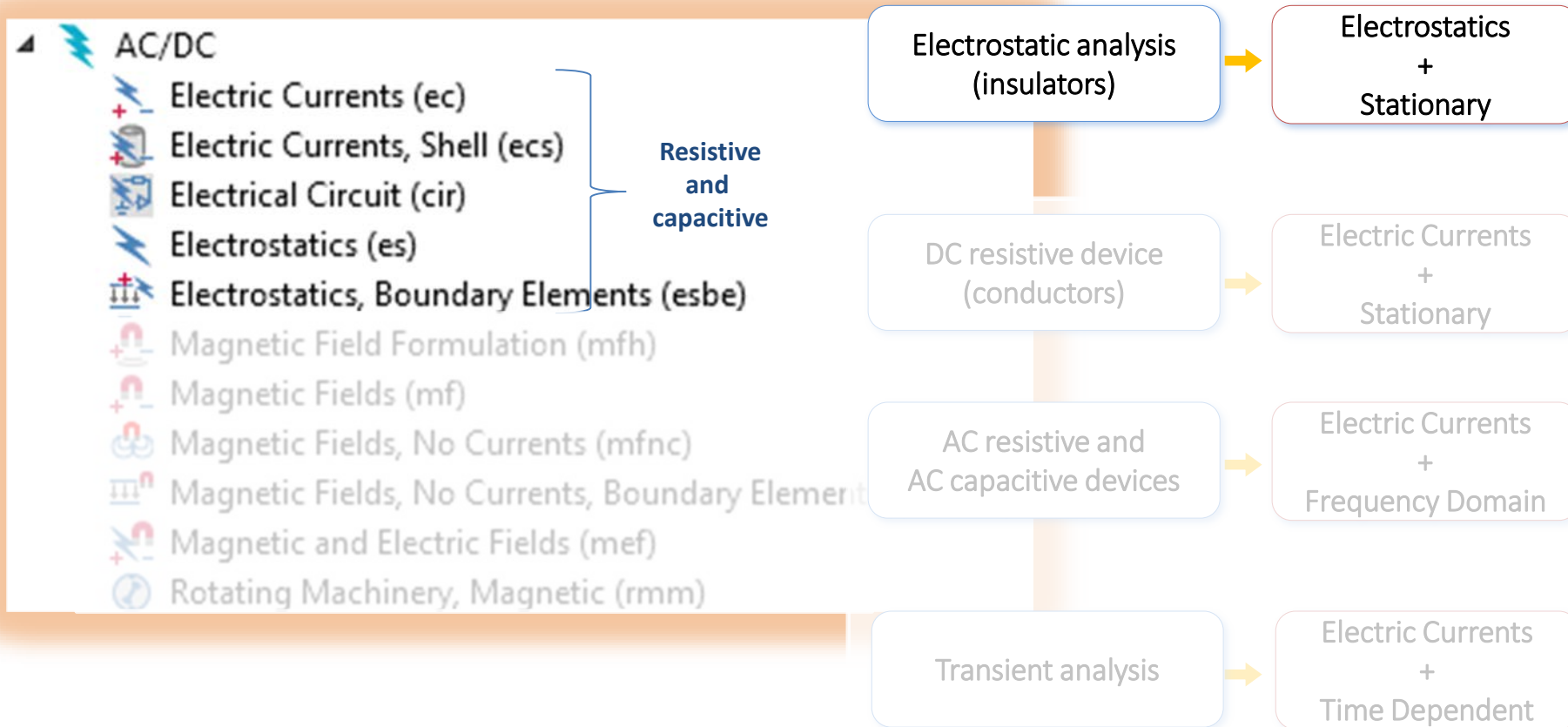
$$\nabla \cdot \mathbf{J} = Q_j$$

Maxwell's Equations

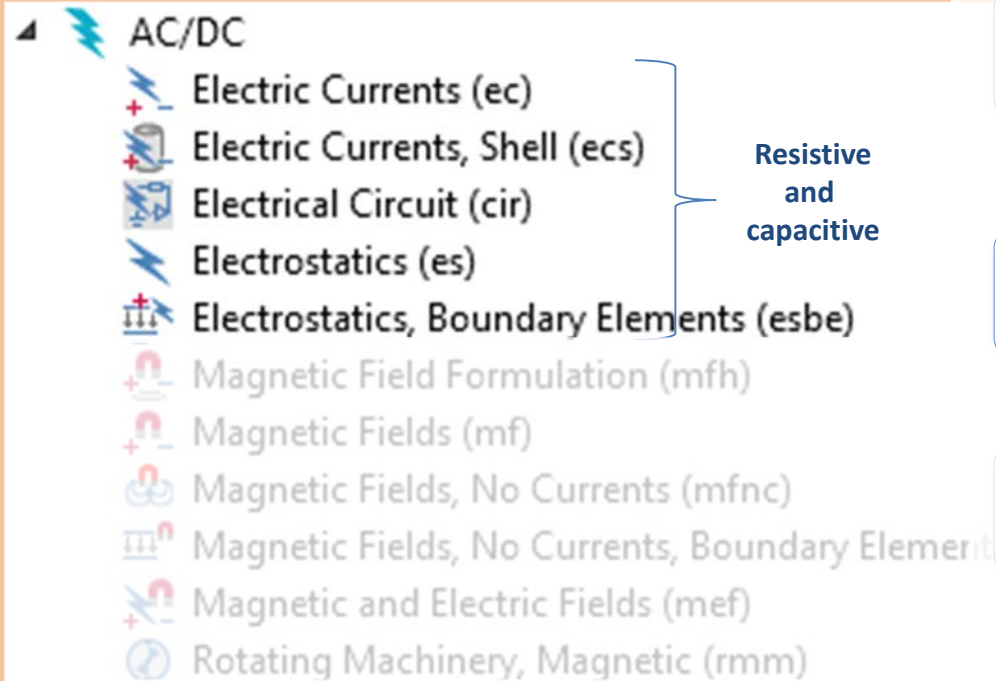
<i>Gauss</i>	$\nabla \cdot \mathbf{D} = \rho$	$\nabla \times \mathbf{E} = 0 - \frac{\partial \mathbf{B}}{\partial t} - \mathbf{j} \omega \mathbf{B}$	<i>Faraday's law</i>
<i>M-Gauss</i>	$\nabla \cdot \mathbf{B} = 0$	$\nabla \times \mathbf{H} = 0 + \mathbf{J} + \frac{\partial \mathbf{D}}{\partial t} + \mathbf{j} \omega \mathbf{D}$	<i>Maxwell-Ampère's law</i>



Resistive and Capacitive Devices Modelling



Resistive and Capacitive Devices Modelling



Electrostatic analysis
(insulators)

Electrostatics
+
Stationary

DC resistive device
(conductors)

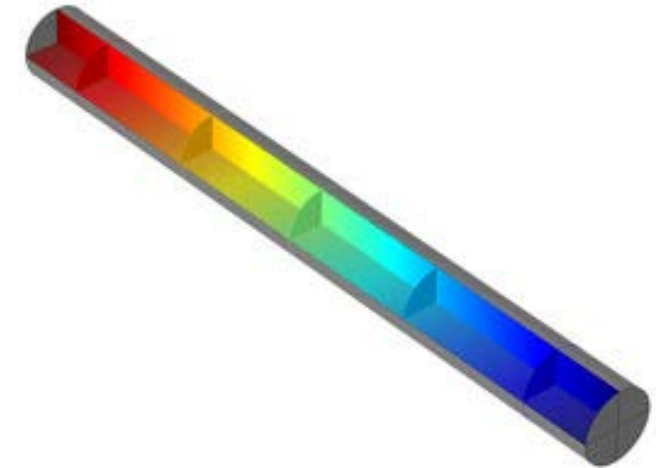
Electric Currents
+
Stationary

AC resistive and
AC capacitive devices

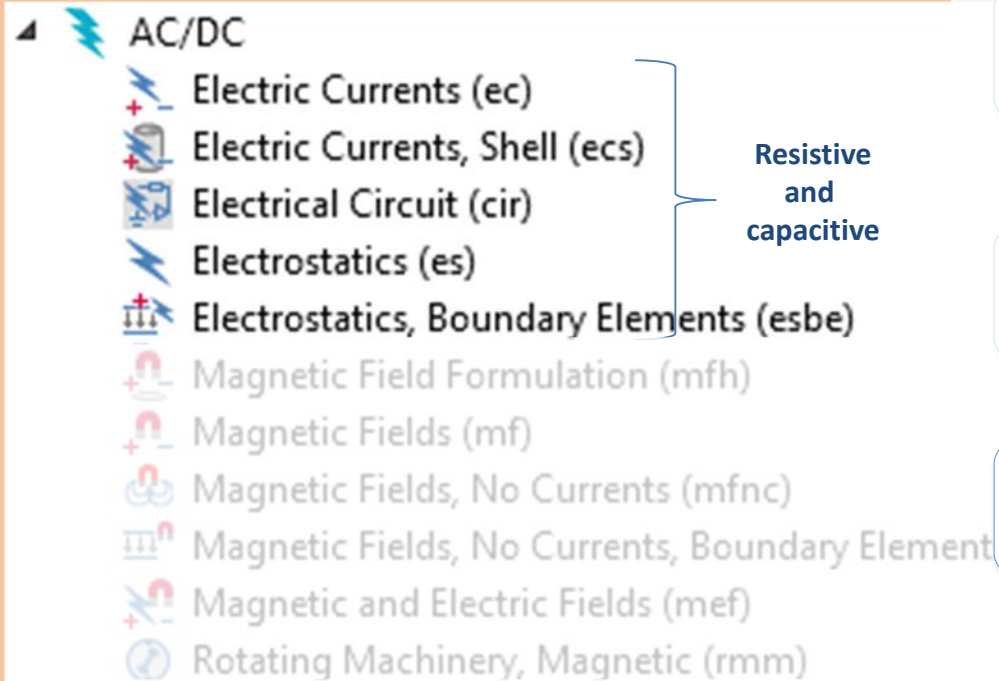
Electric Currents
+
Frequency Domain

Transient analysis

Electric Currents
+
Time Dependent



Resistive and Capacitive Devices Modelling



Electrostatic analysis
(insulators)

Electrostatics
+
Stationary

DC resistive device
(conductors)

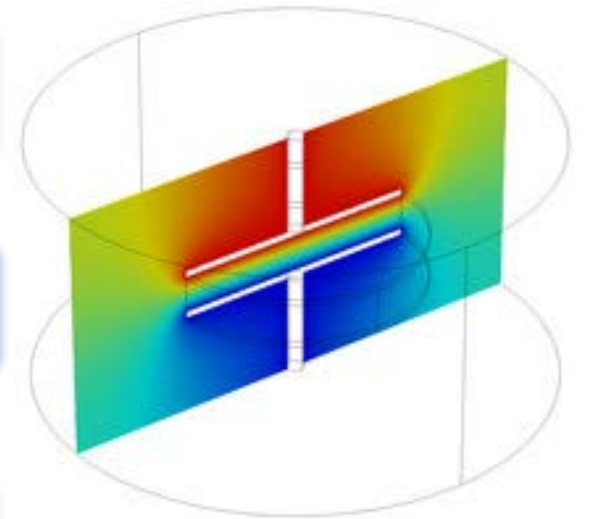
Electric Currents
+
Stationary

AC resistive and
AC capacitive devices

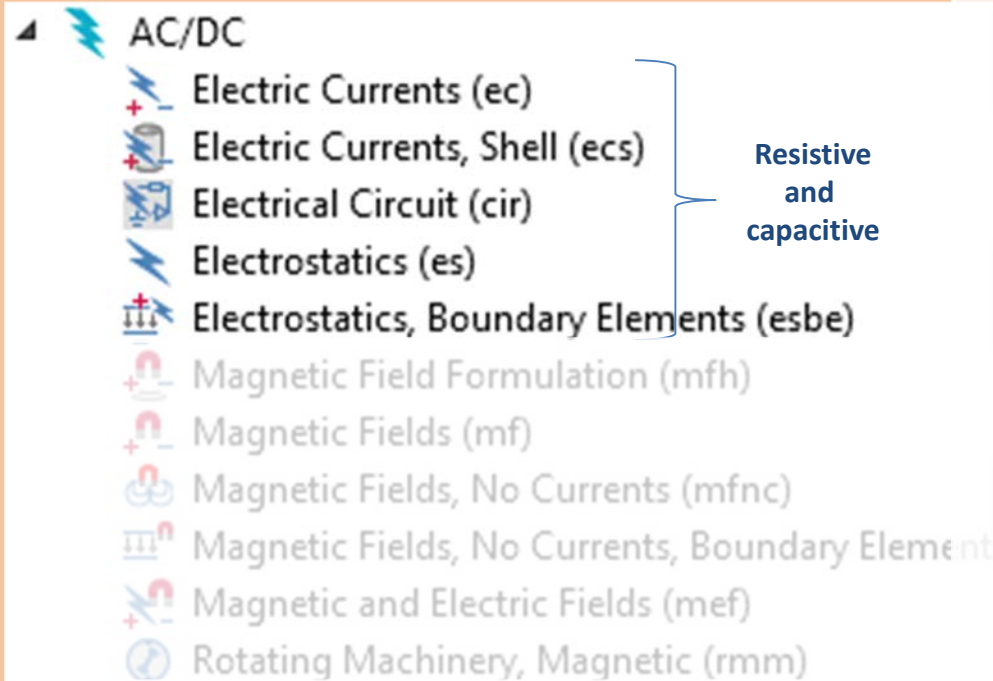
Electric Currents
+
Frequency Domain

Transient analysis

Electric Currents
+
Time Dependent



Resistive and Capacitive Devices Modelling



Electrostatic analysis
(insulators)

Electrostatics
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Stationary

DC resistive device
(conductors)

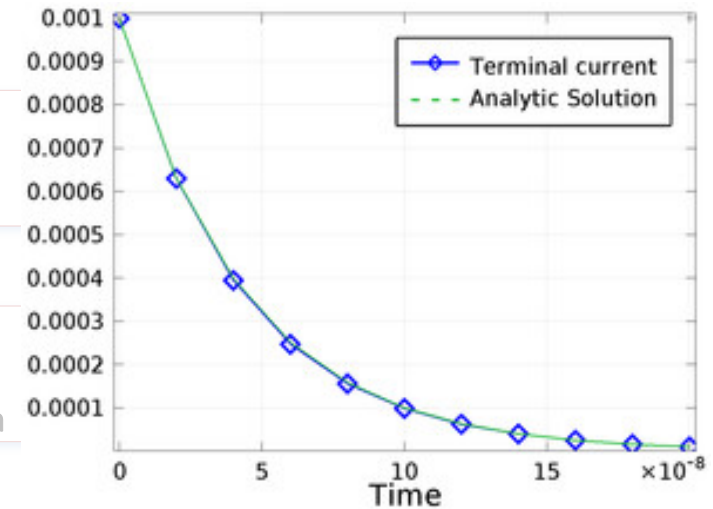
Electric Currents
+
Stationary

AC resistive and
AC capacitive devices

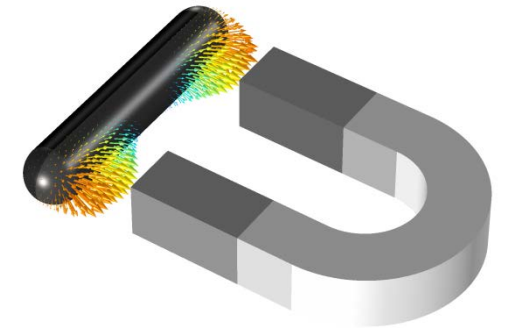
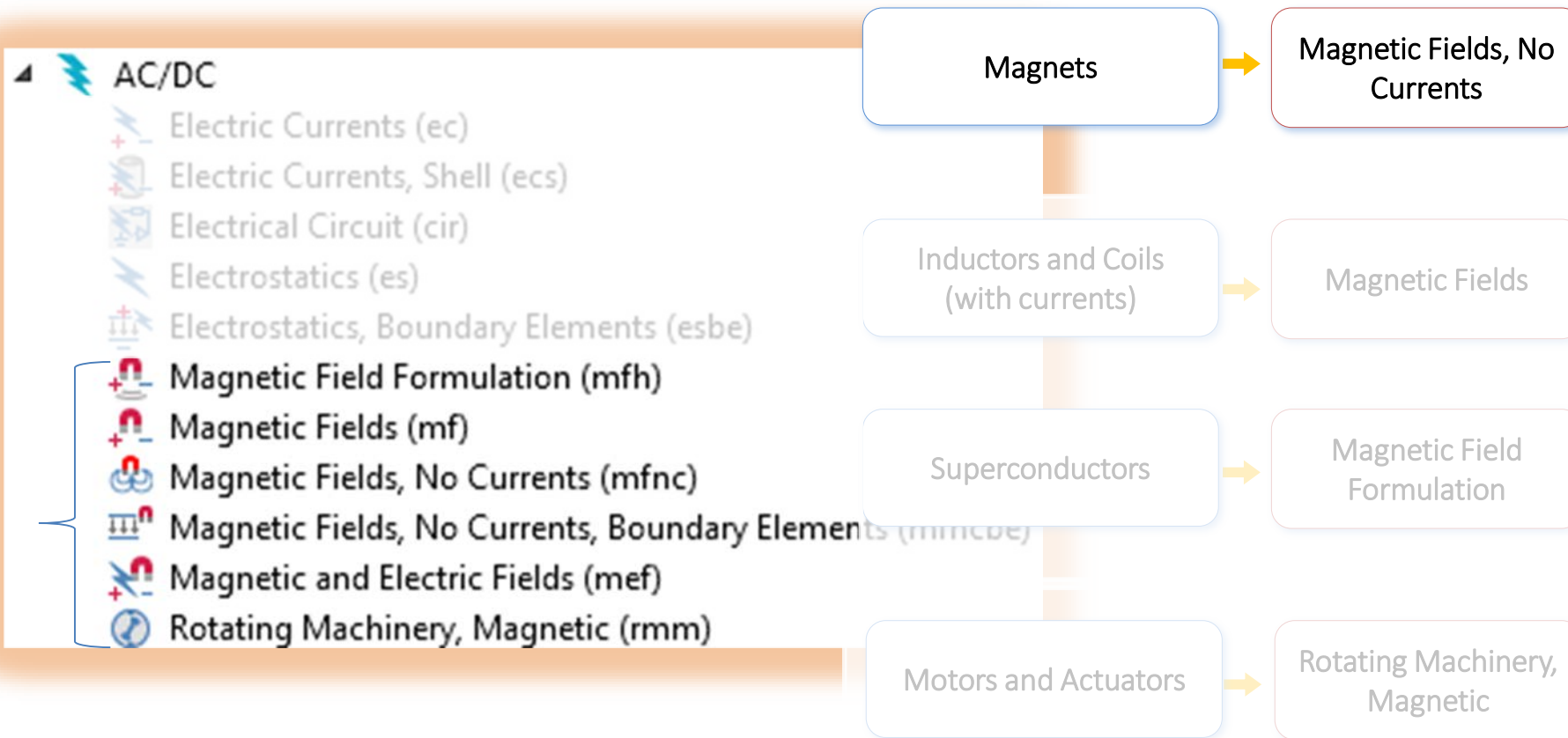
Electric Currents
+
Frequency Domain

Transient analysis

Electric Currents
+
Time Dependent



Magnets, Coils and Motors Modelling



Skin Depth, Wavelength, Relaxation Time

- Skin depth δ
- Wavelength λ
- Charge relaxation time τ

$$\delta = \frac{1}{\operatorname{Re}(\sqrt{i\omega\mu_0\mu_r(\sigma + i\omega\varepsilon_0\varepsilon_r)})} \approx \sqrt{\frac{2}{\omega\mu\sigma}} \approx \frac{503}{\sqrt{\sigma\mu_r f}}, \quad J(d) = J_s e^{-d/\delta}$$

$$\lambda_0 = \frac{c}{f}, \quad \lambda = \frac{\lambda_0}{n}$$

$$\tau = \frac{\varepsilon}{\sigma}, \quad \rho_f(t) = \rho_0 e^{-t/\tau}$$

Magnets, Coils and Motors Modelling

AC/DC

- Electric Currents (ec)
- Electric Currents, Shell (ecs)
- Electrical Circuit (cir)
- Electrostatics (es)
- Electrostatics, Boundary Elements (esbe)
- Magnetic Field Formulation (mfh)**
- Magnetic Fields (mf)**
- Magnetic Fields, No Currents (mfnc)**
- Magnetic Fields, No Currents, Boundary Elements (mfncbe)**
- Magnetic and Electric Fields (mef)**
- Rotating Machinery, Magnetic (rmm)**

Magnets

Magnetic Fields, No
Currents

Inductors and Coils
(with currents)

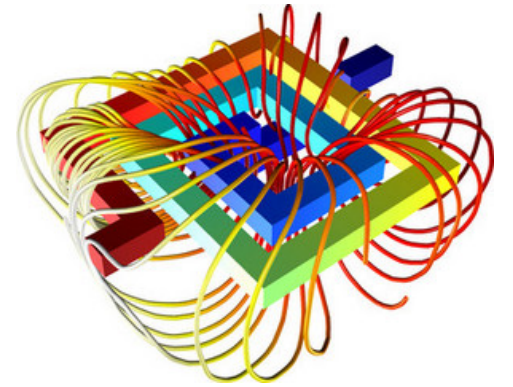
Magnetic Fields or
Magnetic and
Electric Fields

Superconductors

Magnetic Field
Formulation

Motors and Actuators

Rotating Machinery,
Magnetic



Magnets, Coils and Motors Modelling

AC/DC

- Electric Currents (ec)
- Electric Currents, Shell (ecs)
- Electrical Circuit (cir)
- Electrostatics (es)
- Electrostatics, Boundary Elements (esbe)
- Magnetic Field Formulation (mfh)**
- Magnetic Fields (mf)**
- Magnetic Fields, No Currents (mfnc)**
- Magnetic Fields, No Currents, Boundary Elements (mfnb)**
- Magnetic and Electric Fields (mef)**
- Rotating Machinery, Magnetic (rmm)**

Magnets

Magnetic Fields, No
Currents

Inductors and Coils
(with currents)

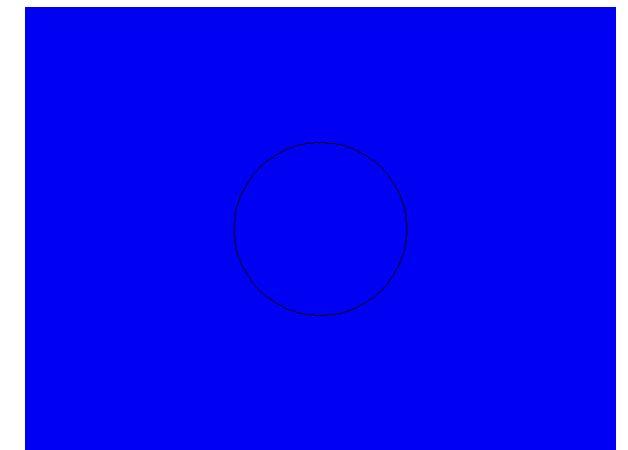
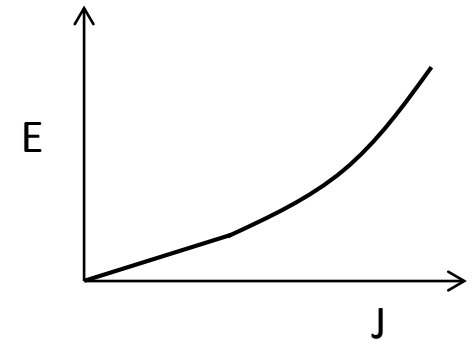
Magnetic Fields or
Magnetic and
Electric Fields

Superconductors

Magnetic Field
Formulation

Motors and Actuators

Rotating Machinery,
Magnetic



Magnets, Coils and Motors Modelling

AC/DC

- Electric Currents (ec)
- Electric Currents, Shell (ecs)
- Electrical Circuit (cir)
- Electrostatics (es)
- Electrostatics, Boundary Elements (esbe)
- Magnetic Field Formulation (mfh)**
- Magnetic Fields (mf)**
- Magnetic Fields, No Currents (mfnc)**
- Magnetic Fields, No Currents, Boundary Elements (mmncbe)
- Magnetic and Electric Fields (mef)**
- Rotating Machinery, Magnetic (rmm)**

Magnets

Magnetic Fields, No
Currents

Inductors and Coils
(with currents)

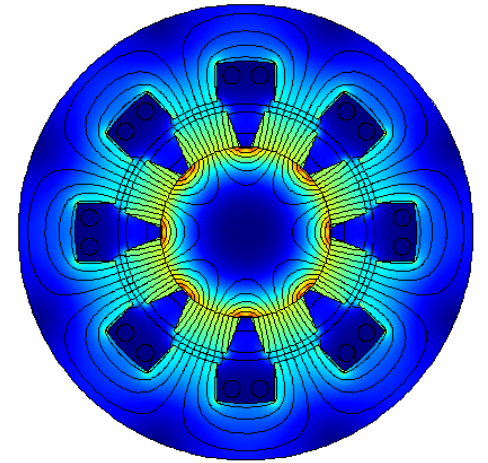
Magnetic Fields or
Magnetic and
Electric Fields

Superconductors

Magnetic Field
Formulation

Motors and Actuators

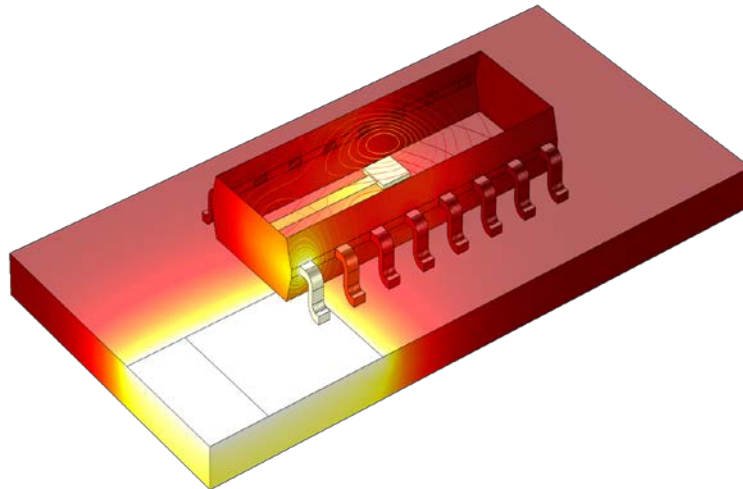
Rotating Machinery,
Magnetic



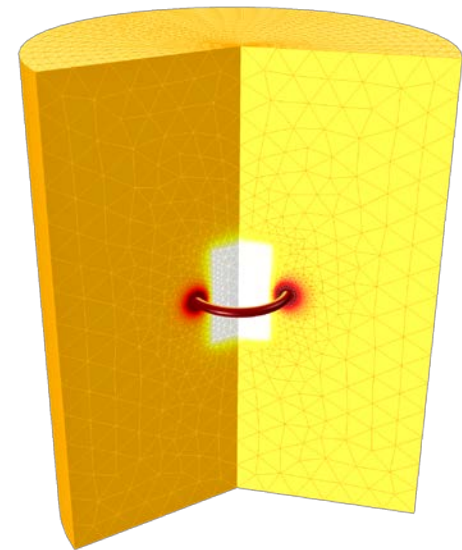
Whenever there are Electromagnetic Losses, there is a Rise in Temperature

- Specialized user interfaces and solvers address the two-way coupled frequency-domain electromagnetic and stationary or time-domain thermal problems

- Heat Transfer
 - Heat Transfer in Solids (ht)
 - Heat Transfer in Fluids (ht)
- Electromagnetic Heating
 - Joule Heating
 - Induction Heating



Joule Heating



Induction Heating

Feature Overview: Domain Conditions

- Full and Reduced Field excitations

Magnetic Fields (mf)

- ▶ Ampère's Law 1
- ▶ Magnetic Insulation 1
- ▶ Initial Values 1
- Equation View

Settings
Magnetic Fields

Label: Magnetic Fields

Name: mf

▶ Domain Selection

▶ Equation

▼ Background Field

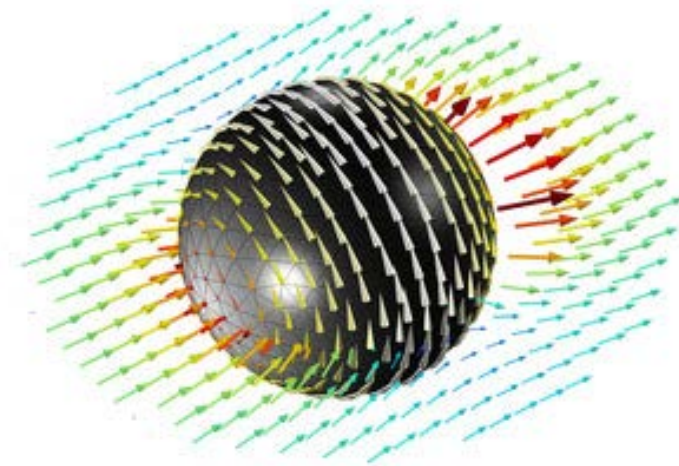
Solve for:
Reduced field

Background field specification:
Magnetic vector potential

Background magnetic vector potential:

0	x
0	y
$B_0 \cdot y$	z

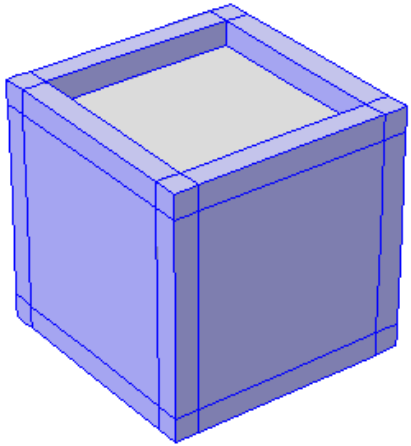
\mathbf{A}_b Wb/m



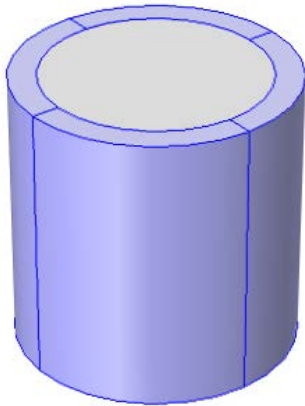
<https://www.comsol.com/model/iron-sphere-in-a-13-56-mhz-magnetic-field-12835>

Feature Overview: Domain Conditions

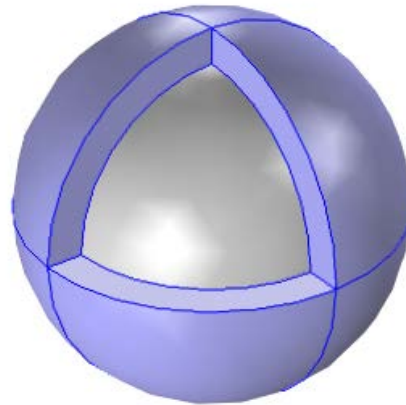
- Full and Reduced Field excitations
- Infinite Elements



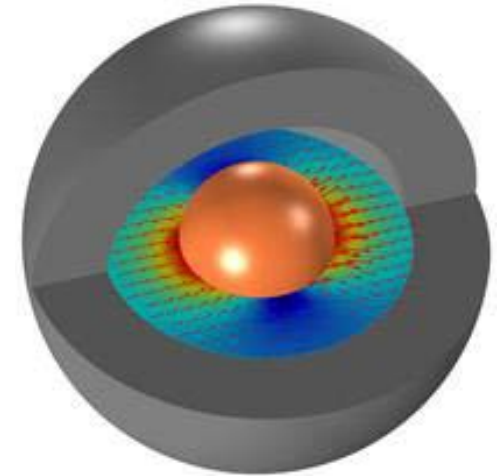
Cartesian Type



Cylindrical Type



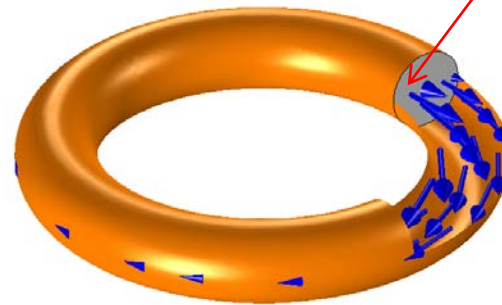
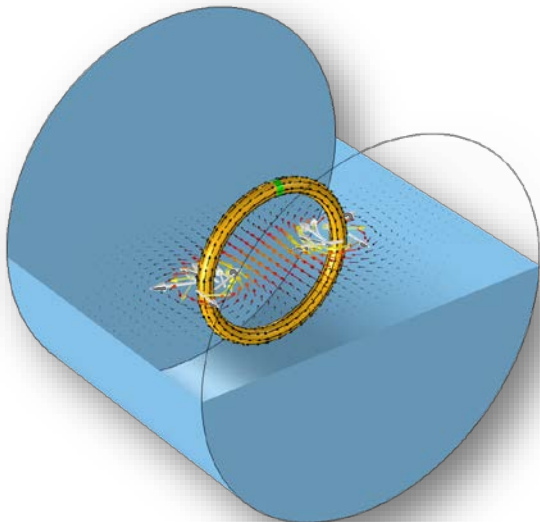
Spherical Type



Tip: if the energy is stored in the center core, the air domain can be roughly **3 to 5 times** the size of the core without Infinite Element Domain.

Feature Overview: Domain Conditions

- Full and Reduced Field excitations
- Infinite Elements
- Coils: Single Conductor Coil

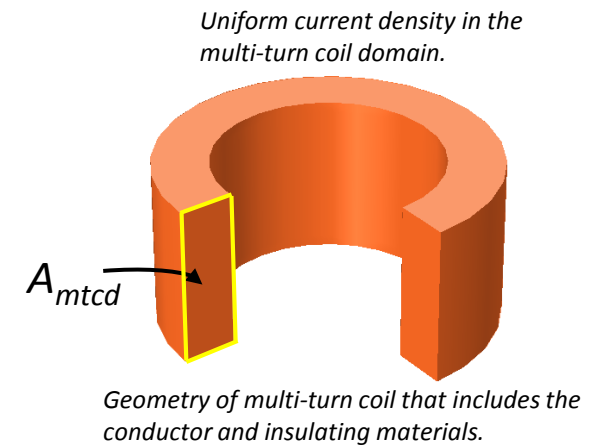
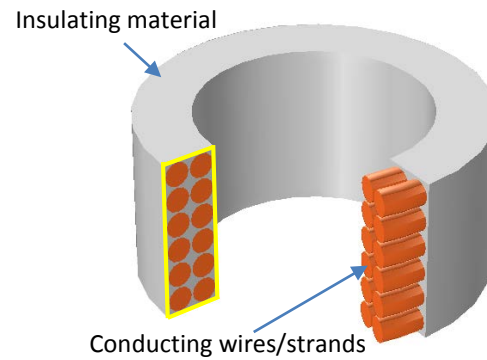
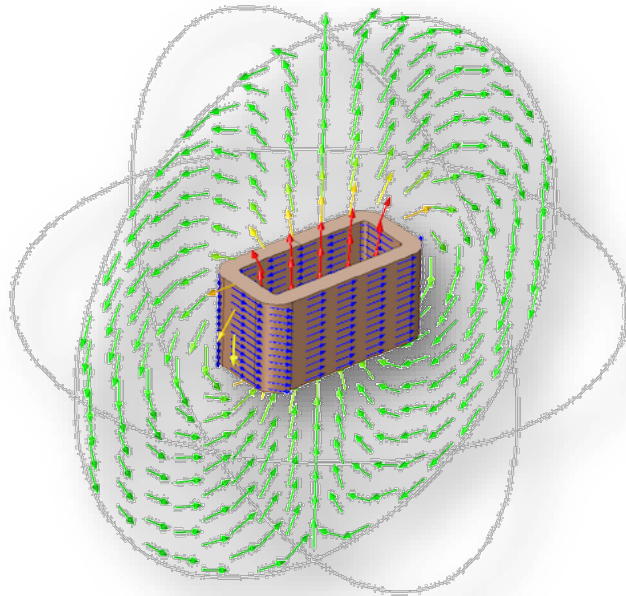


Input

1. Specify the voltage across the boundary
2. Specify the current through the boundary
3. Options to connect to the lumped electrical circuit

Feature Overview: Domain Conditions

- Full and Reduced Field excitations
- Infinite Elements
- Coils: Homogenized Multi-Turn Coil

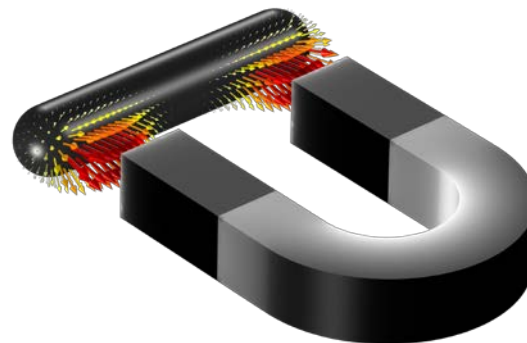


Feature Overview: Data Extraction and Imports

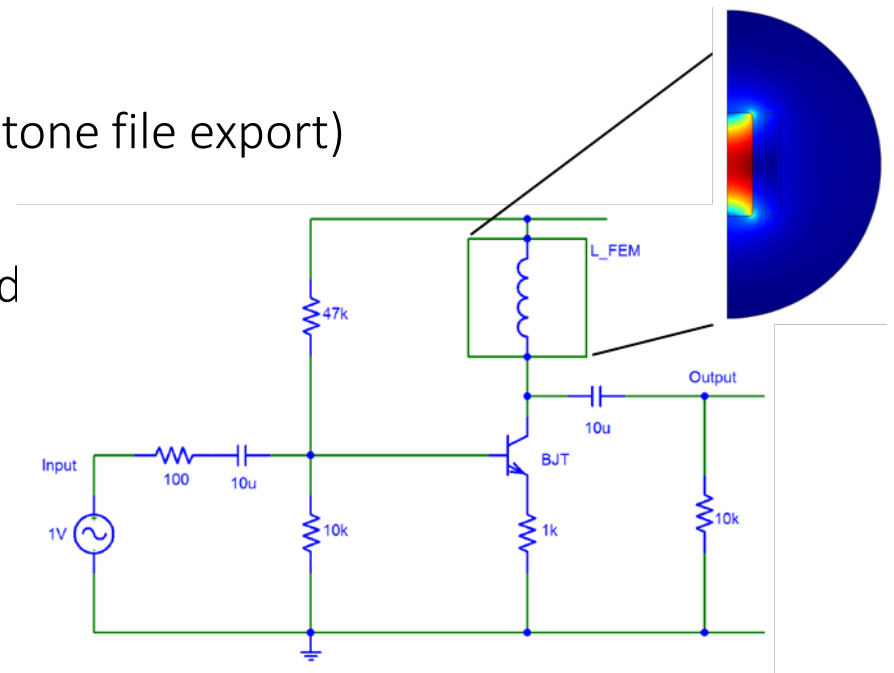
- Resistance, Capacitance, Inductance, and Mutual Inductance
- Impedance, Admittance, and S-parameters (optional Touchstone file export)
- Electromagnetic torque and force calculation due to EM field
- Coupling to Electrical Circuits (supports SPICE netlist)

$$\begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix}$$

Lumped Parameters



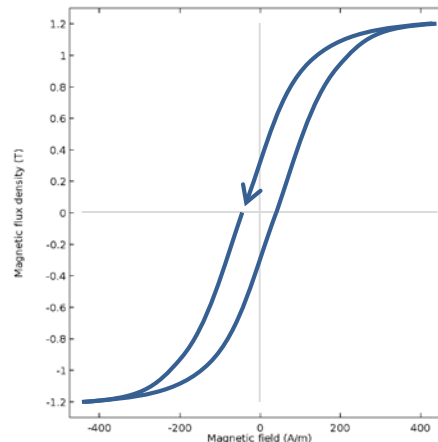
Magnetic Forces



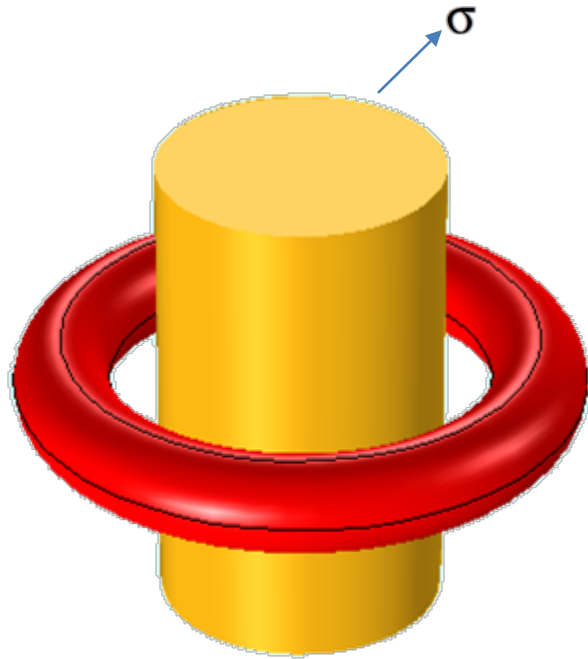
Electrical Circuits

Feature Overview: Material Models

- Constitutive relations $\mathbf{H} \leftrightarrow \mathbf{B}$
 - Relative permeability (user defined)
 - Relative permeability (effective medium)
 - Magnetic losses
 - $\mathbf{H}(\mathbf{B})$ curve, $\mathbf{B}(\mathbf{H})$ curve (user defined)
 - $\mathbf{H}(\mathbf{B})$ curve, $\mathbf{B}(\mathbf{H})$ curve (external)
 - Remanent flux density
 - Magnetization
 - Effective $\mathbf{H}(\mathbf{B})$ curve
 - $\mathbf{H}(\mathbf{B})$ nonlinear permanent magnet
 - Hysteresis (Jiles-Atherton model)
- Constitutive relations $\mathbf{J} \leftrightarrow \mathbf{E}$
 - Electrical conductivity (user defined)
 - Electrical conductivity (effective medium)
 - Electrical conductivity (Archie's law)
 - (Linearized) resistivity
 - $\mathbf{E}(\mathbf{J})$ characteristic
- Constitutive relations $\mathbf{D} \leftrightarrow \mathbf{E}$
 - Relative permittivity (user defined)
 - Relative permittivity (effective medium)
 - Dielectric losses
 - Loss tangent, loss angle
 - Loss tangent, dissipation factor
 - Remanent electric displacement
 - Polarization



Demo: Inductive Heating



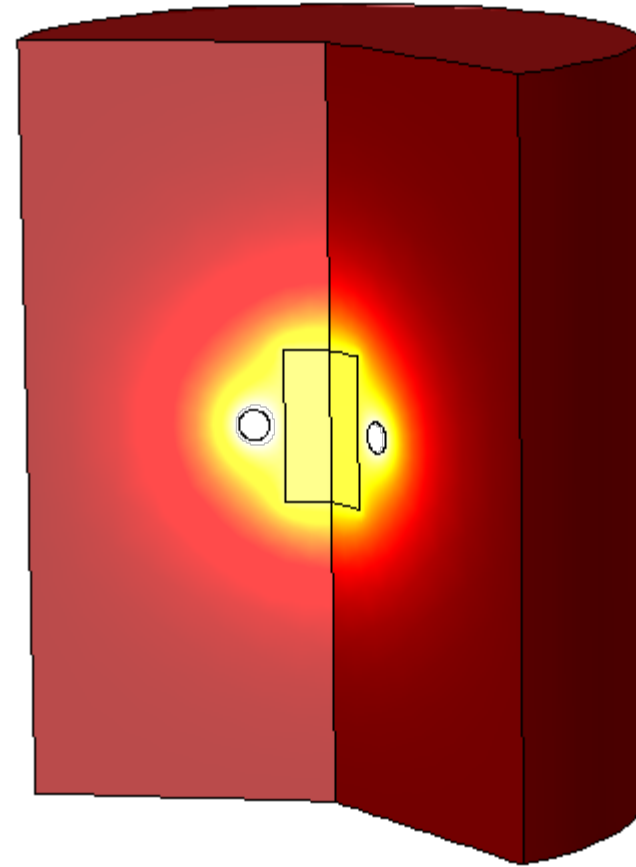
- AC current through a coil heats up the copper core:

$$\sigma = \frac{1}{[\rho_0(1 + \alpha(T - T_0))]}$$

- Multiphysics model
 - Electromagnetics: small time scale
 - Heat transfer: large time scale
- Frequency-Transient analysis

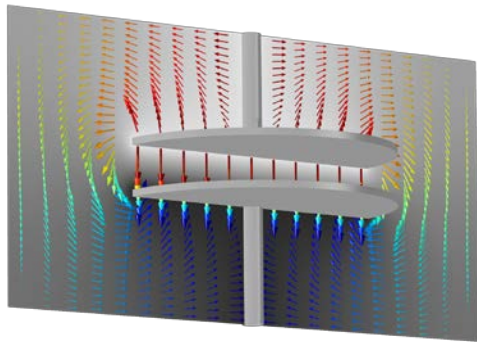
Summary of Workflow

- Select Dimension, Physics, Study
- Create/Import Geometry
- Apply Materials
- Set up Physics
- Mesh
- Solve
- Extract Results

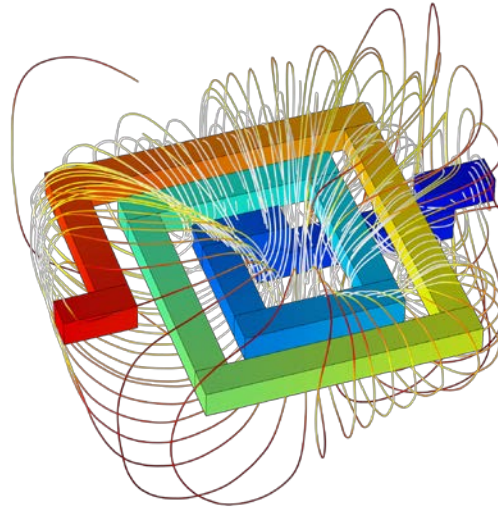


Concluding Remarks: Static Field Modeling

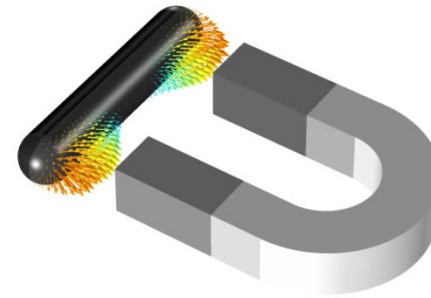
- **Electrostatics** solves for electric fields in perfect insulators
- Stationary **Electric Currents** solves for steady current flow in conductors
- Stationary **Magnetic Fields** solves for the magnetic fields around magnets, and the fields around current carrying objects



Parallel Plate Capacitor,
Electrostatics



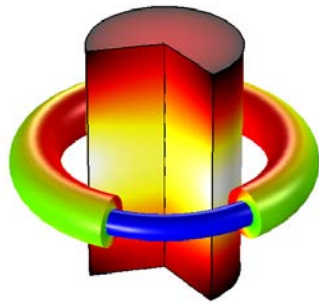
Inductor, DC current flow
and Magnetostatics



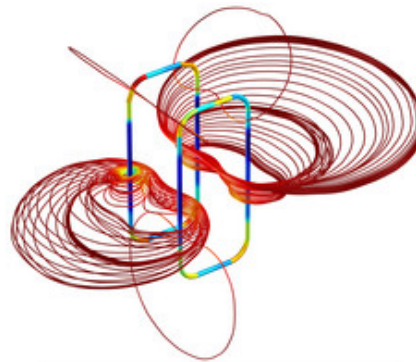
Permanent Magnet,
Magnetostatics

Concluding Remarks: Low Frequency Modeling

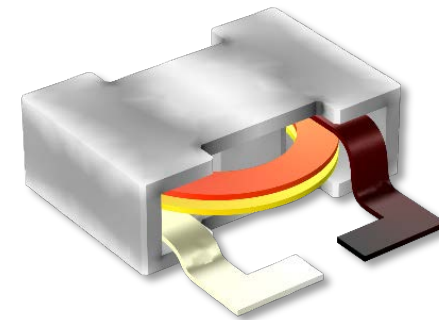
- **Electric Currents** solved in the frequency domain considers both conduction and displacement currents in conductive and dielectric media
- **Magnetic Fields** can be solved for in the frequency domain to find the conduction, displacement, and induction currents
- **Magnetic and Electric Fields** can be solved to find magnetic and electric fields resulting from an applied electric potential



Inductive Heating,
Magnetic Fields



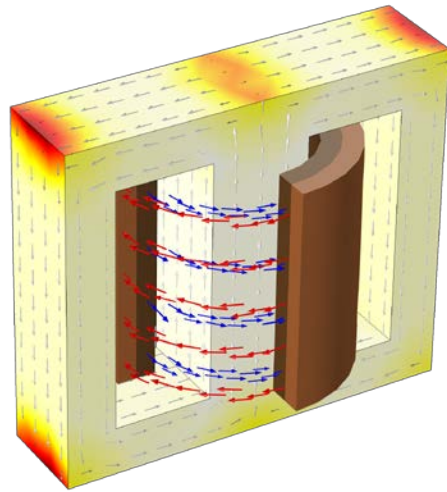
Mutual Inductance,
Magnetic Fields Analysis



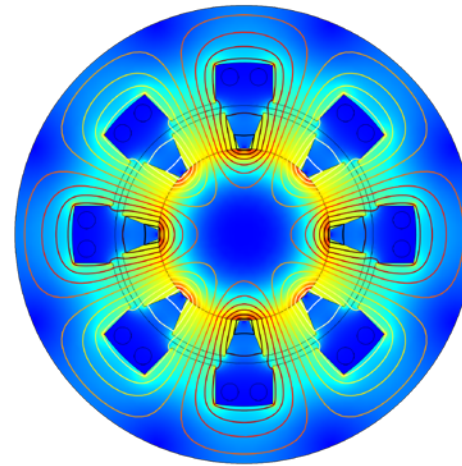
Inductor, Magnetic and
Electric Fields

Concluding Remarks: Transient Modeling

- Transient **Electric Currents** solves for conduction and displacement currents in conductive and dielectric media
- Transient **Magnetic Fields** is suitable for modeling current pulses and nonlinear material response to field strength
- **Rotating Machinery** considers the rotary velocity and acceleration of material



E-Core Transformer, Transient Magnetic Fields



Generator, Rotating Machinery

Questions?